HW4

Computer Exercise

Part a

In Solution PDF

Part b

In Solution PDF

Part c

i. Varying n, sigma constant

```
% Part a and b done on paper
      % Part c_i (varying n, sigma constant)
 3
 4 -
      count = 0;
      kernel = 3;
                                  % based on w true = [1,3,2]'
      mse vector = zeros(5,1);
 7 -
       w_average_matrix = zeros(kernel,5);
       w_true_matrix = zeros(kernel,5);
 8 -
 9
10
11 - \Box for n = [10, 20, 30, 40, 50]
12
13 -
         count = count + 1;
14 -
         A = zeros(2*n+1, kernel);
15 -
         sigma = 1;
16 -
         x_{interim} = -n:n;
17 -
         x = transpose(x_interim*0.1); % turning to vector
18
19
          % A generation
20
21 - for i = 1:kernel
            A(:,i) = x.^i;
22 -
23 -
         end
          % t generation
25
26 -
         t = A(:,1) + 3*A(:,2) + 2*A(:,3);
27
28 -
          w true = pinv(A)*t; % calculating the true w directly from t
29 -
          w_true_matrix(:,count) = w_true;
31 -
          w average interim = zeros(kernel,1);
```

```
32
33 -
            mse_interim = 0;
34
35 -
            for j = 1:100
36
37
                % v generation
38 -
                v = sigma*randn(2*n+1,1);
39
40
                % y generation
41 -
                y = t + v;
42
43 -
                w estimated = pinv(A)*y;
                                               % calculating the estimate of w
44
45 -
                w average interim = w average interim + w estimated; % running sum of w average
46
47 -
                mse_interim = mse_interim + (norm(w_true - w_estimated))^2; % running sum of mse
48
49
50 -
            end
51
52 -
           mse = mse_interim/100;
53 -
           w_average = w_average_interim/100;
54
55 -
           mse vector(count,1) = mse;
56 -
           w_average_matrix(:,count) = w_average;
57
58
59
60 -
61
62 -
      n_range = [10;20;30;40;50];
      disp("The matrix of true w, where each column corresponds to a value of n and the column vector the vecto
63 -
      disp(w_true_matrix)
64 -
65 -
      disp("The matrix of estimated w (averaged over 100 iterations, for each n), where each column corresponds
66 -
      disp(w_average_matrix)
      disp("The averaged MSE over 100 iterations for each n, where rows represent MSE value for each n, is")
67 -
68 -
      disp(mse_vector)
     plot(n_range,mse_vector,'-o')
70 -
71 -
      xlabel('values of n, sigma = 1 (constant)')
72 -
      ylabel('MSE')
73
```

The matrix of true w, where each column corresponds to a value of n and the column vector the vector of w, is,

```
    1.0000
    1.0000
    1.0000
    1.0000

    3.0000
    3.0000
    3.0000
    3.0000

    2.0000
    2.0000
    2.0000
    2.0000
```

As expected, it is [1,3,2]

The matrix of estimated w (averaged over 100 iterations, for each n), where each column corresponds to a value of n and the column vector the vector of averaged w estimate, is,

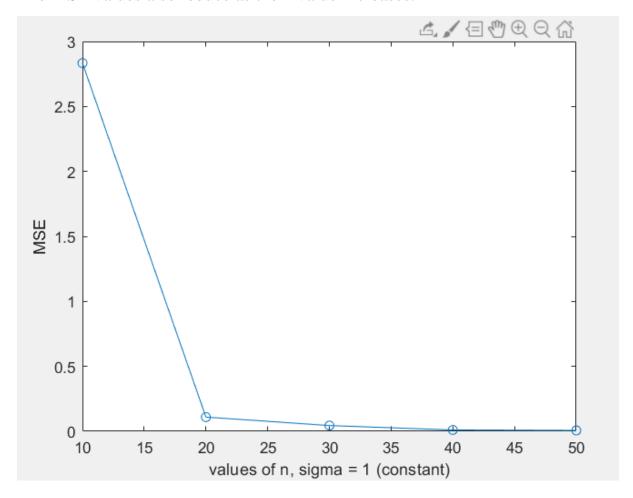
0.9333	1.0302	1.0023	1.0099	1.0042
3.0322	2.9993	2.9981	2.9999	3.0000
2.0261	1.9950	2.0001	1.9990	1.9996

As n increases, the average (over 100 trials) of estimate of **w** becomes more accurate.

The averaged MSE over 100 iterations for each n, where rows represent MSE value for each n, is,

- 2.3952
- 0.1106
- 0.0316
- 0.0174
- 0.0076

The MSE values also reduce as the n value increases.



The above shows the MSE versus n plot with sigma constant

ii. Varying sigma, n constant (n = 20)

```
1
       % Part c ii (varying sigma, n constant)
 2
 3
 4 -
      kernel = 3;
                                % based on w_true = [1,3,2]'
 5 -
     mse vector = zeros(4,1);
     w average matrix = zeros(kernel,4);
 7
 8
9 -
     n = 20;
10 -
     A = zeros(2*n+1, kernel);
11 -
     x_{interim} = -n:n;
12 -
     x = transpose(x_interim*0.1); % turning to vector
13
14
     % A generation
15
16 - ☐ for i = 1:kernel
      A(:,i) = x.^i;
    ^{\lfloor} end
18 -
19
     % t generation
21 -
     t = A(:,1) + 3*A(:,2) + 2*A(:,3);
22
23 -
      mp_i = pinv(A); % as A stays same, irrespective of sigma, for a given n, we
24
25 - w true = mp i*t; % calculating the true w directly from t
27 -
     count = 0;
29 - \Box for sigma = [0.1, 1, 3, 5]
30
31 -
         count = count + 1;
32
```

```
32
33 -
           w average interim = zeros(kernel,1);
34
           mse interim = 0;
35 -
36
37 -
     ψ.
          for j = 1:100
38
39
               % v generation
40 -
               v = sigma*randn(2*n+1,1);
41
               % y generation
42
43 -
               y = t + v;
44
               w_estimated = mp_i*y; % calculating the estimate of w
45 -
46
47 -
               w_average_interim = w_average_interim + w_estimated; % running sum
48
49 -
               mse interim = mse interim + (norm(w true - w estimated))^2; % runni
50
51
52 -
          end
53
          mse = mse interim/100;
54 -
55 -
           w_average = w_average_interim/100;
56
57 -
          mse vector(count,1) = mse;
58 -
           w average matrix(:,count) = w average;
59
60
61
62 -
      └ end
63
64 -
       sigma range = [0.1;1;3;5];
65 -
       disp("The matrix of true w, obtained same for all sigma (obviously) is")
66 -
       disp(w true)
67 -
       disp("The matrix of estimated w (averaged over 100 iterations, for each sig
68 -
       disp(w average matrix)
69 -
       disp("The averaged MSE over 100 iterations for each sigma, where rows repre
       disp(mse_vector)
70 -
71
72 -
       plot(sigma range, mse vector, '-o')
73 -
       xlabel('values of sigma, n = 20 (constant)')
74 -
       ylabel('MSE')
75
```

The code is pretty similar to c, Part i.

The matrix of true w, obtained same for all sigma (obviously) is,

- 1.0000
- 3.0000
- 2.0000

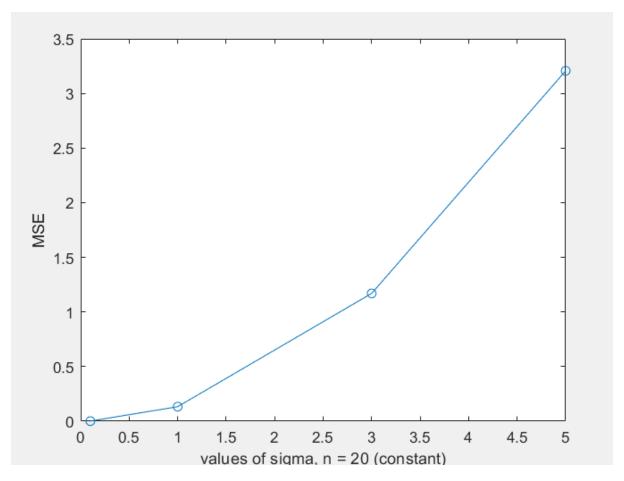
The matrix of estimated w (averaged over 100 iterations, for each sigma), where each column corresponds to a value of sigma and the column vector the vector of averaged w estimate, is,

0.9986	0.9978	1.1565	1.2948
3.0007	2.9989	2.9924	3.0163
2.0009	1.9951	1.9407	1.9570

The averaged MSE over 100 iterations for each sigma, where rows represent MSE value for each sigma, is,

- 0.0012
- 0.1332
- 1.1697
- 3.2069

The curve is,



As expected, as the variance of the added noise increases, the MSE increases and the estimate of **w** becomes more and more inaccurate.

Variance of $z*sigma = (sigma)^2$ Variance of $z = (sigma)^2$

Since z is standard normal, with zero mean and unit variance.

Thus, as the value of added distortion to **t** increases, error in **w**, increases.

$$y = t + v = t + z*sigma$$

Thus, by increasing sigma, we increase both the variance (how much the noise varies) as well as the overall value of the noise (the probability of larger values appearing in noise term increases as the value of sigma increases).

Thus, with increase in sigma, due to these reasons, MSE increases.

iii. For Model with x and x³ (underfit)

PART 1 – Varying n with sigma constant

```
1
       % c iii Part1
 3
       % NOTE :
       % We assume that the t observed is observed still from the true model with
 4
       % the added noise. Our model has changed, true model has not.
 7
       % Thus, A will be formed with respect to our new model, w corresponds to w
       % of our new model, y = t + v is generated with v generated as before and t
 8
 9
       % generated according to our true model, not the mismatched model. We
       % observe x and t and we are simulating using y, the observed t. Thus y
10
       % doesn't change despite the change in our model. Thus the rule to generate
11
       % t still stays the same.
12
13
       % w true will be obtained without the noise added and w estimate with the
14
       % noise added.
15
16
17
       % t according to our new mismatched model will be calculated after we
       % obtain w, using the new model. t true will then be the observed values of
18
       % t, or the values to which model is fit, i.e. true t value is the one
19
20
       % generated by the true model alongside the added error (or t which will be
       % used to obtain w)
21
       % NOTE : True t and obtained t won't be stored for each n (averaged
23
       % obviously over 100 trials) and stored, since it hasn't been asked, and we
24
       % don't want to increase unneccessary computation. Obviously doing so
       % wouldn't at all be difficult and would need around 1-2 more lines of
26
       % code. So it has been avoided here.
27
28
29
       % Part c iii Model1 Part1 (varying n, sigma constant) (Model is the one
       % which is underfit to the true model, i.e. the non-noisy version of
31
       % the true model)
32
```

```
32
33 -
      count = 0;
                        % for t generation, the true one
34 -
      kernel = 3;
35 -
     mse_vector = zeros(5,1);
36 -
      recon mse vector = zeros(5,1);
37 -
      kernel_mis = 2;
38 -
       w_average_matrix = zeros(kernel_mis,5);
39 -
       w true matrix = zeros(kernel mis,5);
40
41
42 - \Box for n = [10, 20, 30, 40, 50]
44 -
         count = count + 1;
45 -
         A = zeros(2*n+1, kernel);
46 -
         sigma = 1;
47 -
         x interim = -n:n;
48 -
         x = transpose(x_interim*0.1); % turning to vector
49
50
         % A generation, true A, A that gives true t
51
52 - for i = 1:kernel
53 -
           A(:,i) = x.^i;
54 -
         end
55
56
          % t generation
          t = A(:,1) + 3*A(:,2) + 2*A(:,3); % true t
57 -
58
         % A, for our model, generation
59
```

```
60
61 -
         A_mis = zeros(2*n+1,kernel_mis);
62
63 - 📥
         for i = 1:kernel_mis
          A_{mis}(:,i) = x.^{(2*i-1)}; % our kernel model
64 -
65 -
66
67
68 -
         w true = pinv(A mis)*t;
69 -
         w_true_matrix(:,count) = w_true;
70
71 -
         w_average_interim = zeros(kernel_mis,1);
72
73 -
        mse interim = 0;
74
75 -
         recon mse interim = 0;
76
77 - \Box for j = 1:100
78
79
            % v generation
80 -
            v = sigma*randn(2*n+1,1);
81
82
             % y generation
83 -
            y = t + v;
                                % observed y
84
            w_estimated = pinv(A_mis)*y; % calculating the estimate of w
85 -
86
87 -
            y_estimated = A_mis*w_estimated;
88
89 –
             w average interim = w average interim + w estimated; % running sum of w average
90
             mse interim = mse interim + (norm(w_true - w_estimated))^2; % running sum of mse
91 -
```

```
92
93 -
                recon mse interim = recon mse interim + (norm(y - y estimated))^2;
94
95 -
            end
96
            mse = mse interim/100;
97 -
98 -
            recon mse = recon mse interim/100;
            w average = w average interim/100;
99 -
100
101 -
           mse vector(count,1) = mse;
102 -
           recon mse vector(count,1) = recon mse;
103 -
           w average matrix(:,count) = w average;
104
105
106
       L end
107 -
108
109 -
       n range = [10;20;30;40;50];
        disp("The matrix of true w for our model, where each column corresponds to
110 -
111 -
      disp(w true matrix)
      disp("The matrix of estimated w for our model(averaged over 100 iterations,
112 -
113 -
       disp(w average matrix)
      disp("The averaged MSE of w over 100 iterations for each n, where rows rep:
114 -
115 -
      disp(mse vector)
116 -
       disp("The averaged MSE of reconfiguration over 100 iterations for each n, v
       disp(recon_mse vector)
117 -
118
119 -
      figure(1);
120 -
      plot(n range,mse vector,'o-')
121 - xlabel('values of n, sigma = 1 (constant)')
122 -
        ylabel('MSE for w')
123
123
124 -
       figure(2);
125 -
        plot(n range, recon mse vector, 'o-')
126 -
        xlabel('values of n, sigma = 1 (constant)')
127 -
        ylabel('MSE for reconfiguration')
```

```
>> c_iii_Model1_Part1
```

The matrix of true w for our model, where each column corresponds to a value of n and the column vector the vector of w, is,

```
1.0000 1.0000 1.0000 1.0000 1.0000
2.0000 2.0000 2.0000 2.0000 2.0000
```

The matrix of estimated w for our model (averaged over 100 iterations, for each n), where each column corresponds to a value of n and the column vector the vector of averaged w estimate, is,

0.9973	0.9585	1.0251	1.0157	0.9945
1.9959	2.0160	1.9950	1.9988	2.0002

The averaged MSE of w over 100 iterations for each n, where rows represent MSE of w value for each n, is,

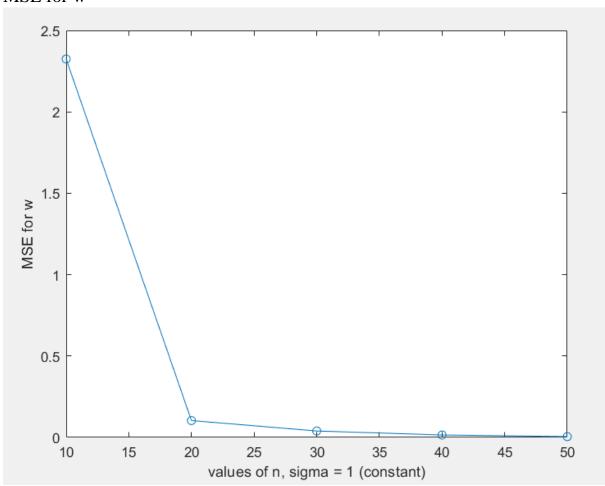
- 2.3247
- 0.1036
- 0.0395
- 0.0149
- 0.0052

The averaged MSE of reconfiguration over 100 iterations for each n, where rows represent MSE of reconfiguration value for each n, is,

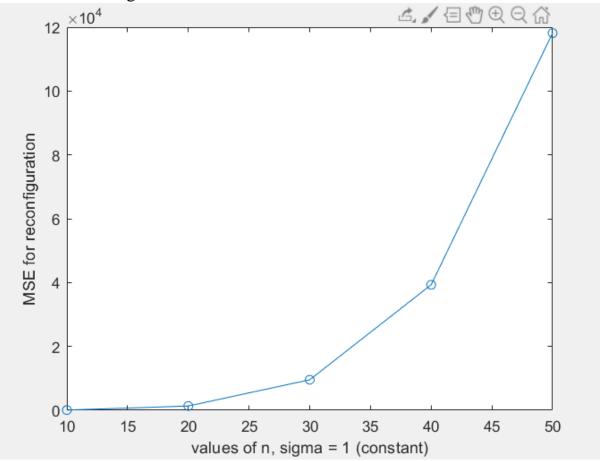
- 1.0e+05 *
- 0.0006
- 0.0134
- 0.0955
- 0.3931
- 1.1815

Plots

MSE for w



MSE for Reconfiguration



The MSE for reconfiguration is extremely large, since, the coefficients of x and x^3 are still close to 1 and 2 as before, but now, we have the x^2 factor missing due to which our estimated y deviates largely from our actual y in general.

PART 2 – Varying sigma with n constant, same model

```
% Part c_iii_Model1_Part2 (varying sigma, n constant) (Model is the one
 2
      % which is underfit to the true model, i.e. the non-noisy version of
 3
      % the true model, with x and x^3 only)
 4
 5
     % Everything same, but now only sigma varies
 6
 7
      count = 0;
8 -
9 -
      kernel = 3;
                                % for t generation, the true one
10 -
      mse_vector = zeros(4,1);
11 -
      recon mse vector = zeros(4,1);
12 -
      kernel mis = 2;
13 -
      w average matrix = zeros(kernel mis,4);
14
15
     n = 20;
16 -
17 -
     A = zeros(2*n+1, kernel);
18 -
     x interim = -n:n;
19 -
      x = transpose(x_interim*0.1); % turning to vector
20
     % A generation, true A, A that gives true t
21
23 - ☐ for i = 1:kernel
24 - A(:,i) = x.^i;
25 -
     L end
26
27
      % t generation
     t = A(:,1) + 3*A(:,2) + 2*A(:,3); % true t
29
      % A, for our model, generation
30
31
32 -
     A mis = zeros(2*n+1, kernel mis);
```

```
_ · · · - ·
33
34 - For i = 1:kernel_mis
35 -
     A_{mis}(:,i) = x.^(2*i-1); % our kernel model
36 - end
37
38 -
     pm_i = pinv(A_mis);
39 -
     w_true = pm_i*t;
40
41 - \Box for sigma = [0.1,1,3,5]
42
43 -
         count = count + 1;
44
45 -
         w average interim = zeros(kernel mis,1);
46
47 -
         mse_interim = 0;
48
49 -
         recon_mse_interim = 0;
50
52
53
            % v generation
54 -
            v = sigma*randn(2*n+1,1);
55
56
             % y generation
57 -
            y = t + v; % observed y
58
59 -
            w_estimated = pm_i*y; % calculating the estimate of w
60
61 -
            y_estimated = A_mis*w_estimated;
62
63 -
            w_average_interim = w_average_interim + w_estimated; % running sum of w_average
```

```
65 -
                mse interim = mse interim + (norm(w true - w estimated))^2; % runni
66
67 -
                recon mse interim = recon mse interim + (norm(y - y estimated))^2;
68
69 -
70
           mse = mse_interim/100;
71 -
72 -
           recon mse = recon mse interim/100;
73 -
           w average = w average interim/100;
74
75 -
           mse vector(count,1) = mse;
76 -
           recon mse vector(count,1) = recon mse;
77 -
            w average matrix(:,count) = w average;
78
79
80
81 -
       L end
82
83 -
       sigma range = [0.1;1;3;5];
84 -
       disp("The true w vector for our model, which is obviously constant for all
85 -
       disp(w_true)
       disp("The matrix of estimated w for our model(averaged over 100 iterations,
86 -
87 -
       disp(w average matrix)
       disp("The averaged MSE of w over 100 iterations for each sigma, where rows
88 -
89 -
       disp(mse vector)
       disp("The averaged MSE of reconfiguration over 100 iterations for each sigm
90 -
91 -
       disp(recon mse vector)
92
93 -
       figure(1);
94 -
       plot(sigma_range,mse_vector,'o-')
95 -
       xlabel('values of sigma, n = 20 (constant)')
96 -
       ylabel('MSE for w')
97
       figure(2);
98 -
99 -
       plot(sigma range, recon mse vector, 'o-')
       xlabel('values of sigma, n = 20 (constant)')
100 -
        ylabel('MSE for reconfiguration')
101 -
102
```

```
>> c_iii_Model1_Part2
```

The true w vector for our model, which is obviously constant for all sigma, since n is constant is

1.0000

2.0000

The matrix of estimated w for our model(averaged over 100 iterations, for each sigma), where each column corresponds to a value of sigma and the column vector the vector of averaged w estimate, is

```
0.9991 0.9937 0.8778 0.7348
2.0004 2.0037 2.0665 2.1051
```

The averaged MSE of w over 100 iterations for each sigma, where rows represent MSE of w value for each sigma, is

0.0010

0.1453

1.0021

2.7495

The averaged MSE of reconfiguration over 100 iterations for each sigma, where rows represent MSE of reconfiguration value for each sigma, is

1.0e+03 *

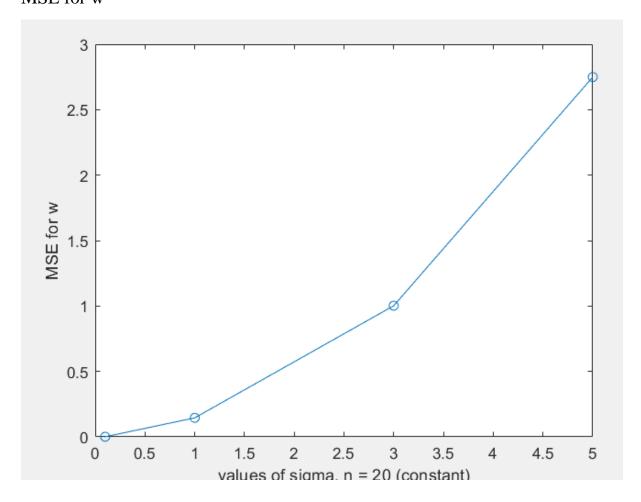
1.3007

1.3314

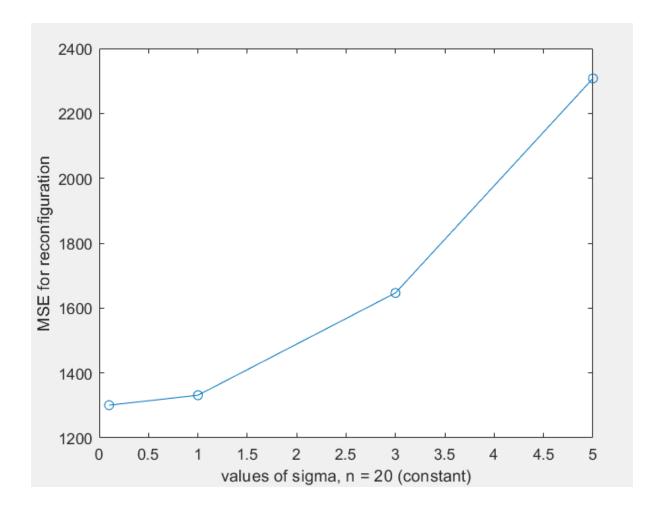
1.6466

2.3078

Plots MSE for w



MSE for Reconfiguration



As seen before, as sigma increases, both the MSE has a tendency to increase. The same previous explanation goes here as well.

iii. For Model with terms till and including x^4 (overfit) PART 1 – Varying n with sigma constant

```
1 % Part c iii Model2 Partl (varying n, sigma constant) (Model is the one
      % which is overfit to the true model)
 3
 4
      % Things same as before
 5
      count = 0;
 6 -
 7 -
      kernel = 3;
                                 % for t generation, the true one
 8 -
      mse vector = zeros(5,1);
9 -
      recon_mse_vector = zeros(5,1);
10 -
       kernel mis = 5;
                         % the overfit model
11 -
      w average matrix = zeros(kernel mis,5);
12 -
       w_true_matrix = zeros(kernel_mis,5);
13
15 - \bigcirc \text{ for } n = [10, 20, 30, 40, 50]
17 -
         count = count + 1;
18 -
          A = zeros(2*n+1, kernel);
19 -
          sigma = 1;
20 -
          x interim = -n:n;
          x = transpose(x_interim*0.1); % turning to vector
21 -
22
23
          % A generation, true A, A that gives true t
24
25 - for i = 1:kernel
26 -
             A(:,i) = x.^i;
27 -
          end
28
          % t generation
29
          t = A(:,1) + 3*A(:,2) + 2*A(:,3); % true t
30 -
31
32
          % A, for our model, generation
```

```
34 -
         A_mis = zeros(2*n+1,kernel_mis);
35
36 - for i = 1:kernel_mis
           A mis(:,i) = x.^(i-1); % our kernel model
37 -
38 -
          end
39
40
41 -
         w_true = pinv(A_mis)*t;
         w_true_matrix(:,count) = w_true;
42 -
43
44 -
         w average interim = zeros(kernel mis,1);
45
46 -
         mse interim = 0;
47
48 -
         recon_mse_interim = 0;
49
50 - \Box for j = 1:100
51
52
             % v generation
53 -
             v = sigma*randn(2*n+1,1);
54
             % y generation
56 -
             y = t + v;
                            % observed y
57
58 -
            w_estimated = pinv(A_mis)*y; % calculating the estimate of w
59
60 -
            y estimated = A mis*w estimated;
61
             w average interim = w average interim + w estimated; % running sum of w
62 -
63
64 -
            mse interim = mse interim + (norm(w true - w estimated))^2; % running su
```

```
65
66 -
                recon mse interim = recon mse interim + (norm(y - y estimated))^2
67
68 -
            end
69
70 -
            mse = mse_interim/100;
71 -
            recon mse = recon mse interim/100;
72 -
            w average = w average interim/100;
73
74 -
           mse vector(count,1) = mse;
75 -
            recon mse vector(count,1) = recon mse;
            w average matrix(:,count) = w average;
76 -
77
78
79
80 -
       ∟end
81
82 -
        n range = [10;20;30;40;50];
        disp("The matrix of true w for our model, where each column corresponds t
83 -
84 -
        disp(w true matrix)
        disp("The matrix of estimated w for our model (averaged over 100 iteration
85 -
86 -
        disp(w average matrix)
87 -
        disp("The averaged MSE of w over 100 iterations for each n, where rows re
        disp(mse_vector)
88 -
89 -
        disp("The averaged MSE of reconfiguration over 100 iterations for each n,
        disp(recon mse vector)
90 -
91
92 -
       figure(1);
93 -
        plot(n range, mse vector, 'o-')
94 -
        xlabel('values of n, sigma = 1 (constant)')
        ylabel('MSE for w')
95 -
96
91
92 -
        figure(1);
93 -
        plot(n_range,mse_vector,'o-')
        xlabel('values of n, sigma = 1 (constant)')
94 -
95 -
        ylabel('MSE for w')
96
97 -
       figure(2);
98 -
        plot(n range, recon mse vector, 'o-')
99 -
        xlabel('values of n, sigma = 1 (constant)')
100 -
        ylabel('MSE for reconfiguration')
101
102
103
```

```
>> c_iii_Model2_Part1
```

The matrix of true w for our model, where each column corresponds to a value of n and the column vector the vector of w, is

0.0000	0.0000	-0.0000	0.0000	-0.0000
1.0000	1.0000	1.0000	1.0000	1.0000
3.0000	3.0000	3.0000	3.0000	3.0000
2.0000	2.0000	2.0000	2.0000	2.0000
0.0000	0.0000	-0.0000	-0.0000	-0.0000

The matrix of estimated w for our model(averaged over 100 iterations, for each n), where each column corresponds to a value of n and the column vector the vector of averaged w estimate, is

-0.0809	-0.0246	-0.0109	-0.0084	0.0028
0.9675	1.0193	0.9783	1.0082	0.9960
3.3731	3.0623	3.0005	2.9953	2.9994
2.0593	1.9947	2.0051	1.9995	2.0006
-0.2965	-0.0184	-0.0003	0.0005	-0.0000

The averaged MSE of w over 100 iterations for each n, where rows represent MSE of w value for each n, is

14.9549

0.4332

0.1175

0.0672

0.0372

The averaged MSE of reconfiguration over 100 iterations for each n, where rows represent MSE of reconfiguration value for each n, is

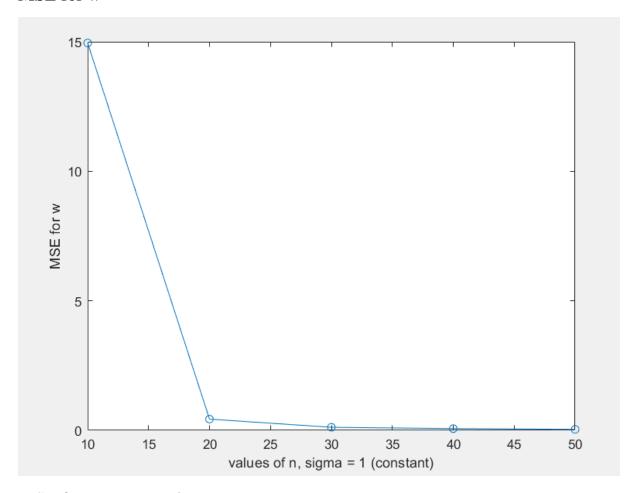
14.9236

35.6173

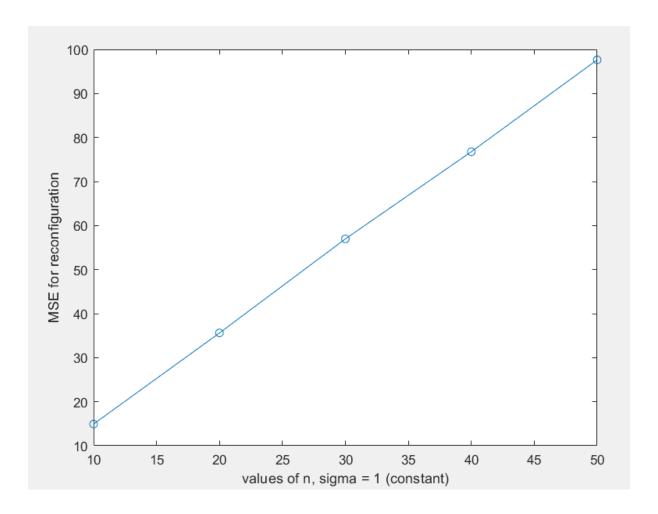
56.979076.771197.6454

Plots

MSE for w



MSE for Reconstruction



As can be seen the MSE for the overfit case is much less than that for the underfit case. Hence, it is obvious that if MSE of reconstruction is our main criteria than overfit model should be selected since it gives us an MSE which is extremely less in comparison to the underfit model.

PART 1 – Varying sigma with n constant

```
1
      % Part c iii Model2 Part2 (varying sigma, n constant) (Model is the one
      % which is overfit to the true model)
 2
 3
      % Everything same, but now only sigma varies
 4
 5
 7 -
      count = 0;
 8 -
      kernel = 3;
                               % for t generation, the true one
9 -
      mse vector = zeros(4,1);
10 -
      recon_mse_vector = zeros(4,1);
11 -
      kernel_mis = 5;
12 -
      w average matrix = zeros(kernel mis,4);
13
14
15 -
     n = 20;
16 -
     A = zeros(2*n+1, kernel);
17 -
      x_{interim} = -n:n;
18 -
      x = transpose(x_interim*0.1); % turning to vector
19
20
      % A generation, true A, A that gives true t
21
22 - For i = 1:kernel
      A(:,i) = x.^i;
23 -
     end
24 -
25
      % t generation
27 -
      t = A(:,1) + 3*A(:,2) + 2*A(:,3); % true t
28
29
      % A, for our model, generation
30
     A mis = zeros(2*n+1, kernel mis);
31 -
32
```

```
33 - ☐ for i = 1:kernel mis
34 - A_{mis}(:,i) = x.^(i-1); % our kernel model
35 - end
36
37 -
     pm_i = pinv(A_mis);
38 - w_true = pm_i*t;
39
40 - \Box for sigma = [0.1,1,3,5]
41
42 -
        count = count + 1;
43
44 -
         w average interim = zeros(kernel mis,1);
45
        mse interim = 0;
46 -
47
48 -
        recon mse interim = 0;
49
50 -   for j = 1:100
51
             % v generation
52
53 -
             v = sigma*randn(2*n+1,1);
54
55
             % y generation
56 -
             y = t + v; % observed y
57
58 -
            w_estimated = pm_i*y; % calculating the estimate of w
59
60 -
           y_estimated = A_mis*w_estimated;
61
62 -
           w average interim = w average interim + w estimated; % running sum
63
64 -
             mse interim = mse interim + (norm(w true - w estimated))^2; % runni
```

```
65
              66 -
              recon mse interim = recon mse interim + (norm(y - y estimated))^2;
67
68 -
          end
69
70 -
          mse = mse interim/100;
71 -
          recon mse = recon mse interim/100;
72 -
          w average = w average interim/100;
73
74 -
          mse vector(count,1) = mse;
75 -
          recon mse vector(count,1) = recon mse;
          w average matrix(:,count) = w average;
76 -
77
78
79
80 -
      ∟end
81
82 -
      sigma_range = [0.1;1;3;5];
       disp("The true w vector for our model, which is obviously constant for all
83 -
84 -
     disp(w true)
85 -
     disp("The matrix of estimated w for our model(averaged over 100 iterations,
86 -
      disp(w average matrix)
87 -
      disp("The averaged MSE of w over 100 iterations for each sigma, where rows
88 -
      disp(mse vector)
89 -
      disp("The averaged MSE of reconfiguration over 100 iterations for each sign
90 -
      disp(recon mse vector)
91
92 -
      figure(1);
93 - plot(sigma_range, mse_vector, 'o-')
94 - xlabel('values of sigma, n = 20 (constant)')
      ylabel('MSE for w')
95 -
96
97 -
       figure(2);
98 -
      plot(sigma range, recon mse vector, 'o-')
      xlabel('values of sigma, n = 20 (constant)')
100 -
       ylabel('MSE for reconfiguration')
101
```

```
>> c_iii_Model2_Part2
```

The true w vector for our model, which is obviously constant for all sigma, since n is constant is

0.0000 1.0000

3.0000

2.0000

The matrix of estimated w for our model(averaged over 100 iterations, for each sigma), where each column corresponds to a value of sigma and the column vector the vector of averaged w estimate, is

-0.0032	-0.0155	0.1085	-0.0525
1.0011	1.0133	0.8659	1.0348
3.0037	3.0665	2.9011	3.0538
2.0001	2.0015	2.0399	1.9652
-0.0007	-0.0222	0.0186	-0.0108

The averaged MSE of w over 100 iterations for each sigma, where rows represent MSE of w value for each sigma, is

0.0043

0.3726

3.6304

10.5548

The averaged MSE of reconfiguration over 100 iterations for each sigma, where rows represent MSE of reconfiguration value for each sigma, is

0.3584

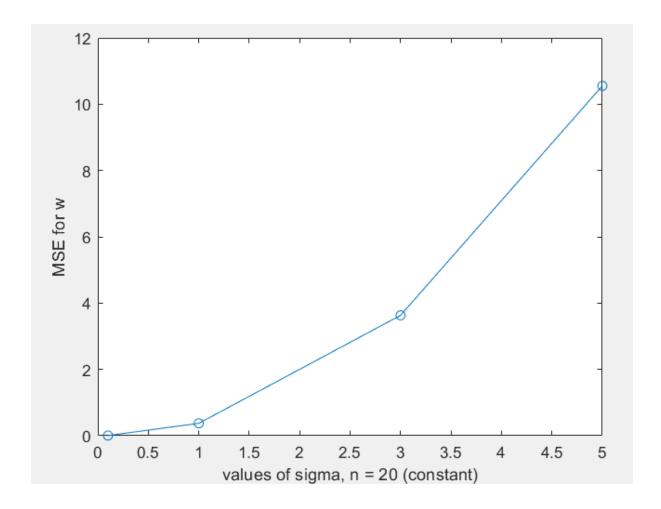
37.0618

318.1502

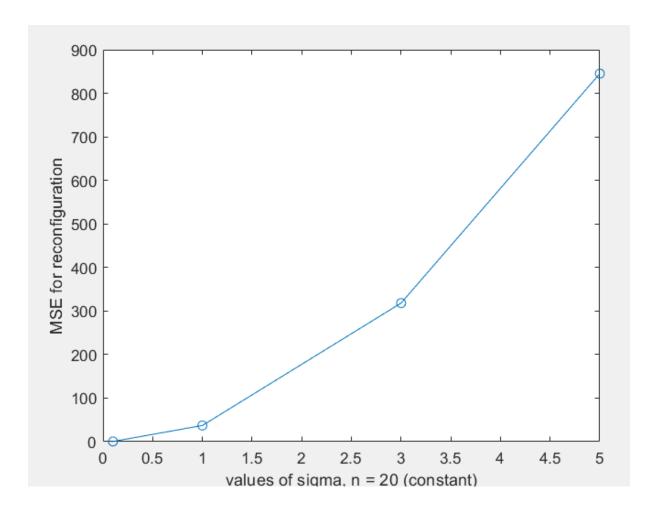
845.2264

Plots

MSE for w



MSE for Reconstruction



Similar results with similar explanation

iv. Comment on Results

It is definitely worse, MSE wise, to underestimate/underfit the model. Thus, the underestimated/underfit model had an excruciatingly worse MSE compared to the overfit/overestimated version which had a comparatively much better MSE.

However, with overfitting we do have an issue where the model is so overfit, that we can't have good model generalization to the test data, increasing the test MSE. This fact is also known as the bias-variance trade-off in machine learning algorithms.

Underfit model, have, higher training MSE but generalize better and may have low test MSE, sometimes even lower than the Overfit model.			
END			