



Deep Neural Network Compression

Cosimo Rulli
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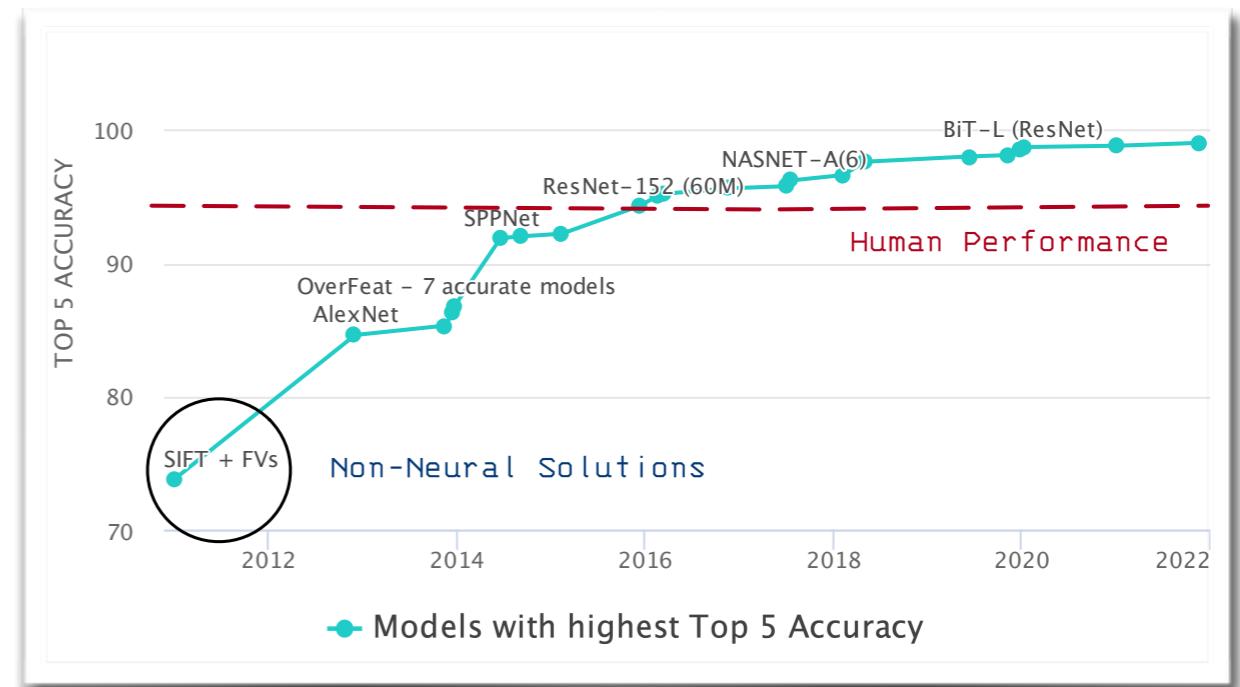
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Supervisors

Franco Maria Nardini and Rossano Venturini

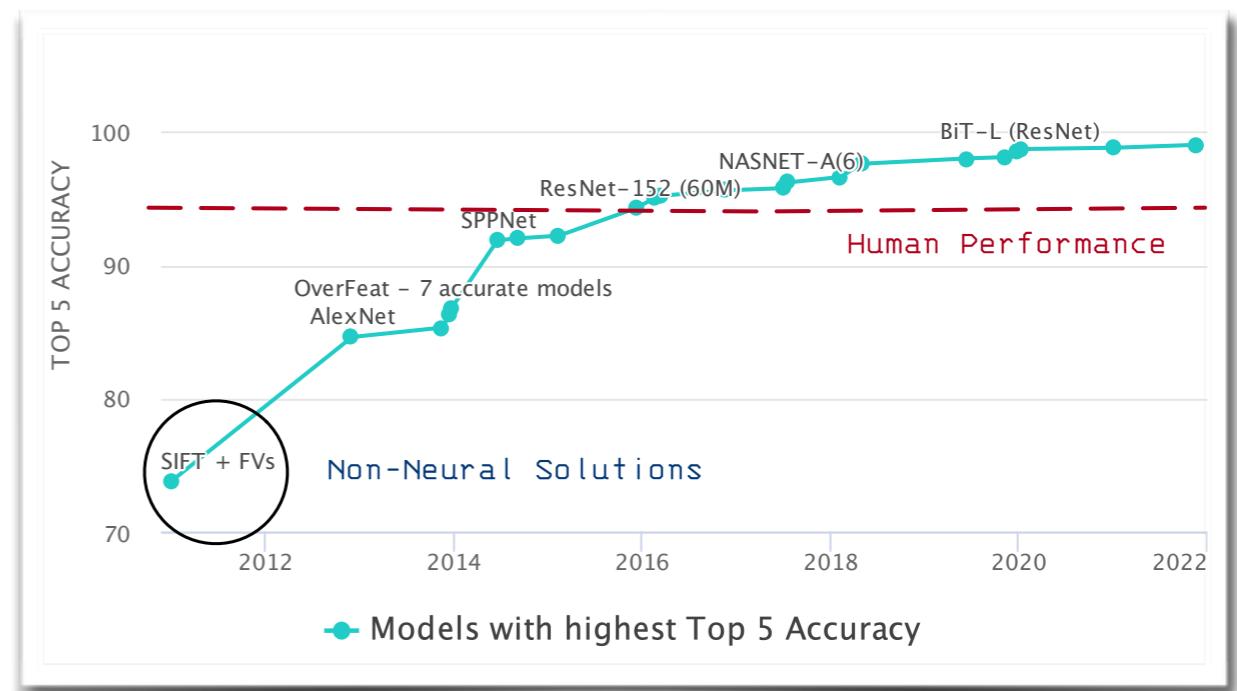
Deep Neural Networks..

- **Leading AI solution, unprecedented and super-human performance**



Deep Neural Networks..

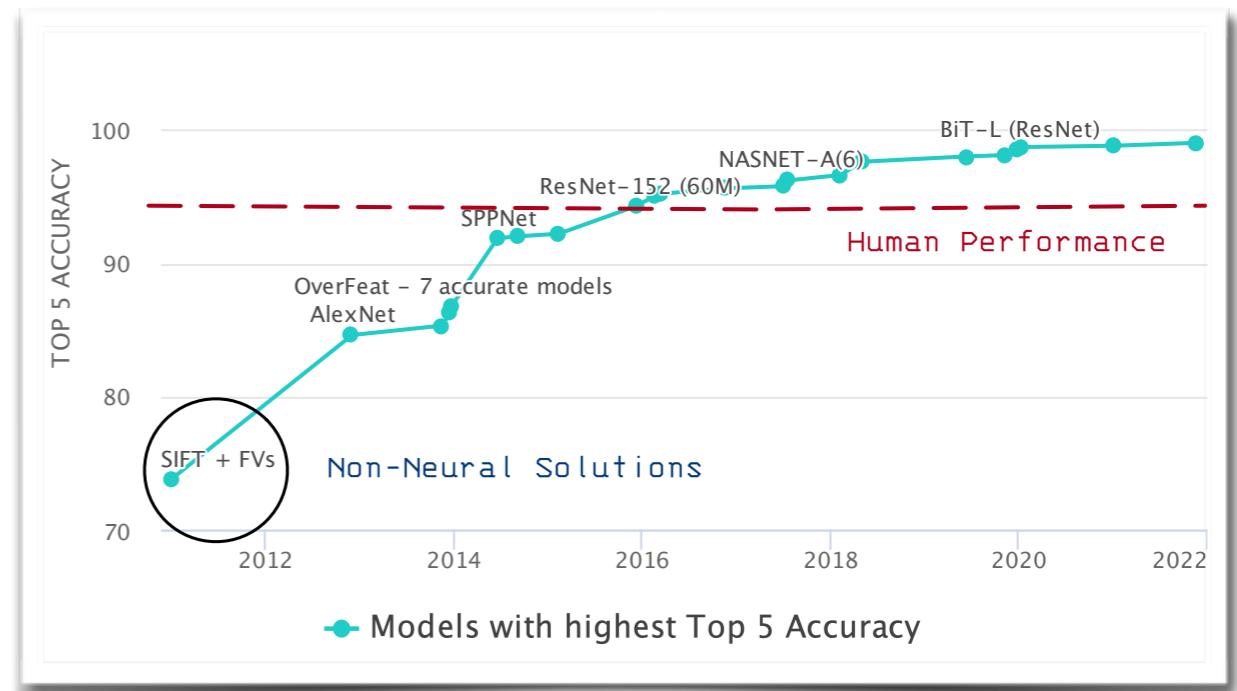
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- ▶ **Main Features**

Deep Neural Networks..

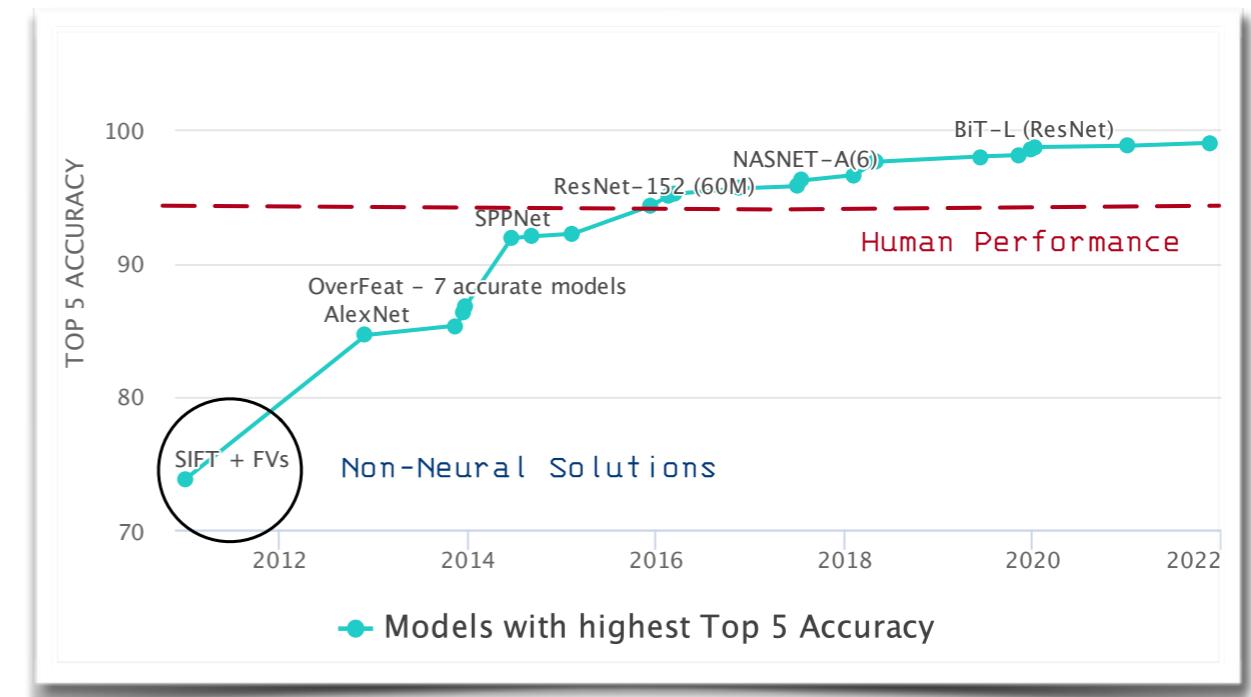
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- ▶ **Main Features**
 - ▶ **Representation Learning**

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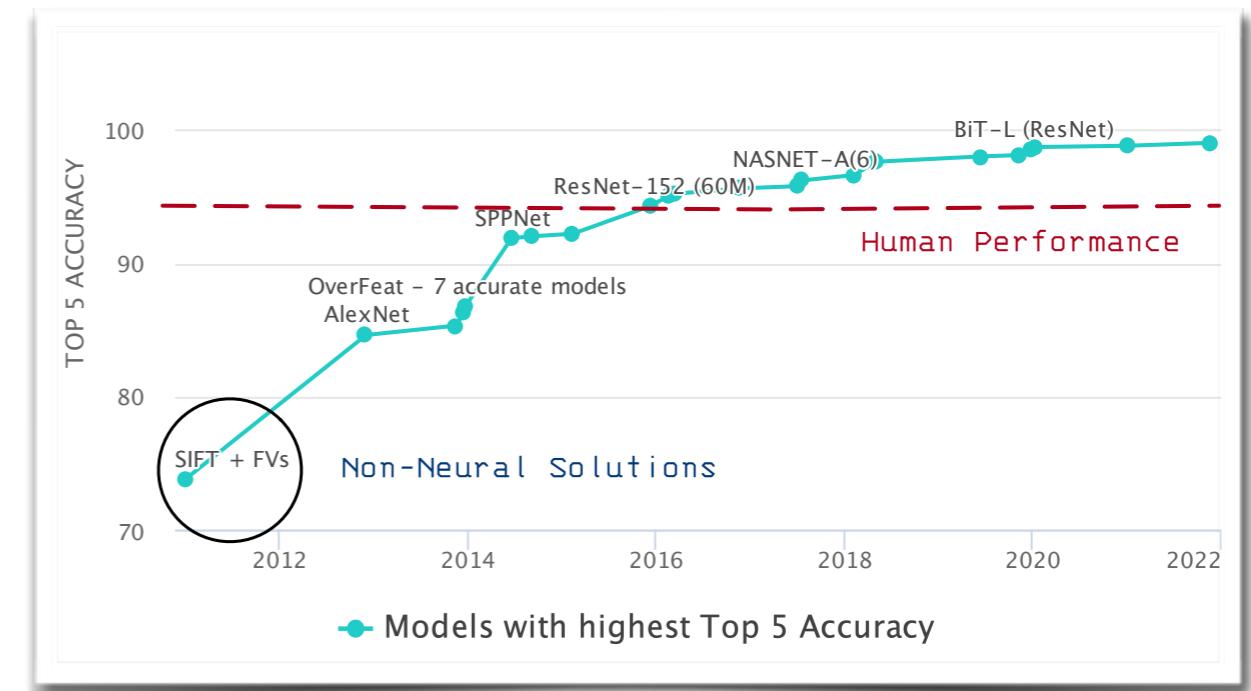
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 - ▶ **Theoretical Universal Approximators**

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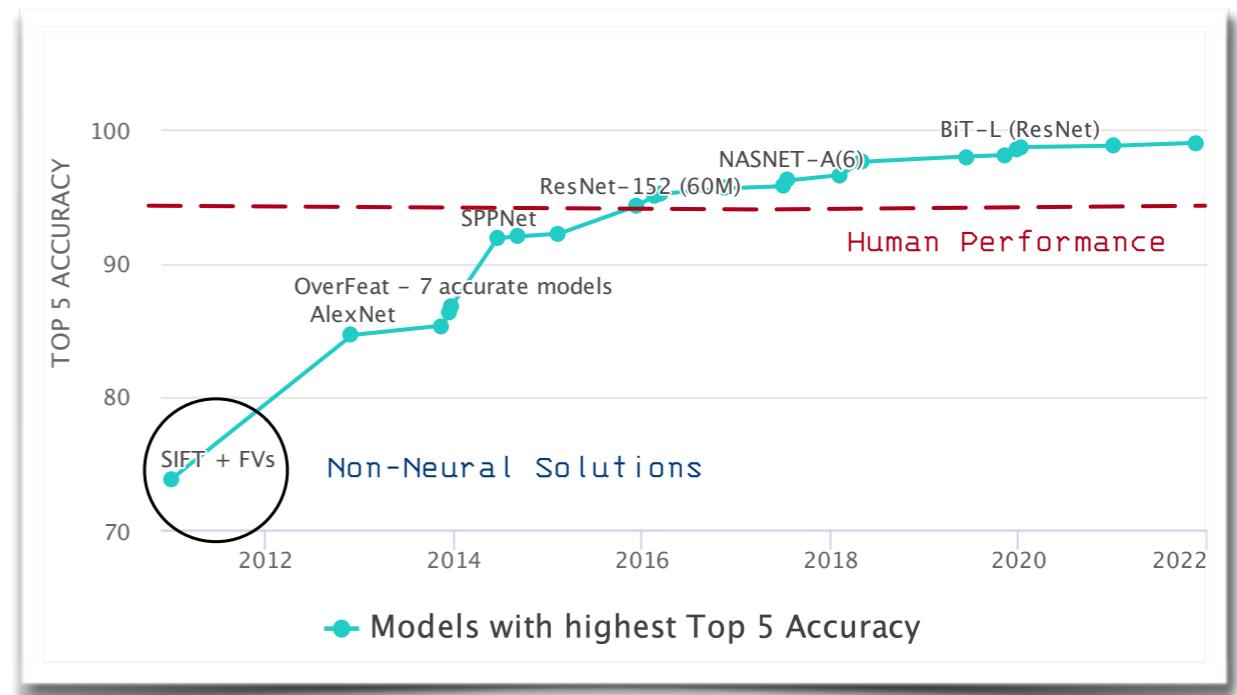
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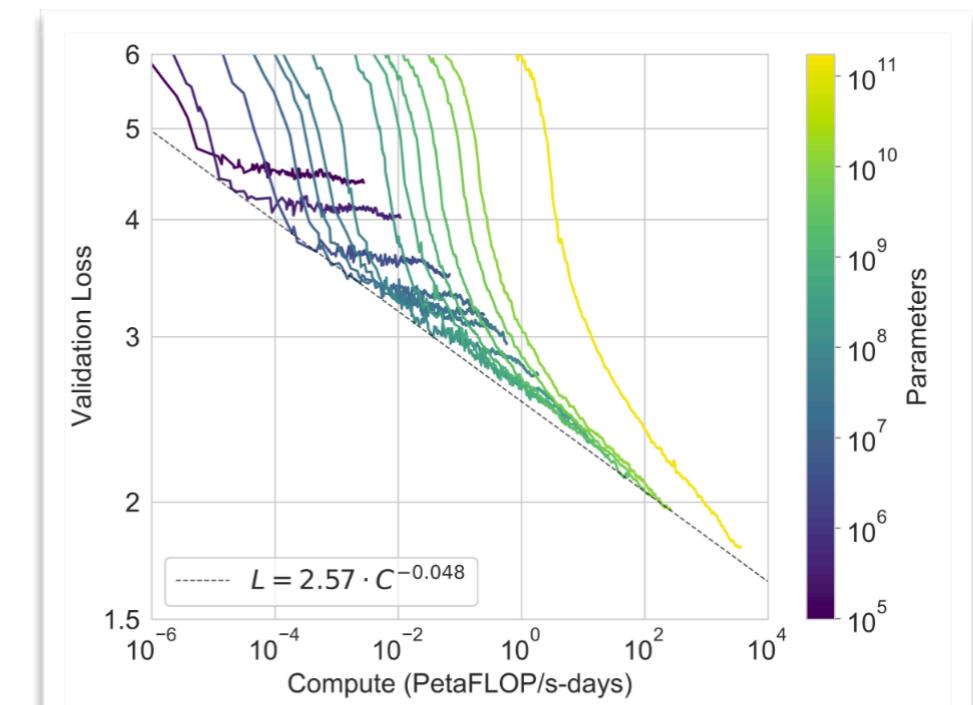
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 - ▶ **Accuracy scales with model size and training epochs**

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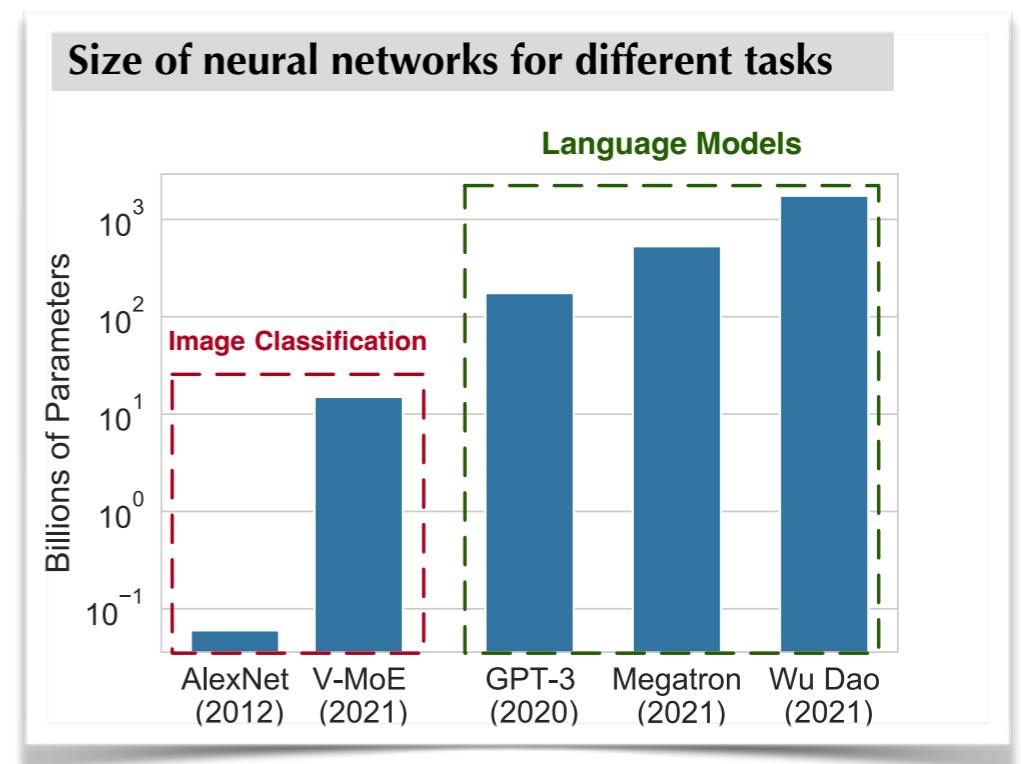


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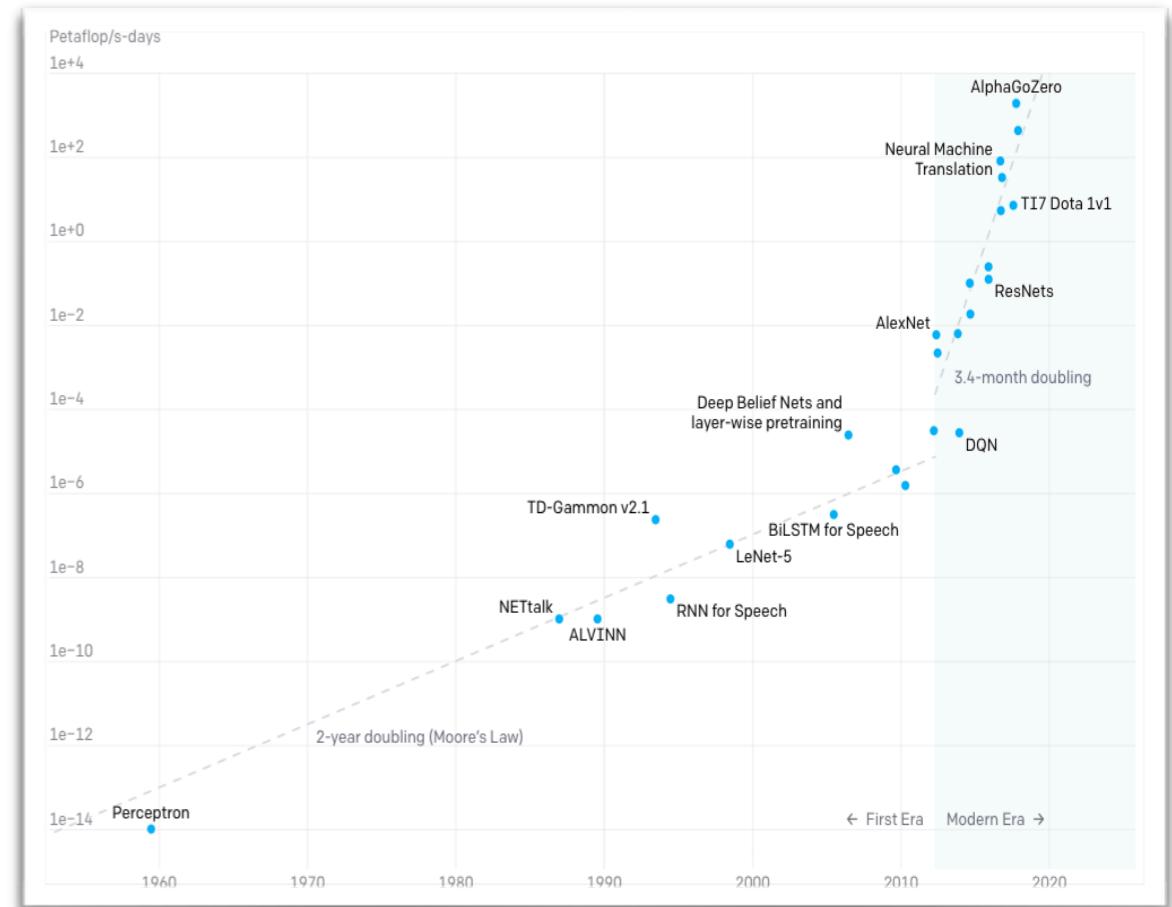
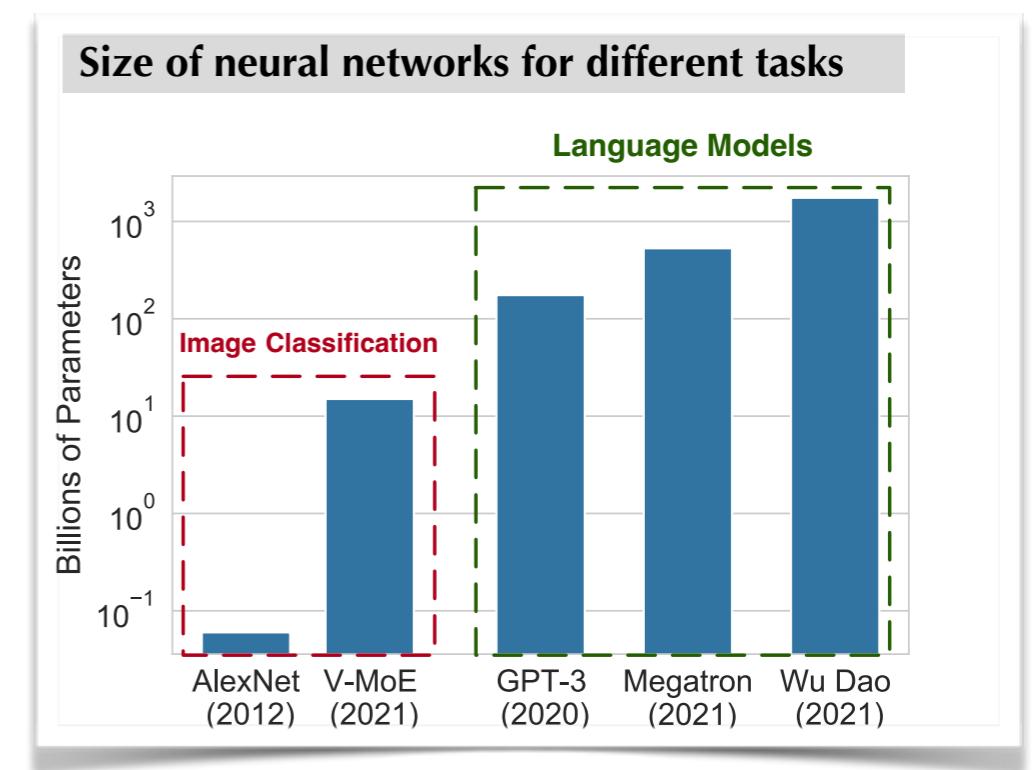
..are Getting Huge

- ▶ **Image Classification.** current state-of-the-art ~100x larger than AlexNet
- ▶ **Language Models.** Huge architectures up to **1.75 trillions** of parameters



..are Getting Huge

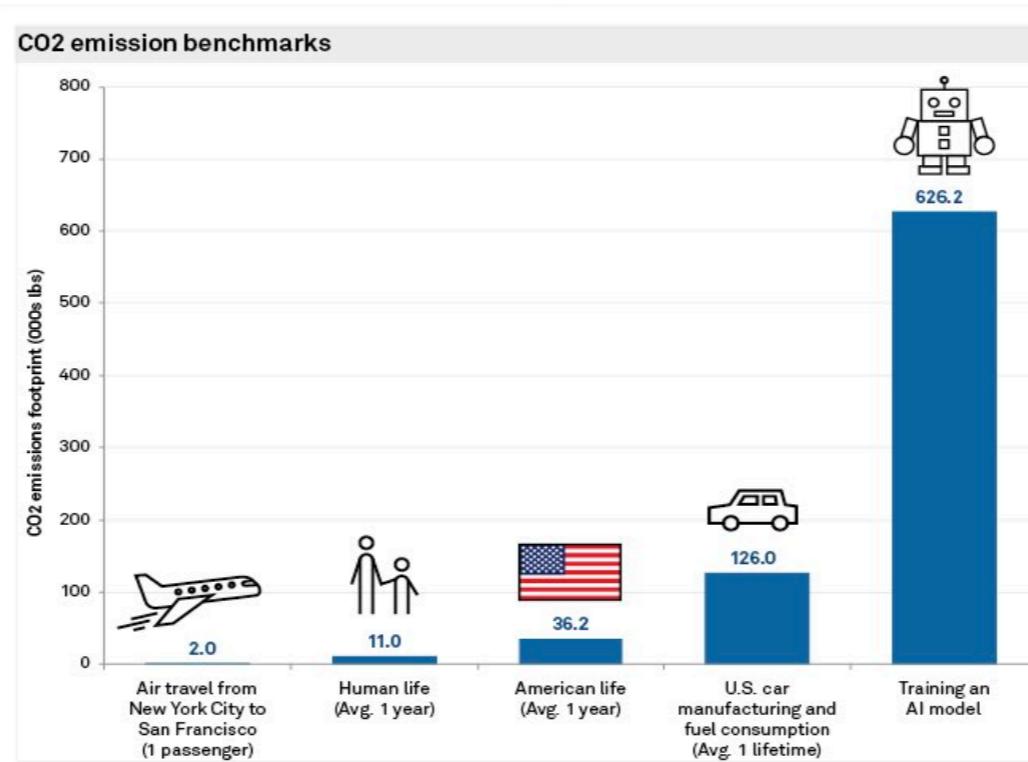
- ▶ **Image Classification.** current state-of-the-art ~100x larger than AlexNet
- ▶ **Language Models.** Huge architectures up to **1.75 trillions** of parameters
- ▶ Consequent growth of **computational burden**
- ▶ **Petaflop/s-day** increase faster than Moore's law



Training is costly

Model	Hardware	Power (W)	Hours	kWh·PUE	CO ₂ e	Cloud compute cost
T2T _{base}	P100x8	1415.78	12	27	26	\$41–\$140
T2T _{big}	P100x8	1515.43	84	201	192	\$289–\$981
ELMo	P100x3	517.66	336	275	262	\$433–\$1472
BERT _{base}	V100x64	12,041.51	79	1507	1438	\$3751–\$12,571
BERT _{base}	TPUv2x16	—	96	—	—	\$2074–\$6912
NAS	P100x8	1515.43	274,120	656,347	626,155	\$942,973–\$3,201,722
NAS	TPUv2x1	—	32,623	—	—	\$44,055–\$146,848
GPT-2	TPUv3x32	—	168	—	—	\$12,902–\$43,008

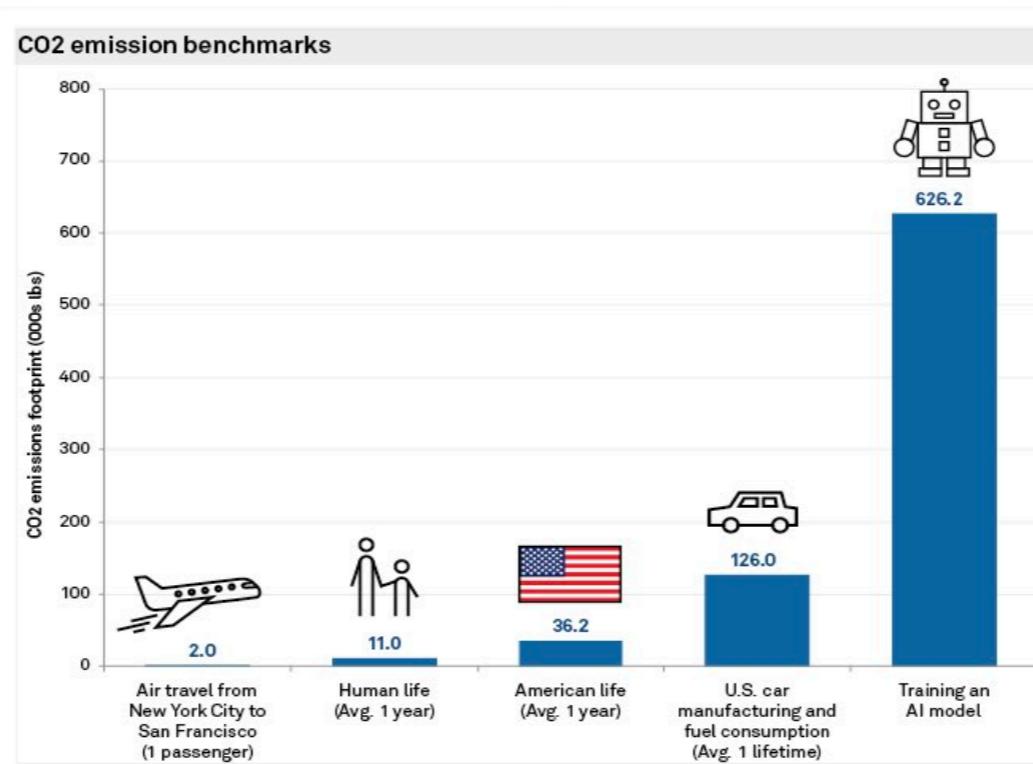
Table 3: Estimated cost of training a model in terms of CO₂ emissions (lbs) and cloud compute cost (USD).⁷ Power and carbon footprint are omitted for TPUs due to lack of public information on power draw for this hardware.



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Inference

- ▶ A lot of inferences
 - 200 trillions of inference per day at Facebook¹
 - 90% of **workload** spent on inference at Amazon, NVIDIA²
- ▶ Inference is resource **constrained** on the edge (IoT, Industry 4.0)

Phase	Freq.	FLOPs	Devices	Constraints
Training	1	10^{15} (day)	Cloud, Servers	None
Inference	∞	$10^9 \div 10^{12}$	Embedded smartphones PC	Memory Time Energy

¹<https://engineering.fb.com/data-center-engineering/accelerating-infrastructure/>

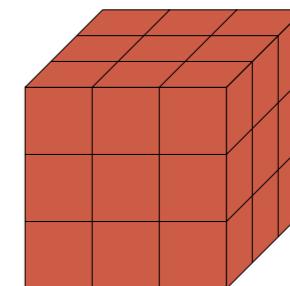
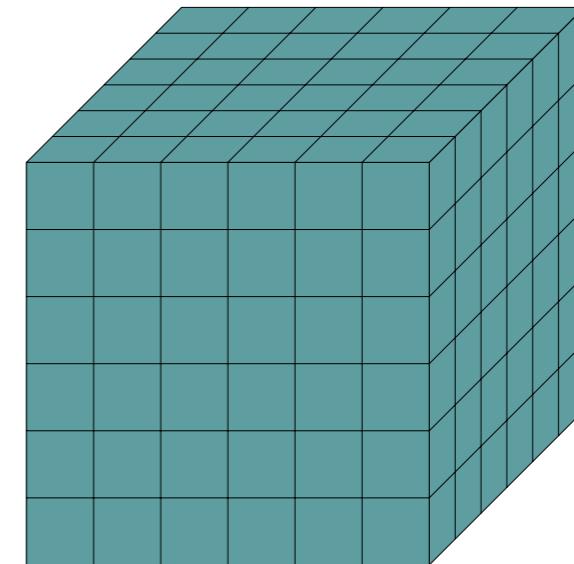
²<https://arxiv.org/pdf/2104.10350.pdf>

Over-parametrization

- ▶ More **equations** (parameters) than **unknowns** (data samples)

- ▶ In general
 - ↓ Over-fitting
 - ↓ Poor performances

- ▶ Neural Networks
 - ↑ Eases optimization
 - ↑ Increases generalization



“Pluralitas non est ponenda sine necessitate”

- novacula Occami

Model Compression

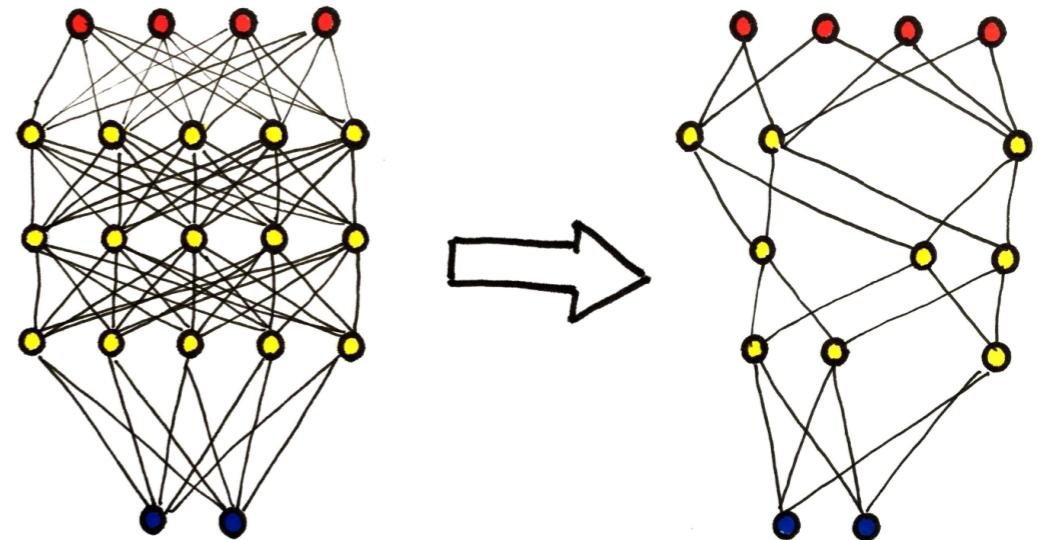
Model Compression

- ▶ Leverages over-parametrization to **compress** DNNs **without** accuracy **degradation**
- ▶ **Reducing**
 - ▶ Memory impact
 - ▶ Inference time
 - ▶ Energy consumption
- ▶ Main methods
 - ▶ **Pruning**
 - ▶ **Quantization**
 - ▶ **Knowledge Distillation**
 - ▶ and more..

Pruning

Pruning

- ▶ Pruning techniques remove **unnecessary** parameters from neural networks
- ▶ Removing = set to 0
- ▶ Reduces **memory** impact, **energy** consumption and speedup **inference**

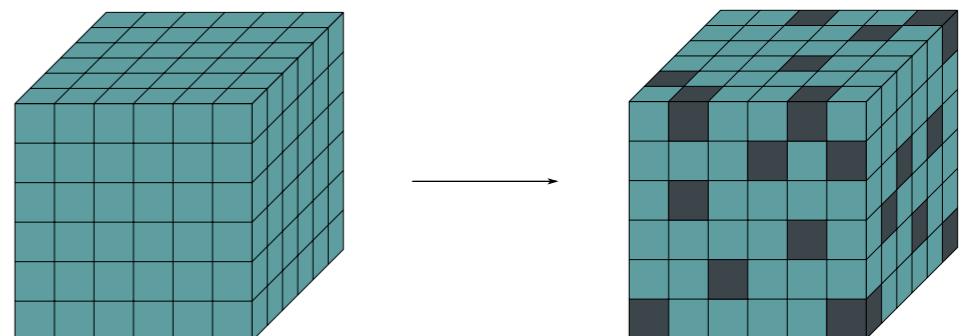


Element-wise vs Structured

- ▶ **Element-wise.** Removes single weights producing sparse tensors

↑ High memory compression

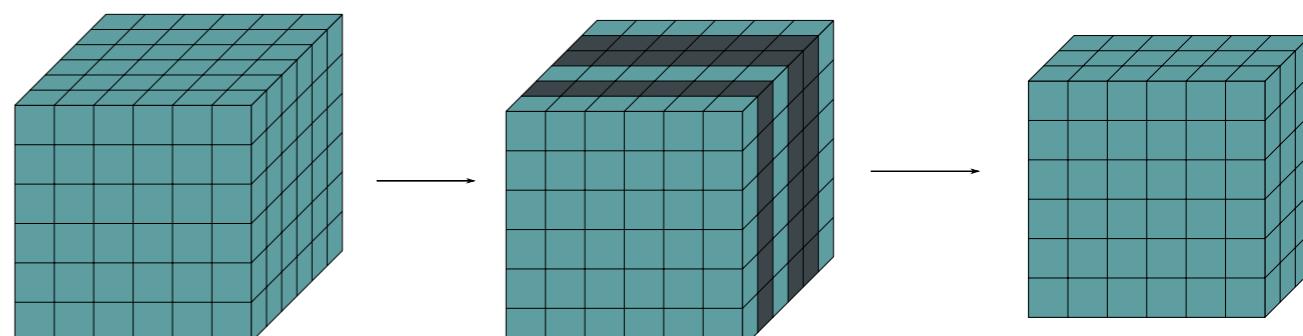
↓ Requires sparse multiplication



Element-wise

- ▶ **Structured.** Removes entire structures (columns, filters)

↑ Direct speedup



Structured

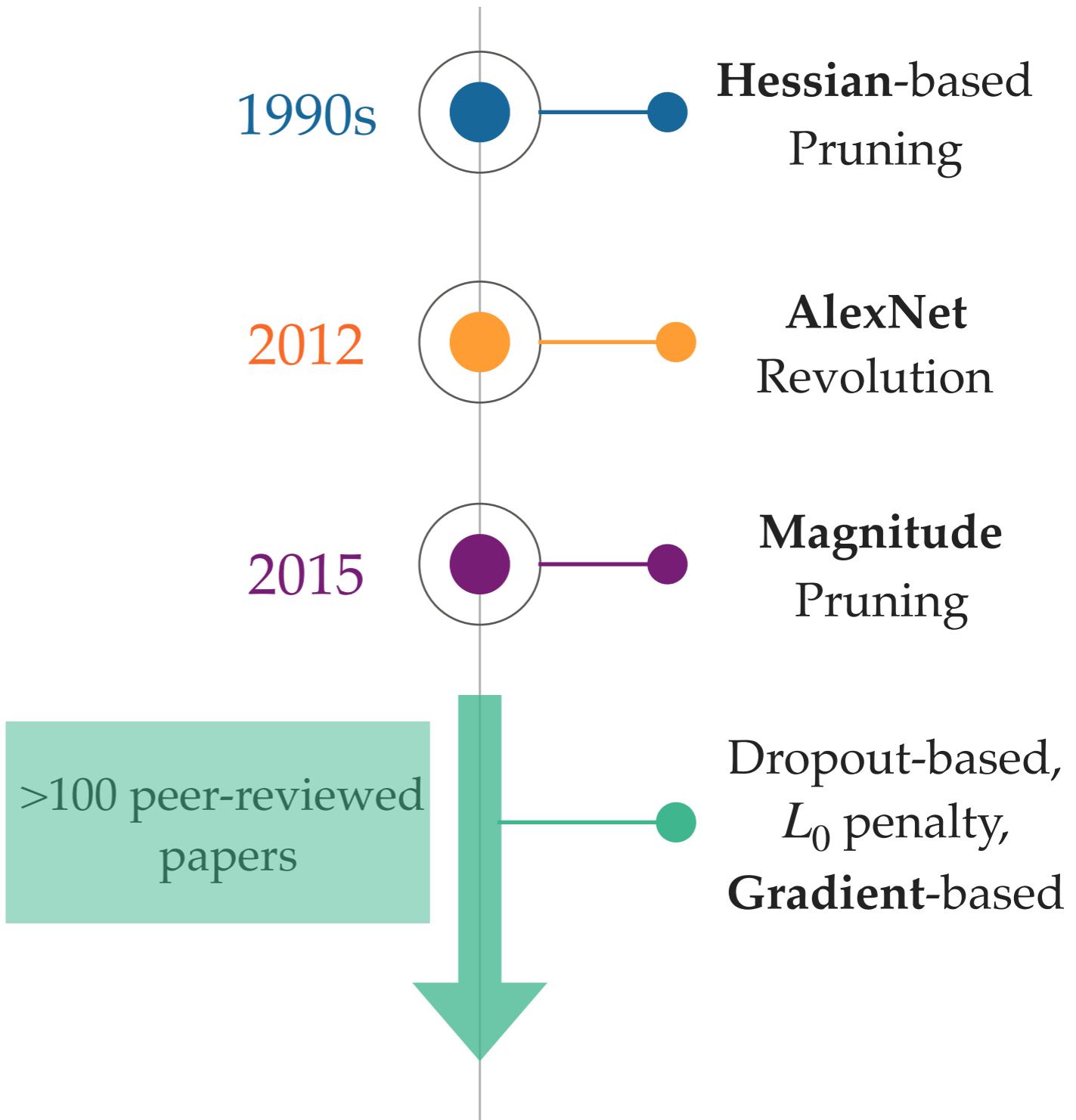
↓ Reduced memory compression

What to Prune?

- ▶ How to **select** which the parameters to prune?
- ▶ With n parameters, 2^n possible pruning patterns
- ▶ **Heuristic** to estimate weight importance, or **penalty** to induce sparsity

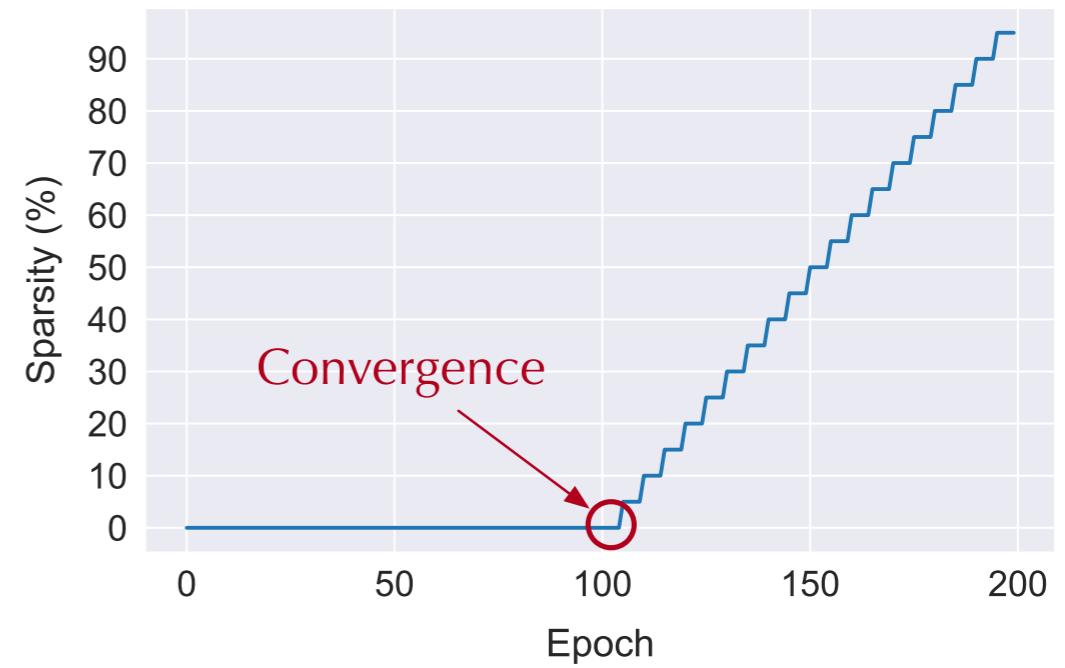
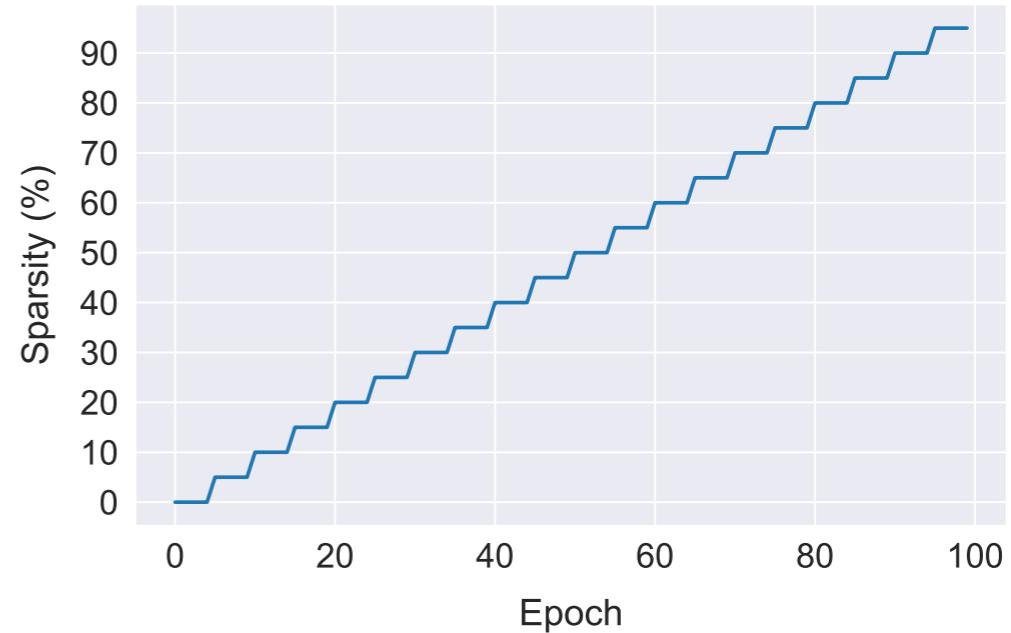
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When to Prune?

- ▶ **During Training.** The model is trained to be sparse
 - ▶ Same budget as standard training
- ▶ **Fine-tuning.** Pruning is applied on a trained, dense model.
 - ▶ Better accuracy



Pruning Performance

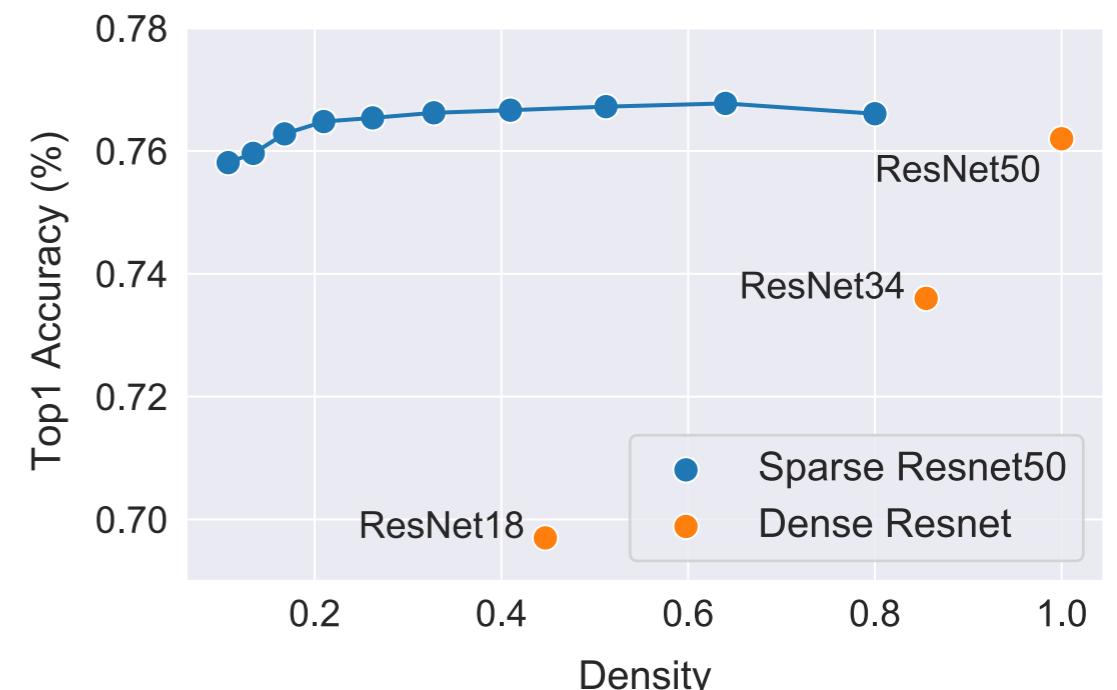
- ▶ Magnitude-based, element-wise pruning, ResNet50 on ImageNet

- ▶ **Element-Wise Pruning.**

- ↑ 90% sparse, no accuracy drop

- ↑ +6% accuracy w.r.t to dense model w/ i same parameters

- ↓ Sparse format overhead not included



Research Question

- ▶ Pruning is a very **effective** compression technique, but
- ▶ **RQ1.** Is there any more **principled** and effective heuristic than magnitude?
- ▶ **RQ2.** What is the relationship between **learning** and **sparsity**?
- ▶ **RQ3.** Can we train sparse network from scratch?
- ▶ And many more..

Quantization

Quantization

- ▶ Classical Computer Science problem
- ▶ Large input values set -> small output values set
- ▶ Specific features of **neural quantization**
 - ▶ Heavily **over-parametrized** model
 - ▶ **Decoupling** between training and inference

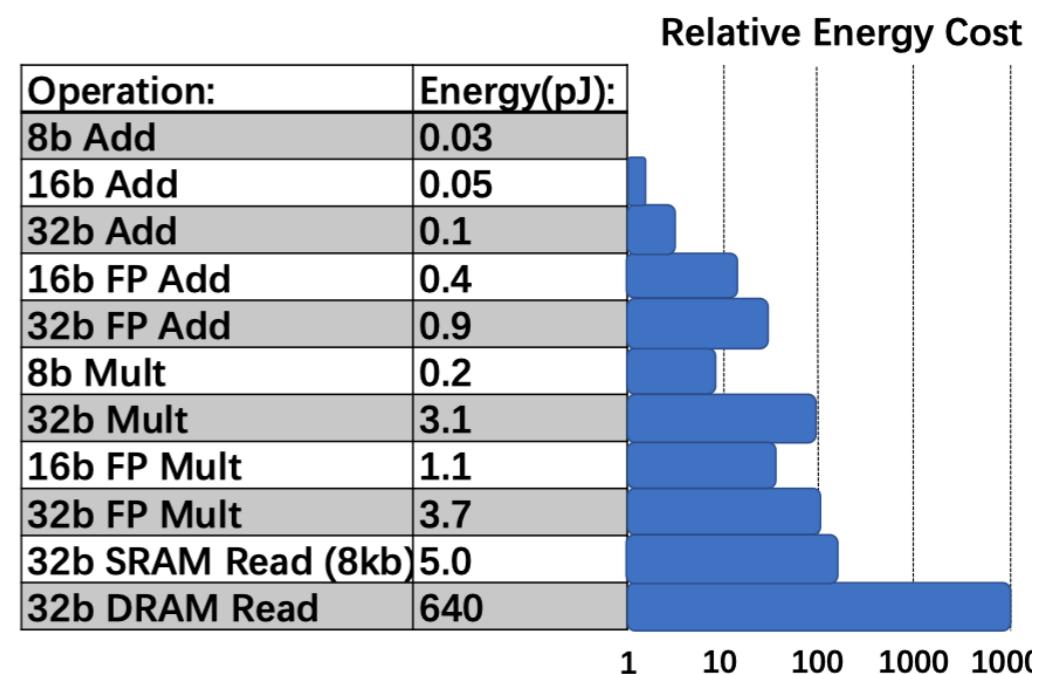
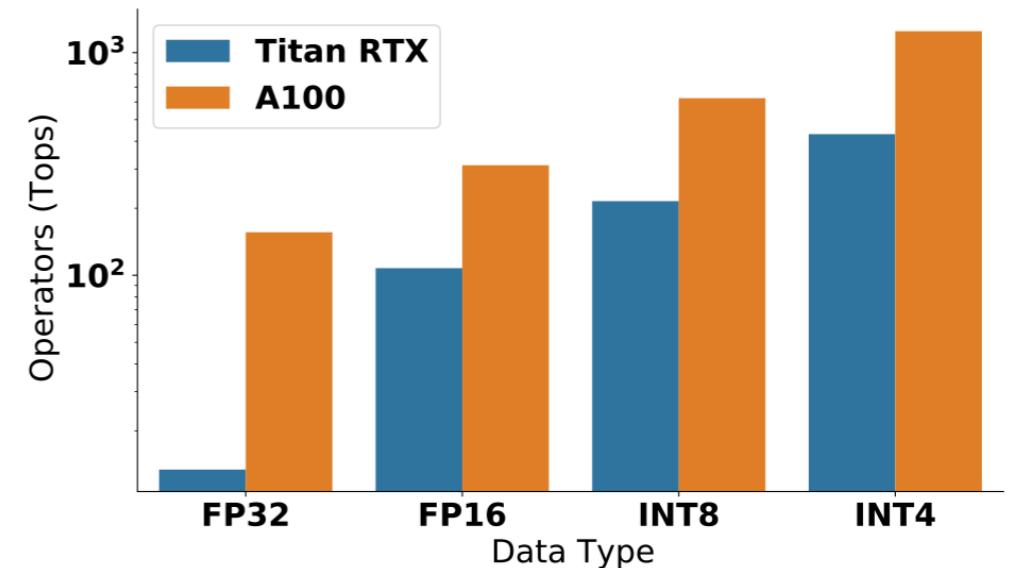
2,09	7,48	2,92	4,16
8,25	3,59	1,04	4,66
10,62	5,32	2,63	4,34
0,58	5,08	1,40	8,58



2	7	3	4
7	4	1	5
7	5	3	4
1	5	1	7

Why Quantization?

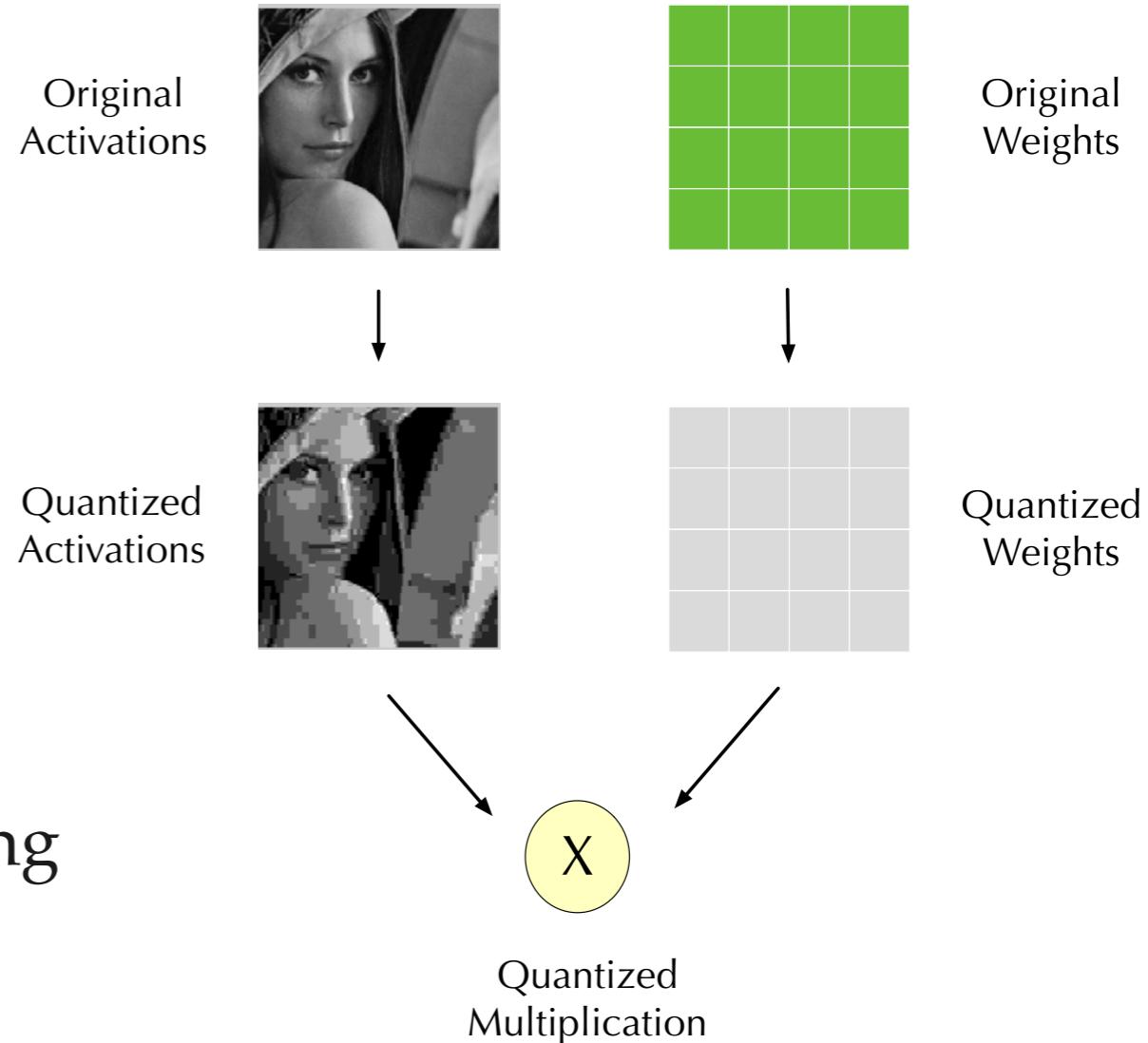
- ▶ Quantization delivers benefits **both in training and inference**
- ▶ Quantized models offers
 - ▶ Reduced **memory** impact
 - ▶ **Faster** operations
 - ▶ Reduced **energy** consumption



Weights and Activations

- ▶ **Quantize weights.**

- ▶ Offline
 - ▶ Weights can be **optimized**



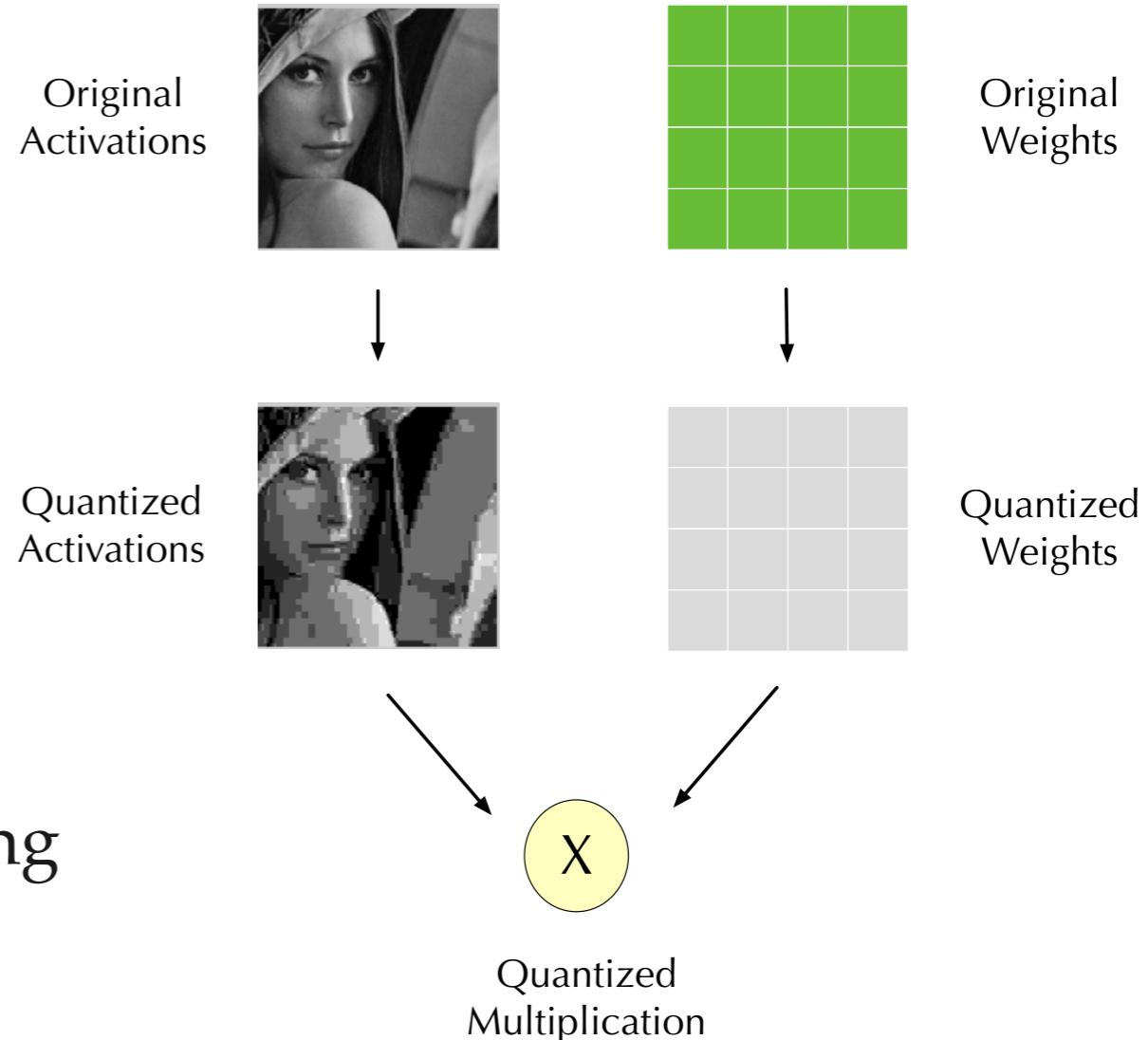
- ▶ **Quantize activations.**

- ▶ Online (inference time) -> computing stats is **costly** (min, max,...)
- ▶ No optimization

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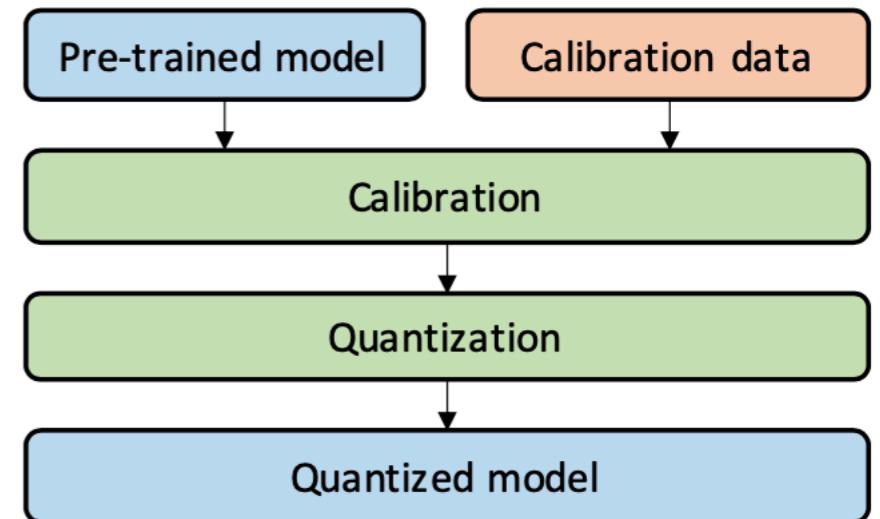
Quantizing activations has a huge impact on accuracy

Fine-Tuning

- ▶ **Post-training Quantization (PTQ).**

↑ No re-training (~)

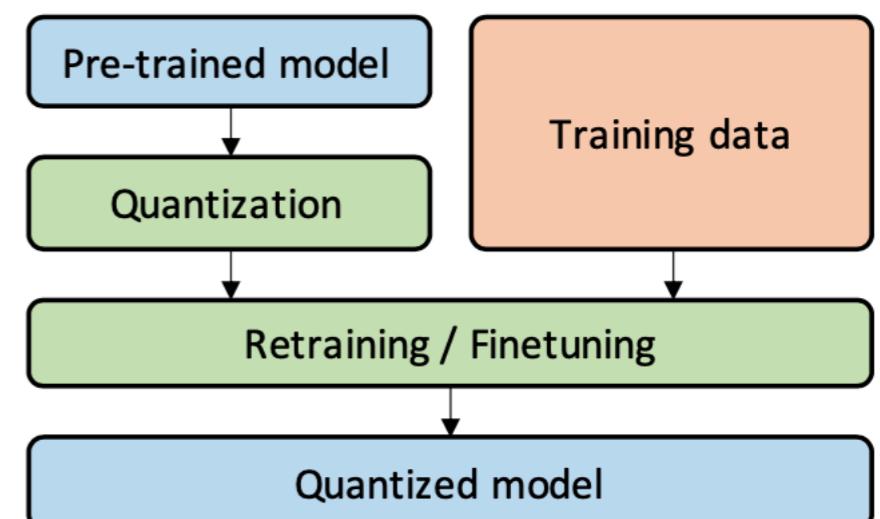
↓ Reduced precision



- ▶ **Quantization-Aware Training (QAT)**

↑ High precision

↓ Costly re-training phase



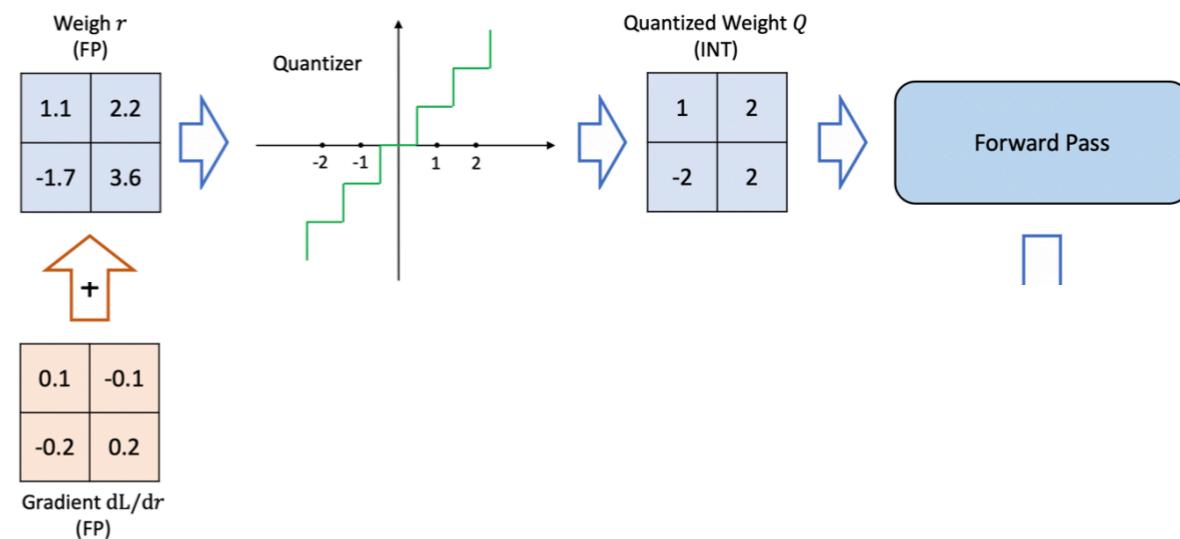
Quantization-Aware Training

- **Methodology.** Weights quantized after each gradient update

- **Requirements.** Backward and gradient update in **full-precision** for numerical reasons

- **Problem.** Quantizer gradient is **zero** almost everywhere

- **Solution.** Straight-Through Estimator (STE)



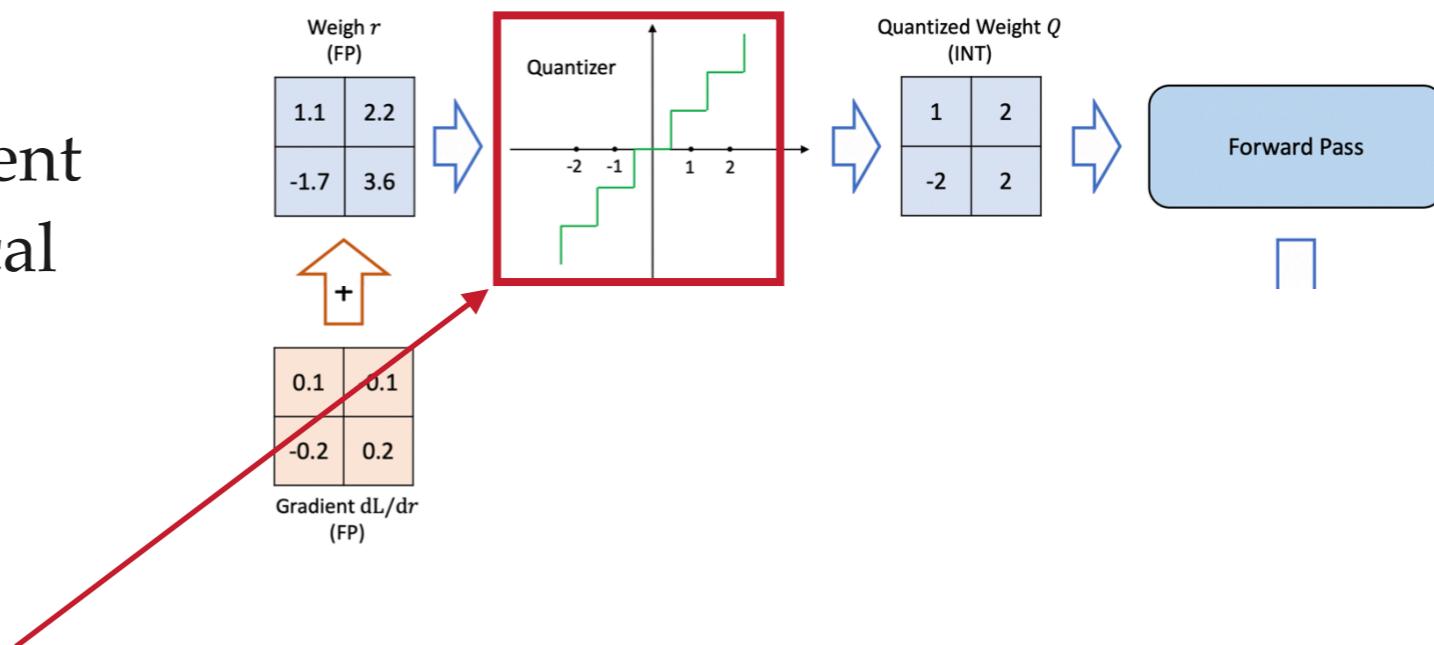
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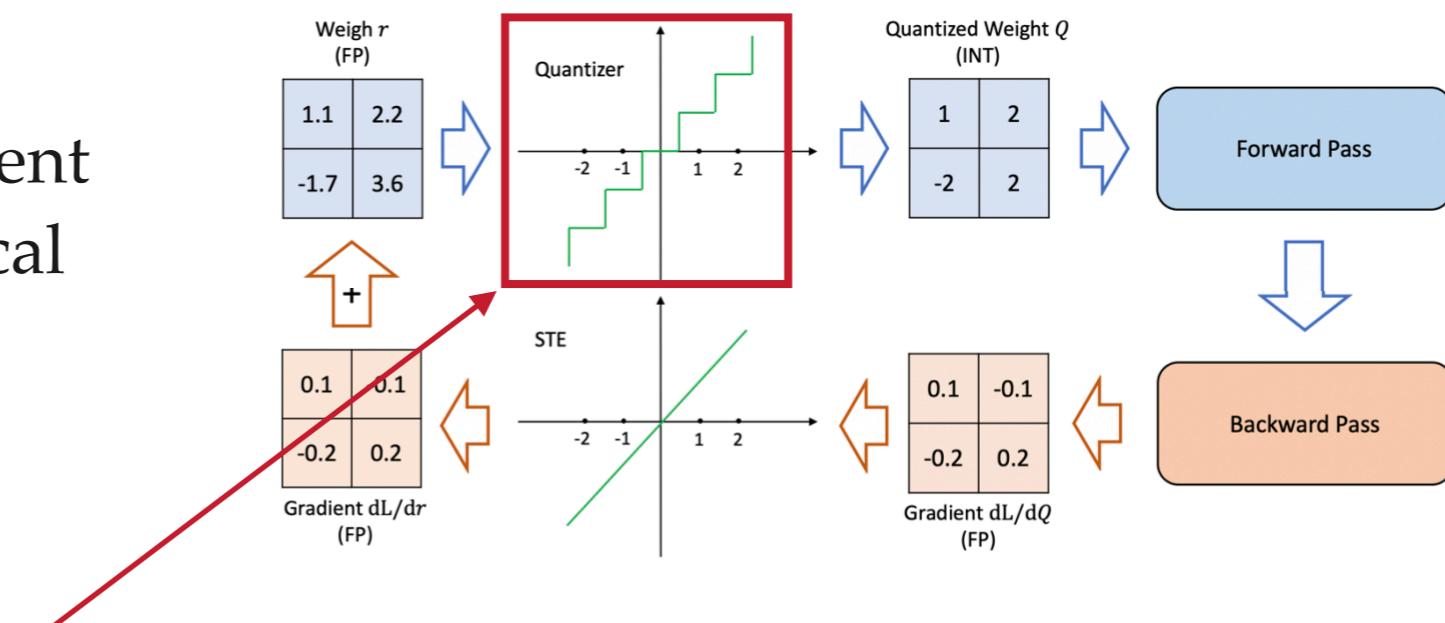
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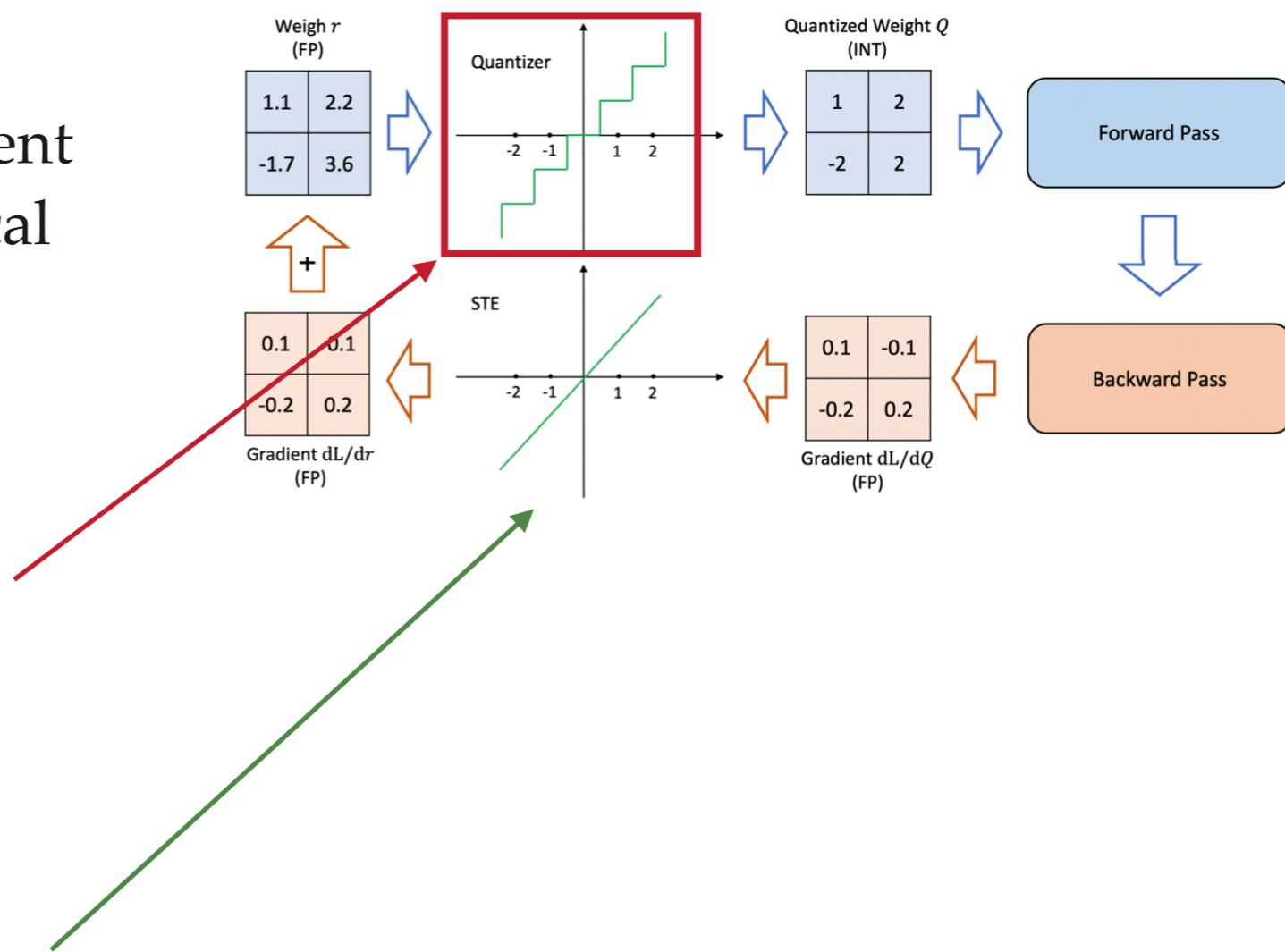
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Quantization Performance

- ▶ **Fully-quantized training**

Optimizer	Task	Model	Metric	Time	Mem saved
32-bit Momentum	MoCo v2	ResNet-50	67.3	30 days	0.0 GB
8-bit Momentum	MoCo v2	ResNet-50	67.4	28 days	0.1GB
32-bit Adam	LM	Transformer-1.5B	9.0	308 days	0.0 GB
8-bit Adam	LM	Transformer-1.5B	9.0	297 days	8.5GB
32-bit Adam	LM	GPT3-Medium	10.62	795 days	0.0 GB
8-bit Adam	LM	GPT3-Medium	10.62	761days	1.7GB

- ▶ **PTQ vs QAT - ResNet18 on Imagenet**

- ▶ PTQ ~0.1 training budget w.r.t. QAT
- ▶ QAT lossless quantization up to 3/3

W/A	Approach	Top1
Baseline	PTQ	71.1
	QAT	69.9
4/4	PTQ	69.1
	QAT	70.6
3/3	PTQ	65.6
	QAT	69.7
2/2	PTQ	51.1
	QAT	67.0

Quantization Performance

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Dettmers, Tim, et al. "8-bit Optimizers via Block-wise Quantization." *International Conference on Learning Representations*. 2022.

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Wei, Xiuying, et al. "QDrop: Randomly Dropping Quantization for Extremely Low-bit Post-Training Quantization." *International Conference on Learning Representations*. 2021.

Lee, Junghyup, Dohyung Kim, and Bumsub Ham. "Network quantization with element-wise gradient scaling." *Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition*. 2021

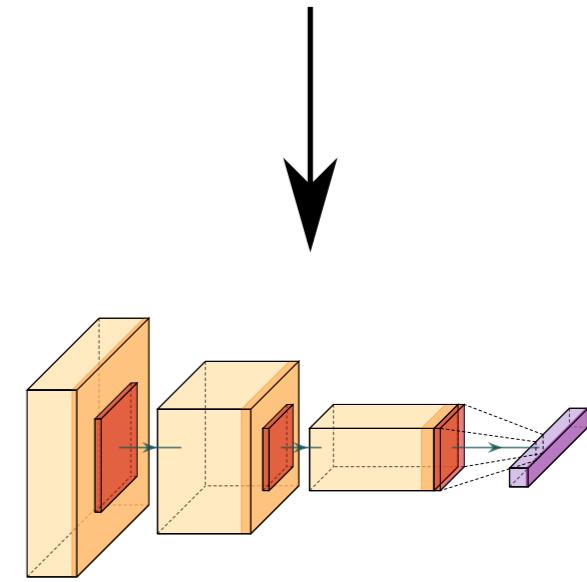
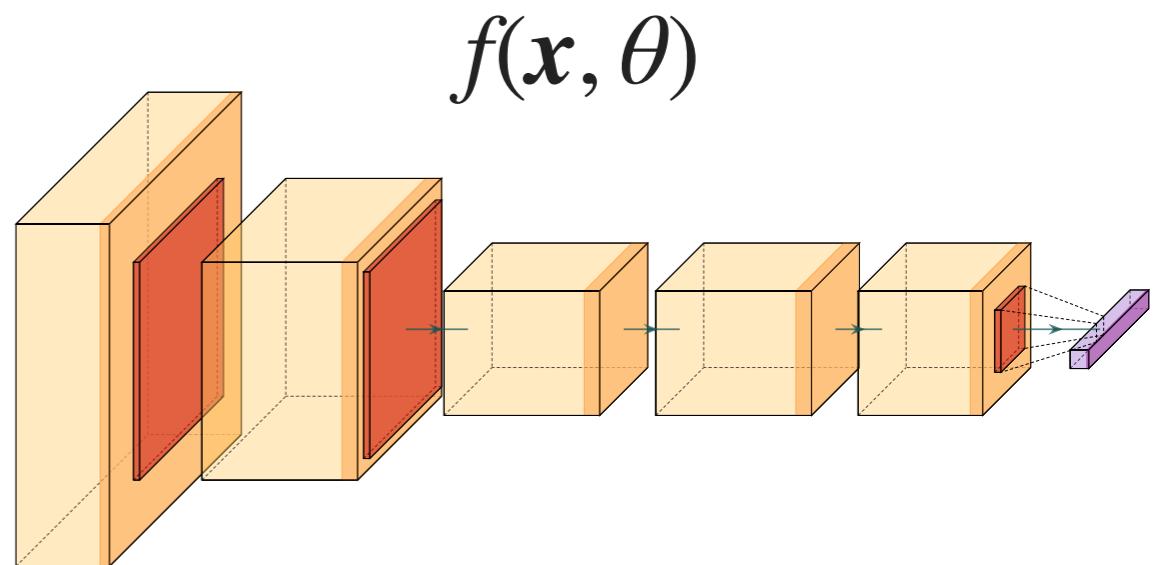
Research Question

- ▶ Quantization is an extremely effective solution
- ▶ **RQ1.** Can we produce extreme low-bits models as effective as full-precision ones?
- ▶ **RQ2.** Can we go beyond STE?
- ▶ **RQ3.** Can we use FPGA and ASIC to fully leverage the benefit of quantization?
- ▶ And many more..

Knowledge Distillation

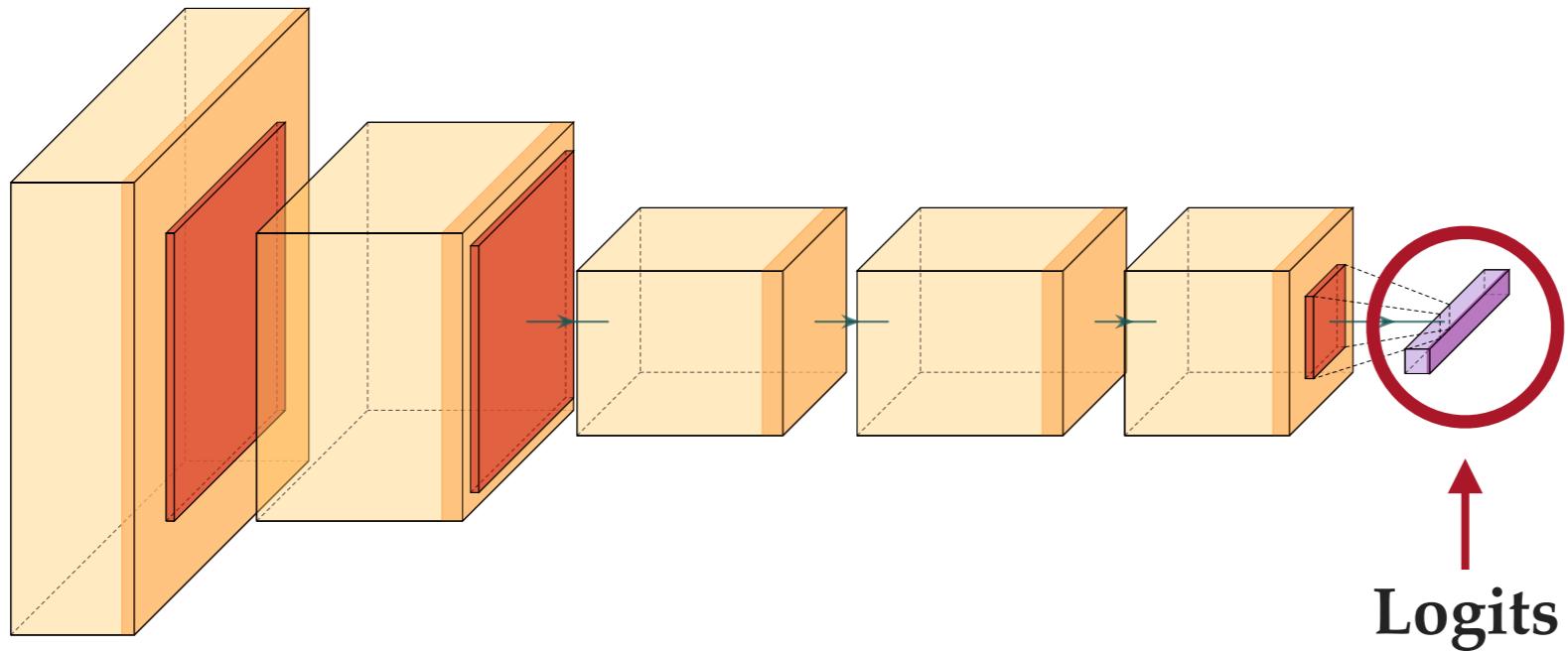
Knowledge Distillation

- ▶ Training paradigm that involves
 - **Student:** the model to be trained.
Small, shallow and deployment oriented
 - **Teacher:** pre-trained. Deep and effective
- ▶ The student cannot learn the same function $f(x, \theta)$ as the teacher **extrapolating** it from the examples
- ▶ It could by **mimicking** its outputs on the samples



$$f(x, \theta') \sim f(x, \theta)$$

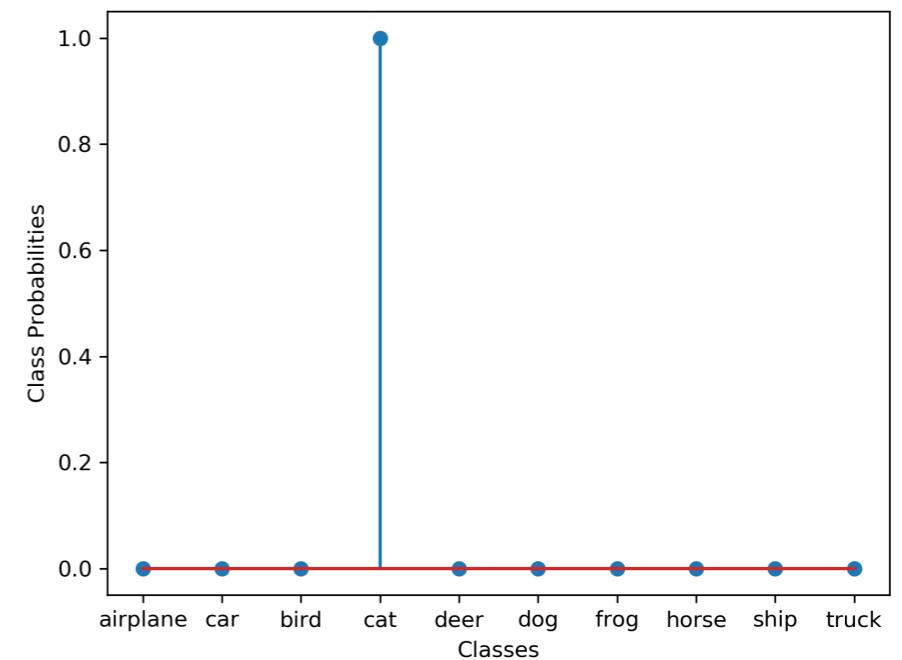
Logits



- ▶ **Logits.** $z \in R^c$, with c number of classes.
- ▶ **Class Probabilities.** $p_i = \text{softmax}(z_i)$

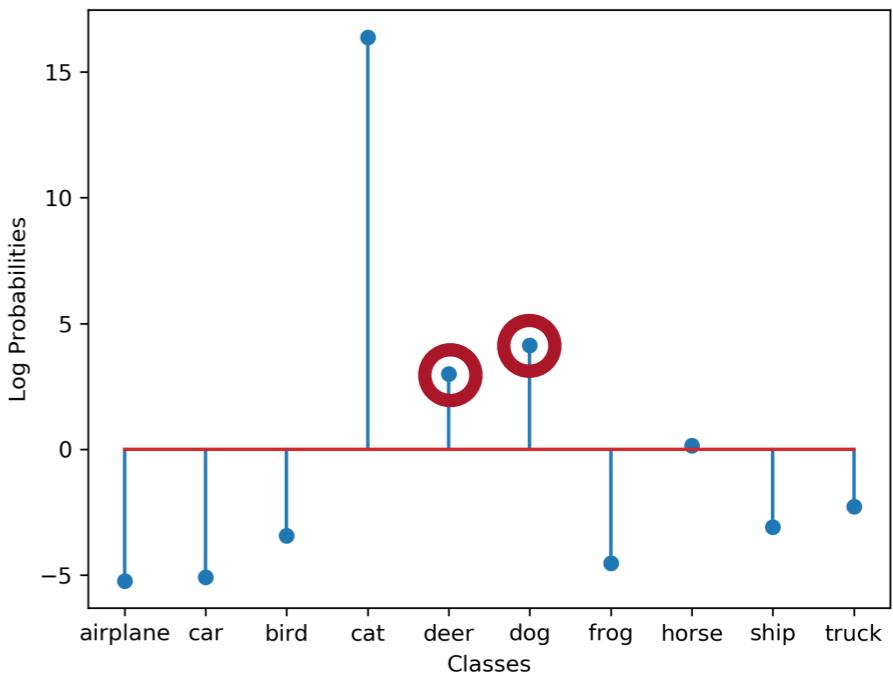
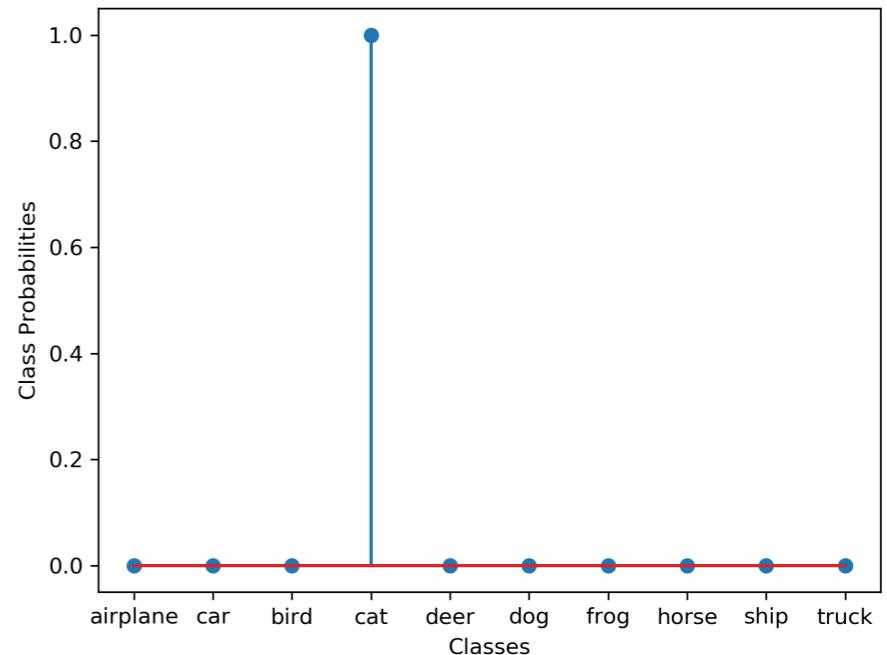
Logits Approximation

- ▶ **One-hot encoded label**
 - ▶ Single class information



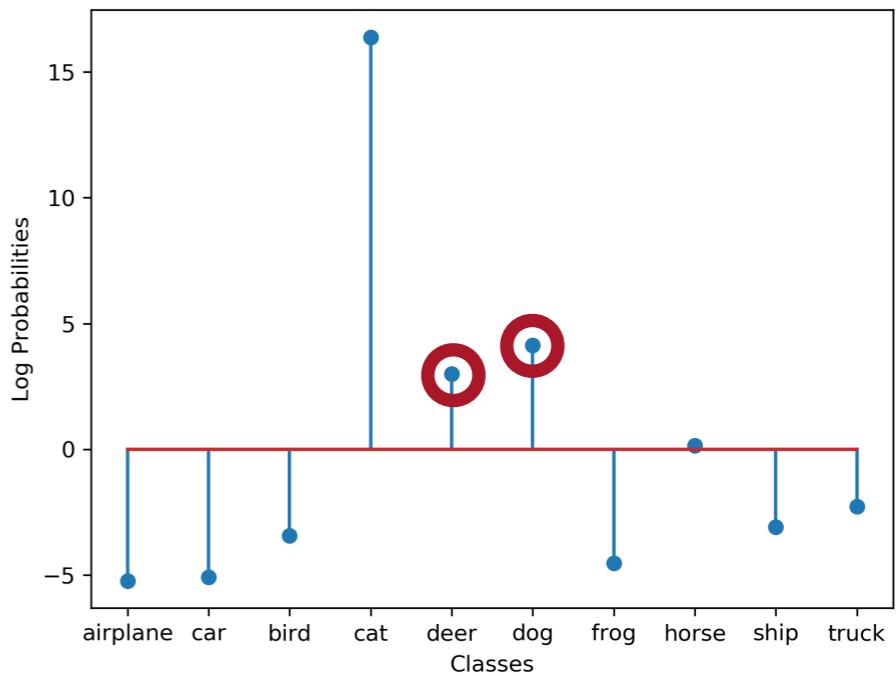
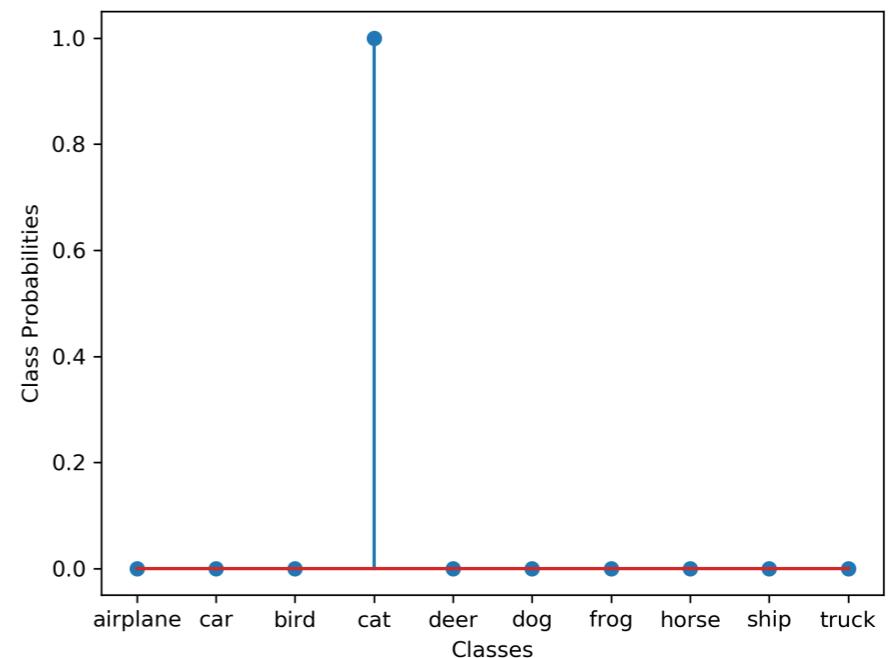
Logits Approximation

- ▶ One-hot encoded label
 - ▶ Single class information
- ▶ Teacher logits.
 - ▶ Multi-class and intra-class information



Logits Approximation

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Train the student to approximate the logits of the teacher

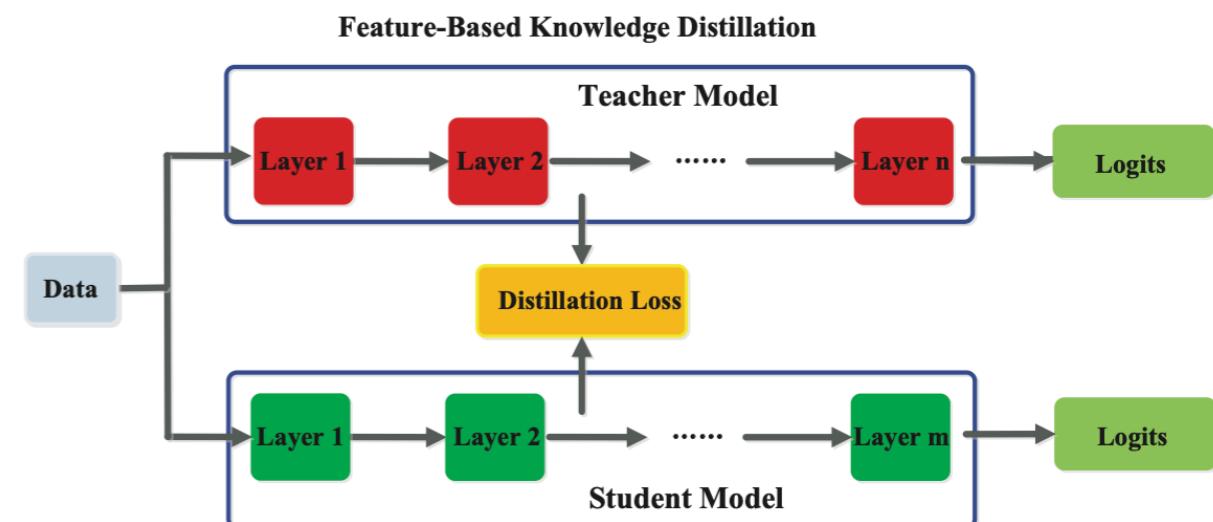
Feature Approximation

- ▶ Features **representation** encodes inner knowledge of the teacher

- ▶ Forcing the **student activations** to be similar to the teacher ones

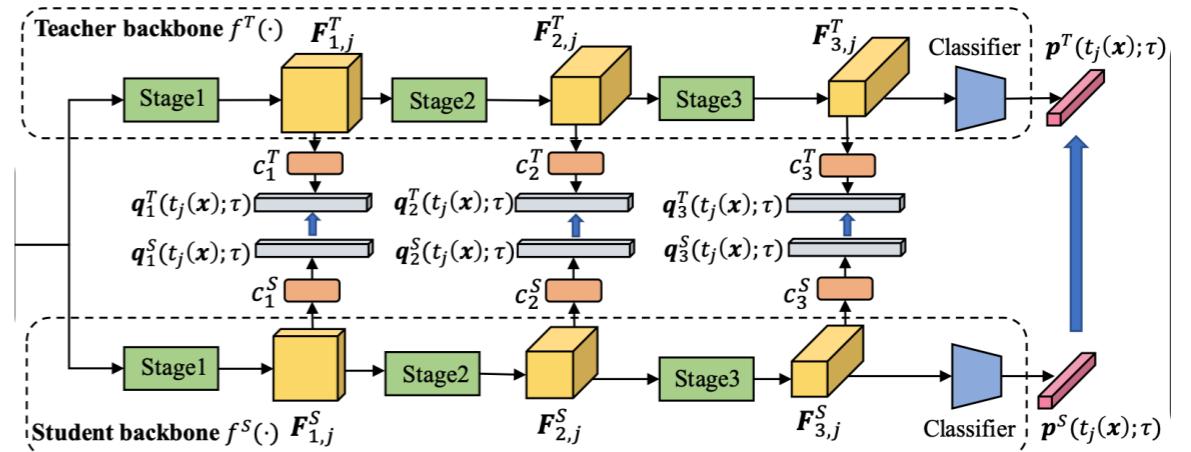
$$L_{\text{tot}} = \boxed{H(x, y)} + \boxed{L(\phi_t(x), \phi_s(x))}$$

↑
Classical Loss ↑
Hint Loss



Knowledge Distillation Performance

- ▶ Multi-level distillation



- ▶ Performance on ImageNet

- ▶ + 2.6 % Top1 w.r.t to standard training
- ▶ No inference overhead

Model	Top1
Student	69.8
Teacher	73.3
Student + KD	72.4

Research Question

- ▶ Knowledge Distillation is effective but..
- ▶ **RQ1.** Poor theoretical basis
- ▶ **RQ2.** Knowledge distillation vs label smoothing?
- ▶ **RQ3.** Combinations with other compression methods?
- ▶ And many more..

Research Question

Thanks for the attention!

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