

Heaps

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Section I

Heap

Representations

1. What is a heap?

- A Binary tree with added constraints
- When writing methods with heaps, we seek to always retain these heap properties



Property 1: Parents > Children

- Min heap: each parent is lesser than both of its children
 - The smallest element is stored at the root
 - Sibling Nodes have no relation
 - Unlike BSTs, the left node does not have to be less than the right node
- Max heap: similar properties, but with the largest element stored at the root

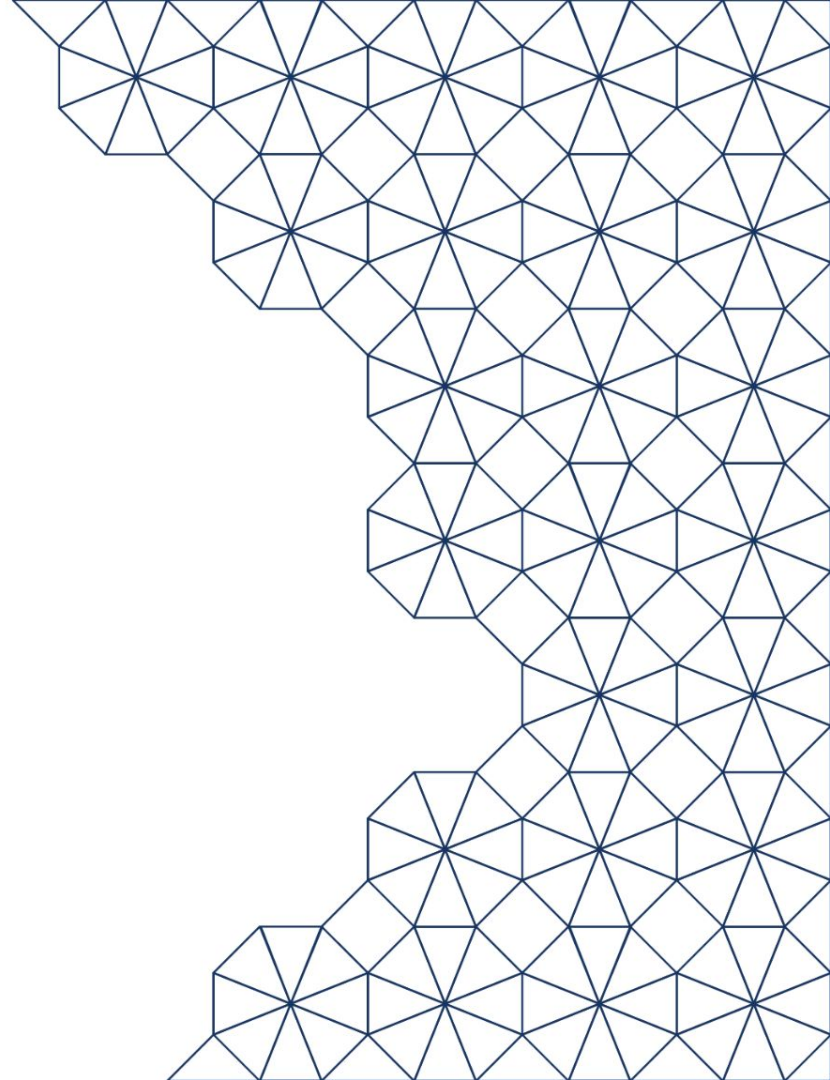
Property 2: Completeness

- During insertion, we must insert into the bottom of the heap
 - Ensures a more balanced heap



Representing Heaps

- Store the root at index 1
- If node is located at position n
 - Left Child: $2n$
 - Right Child: $2n + 1$

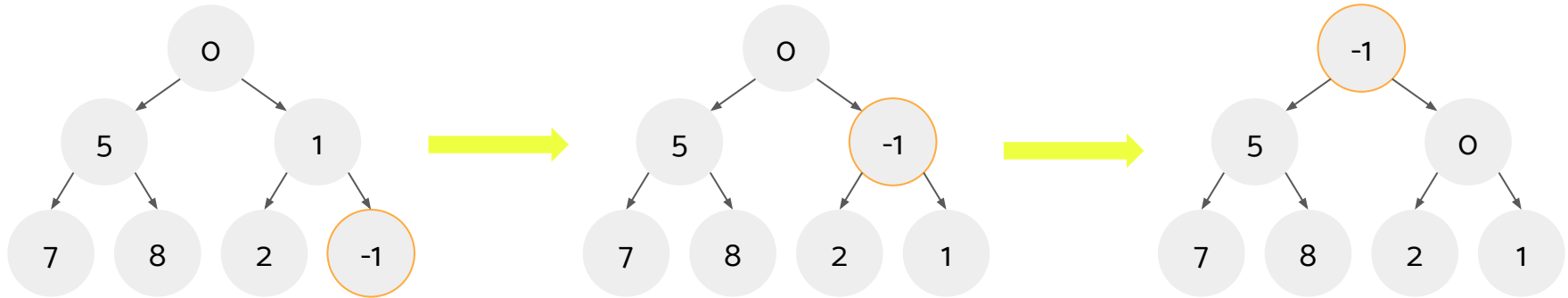


Section II

Heap Methods

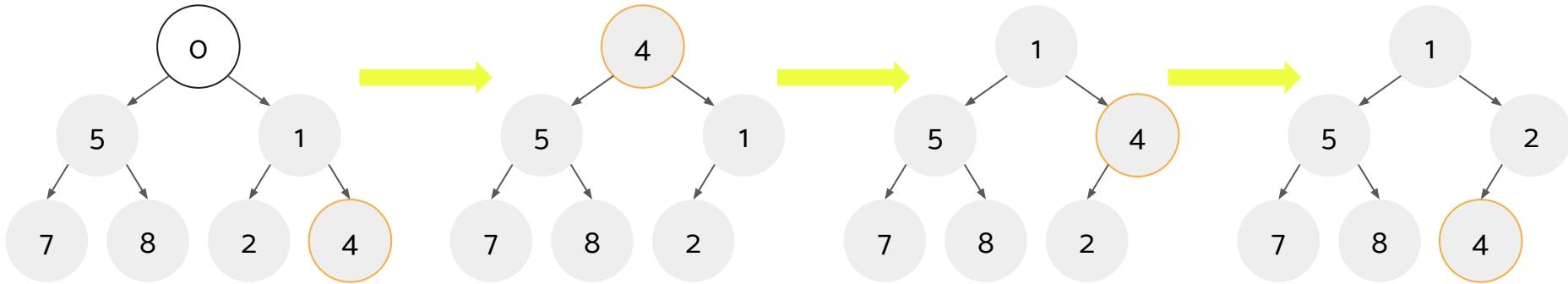
Insertion into (Min-)Heaps

We insert elements into the next available spot in the heap and **bubble up** as necessary: if a node is smaller than its parent, they will swap. (Check: what changes if this is a max heap?)



RemoveMin from (Min-)Heaps

We swap the last element with the root, remove the last element, and **bubble down** as necessary: if a node is greater than its children, it will swap with the lesser of its children. (Check: what changes if this is a max heap?)



Find

- Heaps aren't BSTs, so searching generally takes $O(N)$ time

Heap Asymptotics

<u>Operation</u>	<u>Runtime</u>
insert	$\Theta(\log N)$
findMin	$\Theta(1)$
removeMin	$\Theta(\log N)$

Thank you! Good luck :)