

# NFA-to-DFA conversion

Slides from

<http://web.cecs.pdx.edu/~harry/compilers/slides/LexicalPart3.pdf>

# Two ways to deal with an NFA

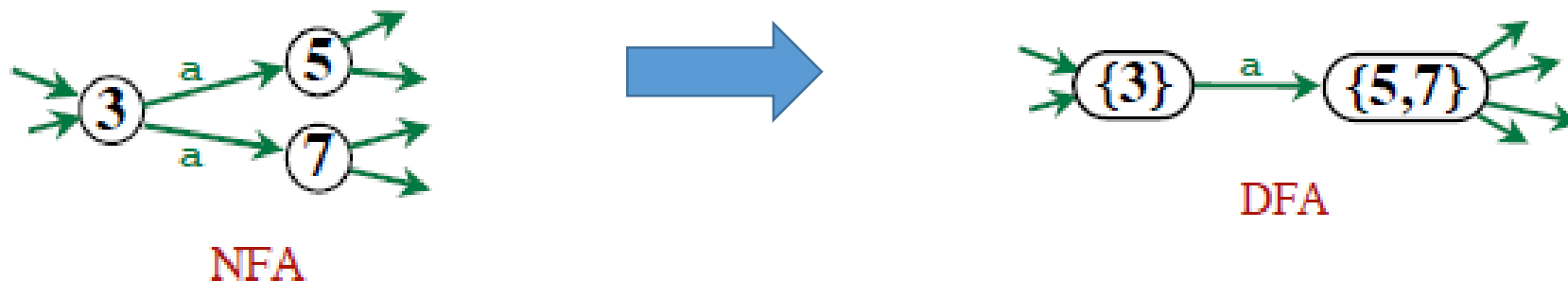
- Use the NFA directly
- Convert the NFA to an equivalent DFA first

# Use NFA directly

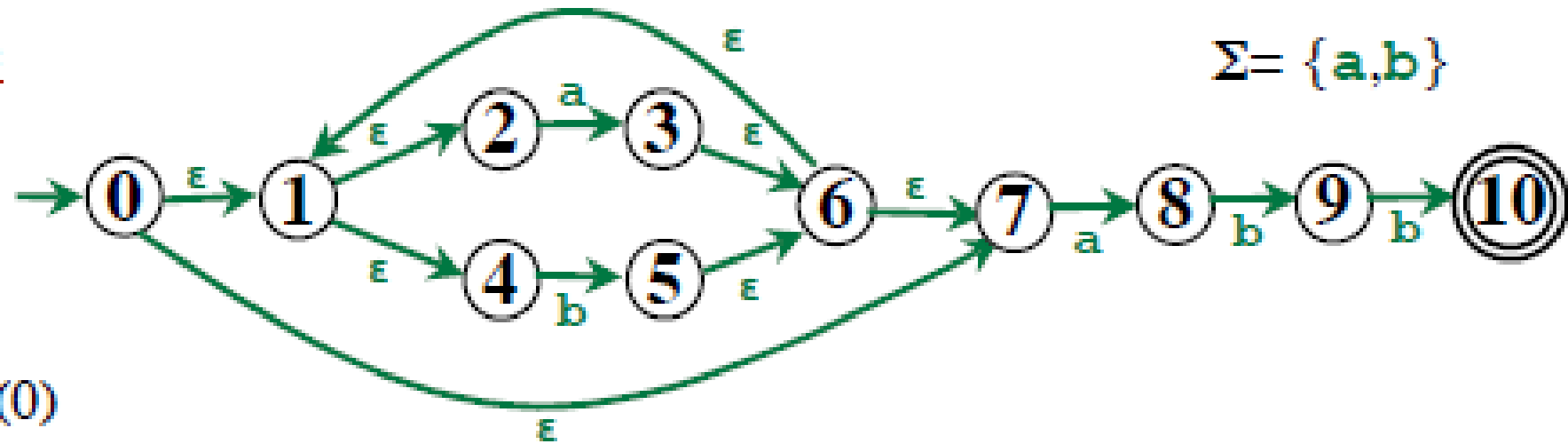
- Your code will keep track of “current search states”. Once you reach the end of the input symbol sequence, check one of the current search states is a final state.
- Note that you do not need to enumerate all possible paths explicitly. You just need to keep track of multiple current search states.
- The method is explained in Section 2.2.5 in Jurasfsky & Martin (2<sup>nd</sup> edition).

# Converting an NFA to an equivalent DFA

- Input: an NFA
- Output: a DFA, which is equivalent
- Idea: Each state in the DFA corresponds to a set of NFA states



## Example

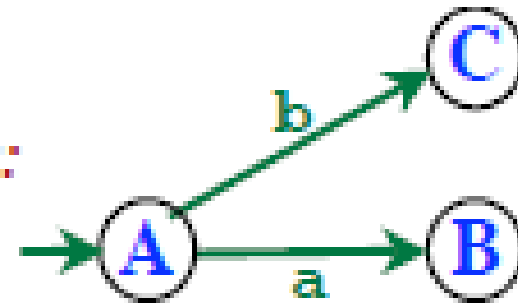


Start state:

$$\begin{aligned} &\epsilon\text{-Closure}(0) \\ &= \{0, 1, 2, 4, 7\} = A \end{aligned}$$

$$\begin{aligned} &\text{Move}_{\text{DFA}}(A, a) \\ &= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, a)) \\ &= \epsilon\text{-Closure}(\{3, 8\}) \\ &= \{1, 2, 3, 4, 6, 7, 8\} = B \end{aligned}$$

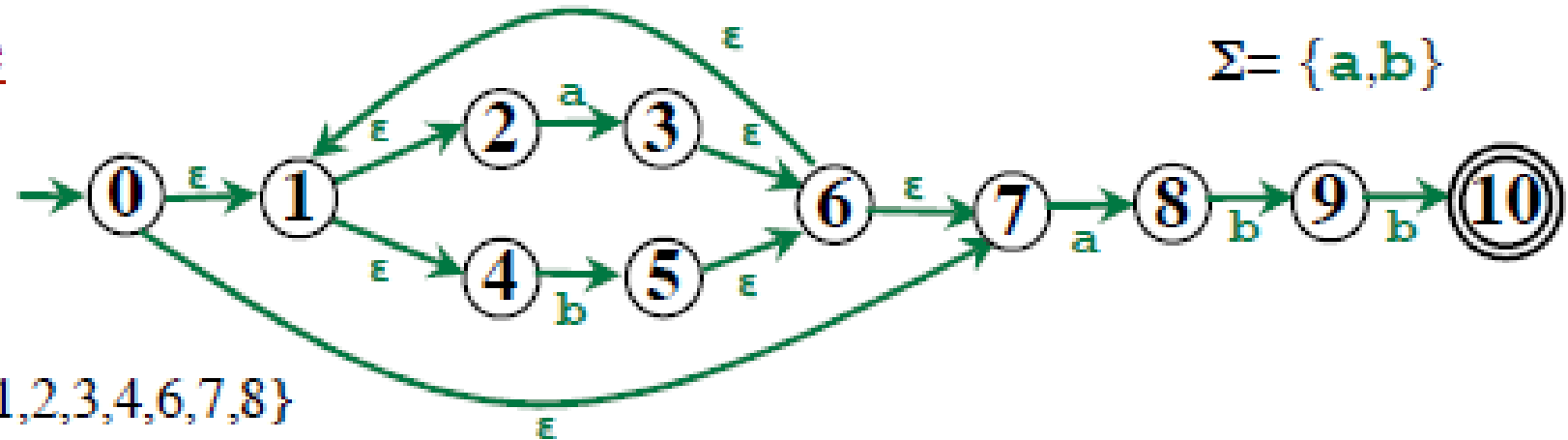
*So far:*



$$\begin{aligned} &\text{Move}_{\text{DFA}}(A, b) \\ &= \epsilon\text{-Closure}(\text{Move}_{\text{NFA}}(A, b)) \\ &= \epsilon\text{-Closure}(\{5\}) \\ &= \{1, 2, 4, 5, 6, 7\} = C \end{aligned}$$

A is now done; mark it!  
B and C are unmarked.  
Let's do B next...

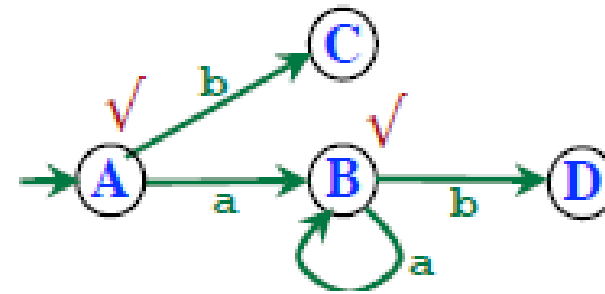
## Example



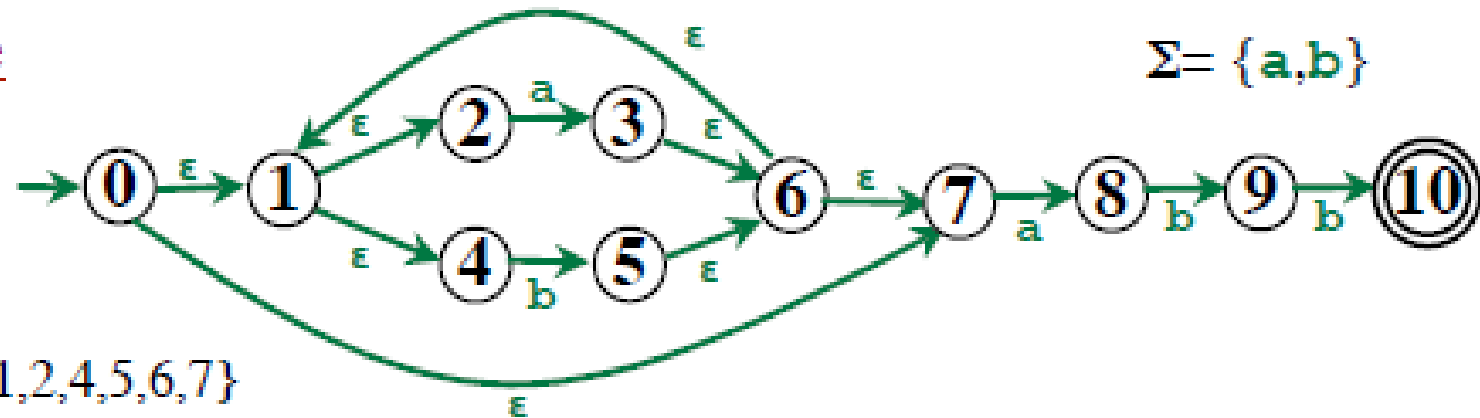
Process  $B = \{1, 2, 3, 4, 6, 7, 8\}$

$\text{Move}_{\text{DFA}}(B, a)$   
=  $\epsilon$ -Closure ( $\text{Move}_{\text{NFA}}(B, a)$ )  
=  $\epsilon$ -Closure ( $\{3, 8\}$ )  
=  $\{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(B, b)$   
=  $\epsilon$ -Closure ( $\text{Move}_{\text{NFA}}(B, b)$ )  
=  $\epsilon$ -Closure ( $\{5, 9\}$ )  
=  $\{1, 2, 4, 5, 6, 7, 9\} = D$



## Example



Process  $C = \{1, 2, 4, 5, 6, 7\}$

$\text{Move}_{\text{DFA}}(C, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(C, b) = \{1, 2, 4, 5, 6, 7\} = C$

Process  $E = \{1, 2, 4, 5, 6, 7, 10\}$

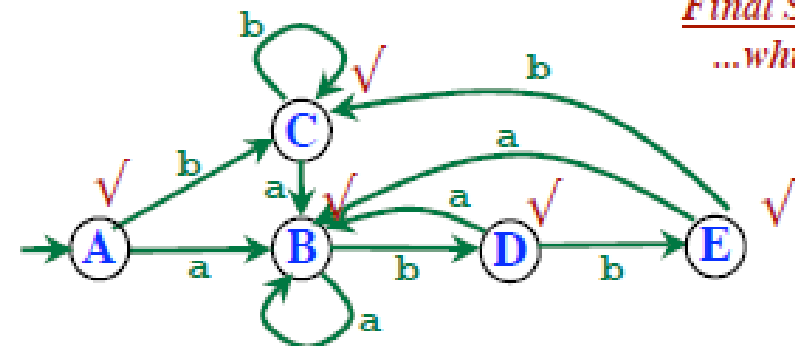
$\text{Move}_{\text{DFA}}(E, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(E, b) = \{1, 2, 4, 5, 6, 7\} = C$

Process  $D = \{1, 2, 4, 5, 6, 7, 9\}$

$\text{Move}_{\text{DFA}}(D, a) = \{1, 2, 3, 4, 6, 7, 8\} = B$

$\text{Move}_{\text{DFA}}(D, b) = \{1, 2, 4, 5, 6, 7, 10\} = E$



Final States in DFA?

...which state(s) contain 10?

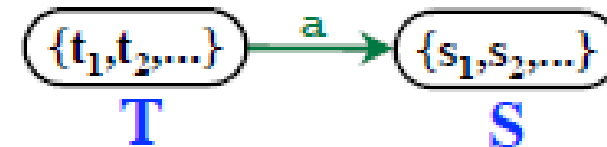
## Algorithm: Convert NFA to DFA

```
 $S_{DFA} = \{\}$   
Add  $\epsilon$ -Closure( $s_0$ ) to  $S_{DFA}$  as the start state  
Set the only state in  $S_{DFA}$  to "unmarked"  
while  $S_{DFA}$  contains an unmarked state do  
  Let  $T$  be that unmarked state  
  Mark  $T$   
  for each  $a$  in  $\Sigma$  do  
     $S = \epsilon$ -Closure(MoveNFA( $T, a$ ))  
    if  $S$  is not in  $S_{DFA}$  already then  
      Add  $S$  to  $S_{DFA}$  (as an "unmarked" state)  
    endif  
    Set MoveDFA( $T, a$ ) to  $S$   
  endFor  
endWhile  
for each  $S$  in  $S_{DFA}$  do  
  if any  $s \in S$  is a final state in the NFA then  
    Mark  $S$  as a final state in the DFA  
  endif  
endFor
```

*A set of NFA states*

*Everywhere you could possibly get to on an  $a$*

*i.e., add an edge to the DFA...*





# More examples

- <https://www.youtube.com/watch?v=U71roXRINlg>
- <https://www.youtube.com/watch?v=--CSVsFIDng>
- <https://www.youtube.com/watch?v=WSGcmaHNBFM>