

Problem #2 (Part 1):

$$Q = \begin{pmatrix} 10^{-4} & 2 * 10^{-5} \\ 2 * 10^{-5} & 10^{-4} \end{pmatrix} \quad R = \begin{pmatrix} 10^{-2} & 5 * 10^{-3} \\ 5 * 10^{-3} & 10^{-2} \end{pmatrix}$$

The time update equations are:

$$\begin{aligned}\widehat{x}_k^- &= A \widehat{x}_{k-1} + B u_{k-1} \\ P_k^- &= AP_{k-1}A^T + Q\end{aligned}$$

The measurement update equations are:

$$\begin{aligned}\widehat{x}_k &= \widehat{x}_k^- + K_k (Z_k - H \widehat{x}_k^-) \\ K_k &= \frac{P_k^- H^T}{H P_k^- H^T + R} \\ P_k &= (I - K_k H) P_k^-\end{aligned}$$