



SPECIFICITY AND CONSTRAINTS IN PEPTIDE-PROTEIN BINDINGS IN THE MOUSE PROTEOME

Report for 3rd Year Research Project

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Part I

Introduction

This report details the work done towards the fulfillment of the requirements of the department of Physics at Ecole Polytechnique. I undertook this research project under the guidance of Dr. Remi Monasson at the Laboratoire de Physique Theorique at the Ecole Normale Supérieure in Paris.

The aim of the project was to study the interactions between short peptide chains and a specific section of signalling proteins called PDZ Domains. One of the aspects that we study here is the specificities of interactions between peptides and PDZ domains. It is well known that macromolecules such as proteins and enzymes interact in a specific manner with other macromolecules and biomolecules. What interested us over the course of the study are the constraints present in the peptide sequences due to the specificity of their interactions with PDZ domains. We will also have an occasion to understand similar constraints on the PDZ domain sequences.

This report is organized as follows. After a brief introduction to the biological importance of PDZ Domains, we explain the experiments performed by **Insert reference here**. Using these experiments, Stiffler et al created a model which is capable of predicting whether a peptide will bind to a PDZ domain given the sequence of the peptide. We shall explain the data that Stiffler et al have provided. The first two models that we propose utilise the data provided by Stiffler et al.

Once the data presented and the biological context established, we present a first model which seeks to understand the constraints imposed on the peptide sequences under the effect of mutations. We present the results derived from this model and discuss the limitations. A second improved model is then proposed which considers error rates as probabilities. We present some interesting observations on the basis of this model. In particular, we show how certain positions are particularly constrained over all peptides and present a simple way of calculating the level of constraint.

Finally, to render the study of peptide-PDZ domain specificity complete, we explain how we could integrate the PDZ Domain sequences into the modeling. This is done by a regression method called the *Lasso*. We shall have the chance to present the lasso method in more detail in the relevant section.

We conclude with a summary of our findings and possible directions of further improvements.

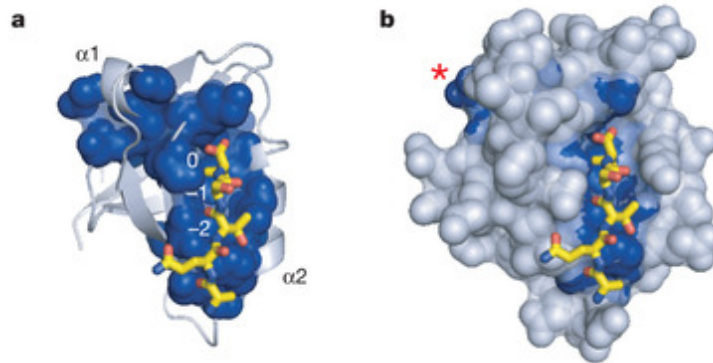


Figure 1: Left: We show the PDZ domain (in blue) with the target peptide (yellow). The C-terminal of the target peptide is numbered 0 whilst the preceding amino acids are numbered in descending order. **Right:** The position of the PDZ-Domain within the parent protein is shown. The position marked with a little star shows that during the binding process there are other parts of the PDZ domain which are involved and not just the binding pocket

1 PDZ Domains

Let us begin by explaining PDZ Domains, their importance, their structure and how they bind to other macromolecules. PDZ domains are short sections of proteins composed of 80-90 amino acids. PDZ Domains are usually found in signaling proteins where they regulate processes such as the separation of cell membranes. PDZ itself is an acronym for the first three letters of three proteins: Post-synaptic density protein (PSD95), Drosophila disc large tumor suppressor (Dlg1) and zonula occludens-1 protein (zo-1)

PDZ Domains are usually composed of 80-90 amino acids and many PDZ domains can be present within a single protein. Multiple domains within the same protein can have similar functions or different functions, each of which will bind to a different part of the target protein or a different protein altogether.

PDZ Domains always bind to the C-terminal of certain specific sections of the target proteins. The binding occurs within a binding pocket formed by the domain. The binding pocket are usually formed by the first 20 amino acids. A diagram showing the positions of the binding pocket as well as the target peptide are shown below.

2 Explanation of the data of Stiffler et al

Now that we have given a small introduction to PDZ domains we shall explain the work done by Stiffler and co-authors which we sought to extend and improve upon.

The article that we have considered is titled "PDZ domain binding specificity is optimized across

the mouse proteome". In this article, Michael Stiffler and co-authors sought to characterise the selectivity between 157 PDZ domains and 217 target peptides found in the mouse proteome. To this end, they created a model which could predict whether a given PDZ domain would bind to a target peptide given the sequence of the target peptide.

In their model, the last 5 positions near the C-terminal of the target peptide are considered. The model can be summarized in the following simple equation:

$$\phi_i = \sum_{p,q} A_{p,q} \theta_{i,p,q} > \tau_i \quad (1)$$

where for a given PDZ Domain i , we can calculate a binding score ϕ_i . A is an indicator of the peptide sequence : $A_{p,q} = 1$ if the amino acid at position p of the peptide is q and $A_{p,q} = 0$ otherwise. The numbers $\theta_{i,p,q}$ are the parameters that need to be fit to the experimental data. τ_i is a scoring threshold which is different for each domain i . The values $\theta_{i,p,q}$ are to be interpreted in the following fashion: $\theta_{i,p,q} > 0$ if the PDZ Domain i prefers amino acid q at position p more than the other PDZ domains, negative if it prefers it less, and 0 if it has no bias relative to the other domains. τ_i is defined as the m th percentile of the ϕ_i 's for all the peptides in the model that bound to the domain i . To make predictions using this model, it suffices to know the sequence of the target peptide and compute $\phi_i - \tau_i$ for the domain i . If the domain binds with the target protein then this number is positive and negative otherwise.

The data used to fit the model was obtained by protein micro-array assays. Each PDZ Domain-peptide pair under consideration was verified for binding during the experiment. The researchers were able to model 74 domains among the 157 domains experimented upon. The experimental results of these experiments are available to us in the form of an interaction matrix which tells us whether a PDZ domain i binds to a target peptide j or not.

For each of the 74 domains successfully modeled, we also possess the parameters $\theta_{i,p,q}$ allowing us to test the model on newer peptide sequences. We also possess the error rates for the model. These are given in terms of false positive and false negative rates. These error rates interpreted as empirical probabilities were used in one of the models presented later in the report.

3 Questions asked and answered

With the biological context established and the various data that we possess explained, let us now briefly discuss the questions that we sought to answer over the course of the project.

Firstly, we sought to understand the effect of mutations on the specificity of domain-peptide interactions. It is well known that PDZ domains bind to only certain specific target peptides and not to others. What if the target peptide suffered a point mutation? Will the PDZ domain still bind to the peptide?

A related question concerns the level of constraint imposed on the peptides due to the specificity of their interactions with PDZ domains. If the peptide were to suffer a point mutation and if it continued to bind to the PDZ domain, it then becomes interesting to consider the extent to which the peptide can undergo mutations before it stops binding to the peptide. Inversely, if the peptide doesn't accept many mutations, it is again interesting to analyze whether there are certain positions or amino acids which impose constraints on the sequence.

All such questions were modeled, analyzed and understood in this project.

Part II

First Model

4 Features of the model

Our first model sought to study the effects of the introduction of mutations in the peptide sequences considered by the

5 Results

6 Limitations

Part III

Improvements over first model: Bayesian Modeling

7 Error rates as probabilities

8 Updated Bayesian model

9 Improvements over first model

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11 Interesting observations

Part IV

Integrating PDZ Domain sequences

12 The LASSO

13 Interesting observations

Part V

Conclusion

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