

Q.1

## BIG O NOTATION

The Big O notation, where O stands for 'order of', is concerned with what happens for very large values of  $n$ . For example, if a sorting algorithm performs  $n^2$  operations to sort just  $n$  elements, then that algorithm would be described as an  $O(n^2)$  algorithm.

If  $f(n)$  and  $g(n)$  are the functions defined on a positive integer number  $n$ , then

$$f(n) = O(g(n))$$

That is,  $f$  of  $n$  is Big-O of  $g$  of  $n$  if and only if positive constants  $c$  and  $n_0$  exist, such that  $f(n) \leq cg(n)$ . It means that for large amounts of data,  $f(n)$  will grow no more than a constant factor than  $g(n)$ . We have seen that the Big O notation provides a strict upper bound for  $f(n)$ . This means that the function  $f(n)$  can do better but not worse than the specified value. Big O notation is simply written as  $f(n) \in O(g(n))$  or as  $f(n) = O(g(n))$ .

Here,  $n$  is the problem size and  $O(g(n)) = \{h(n):$

positive constants  $c, n_0$ , such that  $0 \leq h(n) \leq cg(n), \forall n \geq n_0\}$ . Hence, we can say that  $O(g(n))$  comprises a set of all the functions  $h(n)$  that are less than or equal to  $cg(n)$  for all values of  $n > n_0$ .

If  $f(n) \leq cg(n), c > 0, \forall n \geq n_0$ , then  $f(n) = O(g(n))$  and  $g(n)$  is an asymptotically tight upper bound for  $f(n)$ .

Examples of functions in  $O(n^3)$  include:  $n^2, n^3, n^3 + n, 540n^3 + 10$ .

Best case O describes an upper bound for all combinations of input. It is possibly lower than the worst case. For example, when sorting an array the best case is when the array is already correctly sorted.

Worst case O describes a lower bound for worst case input combinations. It is possibly greater than the best case.

## OMEGA NOTATION ( $\Omega$ )

The Omega notation provides a tight lower bound for  $f(n)$ . This means that the function can never do better than the specified value but it may do worse.

notation is simply written as,  $f(n) \in \Omega(g(n))$ , where  $n$  is the problem size and  $\Omega(g(n)) = \{h(n):$  positive constants  $c > 0, n_0$ , such that  $0 \leq cg(n) \leq h(n), \forall n \geq n_0\}$ .

Hence, we can say that  $\Omega(g(n))$  comprises a set of all the functions  $h(n)$  that are greater than or equal to  $cg(n)$  for all values of  $n \geq n_0$

If  $cg(n) \leq f(n), c > 0, \forall n \geq n_0$ , then  $f(n) \in \Omega(g(n))$  and  $g(n)$  is an asymptotically tight lower bound for  $f(n)$ .

Examples of functions in  $\Omega(n^2)$  include:  $n^2, n^2, n^3 + n^2, n^3$

To summarize,

Best case describes a lower bound for all combinations of input. This implies that the function can never get any better than the specified value. For example, when sorting an array the best case is when the array is already correctly sorted.

- Worst case describes a lower bound for worst case input combinations. It is possibly greater than best case. For example, when sorting an array the worst case is when the array is sorted in reverse order.
- If we simply write  $\Theta$ , it means same as best case  $N$ .

### THETA NOTATION ( $\rightarrow$ )

Theta notation provides an asymptotically tight bound for  $f(n)$ .  $\Theta$  notation is simply written as,  $f(n) \in \Theta(g(n))$ , where  $n$  is the problem size and

$\Theta(g(n)) = \{h(n) : \exists \text{ positive constants } c_1, c_2, \text{ and } n_0, \text{ such that } c_1 g(n) \leq h(n) \leq c_2 g(n), n \geq n_0\}$ .

Hence, we can say that  $\Theta(g(n))$  comprises a set of all the functions  $h(n)$  that are between  $c_1 g(n)$  and  $c_2 g(n)$  for all values of  $n \geq n_0$ .

If  $f(n)$  is between  $c_1 g(n)$  and  $c_2 g(n)$ ,  $n \geq n_0$ , then  $f(n) \in \Theta(g(n))$  and  $\Theta(g(n))$  is an asymptotically tight bound for  $f(n)$  and  $f(n)$  is amongst  $h(n)$  in the set.

To summarize,

- The best case in  $\Theta$  notation is not used.
- Worst case  $\rightarrow$  describes asymptotic bounds for worst case combination of input values.
- If we simply write  $\Theta$ , it means same as worst case  $C$ .

Q.2 i) since the 'i' or 2.a' is not present

(We can have multiple logics here for Pseudocode, and its not present in the book )

#### Part 1 of the answer

Step 1: IF START = NULL

    Write "UNDERFLOW"

    Go to Step 10

[END OF IF]

Step 2: SET PTR = START

Step 3: Repeat Steps 4 to 7 while PTR != NULL

Step 4: SET PREPTR = PTR

```

Step 5: SET TEMP = PTR -> NEXT
Step 6: Repeat while TEMP != NULL
    IF TEMP -> DATA = PTR -> DATA
        SET PREPTR -> NEXT = TEMP -> NEXT
        FREE TEMP
        SET TEMP = PREPTR -> NEXT
    ELSE
        SET PREPTR = TEMP
        SET TEMP = TEMP -> NEXT
    [END OF IF]
[END OF LOOP]
Step 7: SET PTR = PTR -> NEXT
[END OF LOOP]

```

Step 8: Go to Sorting Process

#### Option 1:

```

public void RemoveDuplicates(Node<T> head)
{
    // Iterate through the list
    Node<T> iter = head;
    while(iter != null)
    {
        // Iterate to the remaining nodes in the list
        Node<T> current = iter;
        while(current != null && current.Next != null)
        {
            if(iter.Value == current.Next.Value)
            {
                current.Next = current.Next.Next;
            }
            current = current.Next;
        }
        iter = iter.Next;
    }
}

```

OR

#### Option 2:

```

void removeDuplicates(struct Node* head) {
    struct Node *current, *prev, *temp;
    current = head;

```

```

while (current != NULL && current->next != NULL) {
    prev = current;
    temp = current->next;

    while (temp != NULL) {
        if (current->data == temp->data) {
            prev->next = temp->next;
            free(temp);
            temp = prev->next;
        } else {
            prev = temp;
            temp = temp->next;
        }
    }
    current = current->next;
}
}

```

## Part 2 of answer

Step 9: IF START = NULL OR START -> NEXT = NULL

Return

[END OF IF]

Step 10: Repeat Steps 11 to 13 while PTR != NULL

Step 11: SET INDEX = PTR -> NEXT

Step 12: Repeat while INDEX != NULL

IF PTR -> DATA > INDEX -> DATA

SWAP PTR -> DATA and INDEX -> DATA

SET INDEX = INDEX -> NEXT

[END OF LOOP]

Step 13: SET PTR = PTR -> NEXT

[END OF LOOP]

Step 14: EXIT

## Along w code

Sort krneke bhi multiple logics ho sakte hai :

```

struct node *sort_list(struct node *start)
{
    struct node *ptr1, *ptr2;
    int temp;
    ptr1 = start;
    while(ptr1 -> next != NULL)

```

```

{
    ptr2 = ptr1 -> next;
    while(ptr2 != NULL)
    {
        if(ptr1 -> data > ptr2 -> data)
        {
            temp = ptr1 -> data;
            ptr1 -> data = ptr2 -> data;
            ptr2 -> data = temp;
        }
        ptr2 = ptr2 -> next;
    }
    ptr1 = ptr1 -> next;
}
return start; // Had to be added
}

```

```

void displayList(struct Node* head) {
    struct Node* temp = head;
    while (temp != NULL) {
        printf("%d -> ", temp->data);
        temp = temp->next;
    }
    printf("NULL\n");
}

```

Q.2 (ii)

Part 1 of answer

Step 1: IF AVAIL = NULL

Write OVERFLOW

Go to Step 11

[END OF IF]

Step 2: SET NEW NODE

AVAIL

Step 3: SET AVAIL = AVAIL -> NEXT

Step 4: SET NEW\_NODE -> DATA = VAL

Step 5: SET PTR = START

Step 6: Repeat Step 7 while PTR -> NEXT != START

Step 7: PTR = PTR -> NEXT

[END OF LOOP]

Step 8: SET NEW\_NODE -> NEXT = START

Step 9: SET PTR -> NEXT = NEW\_NODE

Step 10: SET START = NEW\_NODE

Step 11: EXIT

### Along w code

```
struct node *insert_beg(struct node *start)
{
    struct node *new_node, *ptr;
    int num;
    printf("\n Enter the data : ");
    scanf("%d", &num);
    new_node = (struct node *)malloc(sizeof(struct node)); new_node -> data = num;
    ptr = start;
    while(ptr -> next != start)
    ptr = ptr -> next; ptr -> next = new_node;
    new_node -> next = start; start = new_node; return start;
}
```

### Part 2 of answer

Step 1: IF START = NULL

Write UNDERFLOW

Go to Step 8

[END OF IF]

Step 2: SET PTR = START

Step 3: Repeat Steps 4 and 5 while PTR -> NEXT != START

Step 4: SET PREPTR = PTR

Step 5: SET PTR = PTR -> NEXT

[END OF LOOP]

Step 6: SET PREPTR-> NEXT = START

Step 7: FREE PTR

Step 8: EXIT

### Along w code

```
struct node *delete_end(struct node *start)
{
    struct node *ptr, *preptr; ptr = start;
    while(ptr -> next != start) {
    preptr = ptr; ptr = ptr -> next;
    }
    preptr -> next = ptr -> next; free(ptr);
    return start;
}
```

### Q.3 (ii)

Step 1: Start

Step 2: Input the number N

Step 3: Initialize an empty stack

Step 4: Repeat Steps 5 and 6 while  $N > 0$

Step 5: Extract the last digit of N using  $\text{digit} = N \% 10$

Step 6: Push digit onto the stack and update  $N = N / 10$

[END OF LOOP]

Step 7: Initialize  $\text{reversedNum} = 0$  and  $\text{place} = 1$

Step 8: Repeat Steps 9 and 10 while the stack is not empty

Step 9: Pop the top element from the stack

Step 10: Update  $\text{reversedNum} = \text{reversedNum} + (\text{popped\_digit} * \text{place})$

Step 11: Multiply  $\text{place} = \text{place} * 10$

[END OF LOOP]

Step 12: Store  $\text{reversedNum}$  as the final reversed number

Step 13: Print  $\text{reversedNum}$

Step 14: End

```
#include <stdio.h>
#include <stdlib.h>
#define MAX 10
int stk[MAX], top = -1;
void push(int val) {
    stk[++top] = val;
}
int pop() {
    return stk[top--];
}
int main() {
    int num, val, i, reversedNum = 0, place = 1;
    printf("\n Enter a number: ");
    scanf("%d", &num);
    while (num > 0) {
        push(num % 10);
        num /= 10;
    }
    while (top != -1) {
        val = pop();
        reversedNum = reversedNum * 10 + val;
    }
    printf("\n Reversed Number: %d\n", reversedNum);
    return 0;
}
```