

Practical - 4

Aim - Basic of R Software

- 1) R is a software for statistical analysis and data
- 2) It is effective data handling software and outcome storage.
- 3) Capable of graphical display.
- 4) It is free.

1) $4+6+8 \div 2-5$

$> 4+6+8 \div 2-5$

[I] 9

2) $2^2 + 1 - 3 + \sqrt{5}$

$> 2^2 + \text{abs}(-3) + \text{sqrt}(45)$

[I] 13.7082

3) $5^3 + 7 \times 5 \times 8 + 46 / 5$

$> 5^3 + 7 * 5 * 8 + 46 / 5$

[I] 414.2

4) $\sqrt{4^2 + 5 \times 3 + 7/6}$

$\rightarrow \text{sqrt } (4^4 + 5 \times 3 + 7/6)$

[5] 5.671567

2) 1) $(2, 3, 5, 7)^{*2}$

[1] 4, 6, 10, 14

2) $c((2, 3, 5, 7)^{*c(2, 3)})$

[2] 49 10 21

3) $c((4, 6, 8, 9, 4, 5)^{c(1, 2, 3)})$

[1] 4, 36 512 9162 125.

4) $c((6, 2, 7, 5) | c(4, 5))$

[1] 1.50 0.40 1.75 1.00

$$③ x = 20 \Rightarrow y = 30 \Rightarrow z = 2$$

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$$x^2 + y^3 + z$$

$$\text{[1]} 27402$$

$$\rightarrow \sqrt{x^2 + y^2}$$

$$\text{[1]} 20.73644$$

$$\rightarrow x^2 + y^2$$

$$\text{[1]} 1300$$

④ $x \leftarrow \text{matrix} \left(\text{nrow} = 4, \text{ncol} = 2 \right)$

$\text{data} = c(1, 2, 3, 4, 5, 6, 7, 8)$

$\rightarrow x \quad [1,] \quad [1,2]$

$[1,] \quad 1 \quad 5$

$[2,] \quad 2 \quad 6$

$[3,] \quad 3 \quad 7$

$[4,] \quad 4 \quad 8$

⑤ $y \leftarrow \text{matrix} \left(\text{nrow} = 3, \text{ncol} = 3, \text{data} = c(10, 12, 15, -5, -4, -6) \right)$

$\rightarrow y \leftarrow [1,] \quad [1,2] \quad [1,3]$

$[1,] \quad 10 \quad -7 \quad 13$

$[2,] \quad 12 \quad -4 \quad 16$

$[3,] \quad 15 \quad -11 \quad 8$

SO

Q) Marks of students of CG Batch B

$x = c(58, 20, 35, 24, 46, 46, 56, 55, 45, 27, 22, 47, 58, 54, 40, 50, 39, 35, 39)$

$\rightarrow x = c(\text{data})$

$\text{meth} = \text{seq}(20, 60, 5)$

$a = \text{cut}(x, \text{breaks}, \text{right} = \text{FALSE})$

$b = \text{table}(a)$

$c = \text{transform}(b)$

Q

q	freq
[20, 25]	3
[25, 30]	2
[30, 35]	1
[35, 40)	4
[40, 45)	1
[45, 50]	3
[50, 55]	2
[55, 60)	4

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Practical 2

→ Probability Distribution

1) Check is following prf or not

x	$P(x)$
0	0.1
1	0.2
2	0.3
3	0.4
4	0.3
5	0.5

If given data is prf then $\sum P(x) = 1$

$$\begin{aligned} \therefore 0.1 + 0.2 - 0.5 + 0.4 + 0.3 + 0.5 \\ = 1.0 \end{aligned}$$

$\therefore P(x) = 0.5$ & cannot be probability mass function

x	$P(x)$
10	0.2
20	0.2
30	0.35
40	0.15
50	0.1

$$\textcircled{1} \quad P(X=0) \geq 0$$

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$$P(X)=1$$

$$= 0.2 + 0.2 + 0.35 + 0.15 + 0.1$$

$$= 1$$

\therefore It is pmf

code

$$\text{Prob} = \{0.2, 0.2, 0.3, 0.15, 0.1\}$$

sum (Prob)

1

2) Find cdf for following

pmf and sketch graph.

$$x \quad 10 \quad 20 \quad 30 \quad 40 \quad 50$$

$$P(X=x) \quad 0.2 \quad 0.2 \quad 0.35 \quad 0.15 \quad 0.1$$

$$F(x) = 0 \quad x < 10$$

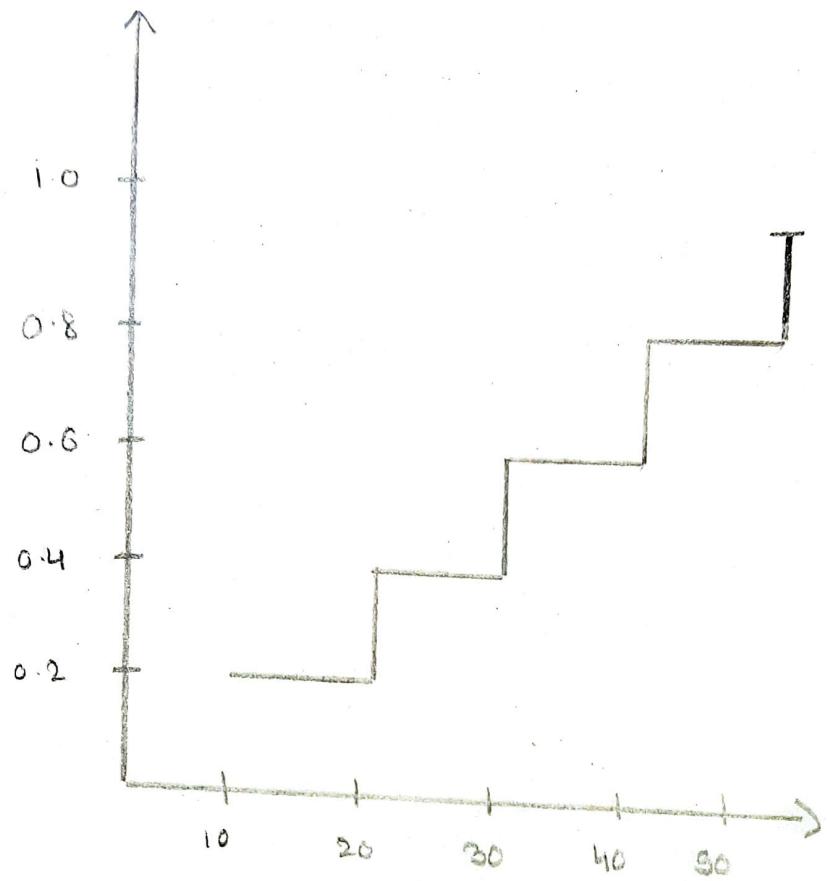
$$0.2 \quad 10 \leq x < 20$$

$$0.4 \quad 20 \leq x < 30$$

$$0.75 \quad 30 \leq x < 40$$

$$0.90 \quad 40 \leq x < 50$$

$$1.0 \quad x \geq 50$$



$$x = c [10, 20, 30, 40, 50]$$

plot = Cdf, cumsum (Prob, "S")



a2) Find

x	1	2	3	4	5	6
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P(x)	0.15	0.25	0.1	0.2	0.2	0.1
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$F(x) = 0$	$x < 1$
0.15	$1 \leq x < 3$
0.40	$2 \leq x < 3$
0.50	$3 \leq x < 4$
0.70	$4 \leq x < 5$
0.90	$5 \leq x < 6$
1.00	$x \geq 6$

$\text{Prob} = C(0.15, 0.25, 0.1, 0.2, 0.2, 0.1)$

sum (prob)

[1] 4

cumsum (prob)

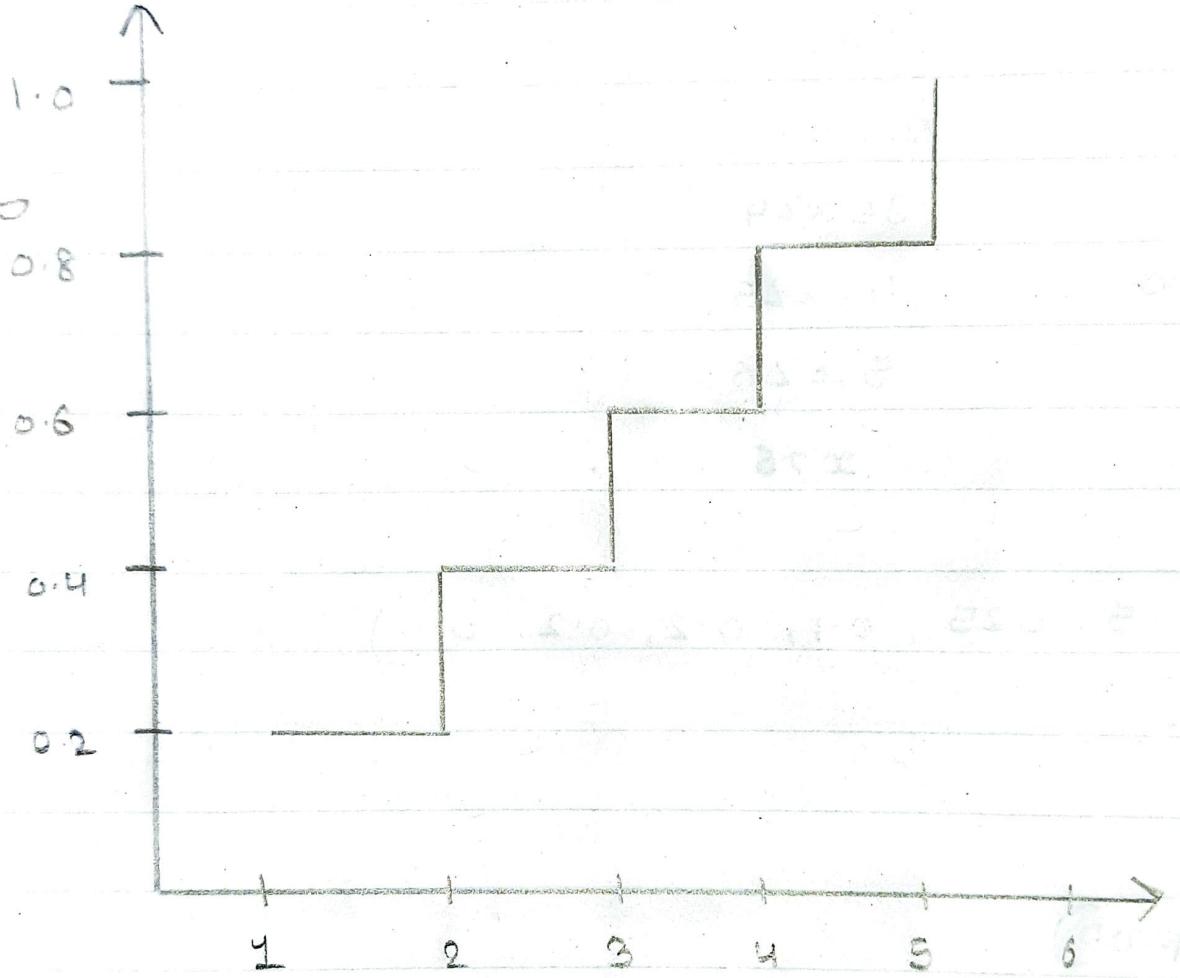
[1] 0.15, 0.40, 0.50, 0.10, 0.90, 1.00

> $x = C(1, 2, 3, 4, 5, 6)$

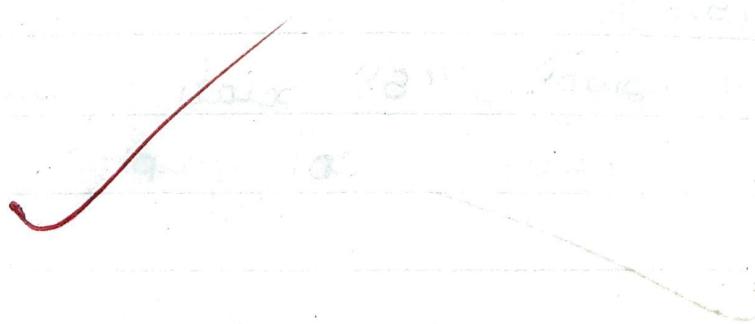
plot (x, cumsum (prob)), "s", xlab = "value", ylab = "cumulative probability", main = "CDF graph", col = "brown")

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cumulative Probability



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→ Binomial Distribution

$P(X=x) = \text{dbinom}(x, n, p)$

$P(X \leq x) = \text{pbinom}(x, n, p)$

If x is unknown

$P_1 = P(X \leq x) = \text{dbinom}(p, n, p)$

1) Find probability of exactly 10 success in 100 trials with $p=0.1$

2) Suppose there are 12 que., each question has 5 option out of which 1 is correct

Find probability of having exactly 4 correct answer.

3) Find complete distribution when $n=5$ and $p=0.1$

— — —

ans)

1) $> x = \text{dbinom}(10, 100, 0.1)$

$> x$

[1] 0.1318653

2) $\text{dbinom}(4, 12, 0.2)$

0.1328756

$\text{pbinom}(4, 12, 0.2)$

0.4274445

$1 - \text{pbinom}(9, 12, 0.2)$

0.01940528

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③ $\text{dbinom}(0:5, 0.1)$

0 - 0.59049

1 - 0.32805

2 - 0.07290

3 - 0.0810

4 - 0.00045

5 - 0.00001

④ $\text{dbinom}(5, 12, 0.25)$

0.1032414

$\text{pbinom}(5, 12, 0.25)$

0.9465978

$1 - \text{pbinom}(7, 12, 0.25)$

0.00278161

$\text{dbinom}(6, 12, 0.25)$

0.04014945



5) X follows binomial distribution with $n=10$, $p=0.3$, plot the graph of pmf and cdf.

$$\textcircled{2}) \quad n = 10$$

$$p = 0.3$$

$$\alpha = 0:n$$

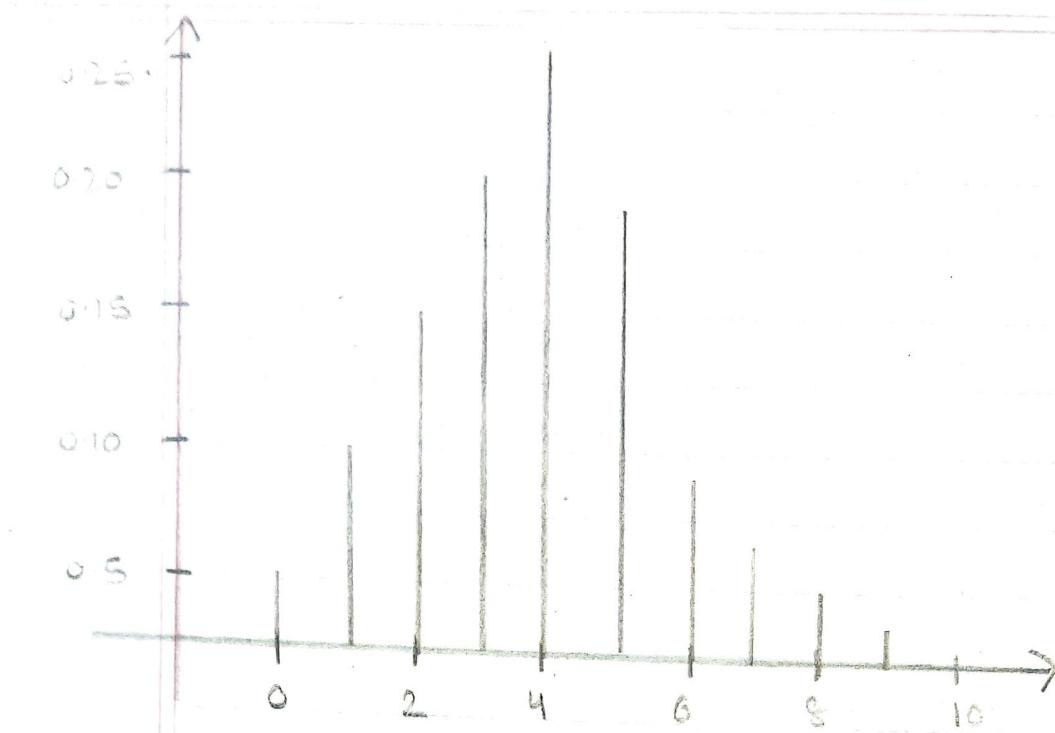
$\text{prob} = \text{dbinom}(\alpha, n, p)$

$\text{curprob} = \text{pbinom}(\alpha, n, p)$

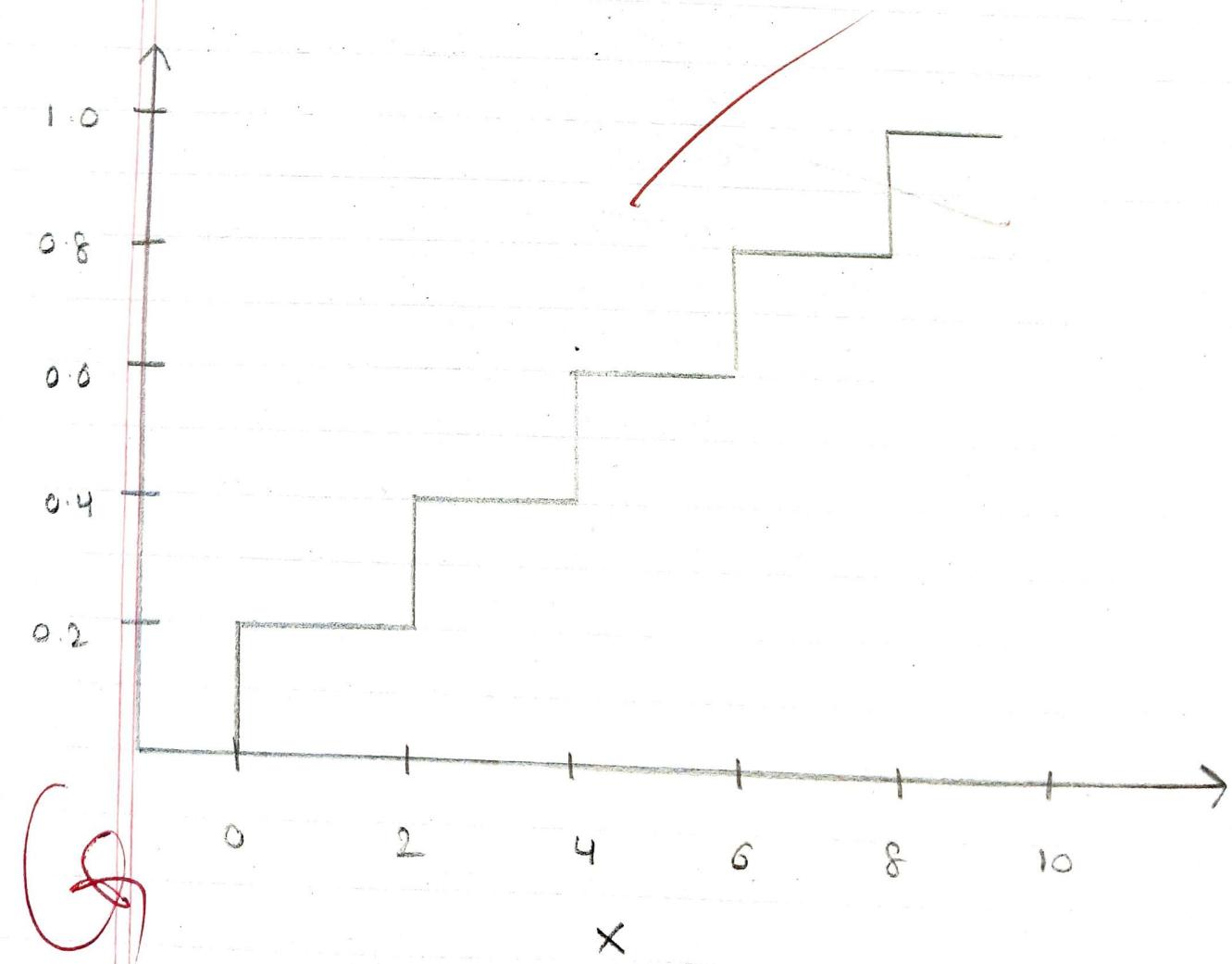
$d = \text{data.frame}(\text{"alpha values"} = \alpha, \text{"probability"} = \text{prob})$.

$\text{print}(d)$

	α values	probability
1	0	0.0282
2	1	0.1210
3	2	0.2234
4	3	0.2668
5	4	0.2001
6	5	0.1029
7	6	0.0367
8	7	0.0090
9	8	0.0014
10	9	0.001
11	10	0.0000



plot (x, curprob, "s")



Normal Distribution

$$1) P(x=x) = \text{dbinom}(x, n, \theta)$$

$$P(x \leq x) = \text{pnorm}(x, \mu, \sigma)$$

$$P(x > x) = 1 - \text{pnorm}(x, \mu, \sigma)$$

To generate random no. from a normal distribution (n random)
the R code is $\text{rnorm}(n, \mu, \sigma)$

1) A random var x follows nor. distribution with mean $= \mu = 12$
and SD $= \sigma = 3$.

Find ① $P(x \leq 15)$

$$P(10 \leq x \leq 13)$$

~~$$P(x > 14)$$~~

Code

$$p1 = \text{pnorm}(15, 12, 3)$$

p1

[1] 0.8413447

$$\text{cat} ("P(x \leq 15) = ", p1)$$

$$P(x \leq 15) = 0.8413447$$

$$p2 = \text{pnorm}(13, 12, 3) - \text{pnorm}(10, 12, 3)$$

p2

[1] 0.3780661

cat $(P(x_{10} < \infty = 13) = ", p_2)$

$p_3 = 1 - \text{pnorm}(14, 12, 3)$

p_3

[1] 0.252495

cat $("P(x > 14) = ", p_3)$

$P(x > 14) = 0.62524925$

$p_4 = \text{pnorm}(5, 12, 3)$

p_4

[1] 15.254723 16.548505 11.280515

6.419944 12.272460

2) $x \sim N(30, 100), \sigma = 10$

1) $P(x \leq 40)$

$P(x \geq 85)$

$P(25 < x < 35)$

Find R such that $P(x < R) = 0.6$



$F = \text{pnorm}(0.6, 30, 10)$

F

0.8413447

$F_1 = 1 - \text{pnorm}(35, 30, 10)$

F_1

0.3095375.

$F_2 = \text{pnorm}(55, 30, 10) - \text{pnorm}(0.6, 30, 10)$

F_2

0.3829249.

$F_B = \text{dnorm}(0.6, 30, 10)$

F_B

32.53347

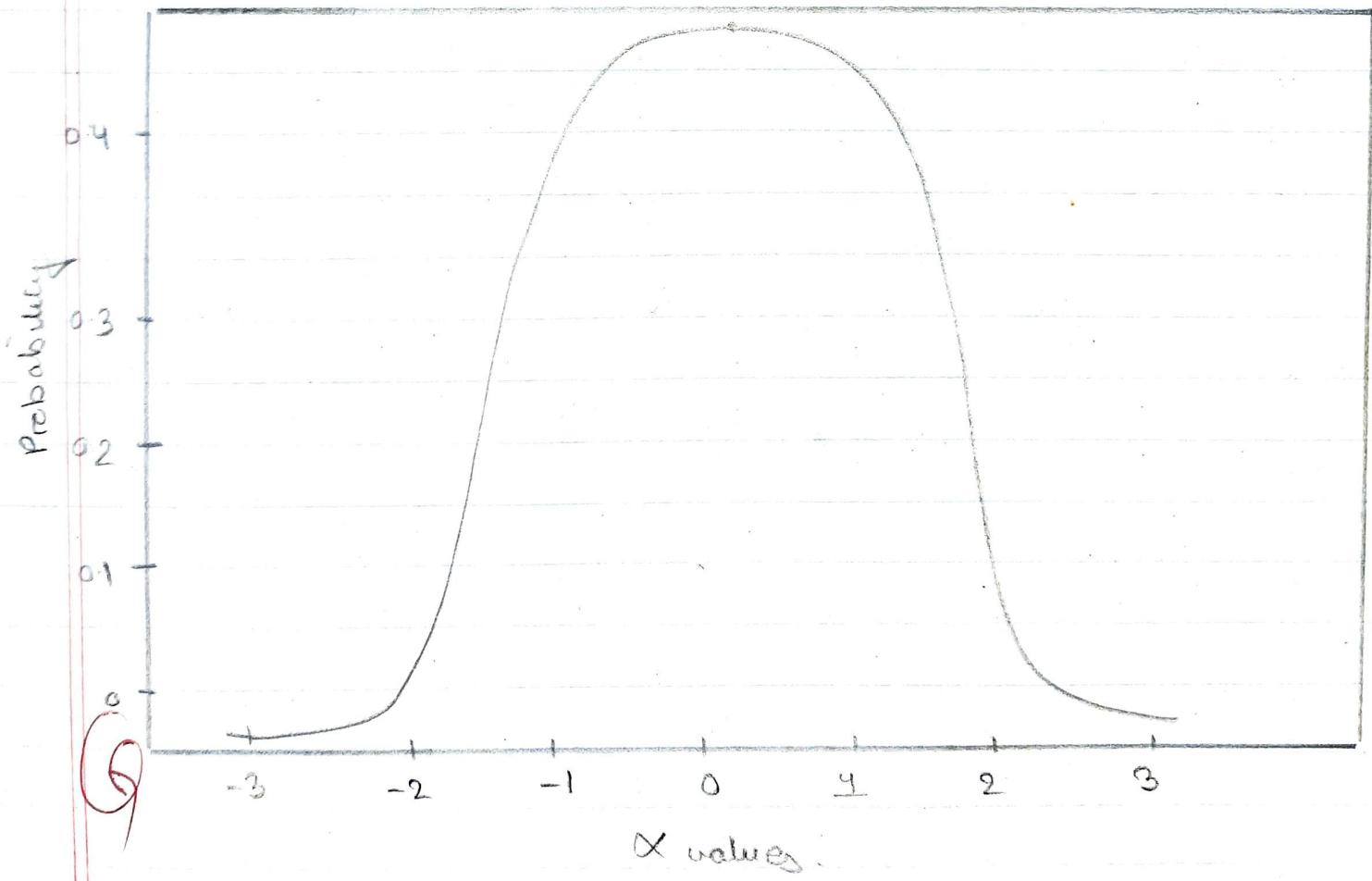
5) Plot standard deviation normal graph

$x = \text{seq}(-3, 3, by = 0.1)$

$y = \text{dnorm}(x)$

plot(x, y, xlab = "x values", ylab = "probability", main = "standard normal graph").

Standard Normal Graph.



Normal and t-test

$H_0: \mu = 15$ $H_1: \mu \neq 15$

Test the hypothesis

Random sample of size 400 is drawn and it is calculated.

The sample mean is 14.

SD is 3.

Test hypothesis at S.I. level of significance

code :

$$\mu_{20} = 15$$

$$m_{\bar{x}} = 14$$

$$n = 400$$

$$sd = 3$$

$$z_{cal} = \frac{(\bar{x}_{20} - \mu_{20})}{(sd / \sqrt{n})}$$

$$z_{cal}$$

$$-6.6667$$

cat ("calculate value of z is ", z_{cal})

calculated value of z is -6.66667

$$pvalue = 2 * (1 - pnorm(zabs(z_{cal})))$$

pvalue

$$2.616716e-11$$

value < 0.05 we will get reject value of $H_0: \mu = 15$.

(ii)

② $H_0: \mu = 12.5$ from following sample at 5% level of significance.

$$x = c(12.25, 11.97, 12.15, 12.08, 12.31, 12.28, 12.31, 12.28, 11.94, 11.89, 12.16, 12.04)$$

$$n = \text{length}(x)$$

$$n$$

$$10$$

$$\bar{x} = \text{mean}(x)$$

$$\bar{x}$$

$$12.07$$

$$\text{var} = (n-1) * \text{var}(x) / n$$

$$0.019821$$

$$sd = \sqrt{\text{var}}$$

$$sd$$

$$0.1397176$$

$$m_0 = 12.5$$

$$t = (\bar{x} - m_0) / (sd / \sqrt{n})$$

$$t$$

$$-8.894909$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(\text{abs}(t)))$$

$$\text{pvalue}$$

$$0$$

∴ The value is less than 0.05 the value is accepted.

⑤ Test hypothesis $H_0: \mu = 10$ against $H_1: \mu \neq 10$. A random sample size of 400 is drawn with sample mean ≈ 10.2 and $sd = 2.25$.

$$m_0 = 10$$

$$n = 400$$

$$\bar{x}_{\text{obs}} = 10.2$$

$$sd = 2.25$$

$$z_{\text{cal}} = (\bar{x}_{\text{obs}} - m_0) / (sd / \sqrt{n})$$

$$z_{\text{cal}}$$

$$1.77778$$

$$\text{pvalue} = 2 * (1 - \text{pnorm}(|z_{\text{cal}}|))$$

$$\text{pvalue}$$

$$0.07544036$$

Value is greater than 0.05

H_0 is accepted.

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Last year farmer last 20% of crop. A random sample of 60 fields are collected and found a field crop are insect polluted.

Test hypothesis at 1% significance

$$P = 0.2$$

$$\rho = 9160$$

$$n = 60$$

$$z_{\text{cal}} = \frac{(p - p_0)}{\sqrt{p_0(1-p_0)/n}}$$

$$z_{\text{cal}}$$

$$0.9687458$$

$$p\text{value} = 2 * \text{C1-ppnorm}(\text{abs}(z_{\text{cal}}))$$

$$p\text{value}$$

$$0.3329216$$

Value is accepted.

(8)