

Large Sample Test

① Let population mean Carrawit spent per customer in a restaurant is 250.

A sample of 100 customer selected. A sample mean is calculated as 275 and sd 30.

Test hypothesis that population mean 250 or not at 5% level of significance

② A random sample test 1000 students it is found that 750 use pen test.

The hypothesis that population proportion is 0.08 at 1% level of significance.

$$\mu_0 = 250$$

$$\bar{x} = 275$$

$$sd = 30$$

$$n = 100$$

$$z_{cal} = (\bar{x} - \mu_0) / (sd / \sqrt{n})$$

$$z_{cal} = (\text{"value of } z \text{ is"} = \text{"}, z_{cal})$$

$$8.333333$$

$$p\text{-value} = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$$

$$p\text{-value}$$

$$0$$

value is less than 0.05 we will reject

The value of $H_0 = \mu = 250$.

③ $p = 0.6$

$\alpha = 1 - p$

$P = 750 / 1000$

$n = 1000$

$z_{cal} = (p - \bar{p}) / \sqrt{\bar{p} * \alpha / n}$

calc value of z is : z_{cal}

value of z is -3.952847

$pvalue = 2 * C1 - pnorm (abs (z_{cal}))$

pvalue

$7.72268 e^{-05}$

③ Random sample of size 1000 and 2000 are drawn from 2 population with some 502.5 the 5 sample means are 67.5 and 68

Test hypothesis $\mu_1 = \mu_2$ at 5% level of significance.

④ A study was in 2 Hospital is given below test claim 2 hospital have same level of noise at 1% level of significance

Hos A

84

61.2

7.9

Hos B

34

59.4

7.5

③ $n_1 = 1000$

$n_2 = 2000$

$\bar{x}_1 = 67.5$

$s_1 = 2.5$

$s_2 = 2.5$

$$z_{cal} = (\bar{x}_1 - \bar{x}_2) / \sqrt{s_1^2/n_1 + s_2^2/n_2}$$

z_{cal}

-5.163975

$pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$

$pvalue$

$2.41754e-07$ (Rejected)

④ $n_1 = 84$

$n_2 = 34$

$\bar{x}_1 = 61.2$

$\bar{x}_2 = 59.4$

$s_1 = 7.9$

$s_2 = 7.5$

$$z_{cal} = (\bar{x}_1 - \bar{x}_2) / \sqrt{s_1^2/n_1 + s_2^2/n_2}$$

z_{cal}

1.62528

$pvalue = 2 * (1 - \text{pnorm}(\text{abs}(z_{cal})))$

$pvalue$

0.250211

$H_0: P_1 = P_2$ against $H_1: P_1 \neq P_2$

$$n_1 = 600$$

$$n_2 = 900$$

$$P_1 = 400/600$$

$$P_2 = 450/900$$

$$p = \frac{(n_1 \times P_1 + n_2 \times P_2)}{(n_1 + n_2)}$$

p

$$0.566667$$

$$q = 1 - p$$

q

$$0.4333333$$

$$z_{cal} = \frac{(P_1 - P_2)}{\sqrt{p \times q \times \left(\frac{1}{n_1} + \frac{1}{n_2} \right)}}$$

z_{cal}

$$6.381534$$

$$pvalue = 2 \times (1 - \text{norm}(\text{abs}(z_{cal})))$$

$pvalue$

$$1.73322e-10$$

\therefore value is less than 0.01 the value is rejected.

Small Sample Test.

- ① The marks are 10 stud are given by 63, 67, 66, 68, 69, 70, 70, 71, 72. Test hypothesis that sample comes from population with avg marks 66.

$$H_0: \mu = 66$$

$$n = 10 \quad (63, 66, 67, 68, 70, 70, 71, 72)$$

t-test (2)

One Sample Test

data : α

$$t = 68.319, \quad df = 9, \quad pvalue = 1.588 e^{-13}$$

alternative hypothesis mean is not equal to 10.95%

confidence interval 65.65171 70.14829

sample estimates

mean of α

Sample test

$$67.9$$

Since pvalue is smaller we reject the significance of at 5% level of significance

$$\alpha = 0.05$$

if $pvalue > 0.05$ then cat ("accept H_0 ") else cat ("reject H_0 ")

③ 2 groups of stud scored following marks.

Test hypothesis no. of significance btw 2 group.

Grp1 = (18, 27, 21, 17, 20, 17, 23, 20, 22, 21)

Grp2 = (16, 20, 14, 21, 20, 18, 13, 15, 17, 21)

t-test (α)

Two sample

data : x y

t = 2.2573 df = 16.376 pvalue = 0.03748

alternative hypothesis true diff in means is not equal to 0

95% confidence interval

0.1628205 5.0371795

sample estimates :-

mean of x mean of y

20.1

17.5

rejected

- ③ The sale data of 6 shops before and after are special campaign given below

before : 53, 28, 31, 48, 50, 42

after : 58, 29, 30, 55, 56, 45

Test hypothesis that campaign is effective.

⇒ H_0 : There is no sig diff of sales before and after campaign

$x = c(53, 28, 31, 48, 50, 42)$

$y = c(58, 29, 30, 55, 56, 45)$

t-test Cx, y , paired = T, alternative = "greater")

paired t-test

data = x and y

$t = -2.7815$, $df = 5$, $pvalue = 0.9806$

alternative hypo : true diff in means is greater than 0.95 percent confidence interval

-6.035547

INR

Sample estimates :

mean of diff -3.5

Accepted.

medical shops . 2 groups of patient

10, 12, 13, 11, 14

8, 9, 12, 14, 15, 10, 19.

If there is sig diff btw 2 medicines

H_0 : there is no sig diff

$x = c(10, 12, 13, 11, 14)$

$x = y(8, 9, 12, 14, 15, 10, 19)$

Sample t-test

$t = 0.80384$

$df = 9.7994$

$pvalue = 0.440$

95 percent confidence interval

-1.781171

mean of x

12

~~3~~

3.781171

~~y~~
11

Accept 5% level of significance

① $\mu : \mu = 55$

$H_1 : \mu \neq 55$

$n = 100$

$\mu_{0c} = 52$

$\mu_0 = 55$

$sd = 7$

$z_{cal} = (\mu_{0c} - \mu_0) / (sd / \sqrt{n})$

z_{cal}

$[1] = -4.285714$

$pvalue = 2 * (1 - pnorm (abs(z_{cal})))$

$pvalue$

$[1] 1.82153 e-05$

we reject

② $p = 350/700$

$H_0 : p = 1/2$

$n = 700$

$p = 0.5$

$q = 1 - p$

$z = (p - p) / (\sqrt{p * q * n})$

z

$[1] 0$

$pv = 2 * (1 - pnorm (abs(z)))$

$[1] = 1$

Accept pvalue at $H_0 : p = 1/2$

$$③ \quad n_1 = 1000$$

$$n_2 = 1500$$

$$p_1 = 0.02$$

$$p_2 = 0.01$$

$$P = (n_1 * p_1 + n_2 * p_2) / (n_1 + n_2)$$

P

$$[1] \quad 0.04$$

$$q = 1 - P$$

$$Z = (p_1 - p_2) / \sqrt{P * q * (1/n_1 + 1/n_2)}$$

Z

$$[1] \quad 0.003474737$$

$$p_v = 2 * (1 - pnorm (abs(Z)))$$

p_v

$$[1] \quad 0.03708364$$

we reject.

$$④ \quad H_0: \mu = 100$$

$$m_x = 99$$

$$sd = 8$$

$$m_0 = 100$$

$$n = 44$$

$$Z = (m_x - m_0) / (sd / (\sqrt{n}))$$

Z

$$[1] \quad -2.5$$

$$p_v = 2 * (1 - pnorm (abs(Z)))$$

$$[1] \quad 0.01241933$$

⑤ H_0 :

$$x = c(63, 63, 68, 69, 71, 71, 72)$$

$$t \sim t(\text{length}(x))$$

one sample T. Test

$$t = 47.94$$

$$df = 6$$

$$p\text{-value} = 5.522e^{-09}$$

alternative

$$69.66479$$

$$71.62092$$

mean of x

$$68.14286$$

we reject H_0 .

⑥ H_0

$$n = 100$$

$$\mu_0 = 1200$$

$$\mu_x = 1150$$

$$z = (\bar{x} - \mu_0) / (sd / \sqrt{n})$$

$$z$$

$$[1] 4$$

$$p\text{-value} = 2 * (1 - pnorm(abs(z)))$$

$$[1] 6.334248e^{-05}$$

we reject.

71

$$\textcircled{a} \quad n_1 = 200$$

$$n_2 = 300$$

$$p_1$$

$$p_2$$

$$p = \frac{(n_1 \cdot p_1 + n_2 \cdot p_2)}{(n_1 + n_2)}$$

$$q = 1 - p$$

$$[z] = 0.9128709$$

$$p_v = [2 \cdot z \cdot (1 - p) \cdot \text{norm}(\text{abs}(z))]$$

$$p_v [z] = 0.3613104$$

we accept.

(S)

