

Practical - 1Aim - Basic of R Software

- 1) R is a software for statistical analysis and data
- 2) It is effective data handling software and outcome storage.
- 3) Capable of graphical display.
- 4) It is free.

1) $4+6+8 \div 2-5$

$> 4+6+8 \div 2-5$

[1] 9

2) $2^2+1-3+\sqrt{5}$

$> 2^2 + \text{abs}(-3) + \text{sqrt}(45)$

[1] 13.7082

3) $5^3+7 \times 5 \times 8+46/5$

$> 5^3+7 * 5 * 8+46/5$

[1] 414.2

$$4) \sqrt{4^2 + 5 \times 3 + 7/6}$$

$$> \text{sqrt}(4^4 + 5 * 3 + 7/6)$$

$$[] \quad 5.671567$$

$$2) \quad 1) \quad (2, 3, 5, 7) * 2$$

$$[] \quad 4, 6, 10, 14$$

$$2) \quad c(2, 3, 5, 7) * c(2, 3)$$

$$[] \quad 4 \ 9 \ 10 \ 21$$

$$3) \quad c(4, 6, 8, 9, 4, 5) ^ c(1, 2, 3)$$

$$[] \quad 4, 36 \quad 512 \quad 9162 \quad 125.$$

$$4) \quad c(6, 2, 7, 5) / c(4, 5)$$

$$[] \quad 1.50 \quad 0.40 \quad 1.75 \quad 1.00$$

$$5) x = 20 > y = 30 > z = 2$$

$$x^2 + y^3 + z$$

02

$$[1] 27402$$

$$> \text{sort}(x^2 + y^3 + z)$$

$$[1] 20.73644$$

$$> x^2 + y^2$$

$$[1] 1300$$

$$4) \text{ xL-matrix } (nrow = 4, ncol = 2)$$

$$\text{data} = c(1, 2, 3, 4, 5, 6, 7, 8)$$

$$> x \quad [1,] \quad [1,2]$$

$$[1,] \quad 1 \quad 5$$

$$[2,] \quad 2 \quad 6$$

$$[3,] \quad 3 \quad 7$$

$$[4,] \quad 4 \quad 8$$

$$5) \text{ yL-matrix } (nrow = 3, ncol = 3, \text{data} = c(10, 12, 15, -5, -4, -6))$$

$$\text{yL} \quad [1,] \quad [1,2] \quad [1,3]$$

$$[1,] \quad 10 \quad -7 \quad 13$$

$$[2,] \quad 12 \quad -4 \quad 16$$

$$[3,] \quad 15 \quad -11 \quad 8$$

c) Ranks of statistics of CS Batch B

$x = c(58, 20, 35, 24, 46, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 3$
 $29, 35, 39)$

$x = c(\text{data})$

$\text{meth} = \text{seq}(20, 60, 5)$

$a = \text{cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

$b = \text{table}(a)$

$c = \text{transform}(b)$

c

q	freq
[20,25]	3
[25,30]	2
[30,35]	1
[35,40]	4
[40,45]	1
[45,50]	3
[50,55]	2
[55,60]	4



Practical 2

→ Probability Distribution

1) Check is following pmf or not

x	$P(x)$
0	0.1
1	0.2
2	0.3
3	0.4
4	0.3
5	0.5

If given data is pmf then $\sum P(x) = 1$

$$\therefore 0.1 + 0.2 + 0.3 + 0.4 + 0.3 + 0.5 \\ = 1.8$$

$\therefore P(x) = 0.5$ & cannot be probability mass function

2)

x	$P(x)$
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

$$P(x) \geq 0$$

$$P(x) = 1$$

$$= 0.2 + 0.2 + 0.35 + 0.15 + 0.1$$

$$= 1$$

\therefore It is pmf

code

$$\text{Prob} = c(0.2, 0.2, 0.3, 0.15, 0.1)$$

$$\text{sum}(\text{Prob})$$

$$1$$

2) Find cdf for following pmf and sketch graph.

$$x \quad 10 \quad 20 \quad 30 \quad 40 \quad 50$$

$$P(x) \quad 0.2 \quad 0.2 \quad 0.35 \quad 0.15 \quad 0.1$$

$$F(x) = 0$$

$$x < 10$$

$$0.2$$

$$10 \leq x < 20$$

$$0.4$$

$$20 \leq x < 30$$

$$0.75$$

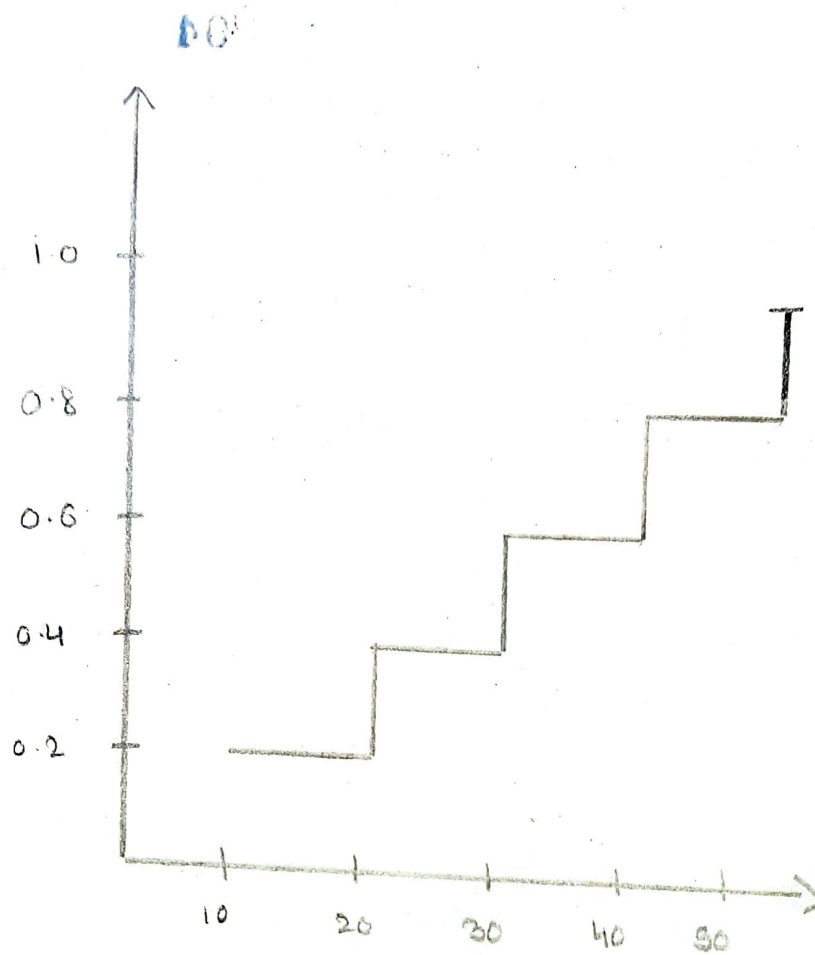
$$30 \leq x < 40$$

$$0.90$$

$$40 \leq x < 50$$

$$1.0$$

$$x \geq 50$$



$x = c(10, 20, 30, 40, 50)$

$plot = C(x, cumsum(Cprob, "S"))$

Q2 Find

x	1	2	3	4	5	6
$P(x)$	0.15	0.25	0.1	0.2	0.2	0.1

$F(x) = 0$	$x < 1$
0.15	$1 \leq x < 3$
0.40	$3 \leq x < 4$
0.50	$4 \leq x < 5$
0.70	$5 \leq x < 6$
0.90	$x \geq 6$
1.00	

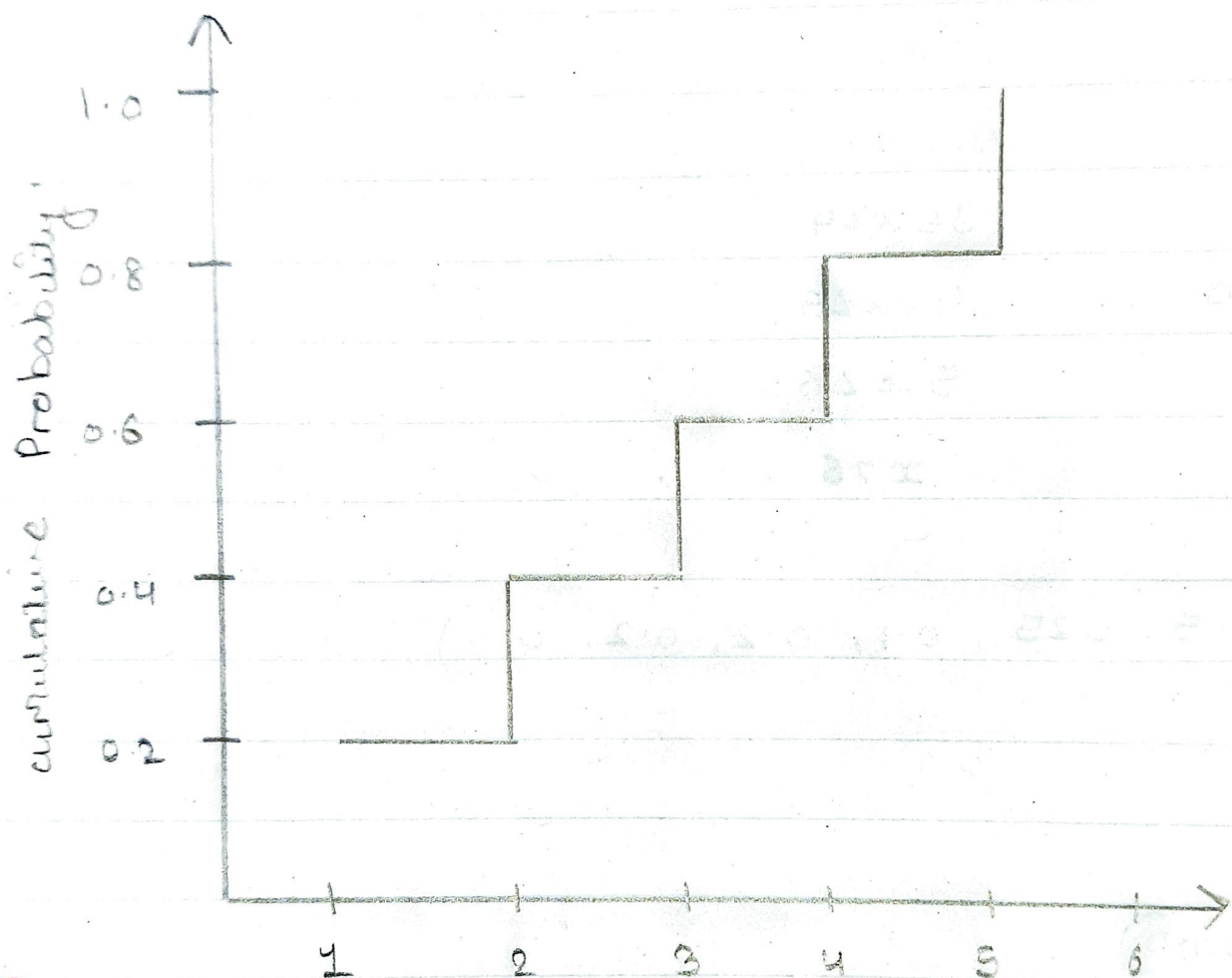
$\text{Prob} = c(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$
 $\text{sum}(\text{cprob})$
 $[1] 1$

$\text{cumsum}(\text{cprob})$

$[1] 0.15, 0.40, 0.50, 0.70, 0.90, 1.00$

$x = c(1, 2, 3, 4, 5, 6)$

$\text{plot}(x, \text{cumsum}(\text{cprob}), "s", \text{xlab} = "value", \text{ylab} = "cumulative probability", \text{main} = "CDF graph", \text{col} = "brown")$



values

→ Binomial Distribution

$$\# P(X=x) = \text{dbinom}(x, n, p)$$

$$\# P(X \leq x) = \text{pnbinom}(x, n, p)$$

If x is unknown

$$P1 = P(X \leq x) = \text{qbinom}(p, n, p)$$

1) Find probability of exactly 10 success in 100 trials with $p=0.1$

2) Suppose there are 12 req. each question has 5 option out of which 1 is correct

Find probability of having exactly 4 correct answer.

3) Find complete distribution when $n=5$ and $p=0.1$

—X—

ans)

$$1) > x = \text{dbinom}(10, 100, 0.1)$$

> x

$$[1] 0.1318693$$

$$2) \text{dbinom}(4, 12, 0.2)$$

$$0.1328736$$

$$\text{pnbinom}(4, 12, 0.2)$$

$$0.4274445$$

$$1 - \text{pnbinom}(9, 12, 0.2)$$

$$0.01940528$$

3) $\text{dbinom}(0:5, 5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.0810

4 - 0.00045

5 - 0.00001

4) $\text{dbinom}(5, 12, 0.25)$

0.1032414

$\text{pbinom}(5, 12, 0.25)$

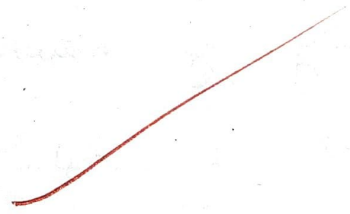
0.9465978

$1 - \text{pbinom}(7, 12, 0.25)$

0.00278191

$\text{dbinom}(6, 12, 0.25)$

0.04014945



5) X follows binomial distribution with $n=10$, $p=0.3$, plot the graph of pmf and cdf.

4) $n = 10$

$p = 0.3$

$x = 0:n$

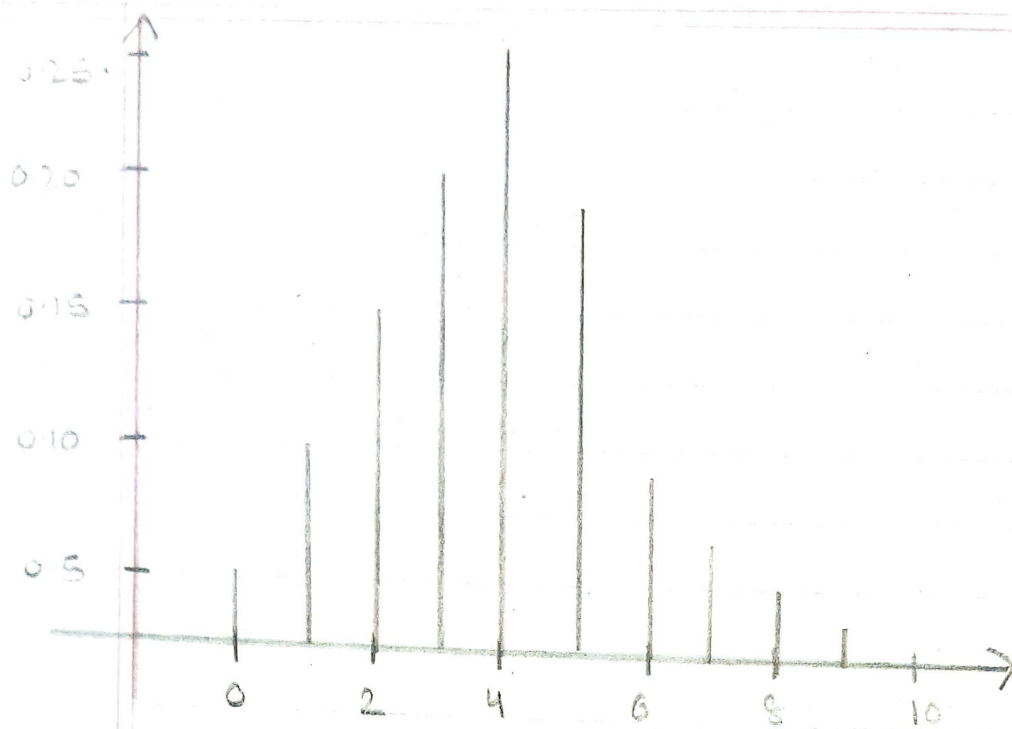
$prob = dbinom(x, n, p)$

$curprob = pbinom(x, n, p)$

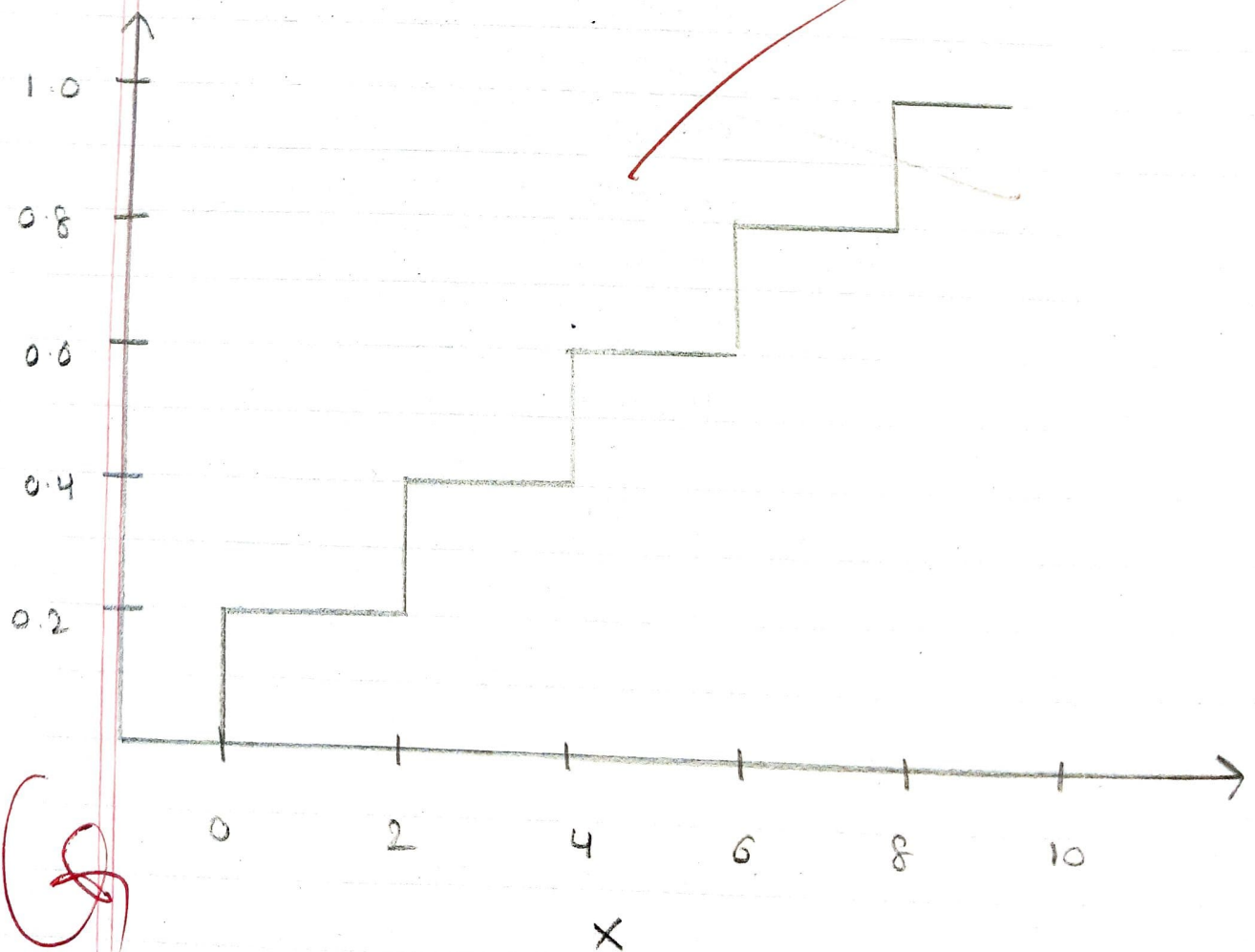
$d = \text{data.frame}("x\text{ values}" = x, "probability" = prob)$

$\text{print}(d)$

	x values	probability
1		
2	0	0.0282
3	1	0.1210
4	2	0.2234
5	3	0.2668
6	4	0.2001
7	5	0.1029
8	6	0.0367
9	7	0.0090
10	8	0.0014
11	9	0.0001
	10	0.0000



plot (x, cumprob, "S")



Normal Distribution

$$1) P(X=x) = \text{dlnorm}(x, \mu, \sigma)$$

$$P(X \leq x) = \text{pnorm}(x, \mu, \sigma)$$

$$P(X > x) = 1 - \text{pnorm}(x, \mu, \sigma)$$

To generate random no. from a normal distribution (n random)
the R code is `rnorm(n, \mu, \sigma)`

1) A random var x follows nor. distribution with mean = $\mu = 12$
and $SD = \sigma = 3$.

Find ① $P(X \leq 15)$

$$P(10 \leq x \leq 13)$$

$$P(X > 14)$$

Code

$$p1 = \text{pnorm}(15, 12, 3)$$

$p1$

$$[1] 0.8413447$$

$$\text{cat}("P(X \leq 15) = ", p1)$$

$$P(X \leq 15) = 0.8413447$$

$$p2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$$

$p2$

$$[1] 0.3780661$$

$$\text{cat } (p(\text{C10} < x_L = 13) = ", p_2)$$

$$p_3 = 1 - \text{pnorm}(14, 12, 3)$$

p_3

$$[1] 0.252495$$

$$\text{cat } (p(\text{C} > 14) = ", p_3)$$

$$p(\text{C} > 14) = 0.2524925$$

$$p_4 = \text{pnorm}(5, 12, 3)$$

p_4

$$[1] 15.254723$$

$$16.548505$$

$$11.280515$$

$$6.419944$$

$$12.272460$$

$$2) x \sim N(30, 100), \sigma = 10$$

$$1) P(\text{C} \leq 40)$$

$$P(\text{C} > 35)$$

$$P(25 < \text{C} < 35)$$

$$\text{Find } R \text{ such that } P(\text{C} < R) = 0.6$$

$$F = \text{pnorm}(0.6, 30, 10)$$

F

$$0.8413447$$

$$F1 = 1 - \text{pnorm}(35, 30, 10)$$

F1

$$0.3085375$$

$$F2 = \text{pnorm}(35, 30, 10) - \text{pnorm}(0.6, 30, 10)$$

F2

$$0.3829249$$

$F3 = \text{dnorm}(0.6, 30, 10)$

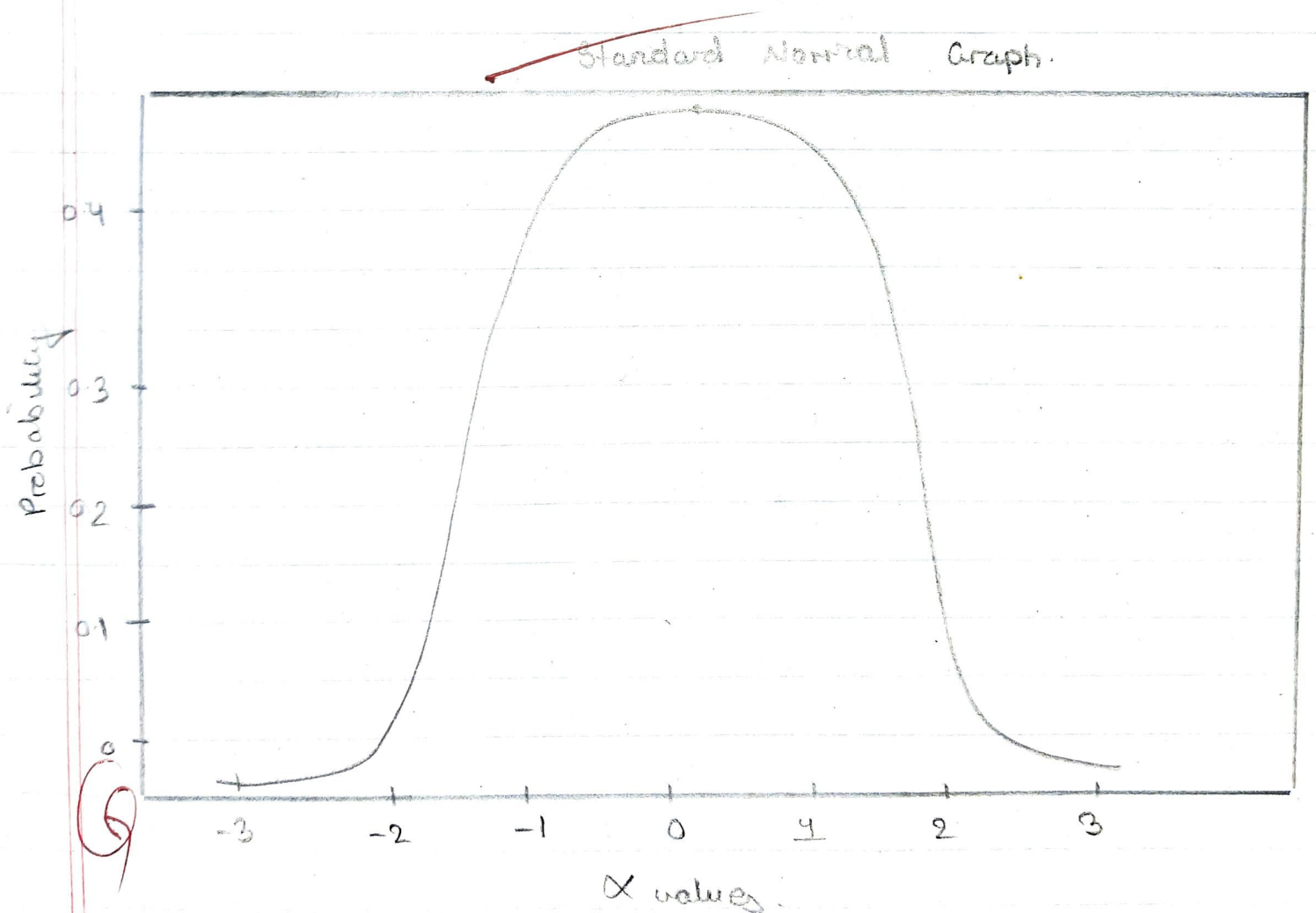
F3

32.53347

5) Plot standard deviation normal graph

$x = \text{seq}(-3, 3, \text{by} = 0.1)$
 $y = \text{dnorm}(x)$

$\text{plot}(x, y, \text{xlab} = "x \text{ values}", \text{ylab} = "probability", \text{main} = "standard normal graph")$



Normal and t-test

$$H_0: \mu = 15 \quad H_1: \mu \neq 15$$

Test the hypothesis

Random sample of size 400 is drawn and it is calculated.

The sample mean is 14.

SD is 3.

Test hypothesis at 5% level of significance

code:

$$\mu_0 = 15$$

$$\mu_x = 14$$

$$n = 400$$

$$sd = 3$$

$$z_{cal} = (\mu_x - \mu_0) / (sd / \sqrt{n})$$

$$z_{cal}$$

$$-6.66667$$

cat ("calculate value of z is =", zcal)

calculated value of z is = -6.66667

$$pvalue = 2 * (1 - pnorm(abs(zcal)))$$

$$pvalue$$

$$2.616716e-11$$

value < 0.05 we will ~~get~~ reject value of $H_0: \mu = 15$.

② $H_0: \mu = 12.5$ from following sample at 5% level of significance.

$x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$

$n = \text{length}(x)$

n

10

$\bar{x} = \text{mean}(x)$

\bar{x}

12.07

$\text{var} = (n-1) * \text{var}(x) / n$

0.019521

$sd = \text{sqrt}(\text{var})$

sd

0.1397176

$\mu_0 = 12.5$

$t = (\bar{x} - \mu_0) / (sd / \text{sqrt}(n))$

t

-8.894909

$p\text{value} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$

$p\text{value}$

0

\therefore The value is less than 0.05 the value is accepted.

- ③ Test hypothesis $\mu_0 = \mu = 10$ against $H_1: \mu \neq 10$. A random sample size of 400 is drawn with sample mean $= 10.2$ and $sd = 2.25$.

$$\mu_0 = 10$$

$$n = 400$$

$$\bar{x} = 10.2$$

$$sd = 2.25$$

$$z_{cal} = (\bar{x} - \mu_0) / (sd / \sqrt{n})$$

$$z_{cal}$$

$$1.77778$$

$$p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$$

$$p\text{-value}$$

$$0.07544036$$

Value is greater than 0.05

It is accepted.

