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**Ex No: 2**

**Date: 2\2\26**

## **Building and Training a Neural Network for Planar Data Classificationn**

### **Objective:**

To build and train a **binary classification neural network with one hidden layer** from scratch using **gradient descent**, and to compare its performance with **logistic regression** on a **non-linearly separable planar dataset**.

### **Descriptions:**

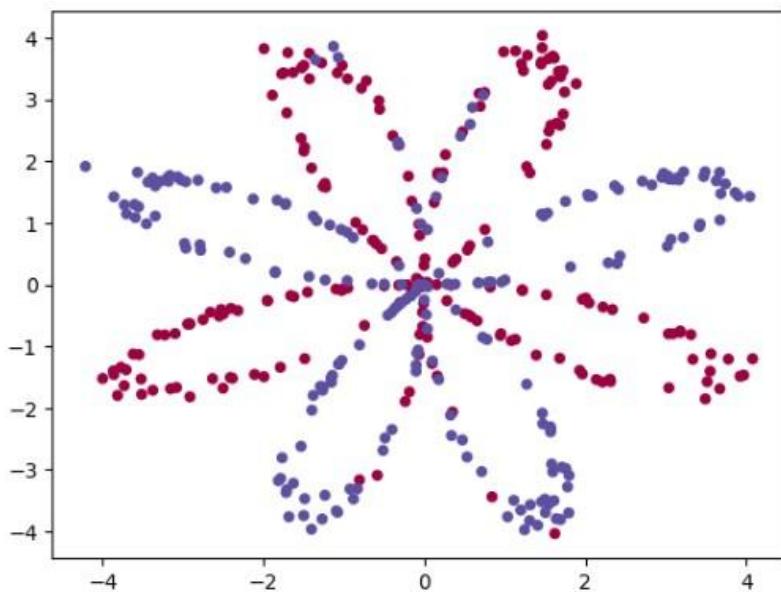
Binary classification is the task of classifying data into two distinct classes.

In this experiment, we classify **2D planar data points** into two categories:

- **1 → Class 1 (Blue points)**
- **0 → Class 0 (Red points)**

The dataset used is a **flower-shaped planar dataset**, where the two classes are **not linearly separable**.

This makes it unsuitable for simple logistic regression and ideal for demonstrating the power of **neural networks with hidden layers**.



**Two models are implemented and compared:**

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## **1. Logistic Regression**

- **No hidden layers**
- **One output neuron**
- **Linear decision boundary**
- **Uses sigmoid activation**

## **2. Neural Network (One Hidden Layer)**

- **One hidden layer with 4 neurons**
- **Tanh activation in hidden layer**
- **Sigmoid activation in output layer**
- **Non-linear decision boundary**

**The neural network is trained using forward propagation, backward propagation, and gradient descent optimization to minimize the cross-entropy loss.**

## **Dataset Description**

- **The dataset consists of 400 data points**
- **Each data point has 2 input features ( $x_1, x_2$ )**
- **Labels are binary (0 or 1)**
- **Data distribution forms a flower-like pattern**
- **Dataset is generated programmatically using `load_planar_dataset()`**

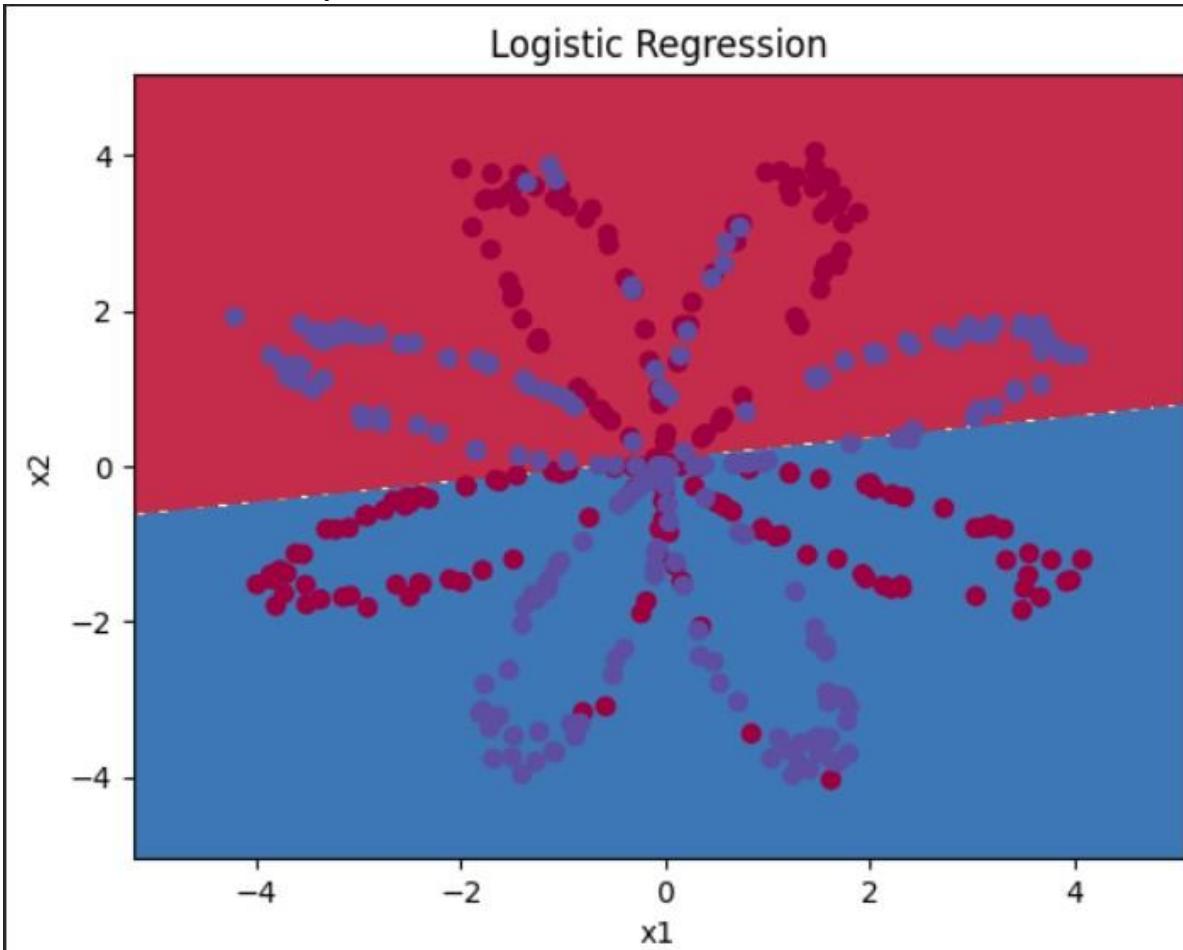
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## Model Architecture

### Logistic Regression Model

- Input Layer: 2 neurons
- Output Layer: 1 neuron
- Activation Function: Sigmoid
- Limitation: Can only learn linear boundaries



### Neural Network Model

- Input Layer: 2 neurons
- Hidden Layer: 4 neurons

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- Output Layer: 1 neuron

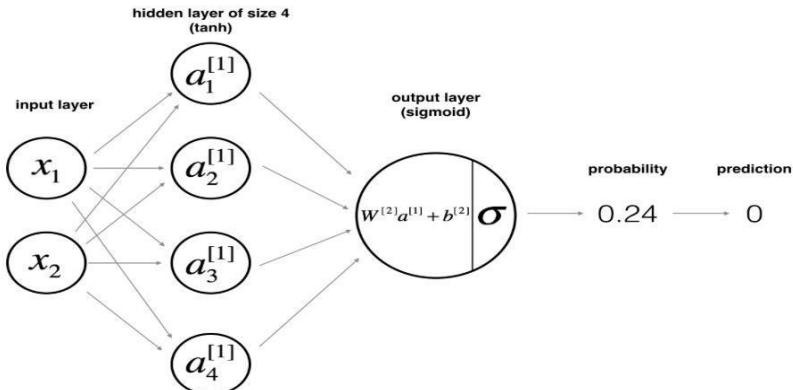
Activation Functions:

- Hidden Layer → tanh

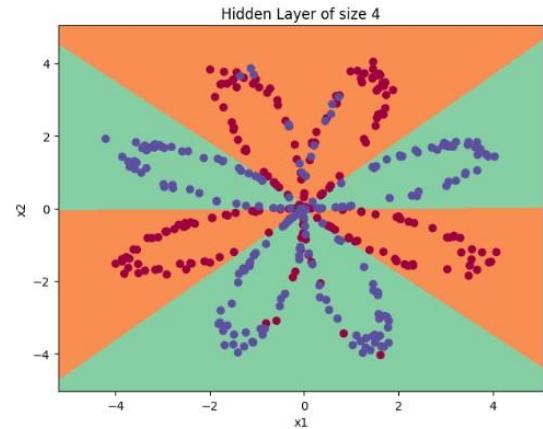
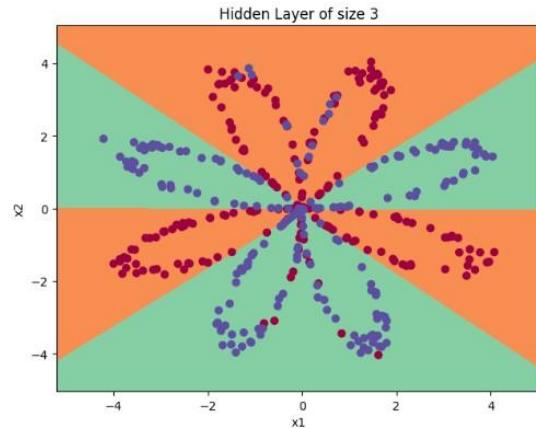
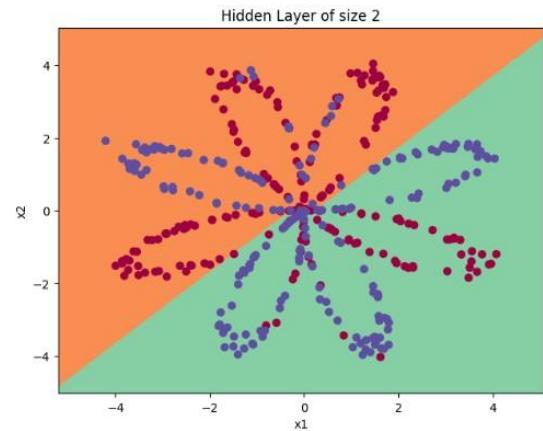
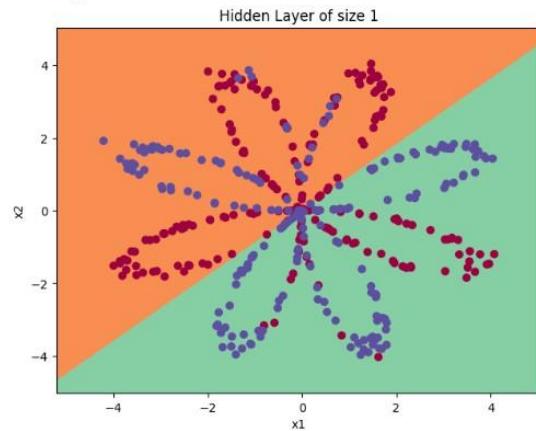
- Output Layer → sigmoid

#### 4 - Neural Network model

Logistic regression did not work well on the "flower dataset". You are going to train a Neural Network with a single hidden layer.



Here is our model:



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## Mathematical Model

### Forward Propagation

**Hidden layer:**

$$Z_1 = W_1 X + b_1$$

$$A_1 = \tanh(Z_1)$$

**Output layer:**

$$Z_2 = W_2 A_1 + b_2$$

$$\hat{y} = \sigma(Z_2)$$

**Loss Function (Cross-Entropy Loss)**

$$J = -\frac{1}{m} \sum [y \log(\hat{y}) + (1 - y) \log(1 - \hat{y})]$$

### Backward Propagation

$$dZ_2 = A_2 - Y$$

$$dW_2 = \frac{1}{m} dZ_2 A_1^T$$

$$dZ_1 = W_2^T dZ_2 \cdot (1 - A_1^2)$$

$$dW_1 = \frac{1}{m} dZ_1 X^T$$

## Algorithm Steps

### 1. Data Loading

- Load planar dataset using helper function
- Visualize dataset using scatter plot

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## **2. Logistic Regression**

- Train baseline logistic regression model
- Plot decision boundary
- Compute accuracy

## **3. Neural Network Construction**

- Initialize parameters
- Perform forward propagation
- Compute cost
- Apply backward propagation
- Update parameters using gradient descent

## **4. Training**

- Train for 10,000 iterations
- Monitor cost reduction

## **5. Evaluation**

- Predict output labels
- Calculate accuracy
- Plot decision boundaries
- Compare results with logistic regression

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## **Results**

### **Logistic Regression**

- Accuracy  $\approx 47\%$
- Decision boundary is almost linear
- Fails to separate flower-shaped data

### **Neural Network**

- Accuracy  $\approx 90\%$
- Decision boundary follows complex flower shape
- Successfully classifies non-linear data

## **Inference**

- Logistic regression is insufficient for non-linearly separable data.
- Adding a hidden layer with non-linear activation enables the model to learn complex patterns.
- Neural networks significantly outperform logistic regression for complex datasets.
- Tanh activation helps in faster convergence and better learning.

## **Conclusion**

**In this experiment, a neural network with one hidden layer was successfully implemented from scratch.**

**The model achieved high accuracy ( $\sim 90\%$ ) on a complex planar dataset, clearly demonstrating the importance of hidden layers and non-linear activation functions in machine learning.**

**This experiment highlights how neural networks overcome the limitations of linear models and are effective for solving real-world classification problems.**

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**GitHub link**

**<https://github.com/diganthrgowdabtech24-star/mlds-lab-2>**