

MATRIX STRUCTURAL ANALYSIS PROJECT

ASTORIA-MEGLER BRIDGE 2D MODEL



GROUP 11

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EXECUTIVE SUMMARY

- In the project, we have analyzed the Astoria-Megler bridge, by making a 2-D model for it. We plotted the deflected shape of the bridge under realistic loading and calculated the bending moment, axial force, and shear force in each member using Matlab.
- All this analysis will provide us with how we can increase the safety of the bridge and optimize it economically.
- The deflected shape will help us select supports so that we can minimize the deflection.
- The bridge is deforming more in the middle span so we can provide support to reduce the deflection.

SALIENT FEATURES

- Total Length: 21,474 feet (6,545 meters)
- Main Span: 1,232 feet (376 meters)
- Width: 28 feet (8.5 meters)
- Number of Lanes: 2
- Construction Period: November 5, 1962 - August 27, 1966

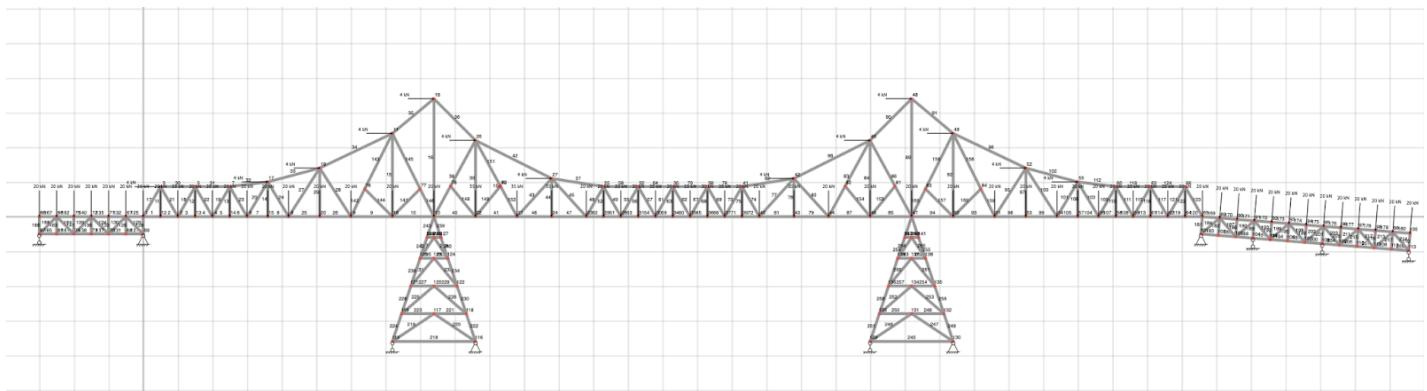
Key Features of the Cantilever Design

- Continuous Truss Structure: The Astoria-Megler Bridge is notable for being the longest continuous truss bridge in North America. This design allows for a seamless distribution of loads across the entire structure, enhancing stability and reducing stress concentrations typically found in traditional cantilever designs, where spans are separate.

- Main Span Configuration: The bridge's main span measures 1,233 feet (376 meters) and is supported by cantilever arms. This central navigation span is unique in that it initially functioned as a cantilever during construction, with the suspended span being temporarily held by the cantilever arms. Once completed, this suspended span was riveted to the cantilever arms, transforming it into a continuous truss rather than an independent suspended structure.
- Innovative Construction Technique: The construction involved an unusual method where segments were fabricated upstream and then barged downstream for assembly. Hydraulic jacks were employed to lift these segments into place, allowing for a more efficient construction process in challenging environmental conditions.
- Robust Wind and Current Resistance: Designed to withstand wind gusts of up to 150 mph (240 km/h) and river currents of 9 mph (14 km/h), the bridge's cantilever structure is engineered for resilience against extreme weather conditions typical of the Pacific Northwest.

PROBLEM DETAILS

- We have replicated a 2D truss structure by analyzing the side view geometry of the Astoria - Megler Bridge constructed in Astoria, USA. There are a total of 141 nodes and 266 members. The Loads and supports have been mentioned with a view of realistic conditions.
- Loads:-
 1. Dead load - the weight of the road
 2. Live load - weight of vehicles
 3. Wind load - force on truss due to wind
- The 2-D structure is shown below with the loads applied:-



- The real image of the bridge is shown below:-



OBJECTIVE

To find:-

1. Deflected shape of truss
2. Unknown reactions
3. Bending moment, shear force, and axial force in each member

SOLUTION APPROACH

COLLECTION OF THE STRUCTURE DATA:

1. Joint Coordinates sheet: Identify the number of joints and name them 1 to Number_of_Nodes. For each joint get x and y coordinates, their expected settlement, concentrated forces, and moments.
2. Member Connectivity sheet: Name the members from 1 to Number_of_members. For each member get the 2 joints it connects. Determine its Area, Modulus of Elasticity, Moment of Inertia, and the distributed force acting on it. For each member define the JOINT_CASE based on the method of release of moment.

CREATION OF THE CODE:

1. **Initialize Workspace**
 - Clear any previous variables and set up a clean environment.
2. **Read Input Data**
 - **Node Coordinates:** Read joint coordinates (including positions and applied forces/moments) from an Excel sheet.
 - **Member Connectivity:** Read member properties (connectivity, material properties, joint types, and applied loads) from an Excel sheet.
3. **Setup Global Stiffness Matrix and Load Vectors**
 - Initialize the global stiffness matrix K_global, fixed-end force vector, nodal forces vector, and settlements vector to zero.
4. **Iterate Over Members**

For each member:

 - Extract member properties: area, elasticity, inertia, load, joint case, and the nodes it connects.

- Compute **member length** and **orientation** using the coordinates of the connected nodes.
- Compute **local stiffness matrix** and **fixed-end forces** based on the joint case (e.g., fully fixed, hinged, etc.).
- Form the **transformation matrix** to convert local stiffness and forces to global coordinates.
- Assemble the member's global stiffness matrix and force contributions into the global system.

5. Apply for Settlements

- Incorporate node settlements into the global system by adding the corresponding displacement terms and their effects on forces.

6. Boundary Conditions

- Remove degrees of freedom (DOFs) associated with restrained nodes by modifying the global stiffness matrix and force vectors.

7. Solve for Displacements

- Compute the displacements of the free DOFs by solving the reduced system:

$$K_{\text{reduced}} \times U_{\text{free}} = F_{\text{reduced}}$$
- Reconstruct the full displacement vector, including zero displacements for restrained DOFs.

8. Calculate Member Forces

For each member:

- Use the member's displacements and the stiffness matrix to compute forces at each end of the member in the global coordinate system.
- Apply fixed-end forces and distributed loads.

9. Output Results

- Write the computed member forces, displacements, and other relevant data in an Excel file.

10. Plotting

- From the original coordinates of nodes and displacements for each node obtained from the solution, get the deformed coordinates of the nodes. Plot both deformed and undeformed shapes. Use a scaling factor to visualize the deformed shape of the structure.

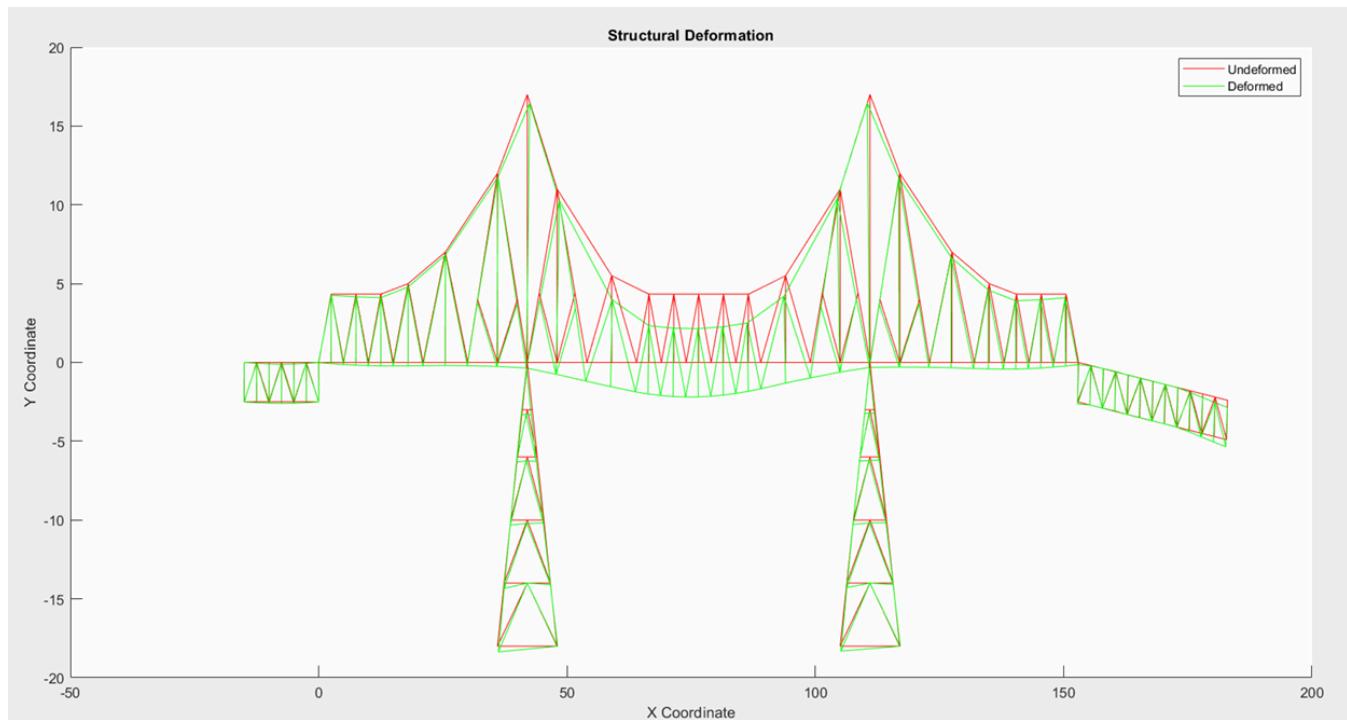
IMPROVEMENT

- In this approach, we won't be able to get the deformed shape of each member. In order to do so we can further divide each member into smaller members considering a sufficient number of nodes along the length of the member. This will give us a better visualization of how each member is deforming.

FINAL RESULTS

The deflected shape obtained shows nodal displacements

Red color - undeformed shape; Green color - Deformed shape



- (i) We can clearly see here that the large deformations in the middle span are due to the absence of ground support in the middle, pointing to lower stiffness.
- (ii) The triangular design of trusses provides excellent stability by efficiently transferring loads from the deck to the bridge supports.
- (iii) As we have applied different types of loads at various points and members it demonstrates a highly efficient and stable structure, capable of withstanding environmental forces while providing safe and reliable transportation.

EXCEL SHEET FOR MEMBER CONNECTIVITY

	A	B	C	D	E	F	G	H
1	Member	Joint 1	Joint 2	Area				JOINT_CASE
2	1	1	12	0.86	2E+11	0.00002	0	1
3	2	12	2	0.86	2E+11	0.00002	0	1
4	3	2	13	0.86	2E+11	0.00002	0	1
5	4	13	4	0.86	2E+11	0.00002	0	1
6	5	4	14	0.86	2E+11	0.00002	0	1
7	6	14	6	0.86	2E+11	0.00002	0	1
8	7	6	15	0.86	2E+11	0.00002	0	1
9	8	15	8	0.86	2E+11	0.00002	0	1
10	9	9	16	0.86	2E+11	0.00002	0	1
11	10	16	10	0.86	2E+11	0.00002	0	1
12	11	12	3	0.86	2E+11	0.00002	0	1
13	12	13	5	0.86	2E+11	0.00002	0	1
14	13	14	7	0.86	2E+11	0.00002	0	1
15	14	15	17	0.86	2E+11	0.00002	0	1
16	15	16	11	0.86	2E+11	0.00002	0	1
17	16	10	18	0.86	2E+11	0.00002	0	1
18	17	1	3	0.86	2E+11	0.00002	0	1
19	18	2	5	0.86	2E+11	0.00002	0	1
20	19	4	7	0.86	2E+11	0.00002	0	1
21	20	6	17	0.86	2E+11	0.00002	0	1
22	21	3	2	0.86	2E+11	0.00002	0	1
23	22	5	4	0.86	2E+11	0.00002	0	1
24	23	7	6	0.86	2E+11	0.00002	0	1
25	24	17	8	0.86	2E+11	0.00002	0	1
26	25	8	20	0.86	2E+11	0.00002	0	1
27	26	20	9	0.86	2E+11	0.00002	0	1
28	27	8	19	0.86	2E+11	0.00002	0	1
29	28	19	9	0.86	2E+11	0.00002	0	1
30	29	20	19	0.86	2E+11	0.00002	0	1
31	30	3	5	0.86	2E+11	0.00002	0	1
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36	35	11	18	0.86	2E+11	0.00002	0	1
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39	38	10	26	0.86	2E+11	0.00002	0	1
40	39	22	26	0.86	2E+11	0.00002	0	1
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228	227	118	120	0.86	2E+11	0.00002	0	1
229	228	119	121	0.86	2E+11	0.00002	0	1
230	229	121	117	0.86	2E+11	0.00002	0	1

230	229	121	117	0.86	2E+11	0.00002	0	1
231	230	120	122	0.86	2E+11	0.00002	0	1
232	231	122	121	0.86	2E+11	0.00002	0	1
233	232	122	123	0.86	2E+11	0.00002	0	1
234	233	123	121	0.86	2E+11	0.00002	0	1
235	234	124	122	0.86	2E+11	0.00002	0	1
236	235	120	124	0.86	2E+11	0.00002	0	1
237	236	124	125	0.86	2E+11	0.00002	0	1
238	237	125	123	0.86	2E+11	0.00002	0	1
239	238	10	126	0.86	2E+11	0.00002	0	1
240	239	126	123	0.86	2E+11	0.00002	0	1
241	240	125	126	0.86	2E+11	0.00002	0	1
242	241	124	127	0.86	2E+11	0.00002	0	1
243	242	127	10	0.86	2E+11	0.00002	0	1
244	243	127	125	0.86	2E+11	0.00002	0	1
245	244	128	129	0.86	2E+11	0.00002	0	1
246	245	128	130	0.86	2E+11	0.00002	0	1
247	246	130	129	0.86	2E+11	0.00002	0	1
248	247	130	131	0.86	2E+11	0.00002	0	1
249	248	131	129	0.86	2E+11	0.00002	0	1
250	249	132	130	0.86	2E+11	0.00002	0	1
251	250	128	132	0.86	2E+11	0.00002	0	1
252	251	132	133	0.86	2E+11	0.00002	0	1
253	252	133	131	0.86	2E+11	0.00002	0	1
254	253	133	134	0.86	2E+11	0.00002	0	1
255	254	47	134	0.86	2E+11	0.00002	0	1
256	255	134	131	0.86	2E+11	0.00002	0	1
257	256	135	133	0.86	2E+11	0.00002	0	1
258	257	132	135	0.86	2E+11	0.00002	0	1
259	258	135	47	0.86	2E+11	0.00002	0	1
260	259	135	136	0.86	2E+11	0.00002	0	1
261	260	136	134	0.86	2E+11	0.00002	0	1
262	261	136	137	0.86	2E+11	0.00002	0	1
263	262	138	136	0.86	2E+11	0.00002	0	1
264	263	138	139	0.86	2E+11	0.00002	0	1
265	264	139	137	0.86	2E+11	0.00002	0	1
266	265	139	140	0.86	2E+11	0.00002	0	1
267	266	141	139	0.86	2E+11	0.00002	0	1

EXCEL SHEET FOR JOINT COORDINATES

1	Joint	X	Y	SETTLEMENT -X	SETTLEMENT -Y	CONC_FORCE_X	CONC_FORCE_Y	CONC_MOMENT_Z
2	1	0	0	0	0	0	-20000	0
3	2	5	0	0	0	0	-20000	0
4	3	2.5	4.33	0	0	4000	0	0
5	4	10	0	0	0	0	-20000	0
6	5	7.5	4.33	0	0	0	0	0
7	6	15	0	0	0	0	-20000	0
8	7	12.5	4.33	0	0	0	0	0
9	8	21	0	0	0	0	-20000	0
10	9	30	0	0	0	0	-20000	0
11	10	42	0	0	0	0	-20000	0
12	11	36	12	0	0	4000	0	0
13	12	2.5	0	0	0	0	-20000	0
14	13	7.5	0	0	0	0	-20000	0
15	14	12.5	0	0	0	0	-20000	0
16	15	18	0	0	0	0	-20000	0
17	16	36	0	0	0	0	-20000	0
18	17	18	5	0	0	4000	0	0
19	18	42	17	0	0	4000	0	0
20	19	25.5	7	0	0	4000	0	0
21	20	25.5	0	0	0	0	-20000	0
22	21	54	0	0	0	0	-35000	0
23	22	48	0	0	0	0	-35000	0
24	23	64	0	0	0	0	-20000	0
25	24	59	0	0	0	0	-35000	0
26	25	66.5	4.33	0	0	0	0	0
27	26	48	11	0	0	4000	0	0
28	27	59	5.5	0	0	4000	0	0
29	28	69	0	0	0	0	-20000	0
30	29	66.5	0	0	0	0	-20000	0
31	30	74	0	0	0	0	-20000	0
32	31	71.5	0	0	0	0	-20000	0
33	32	71.5	4.33	0	0	0	0	0
34	33	79	0	0	0	0	-20000	0
35	34	76.5	0	0	0	0	-20000	0
36	35	76.5	4.33	0	0	0	0	0
37	36	81.5	0	0	0	0	-20000	0

38	37	84	0	0	0	0	-20000	0
39	38	81.5	4.33	0	0	0	0	0
40	39	86.5	0	0	0	0	-20000	0
41	40	89	0	0	0	0	-20000	0
42	41	86.5	4.33	0	0	0	0	0
43	42	94	5.5	0	0	4000	0	0
44	43	94	0	0	0	0	-20000	0
45	44	99	0	0	0	0	-20000	0
46	45	105	11	0	0	4000	0	0
47	46	105	0	0	0	0	-20000	0
48	47	111	0	0	0	0	-20000	0
49	48	111	17	0	0	4000	0	0
50	49	117	12	0	0	4000	0	0
51	50	117	0	0	0	0	-20000	0
52	51	123	0	0	0	0	-20000	0
53	52	127.5	7	0	0	4000	0	0
54	53	127.5	0	0	0	0	-20000	0
55	54	132	0	0	0	0	-20000	0
56	55	135	5	0	0	4000	0	0
57	56	138	0	0	0	0	-20000	0
58	57	135	0	0	0	0	-20000	0
59	58	140.5	0	0	0	0	-20000	0
60	59	143	0	0	0	0	-20000	0
61	60	140.5	4.33	0	0	0	0	0
62	61	145.5	0	0	0	0	-20000	0
63	62	148	0	0	0	0	-20000	0
64	63	145.5	4.33	0	0	0	0	0
65	64	150.5	0	0	0	0	-20000	0
66	65	153	0	0	0	0	-20000	0
67	66	150.5	4.33	0	0	0	0	0
68	67	-2.5	0	0	0	0	-20000	0
69	68	-2.5	-2.5	0	0	0	0	0
70	69	0	-2.5	0	0	0	0	0
71	70	-5	-2.5	0	0	0	0	0
72	71	-5	0	0	0	0	-20000	0
73	72	-7.5	0	0	0	0	-20000	0
74	73	-7.5	-2.5	0	0	0	0	0

75	74	-10	-2.5	0	0	0	0	0
76	75	-10	0	0	0	0	-20000	0
77	76	32	4	0	0	0	0	0
78	77	40	4	0	0	0	0	0
79	78	44.4	4.4	0	0	0	0	0
80	79	51.6	4.4	0	0	0	0	0
81	80	108.6	4.4	0	0	0	0	0
82	81	101.4	4.4	0	0	0	0	0
83	82	113	4	0	0	0	0	0
84	83	121	4	0	0	0	0	0
85	84	-12.5	-2.5	0	0	0	0	0
86	85	-12.5	0	0	0	0	0	0
87	86	-15	-2.5	0	0	0	-20000	0
88	87	-15	0	0	0	0	0	0
89	88	155.5	-0.2	0	0	0	-20000	0
90	89	158	-0.4	0	0	-1595	-19936	0
91	90	160.5	-0.6	0	0	-1595	-19936	0
92	91	163	-0.8	0	0	-1595	-19936	0
93	92	165.5	-1	0	0	-1595	-19936	0
94	93	168	-1.2	0	0	-1595	-19936	0
95	94	170.5	-1.4	0	0	-1595	-19936	0
96	95	173	-1.6	0	0	-1595	-19936	0
97	96	175.5	-1.8	0	0	-1595	-19936	0
98	97	178	-2	0	0	-1595	-19936	0
99	98	180.5	-2.2	0	0	-1595	-19936	0
100	99	183	-2.4	0	0	-1595	-19936	0
101	100	152.8	-2.5	0	0	-1595	-19936	0
102	101	155.3	-2.7	0	0	0	0	0
103	102	157.8	-2.9	0	0	0	0	0
104	103	160.3	-3.1	0	0	0	0	0
105	104	162.8	-3.3	0	0	0	0	0
106	105	165.3	-3.5	0	0	0	0	0
107	106	167.8	-3.7	0	0	0	0	0
108	107	170.3	-3.9	0	0	0	0	0
109	108	172.8	-4.1	0	0	0	0	0
110	109	175.3	-4.3	0	0	0	0	0
111	110	177.8	-4.5	0	0	0	0	0

112	111	180.3	-4.7	0	0	0	0	0
113	112	182.8	-4.9	0	0	0	0	0
114	113	162.8	-3.3	0	0	0	0	0
115	114	36	-18	0	0	0	0	0
116	115	48	-18	0	0	0	0	0
117	116	42	-14	0	0	0	0	0
118	117	46.667	-14	0	0	0	0	0
119	118	37.333	-14	0	0	0	0	0
120	119	42	-10	0	0	0	0	0
121	120	38.667	-10	0	0	0	0	0
122	121	45.333	-10	0	0	0	0	0
123	122	42	-6	0	0	0	0	0
124	123	44	-6	0	0	0	0	0
125	124	40	-6	0	0	0	0	0
126	125	42	-3	0	0	0	0	0
127	126	43	-3	0	0	0	0	0
128	127	41	-3	0	0	0	0	0
129	128	105	-18	0	0	0	0	0
130	129	117	-18	0	0	0	0	0
131	130	111	-14	0	0	0	0	0
132	131	115.667	-14	0	0	0	0	0
133	132	106.333	-14	0	0	0	0	0
134	133	111	-10	0	0	0	0	0
135	134	114.333	-10	0	0	0	0	0
136	135	107.667	-10	0	0	0	0	0
137	136	111	-6	0	0	0	0	0
138	137	113	-6	0	0	0	0	0
139	138	109	-6	0	0	0	0	0
140	139	111	-3	0	0	0	0	0
141	140	112	-3	0	0	0	0	0
142	141	110	-3	0	0	0	0	0

CALCULATED VALUES OF AXIAL FORCE, SHEAR FORCE AND BENDING MOMENTS

F_x_NODEi - Axial Force

F_y_NODEi - Shear Force

M_z_NODEi - Bending Moment

A	B	C	D	E	F	G	H	I	
1	MEMBER_NUMBER	F_x_NODEi	F_y_NODEi	M_z_NODEi	F_x_NODEj	F_y_NODEj	M_z_NODEj	Length	Uniformly_distributed_Load
2	1	-60.01	0.05	0.08	60.01	-0.05	0.04	2.5	0
3	2	-60.02	-0.01	-0.02	60.02	0.01	0	2.5	0
4	3	-182.77	0.01	0.01	182.77	-0.01	0.01	2.5	0
5	4	-182.77	0	-0.01	182.77	0	0	2.5	0
6	5	-143.86	0	0	143.86	0	0.01	2.5	0
7	6	-143.85	-0.01	-0.01	143.85	0.01	0	2.5	0
8	7	80.55	0	-0.01	-80.55	0	0	3	0
9	8	80.55	0	-0.01	-80.55	0	0	3	0
10	9	700.39	0	0	-700.39	0	0	6	0
11	10	700.39	0	0	-700.39	0	-0.01	6	0
12	11	-59.95	-0.01	-0.02	59.95	0.01	-0.01	4.33	0
13	12	-59.99	0	0	59.99	0	0	4.33	0
14	13	-59.99	0	0.01	59.99	0	0.01	4.33	0
15	14	-60	0	0.01	60	0	0.01	5	0
16	15	-100	0	0	100	0	-0.01	12	0
17	16	1103.75	0	0	-1103.75	0	0	17	0
18	17	238.16	0.01	0.03	-238.16	-0.01	0.01	4.99989	0
19	18	76.55	0	0	-76.55	0	0	4.99989	0
20	19	-85.1	0	0	85.1	0	0	4.99989	0
21	20	-268.02	0	0	268.02	0	0	5.83095189	0
22	21	-168.94	0	0	168.94	0	0	4.99989	0
23	22	-7.28	0	0	7.28	0	0	4.99989	0
24	23	173	0	0	-173	0	0.01	4.99989	0
25	24	279.05	0	0.01	-279.05	0	0.01	5.83095189	0
26	25	429.37	0	-0.01	-429.37	0	-0.01	4.5	0
27	26	429.37	0	0	-429.37	0	0	4.5	0
28	27	-379.56	0	0	379.56	0	0	8.32165849	0
29	28	240.31	0	0.01	-240.31	0	0.01	8.32165849	0
30	29	-60.01	0	0.01	60.01	0	0.01	7	0
31	30	219.55	0	0	-219.55	0	0.01	5	0
32	31	261.47	0	0	-261.47	0	0	5	0
33	32	133.39	0	-0.01	-133.39	0	-0.01	5.54065881	0
34	33	-133.57	0	-0.01	133.57	0	-0.01	7.76208735	0
35	34	-492.06	0	-0.01	492.06	0	-0.02	11.6297033	0
36	35	-792.22	0.01	0.04	792.22	-0.01	0.04	7.81024968	0
37	36	-843.72	-0.01	-0.04	843.72	0.01	-0.04	8.48528137	0
38	37	483.54	0	0.01	-483.54	0	0.02	7.59071143	0
39	38	189.87	0	0.02	-189.87	0	0.01	12.5299641	0
40	39	-174.99	0	0	174.99	0	0	11	0
41	40	430.39	0.01	0.04	-430.39	-0.01	0.01	6	0

42	41	430.39	0	0	-430.39	0	0	6	0
43	42	-253.35	0	0.02	253.35	0	0.01	12.2983739	0
44	43	452.72	0	-0.01	-452.72	0	-0.01	7.43303437	0
45	44	-105	-0.01	-0.02	105	0.01	-0.02	5.5	0
46	45	-564.65	0	0	564.65	0	0	7.43303437	0
47	46	-133.22	0	0	133.22	0	0.01	5	0
48	47	-133.23	0.01	0.01	133.23	-0.01	0.01	5	0
49	48	390.07	0	-0.02	-390.07	0	0	4.99989	0
50	49	-234.74	0	-0.01	234.74	0	0	4.99989	0
51	50	-708.09	0.01	0	708.09	-0.01	0.02	2.5	0
52	51	-708.1	0	-0.01	708.1	0	0.01	2.5	0
53	52	-59.99	-0.01	-0.01	59.99	0.01	-0.01	4.33	0
54	53	-896.65	0.01	0	896.65	-0.01	0.02	2.5	0
55	54	-896.65	0	-0.01	896.65	0	0.01	2.5	0
56	55	142.35	0	-0.01	-142.35	0	0	4.99989	0
57	56	-59.99	0	-0.01	59.99	0	0	4.33	0
58	57	-73.08	0	-0.01	73.08	0	0	4.99989	0
59	58	790.18	0	0	-790.18	0	0.02	5	0
60	59	-923.54	0	-0.01	923.54	0	0.02	2.5	0
61	60	-923.54	-0.01	-0.02	923.54	0.01	0	2.5	0
62	61	-19.3	0	-0.01	19.3	0	0.01	4.99989	0
63	62	88.57	0	0	-88.57	0	0.01	4.99989	0
64	63	-59.99	0	0	59.99	0	0	4.33	0
65	64	897.9	0	-0.01	-897.9	0	0.01	5	0
66	65	-788.78	0	-0.01	788.78	0	0.01	2.5	0
67	66	-788.77	-0.01	-0.02	788.77	0.01	0	2.5	0
68	67	-180.95	0	0	180.95	0	0.01	4.99989	0
69	68	-59.99	0	0.01	59.99	0	0.01	4.33	0
70	69	250.22	0	0	-250.22	0	0.01	4.99989	0
71	70	843.97	0	-0.02	-843.97	0	0	5	0
72	71	-492.35	0	-0.01	492.35	0	0	2.5	0
73	72	-492.34	-0.01	-0.02	492.34	0.01	0	2.5	0
74	73	-342.61	0	0	342.61	0	0.01	4.99989	0
75	74	453.38	0.01	0.01	-453.38	-0.01	0.02	4.99989	0
76	75	-59.99	0.01	0.02	59.99	-0.01	0.02	4.33	0
77	76	628.37	-0.01	-0.02	-628.37	0.01	-0.01	5	0
78	77	-638.75	0	0	638.75	0	0	7.43303437	0
79	78	-60.01	0.01	0.02	60.01	-0.01	0.02	5.5	0
80	79	164.03	0	0	-164.03	0	0	5	0
81	80	378.2	0	0.01	-378.2	0	0.01	7.43303437	0
82	81	164.03	-0.01	-0.02	-164.03	0.01	-0.02	5	0
83	82	233.14	-0.01	-0.02	-233.14	0.01	-0.02	7.59071143	0
84	83	-409.89	0	0	409.89	0	-0.01	12.5299641	0
85	84	-99.99	0	0	99.99	0	-0.01	11	0

86	85	614.71	-0.01	0	-614.71	0.01	-0.03	6	0
87	86	49.17	0	-0.02	-49.17	0	-0.02	12.5299641	0
88	87	614.71	0	0	-614.71	0	0	6	0
89	88	-484.92	0	-0.01	484.92	0	-0.02	12.2983739	0
90	89	1151.48	0	0	-1151.48	0	0	17	0
91	90	-895.96	0.01	0.05	895.96	-0.01	0.04	8.48528137	0
92	91	-809.07	-0.01	-0.04	809.07	0.01	-0.04	7.81024968	0
93	92	-100	0	0	100	0	0.01	12	0
94	93	377.66	0	0	-377.66	0	0	6	0
95	94	377.66	0	0.02	-377.66	0	0	6	0
96	95	219.19	0	0	-219.19	0	0	8.32165849	0
97	96	-488.58	0	0.02	488.58	0	0.01	11.6297033	0
98	97	-60	0	-0.01	60	0	-0.01	7	0
99	98	126.95	0	0	-126.95	0	0	4.5	0
100	99	126.94	0	0.01	-126.94	0	0.01	4.5	0
101	100	-364.06	0	0	364.06	0	0	8.32165849	0
102	101	263.84	0	-0.01	-263.84	0	0	5.83095189	0
103	102	-109.41	0	0.01	109.41	0	0.01	7.76208735	0
104	103	-252.29	0	0	252.29	0	0	5.83095189	0
105	104	-205.67	0	0	205.67	0	0	3	0
106	105	-205.67	0.01	0.01	205.67	-0.01	0.01	3	0
107	106	-60	0	-0.01	60	0	-0.01	5	0
108	107	-414.19	0.01	0.01	414.19	-0.01	0.02	2.5	0
109	108	-414.2	0	-0.01	414.2	0	0	2.5	0
110	109	157.42	0	-0.01	-157.42	0	0	4.99989	0
111	110	-59.99	0	-0.01	59.99	0	0	4.33	0
112	111	-62.86	0	0	62.86	0	0	4.99989	0
113	112	181.16	0	0.01	-181.16	0	0.01	5.54065881	0
114	113	-430.87	0.01	0	430.87	-0.01	0.01	2.5	0
115	114	-430.86	-0.01	-0.02	430.86	0.01	0	2.5	0
116	115	-29.52	0	0	29.52	0	0	4.99989	0
117	116	-59.99	0	0	59.99	0	0	4.33	0
118	117	98.79	0	0	-98.79	0	0.01	4.99989	0
119	118	289.99	0	0	-289.99	0	0.01	5	0
120	119	-285.88	0	0	285.88	0	0	2.5	0
121	120	-285.88	0	-0.01	285.88	0	0	2.5	0
122	121	-191.17	0	0	191.17	0	0	4.99989	0
123	122	-60	0	0.01	60	0	0	4.33	0
124	123	260.46	0	0	-260.46	0	0.01	4.99989	0
125	124	225.83	0	-0.01	-225.83	0	-0.01	5	0
126	125	59.04	-0.04	-0.03	-59.04	0.04	-0.07	2.5	0
127	126	0	0.01	0.02	0	-0.01	0.02	2.5	0
128	127	-242.49	-0.01	-0.02	242.49	0.01	0	2.5	0
129	128	286.34	-0.02	-0.01	-286.34	0.02	-0.05	2.5	0

130	129	259.44	0	0	-259.44	0	0.01	3.53553391	0
131	130	-118.07	0	0	118.07	0	0.01	3.53553391	0
132	131	-242.51	0	-0.01	242.51	0	0	2.5	0
133	132	326	0	-0.01	-326	0	0	2.5	0
134	133	60	0	0.01	-60	0	0.01	2.5	0
135	134	33.23	0	-0.01	-33.23	0	0	3.53553391	0
136	135	326	0	-0.01	-326	0	0.01	2.5	0
137	136	0.01	0	0	-0.01	0	0	2.5	0
138	137	-349.5	0	-0.01	349.5	0	0	2.5	0
139	138	-349.5	0.01	0	349.5	-0.01	0.01	2.5	0
140	139	108.18	0	0	-108.18	0	0.01	3.53553391	0
141	140	273	0	0	-273	0	0.01	2.5	0
142	141	59.99	-0.01	-0.01	-59.99	0.01	-0.01	2.5	0
143	142	-315.44	-0.01	-0.01	315.44	0.01	-0.01	4.47213595	0
144	143	-315.44	0	0	315.44	0	-0.01	8.94427191	0
145	144	0	0	0.01	0	0	0.01	5.65685425	0
146	145	96.76	0	-0.01	-96.76	0	0	8.94427191	0
147	146	96.76	0	0.01	-96.76	0	0	4.47213595	0
148	147	0	0	0	0	0	0	5.65685425	0
149	148	0	0	0	0	0	0	5.68506816	0
150	149	0	0	-0.01	0	0	-0.01	5.68506816	0
151	150	-541.05	0	0.01	541.05	0	0	7.51797845	0
152	151	-541.04	0	0.01	541.04	0	0.01	5.01198563	0
153	152	0	0	0	0	0	0	5.68506816	0
154	153	0	0	0	0	0	0	5.68506816	0
155	154	63.16	0	0.01	-63.16	0	0	4.47213595	0
156	155	63.16	0	0	-63.16	0	0.01	8.94427191	0
157	156	0	0	0	0	0	0	5.65685425	0
158	157	-295.58	0	0.01	295.58	0	0	8.94427191	0
159	158	-295.58	0	0.01	295.58	0	0	4.47213595	0
160	159	0	0	-0.01	0	0	-0.01	5.65685425	0
161	160	-136.51	0.01	0.01	136.51	-0.01	0.02	2.5	0
162	161	272.99	0.01	0.01	-272.99	-0.01	0.02	2.5	0
163	162	0	-0.01	-0.02	0	0.01	-0.02	2.5	0
164	163	-193.02	0	0	193.02	0	0	3.53553391	0
165	164	-136.49	0.01	0.01	136.49	-0.01	0.01	2.5	0
166	165	-196.49	-0.01	-0.01	196.49	0.01	-0.02	2.5	0
167	166	0.01	0.01	0.02	-0.01	-0.01	0.02	2.5	0
168	167	193.01	0	0	-193.01	0	0	3.53553391	0
169	168	-130.82	-0.05	-0.06	130.82	0.05	-0.07	2.50798724	0
170	169	-198.42	0.04	0.06	198.42	-0.04	0.04	2.50798724	0
171	170	-198.39	-0.01	0	198.39	0.01	-0.02	2.50798724	0
172	171	184.43	0.04	0.06	-184.43	-0.04	0.04	2.50798724	0
173	172	184.43	-0.02	-0.03	-184.43	0.02	-0.01	2.50798724	0

174	173	-87.76	-0.01	-0.01	87.76	0.01	-0.01	2.50798724	0
175	174	-87.78	-0.01	-0.02	87.78	0.01	-0.02	2.50798724	0
176	175	-679.93	-0.03	-0.02	679.93	0.03	-0.05	2.50798724	0
177	176	-679.94	0.03	0.05	679.94	-0.03	0.02	2.50798724	0
178	177	-180	0.01	0.02	180	-0.01	0.01	2.50798724	0
179	178	-179.99	0.01	0.01	179.99	-0.01	0.01	2.50798724	0
180	179	0	0	0	0	0	0	2.50798724	0
181	180	316.95	0.04	0.05	-316.95	-0.04	0.04	2.50798724	0
182	181	777.98	0	0	-777.98	0	0	2.50798724	0
183	182	376.92	-0.06	-0.06	-376.92	0.06	-0.09	2.50798724	0
184	183	-533	0	0.01	533	0	-0.01	3.54682957	0
185	184	542.82	0.06	0.09	-542.82	-0.06	0.06	2.50798724	0
186	185	59.95	-0.03	-0.04	-59.95	0.03	-0.04	2.50798724	0
187	186	-426.12	0.01	0.02	426.12	-0.01	0	3.54682957	0
188	187	0.04	0	0	-0.04	0	0	2.50798724	0
189	188	-0.02	-0.04	-0.05	0.02	0.04	-0.06	2.50798724	0
190	189	341.44	-0.01	-0.02	-341.44	0.01	-0.03	3.54682957	0
191	190	0	0.02	0.05	0	-0.02	0	2.50798724	0
192	191	59.94	-0.01	-0.01	-59.94	0.01	-0.01	2.50798724	0
193	192	-199.89	0.02	0.04	199.89	-0.02	0.03	3.54682957	0
194	193	-41.85	-0.01	-0.01	41.85	0.01	0	2.50798724	0
195	194	0	0.01	0.02	0	-0.01	0.02	2.50798724	0
196	195	-121.75	0	-0.01	121.75	0	0	3.54682957	0
197	196	-41.84	-0.01	-0.01	41.84	0.01	-0.01	2.50798724	0
198	197	263.18	0	0	-263.18	0	0	3.54682957	0
199	198	59.99	0.02	0.02	-59.99	-0.02	0.02	2.50798724	0
200	199	390.36	-0.01	-0.01	-390.36	0.01	-0.02	2.50798724	0
201	200	0.02	0.03	0.04	-0.02	-0.03	0.04	2.50798724	0
202	201	-348.01	0	0	348.01	0	0	3.54682957	0
203	202	489.37	-0.01	0	-489.37	0.01	-0.02	3.54682957	0
204	203	390.39	-0.03	-0.02	-390.39	0.03	-0.06	2.50798724	0
205	204	60.06	0	0	-60.06	0	0	2.50798724	0
206	205	380.01	0.03	0.05	-380.01	-0.03	0.02	2.50798724	0
207	206	379.98	0.01	0.01	-379.98	-0.01	0.01	2.50798724	0
208	207	40.01	0.01	0.01	-40.01	-0.01	0.01	2.50798724	0
209	208	40	0	0	-40	0	0	2.50798724	0
210	209	40	0	0	-40	0	0	2.50798724	0
211	210	424.17	0.01	0.02	-424.17	-0.01	0	3.54682957	0
212	211	-282.81	0	0	282.81	0	0	3.54682957	0
213	212	197.96	0	0	-197.96	0	0	3.54682957	0
214	213	-56.56	0	0	56.56	0	0	3.54682957	0
215	214	0.02	-0.03	-0.04	-0.02	0.03	-0.03	2.50798724	0
216	215	59.99	-0.01	-0.02	-59.99	0.01	-0.02	2.50798724	0
217	216	0.01	-0.01	-0.01	-0.01	0.01	-0.01	2.50798724	0

APPENDIX

MATLAB CODE

```
% Initialize workspace
clear; clc;

% Define scale factor for plotting
applied_scale_factor = 2000;

% Specify restrained degrees of freedom (DOFs)
restrained_dofs = [205, 206, 260, 301, 302, 311, 323, 338, 344, 346, 347, 386, 388, 389];

% Read joint coordinates and member connectivity from Excel
Node_Coordinates = xlsread("DRSR.xlsx", "Joint Coordinates1");
Member_Connectivity = xlsread("DRSR.xlsx", "Member Connectivity1");

% Get the number of joints and members
[num_joints, ~] = size(Node_Coordinates);
[num_members, ~] = size(Member_Connectivity);

% Initialize global stiffness matrix and force vectors
K_global = zeros(3 * num_joints);
fixed_end_forces = zeros(3 * num_joints, 1);
nodal_forces = zeros(3 * num_joints, 1);
settlements = zeros(3 * num_joints, 1);

% Assemble global stiffness matrix and load vectors
for member = 1:num_members
    % Extract member properties
    area = Member_Connectivity(member, 4);
    elasticity = Member_Connectivity(member, 5);
    inertia = Member_Connectivity(member, 6);
    load_w = Member_Connectivity(member, 7);
    joint_case = Member_Connectivity(member, 8);
    node_i = Member_Connectivity(member, 2);
    node_j = Member_Connectivity(member, 3);

    % Extract settlements
    settlement_x_i = Node_Coordinates(node_i, 4);
    settlement_y_i = Node_Coordinates(node_i, 5);
    settlement_x_j = Node_Coordinates(node_j, 4);
    settlement_y_j = Node_Coordinates(node_j, 5);
```

```

% Extract concentrated forces and moments
conc_force_x_i = Node_Coordinates(node_i, 6);
conc_force_y_i = Node_Coordinates(node_i, 7);
conc_moment_z_i = Node_Coordinates(node_i, 8);
conc_force_x_j = Node_Coordinates(node_j, 6);
conc_force_y_j = Node_Coordinates(node_j, 7);
conc_moment_z_j = Node_Coordinates(node_j, 8);

% Coordinates of nodes
x_i = Node_Coordinates(node_i, 2);
y_i = Node_Coordinates(node_i, 3);
x_j = Node_Coordinates(node_j, 2);
y_j = Node_Coordinates(node_j, 3);

% Calculate member length and orientation
member_length = sqrt((x_j - x_i)^2 + (y_j - y_i)^2);
cos_theta = (x_j - x_i) / member_length;
sin_theta = (y_j - y_i) / member_length;

% Determine local stiffness matrix and fixed-end forces based on joint case
switch joint_case
    case 1
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
             0, 12, 6 * member_length, 0, -12, 6 * member_length;
             0, 6 * member_length, 4 * member_length^2, 0, -6 * member_length, 2 * member_length^2;
             -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
             0, -12, -6 * member_length, 0, 12, -6 * member_length;
             0, 6 * member_length, 2 * member_length^2, 0, -6 * member_length, 4 * member_length^2];
        Q = [0; (load_w * member_length) / 2; (load_w * member_length^2) / 12; 0; (load_w * member_length) / 2; -(load_w * member_length^2) / 12];
    case 2
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
             0, 3, 0, 0, -3, 3 * member_length;
             0, 0, 0, 0, 0, 0;
             -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
             0, -3, 0, 0, 3, -3 * member_length;
             0, 3 * member_length, 0, 0, -3 * member_length, 3 * member_length^2];
        Q = [0; (load_w * member_length) / 2 - (1.5 / member_length) * (load_w * member_length^2) / 12; 0; 0; (load_w * member_length) / 2 + (1.5 / member_length) * (load_w * member_length^2) / 12; -load_w * member_length^2 / 12 - 0.5 * (load_w * member_length^2) / 12];
    case 3
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
             0, 3, 3 * member_length, 0, -3, 0;
             0, 3 * member_length, 3 * member_length^2, 0, -3 * member_length, 0;
             -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
             0, -3, -3 * member_length, 0, 3, 0;
             0, 0, 0, 0, 0, 0];
        Q = [0; (load_w * member_length) / 2 - (1.5 / member_length) * (-load_w * member_length^2) / 12; (load_w * member_length^2) / 12 - 0.5 * (-load_w * member_length^2) / 12; 0;
             (load_w * member_length) / 2 + (1.5 / member_length) * (-load_w * member_length^2) / 12; 0];
    case 4
        kloc = (elasticity * area) / member_length * ...
            [1, 0, 0, -1, 0, 0;
             0, 0, 0, 0, 0, 0;
             0, 0, 0, 0, 0, 0;
             -1, 0, 0, 1, 0, 0;
             0, 0, 0, 0, 0, 0;
             0, 0, 0, 0, 0, 0];
        Q = [0; (load_w * member_length) / 2; 0; 0; (load_w * member_length) / 2; 0];
otherwise
    error('Invalid joint case specified.');
end

% Transformation matrix
T = [cos_theta, sin_theta, 0, 0, 0, 0;
      -sin_theta, cos_theta, 0, 0, 0, 0;
      0, 0, 1, 0, 0, 0;
      0, 0, 0, cos_theta, sin_theta, 0;
      0, 0, 0, -sin_theta, cos_theta, 0;
      0, 0, 0, 0, 0, 1];

% Global stiffness matrix for the member
k_global_member = T' * kloc * T;

% Global DOF indices
global_dof = [3 * (node_i - 1) + 1, 3 * (node_i - 1) + 2, 3 * (node_i - 1) + 3, 3 * (node_j - 1) + 1, 3 * (node_j - 1) + 2, 3 * (node_j - 1) + 3];

% Assemble into global stiffness matrix
K_global(global_dof, global_dof) = K_global(global_dof, global_dof) + k_global_member;

% Account for settlements
delta = zeros(6, 1);
delta(1) = settlement_x_i;
delta(2) = settlement_y_i;
delta(4) = settlement_x_j;
delta(5) = settlement_y_j;
settlements(global_dof([1, 2, 4, 5])) = [settlement_x_i; settlement_y_i; settlement_x_j; settlement_y_j];
z = k_global_member * delta;
fixed_end = T' * Q + z;

% Assemble fixed-end forces
fixed_end_forces(global_dof) = fixed_end_forces(global_dof) + fixed_end;

```

```

% Assemble nodal forces
nodal_forces(global_dof) = nodal_forces(global_dof) + [conc_force_x_i; conc_force_y_i; conc_moment_z_i; conc_force_x_j; conc_force_y_j; conc_moment_z_j];
end

% Apply boundary conditions by removing restrained DOFs
K_reduced = K_global;
nodal_forces_reduced = nodal_forces;
fixed_end_forces_reduced = fixed_end_forces;

for idx = 1:length(restrained_dofs)
    dof = restrained_dofs(idx) - (idx - 1);
    K_reduced(dof, :) = [];
    K_reduced(:, dof) = [];
    nodal_forces_reduced(dof) = [];
    fixed_end_forces_reduced(dof) = [];
end

% Solve for displacements
displacements_reduced = K_reduced \ (nodal_forces_reduced - fixed_end_forces_reduced);

% Reconstruct full displacement vector including restrained DOFs
displacements_full = zeros(3 * num_joints, 1);
free_dofs = setdiff(1:3 * num_joints, restrained_dofs);
displacements_full(free_dofs) = displacements_reduced;
displacements_full = displacements_full + settlements;

% Write member forces to Excel
headers = ["MEMBER_NUMBER", "F_x_NODEi", "F_y_NODEi", "M_z_NODEi", "F_x_NODEj", "F_y_NODEj", "M_z_NODEj", "Length", "Uniformly_distributed_Load"];
writematrix(headers, 'Output DRSR.xlsx', 'Range', 'A1');

for member = 1:num_members
    % Extract member properties
    area = Member_Connectivity(member, 4);
    elasticity = Member_Connectivity(member, 5);
    inertia = Member_Connectivity(member, 6);
    load_w = Member_Connectivity(member, 7);
    joint_case = Member_Connectivity(member, 8);
    node_i = Member_Connectivity(member, 2);
    node_j = Member_Connectivity(member, 3);

    % Coordinates of nodes
    x_i = Node_Coordinates(node_i, 2);
    y_i = Node_Coordinates(node_i, 3);
    x_j = Node_Coordinates(node_j, 2);
    y_j = Node_Coordinates(node_j, 3);

```

```

% Calculate member length and orientation
member_length = sqrt((x_j - x_i)^2 + (y_j - y_i)^2);
cos_theta = (x_j - x_i) / member_length;
sin_theta = (y_j - y_i) / member_length;

% Determine local stiffness matrix and fixed-end forces based on joint case
switch joint_case
    case 1
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
            0, 12, 6 * member_length, 0, -12, 6 * member_length;
            0, 6 * member_length, 4 * member_length^2, 0, -6 * member_length, 2 * member_length^2;
            -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
            0, -12, -6 * member_length, 0, 12, -6 * member_length;
            0, 6 * member_length, 2 * member_length^2, 0, -6 * member_length, 4 * member_length^2];
        Q = [0; (load_w * member_length) / 2; (load_w * member_length^2) / 12; 0; (load_w * member_length) / 2; -(load_w * member_length^2) / 12];
    case 2
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
            0, 3, 0, 0, -3, 3 * member_length;
            0, 0, 0, 0, 0, 0;
            -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
            0, -3, 0, 0, 3, -3 * member_length;
            0, 3 * member_length, 0, 0, -3 * member_length, 3 * member_length^2];
        Q = [0; (load_w * member_length) / 2 - (1.5 / member_length) * (load_w * member_length^2) / 12; 0; 0; (load_w * member_length) / 2 + (1.5 / member_length) * (load_w * member_length^2) / 12; - (load_w * member_length^2) / 12 - 0.5 * (load_w * member_length^2) / 12];
    case 3
        kloc = ((inertia * elasticity) / member_length^3) * ...
            [(area * member_length^2) / inertia, 0, 0, -(area * member_length^2) / inertia, 0, 0;
            0, 3, 3 * member_length, 0, -3, 0;
            0, 3 * member_length, 3 * member_length^2, 0, -3 * member_length, 0;
            -(area * member_length^2) / inertia, 0, 0, (area * member_length^2) / inertia, 0, 0;
            0, -3, -3 * member_length, 0, 3, 0;
            0, 0; (load_w * member_length) / 2 - (1.5 / member_length) * (-load_w * member_length^2) / 12; (load_w * member_length^2) / 12 - 0.5 * (-load_w * member_length^2) / 12; 0];
        Q = [0; (load_w * member_length) / 2 + (1.5 / member_length) * (-load_w * member_length^2) / 12; 0];
    case 4
        kloc = (elasticity * area) / member_length * ...
            [1, 0, 0, -1, 0, 0;
            0, 0, 0, 0, 0, 0;
            0, 0, 0, 0, 0, 0;
            -1, 0, 0, 1, 0, 0;
            0, 0, 0, 0, 0, 0;
            0, 0, 0, 0, 0, 0];
        Q = [0; (load_w * member_length) / 2; 0; 0; (load_w * member_length) / 2; 0];
    otherwise
        error('Joint case not supported');
end

% Transformation matrix
T = [cos_theta, sin_theta, 0, 0, 0, 0;
     -sin_theta, cos_theta, 0, 0, 0, 0;
     0, 0, 1, 0, 0, 0;
     0, 0, 0, cos_theta, sin_theta, 0;
     0, 0, 0, -sin_theta, cos_theta, 0;
     0, 0, 0, 0, 0, 1];

% Global DOF indices
global_dof = [3 * (node_i - 1) + 1, 3 * (node_i - 1) + 2, 3 * (node_i - 1) + 3, 3 * (node_j - 1) + 1, 3 * (node_j - 1) + 2, 3 * (node_j - 1) + 3];

% Extract displacements for member DOFs
displacements_member = displacements_full(global_dof);

% Compute member end forces
member_end_forces = kloc * (T * displacements_member) + Q;

% Prepare data for writing
member_forces_output = round(0.001 * member_end_forces, 2);
data_row = {member, member_forces_output(1), member_forces_output(2), member_forces_output(3), member_forces_output(4), member_forces_output(5), member_forces_output(6),
           member_length, load_w};

% Write data to Excel
writecell(data_row, 'Output DRSR.xlsx', 'Range', strcat('A', num2str(member + 1)));
end

% Plot undeformed and deformed structures
x_coords_undeformed = Node_Coordinates(:, 2);
y_coords_undeformed = Node_Coordinates(:, 3);
x_coords_deformed = x_coords_undeformed + displacements_full(1:3:end) * applied_scale_factor;
y_coords_deformed = y_coords_undeformed + displacements_full(2:3:end) * applied_scale_factor;

figure;
hold on;
for member = 1:num_members
    node_i = Member_Connectivity(member, 2);
    node_j = Member_Connectivity(member, 3);

```

```
% Plot undeformed member
plot([x_coords_undeformed(node_i), x_coords_undeformed(node_j)], [y_coords_undeformed(node_i), y_coords_undeformed(node_j)], 'r');

% Plot deformed member
plot([x_coords_deformed(node_i), x_coords_deformed(node_j)], [y_coords_deformed(node_i), y_coords_deformed(node_j)], 'g');

end
hold off;
legend('Undeformed', 'Deformed');
title('Structural Deformation');
xlabel('X Coordinate');
ylabel('Y Coordinate');
disp('The deformed and undeformed structures have been plotted. The deformation is scaled for visibility.');
fprintf('The deformed shape has been exaggerated %d times for visualization purposes.\n', applied_scale_factor);
```

THANK YOU