



Modélisation de la dynamique d'une population de poisson exploitée par un modèle de production de Biomasse

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UMR DECOD Ecosystem Dynamic and Sustainability

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La modélisation intégrée en écologie statistique

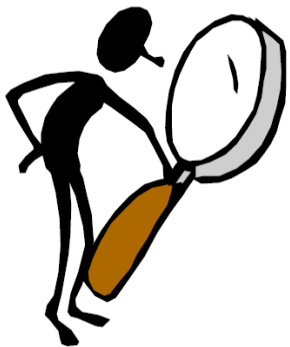
Methodological challenges of statistical ecology

Methodological challenges of Statistical Ecology



■ Model issues

- Multiple form of dependencies (time, space, clustering ...)
- Variability and stochasticity (demographic, environmental)



■ Data issues

- Highly correlated
- Hierarchical structure
- Incomplete (missing data)
- Noisy
- Not directly related to the process of interest

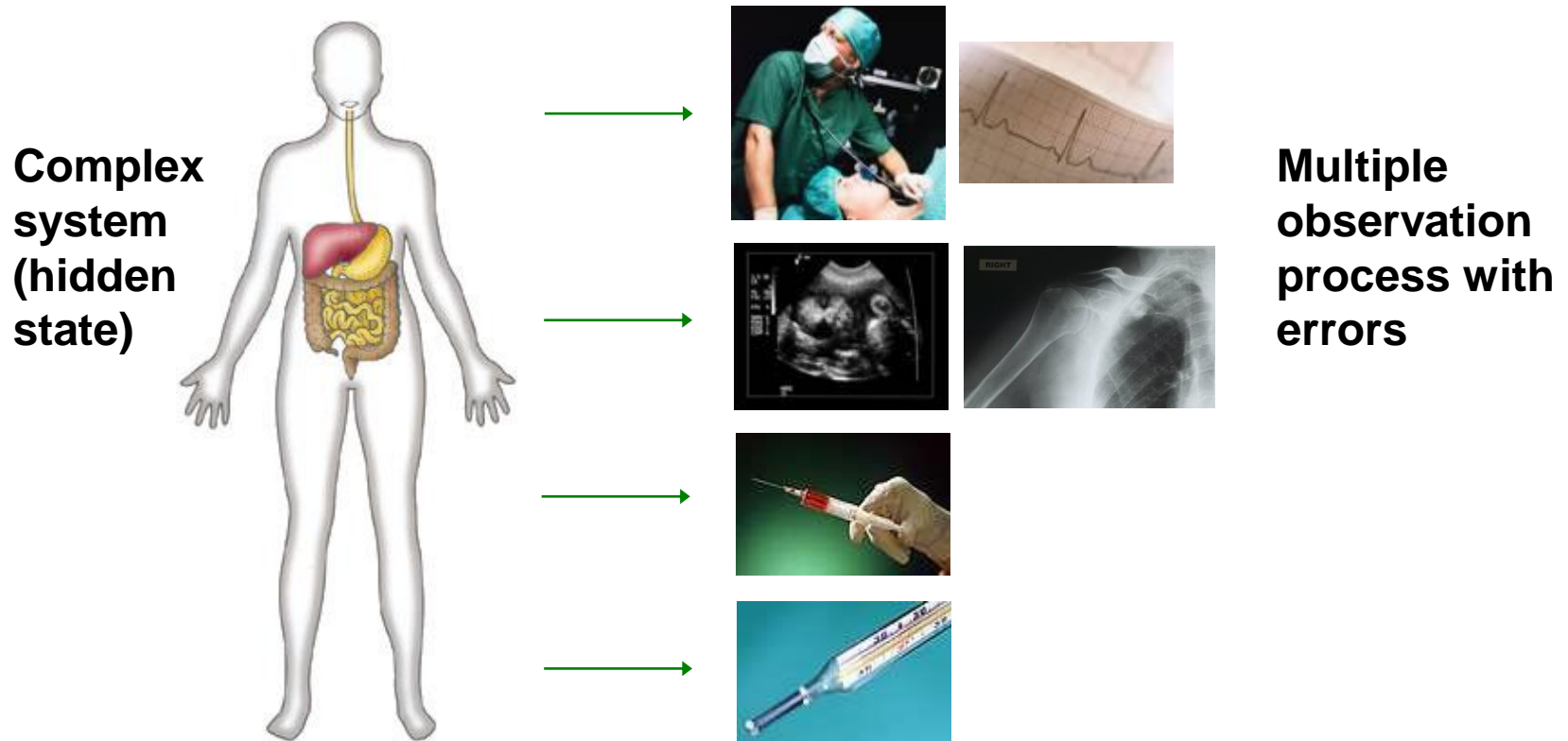
The Ecological Detective - Hilborn et Mangel, 1997

**« *Counting fish is like counting trees,
except they are invisible and they move* »**

R. Sheperd

« *On ne peut pas vider la baignoire* »

Integrating multiple sources of information in complex models



➔ **Requires a flexible approach to fusing models with data, an approach that can accommodate uncertainties in the way ecological processes operate and the way we observe them**

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Hierarchical models
State-space models

Hierarchical models (random effects models)

- **A wide class of models**

Key tools in modern statistical ecology with multiple applications

- **Bayesian or “Classical” framework**

April 2009

HIERARCHICAL MODELS IN ECOLOGY

Ecological Applications, 19(3), 2009, pp. 553–570
© 2009 by the Ecological Society of America

Accounting for uncertainty in ecological analysis: the strengths and limitations of hierarchical statistical modeling

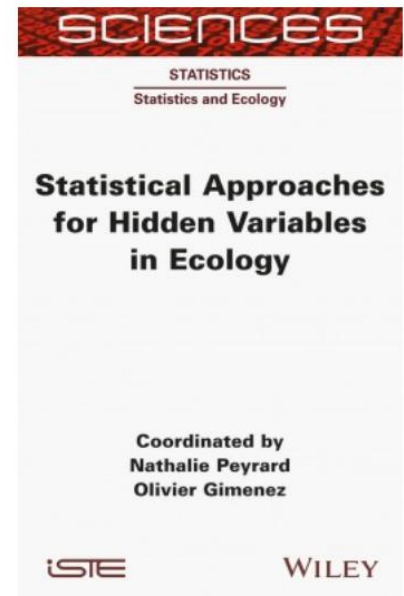
NOEL CRESSIE,^{1,5} CATHERINE A. CALDER,¹ JAMES S. CLARK,² JAY M. VER HOEF,³ AND CHRISTOPHER K. WIKLE⁴

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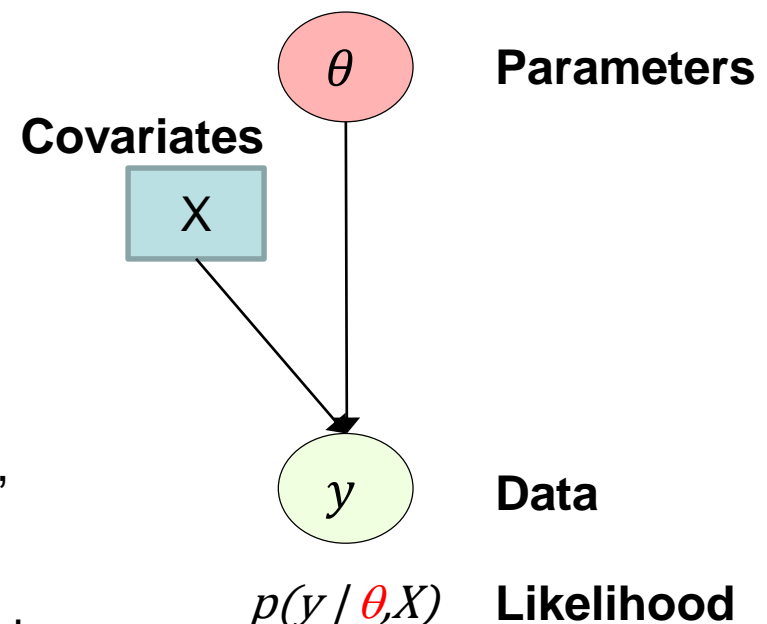


Simple (non hierarchical) models

- “Simple” (non hierarchical) statistical models directly express the sampling distribution of the data y conditionnaly upon parameters θ and fixed covariates X (*the likelihood function*)

$$L(\theta, y, X) = p(y / \theta, X)$$

- Generally limited to correlative approaches, seeking to
 - Estimates “effects” of covariates X
 - Quantify the amount of variance explained by covariates / residual noise



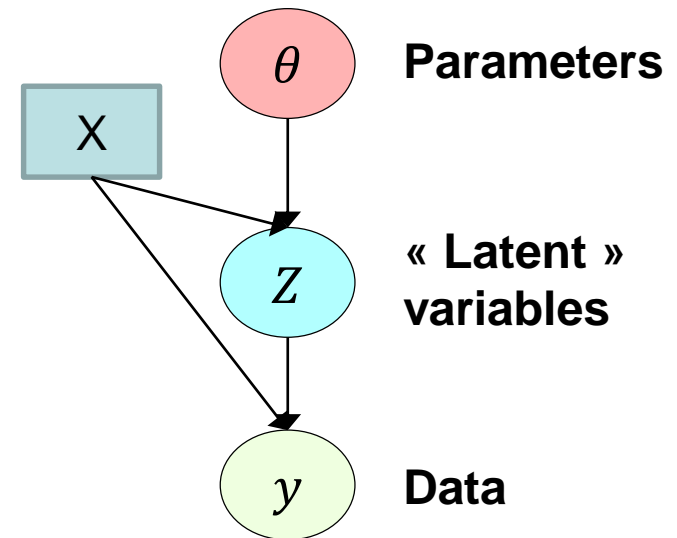
Hierarchical (multi-level) models

- **Hierarchical models** (or multi-level models) **make use of intermediate non observed (latent, hidden) variables**

Observed data, which are random variables at one level, depend upon another set of random variables, generally not observed directly (= the latent variables), at a higher level

The latent variables Z can be structured in multiple layers

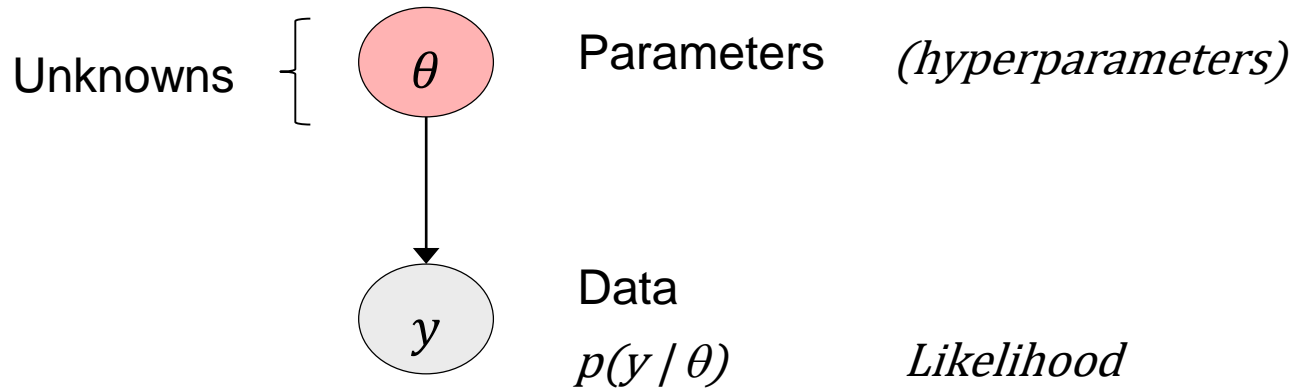
Conditional probability distributions are used to structure the dependencies



Likelihood

$$p(y, Z | \theta, X) = p(Z | \theta, X) \times p(y | Z, \theta, X)$$

Non hierarchical models



Maximum likelihood

Latent states must be integrated out

$$\hat{\theta} = \operatorname{argmax} \{P(y|\theta)\}$$

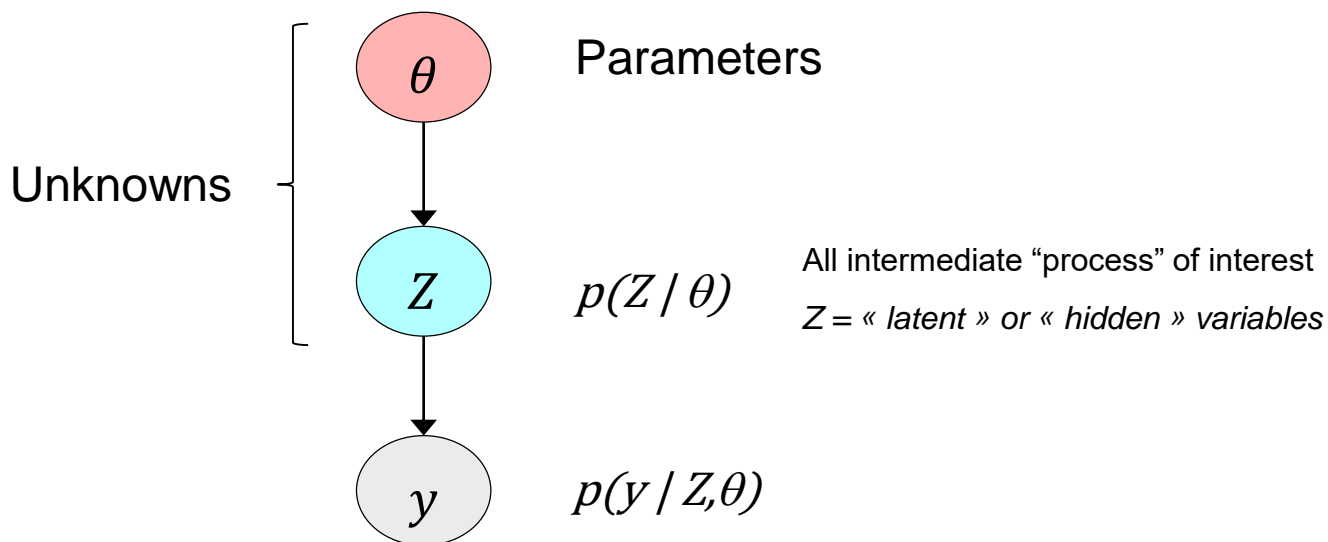
Bayes

Joint posterior distribution

$$P(\theta|y) \propto \underbrace{P(\theta)}_{\text{Param.}} \times \underbrace{P(y|\theta)}_{\text{Lik.}}$$

Inferences on Hierarchical Models

Clark, 2005 ; Buckland et al., 2007 ; Cressie et al., 2009 ; Parent and Rivot, 2013



Maximum likelihood

Latent states must be integrated out

$$\hat{\theta} = \operatorname{argmax} \{L(\theta, y)\} = \operatorname{argmax} \left\{ \int_{\text{States}=Z} L(\theta, Z, y) dz \right\}$$

Bayes

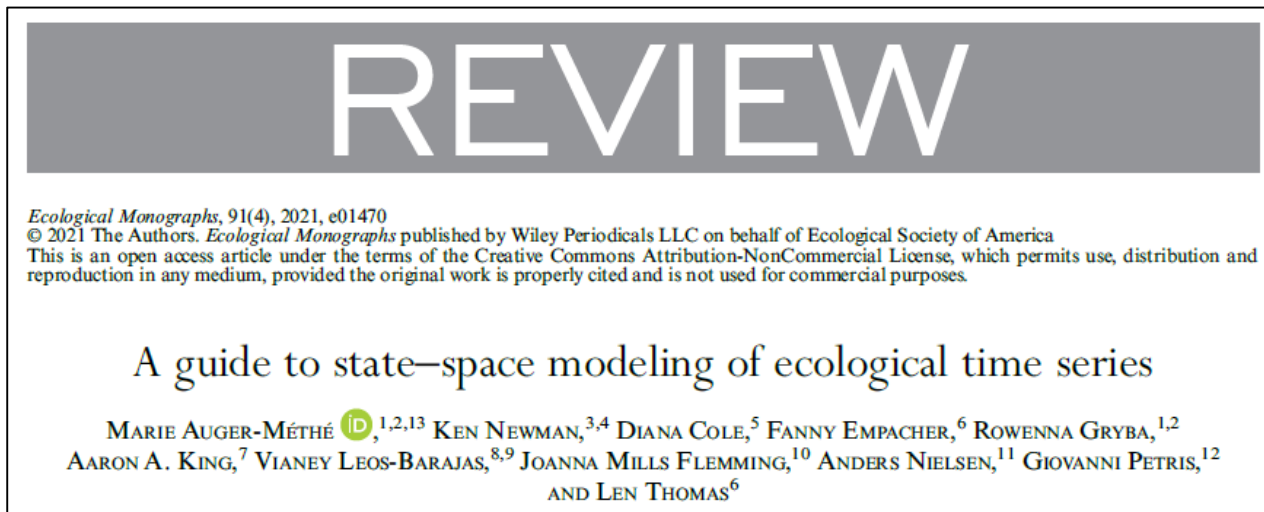
Joint posterior distribution

$$P(\theta, Z | y) \propto \underbrace{P(\theta)}_{\text{Param.}} \times \underbrace{P(z | \theta)}_{\text{Latent var}} \times \underbrace{P(y | Z, \theta)}_{\text{Lik.}}$$

State-space models

- **State-space models** are a special class of hierarchical models where the latent layer has a dynamic dimension (and by extension, spatial or spatio-temporal dimensions)
- In SSMs, inferences on the latent process $Z|\theta$ may have as much interest (or even more) than the top level parameters

Exp : $Z|\theta$ is the population dynamics model with transition rates θ



<https://doi.org/10.1002/ecm.1470>

State-space models

Process equation

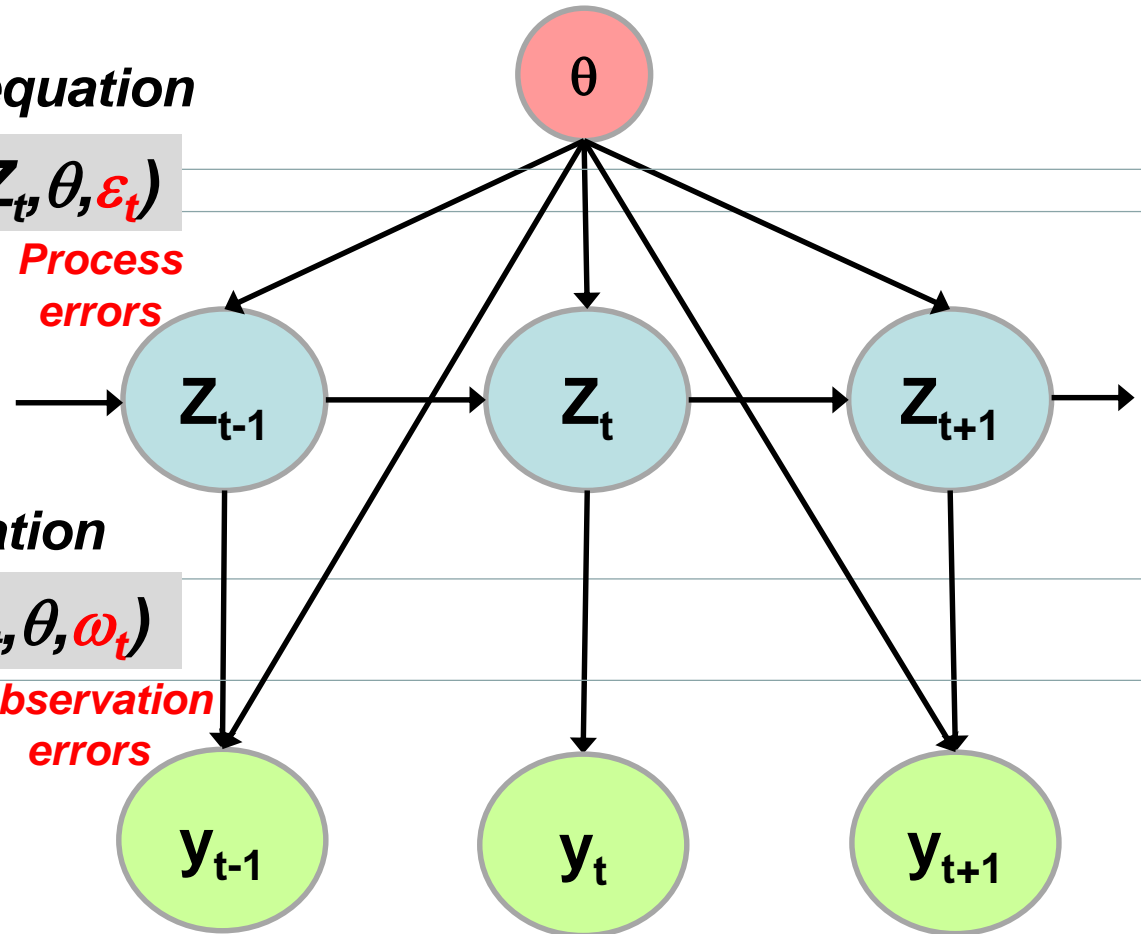
$$Z_{t+1} = f(Z_t, \theta, \varepsilon_t)$$

Process errors

Obs. equation

$$y_t = g(Z_t, \theta, \omega_t)$$

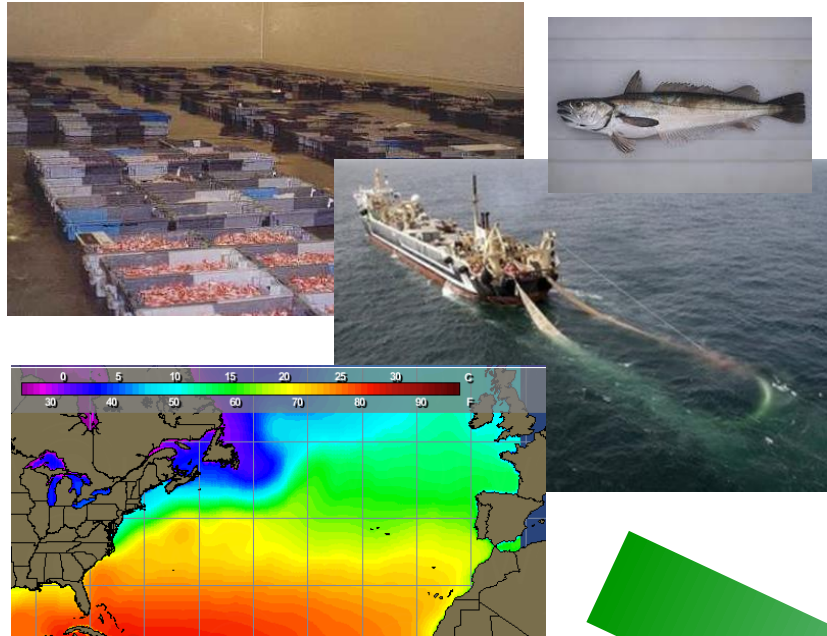
Observation errors



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**Hierarchical models
State-space models
&
Fisheries sciences**

La modélisation : une charnière essentielle



Observations

Modelling

- Demography
- Anthropic pressure
- Envir. pressure
- Inter-specific interactions



**Advice
Decision**

Integrated state-space population models are key tools in fisheries ecology

in particular in modern stock-assessment

“Integrating more data and more biological and ecological knowledge in stock assessments”



Aeberhard, W. H., Mills Flemming, J., & Nielsen, A. (2018). Review of State-Space Models for Fisheries Science. *Annual Review of Statistics and Its Application*, 5(1), 215-235. <https://doi.org/10.1146/annurev-statistics-031017-100427>

Punt, A. E., Dunn, A., Elvarsson, B. P., Hampton, J., Hoyle, S. D., Maunder, M. N., Methot, R. D., & Nielsen, A. (2020). Essential features of the next-generation integrated fisheries stock assessment package : A perspective. *Fisheries Research*, 229, 105617. <https://doi.org/10.1016/j.fishres.2020.105617>

Auger-Méthé, M., Newman, K., Cole, D., Empacher, F., Gryba, R., King, A. A., Leos-Barajas, V., Mills Flemming, J., Nielsen, A., Petris, G., & Thomas, L. (2021). A guide to state-space modeling of ecological time series. *Ecological Monographs*, 91(4), e01470. <https://doi.org/10.1002/ecm.1470>

State-space models



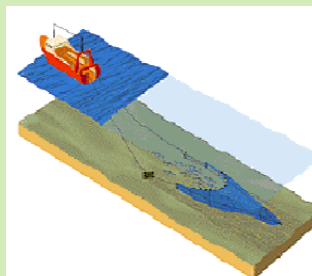
What I want to represent

What I see

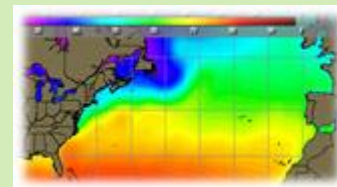
Commercial data



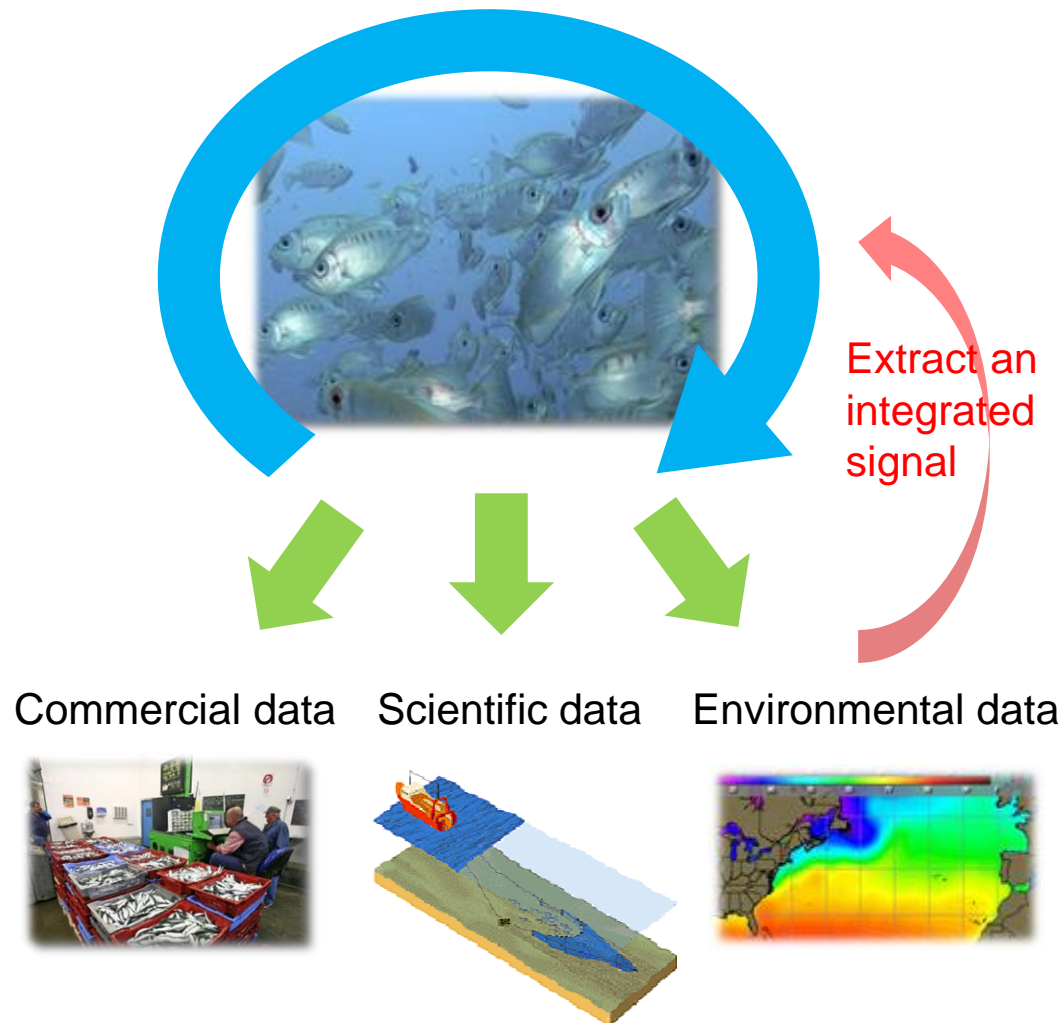
Scientific data



Environmental data



Develop integrated approaches to fusing multiple sources of observations in complex models



Complex ecological systems

- Hidden
- Demography
- Influence of multiple factors
- Multiple sources of variability and uncertainty
- A hierarchy of scales

Multiple observations with errors

- Heterogeneous surveys
- Sampling & measurement errors
- Missing data

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The Namibian hake fishery

Namibian Hake

The most important fish resource in Namibia

2 species

Merluccius capensis (“white hake”)

“white hake”

the dominant species

Merluccius paradoxus

“black hake”

Treated as a single stock

Look very similar

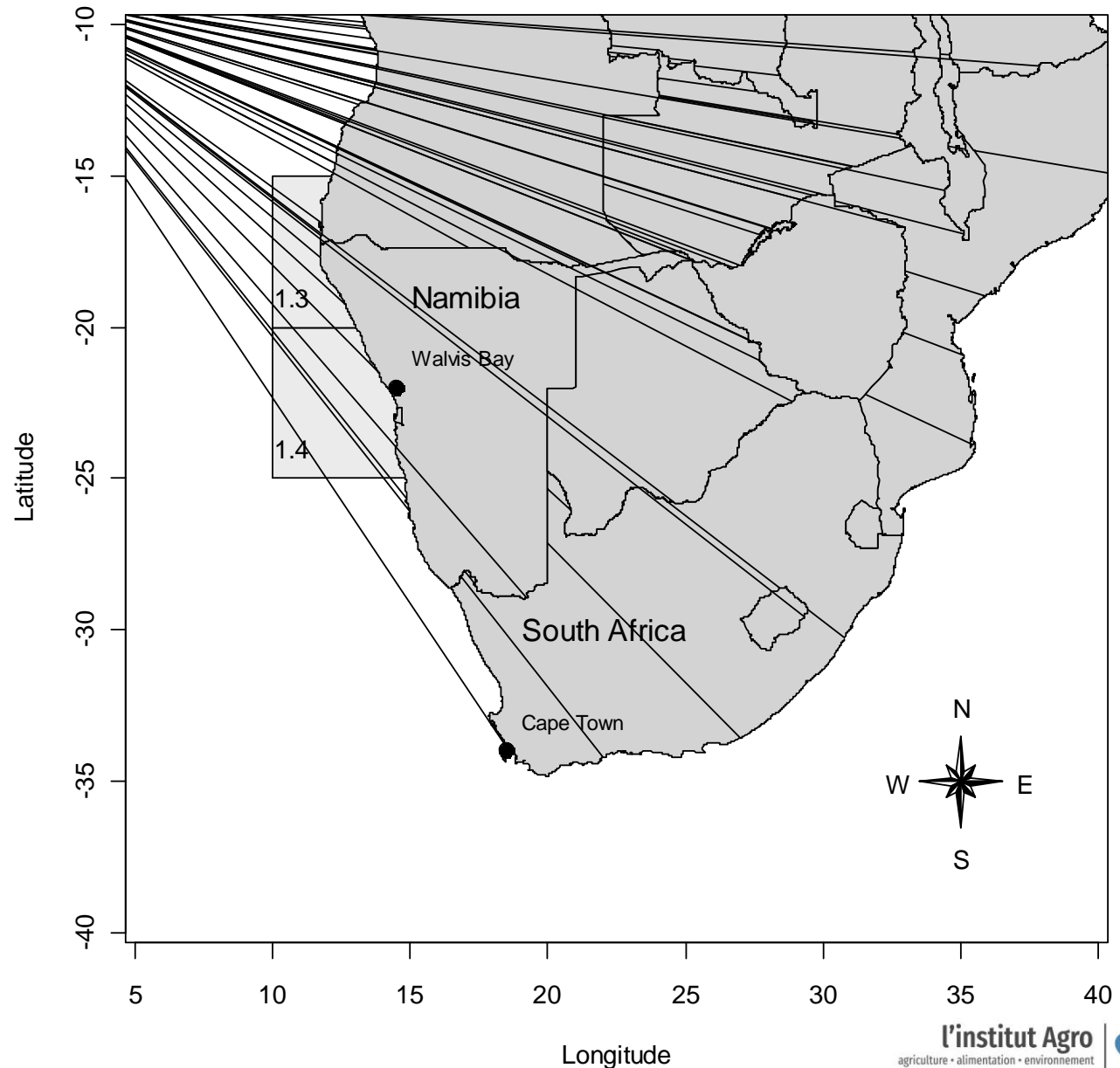
Difficult to record data separately



Merluccius capensis

The Benguela upwelling system

One of the world's major eastern boundary upwelling systems



Namibian Hake fishery - 1964-1988

A textbook case

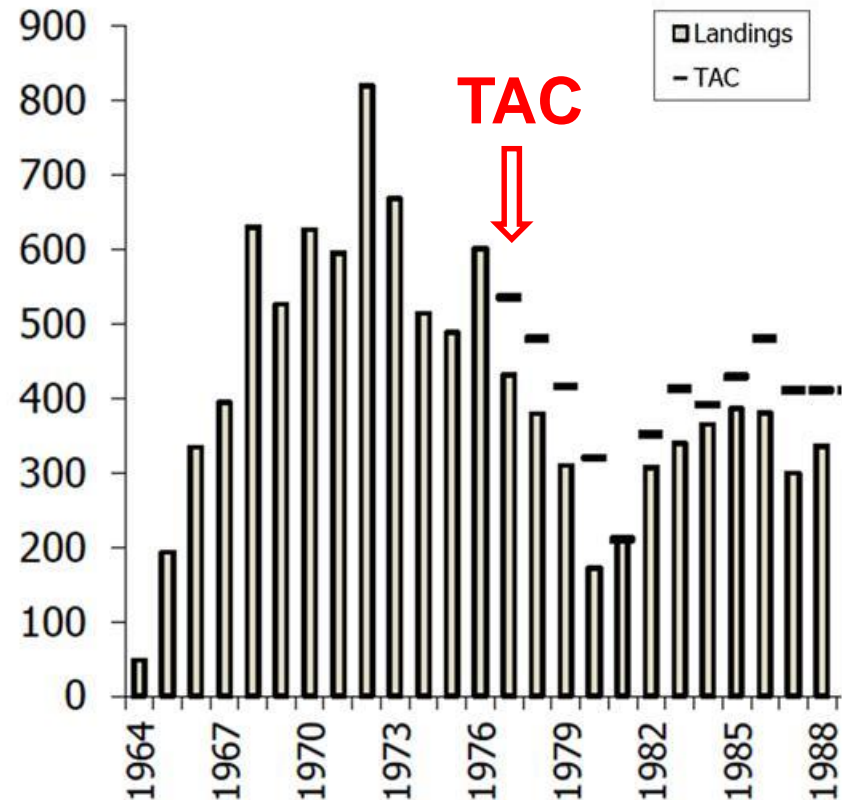
Exploitation of the Namibian hake resource commenced in 1964.

The fishery was unregulated over the period 1964-1976. During this period, an average of about 500 000 tonnes of hake was reported landed per year.

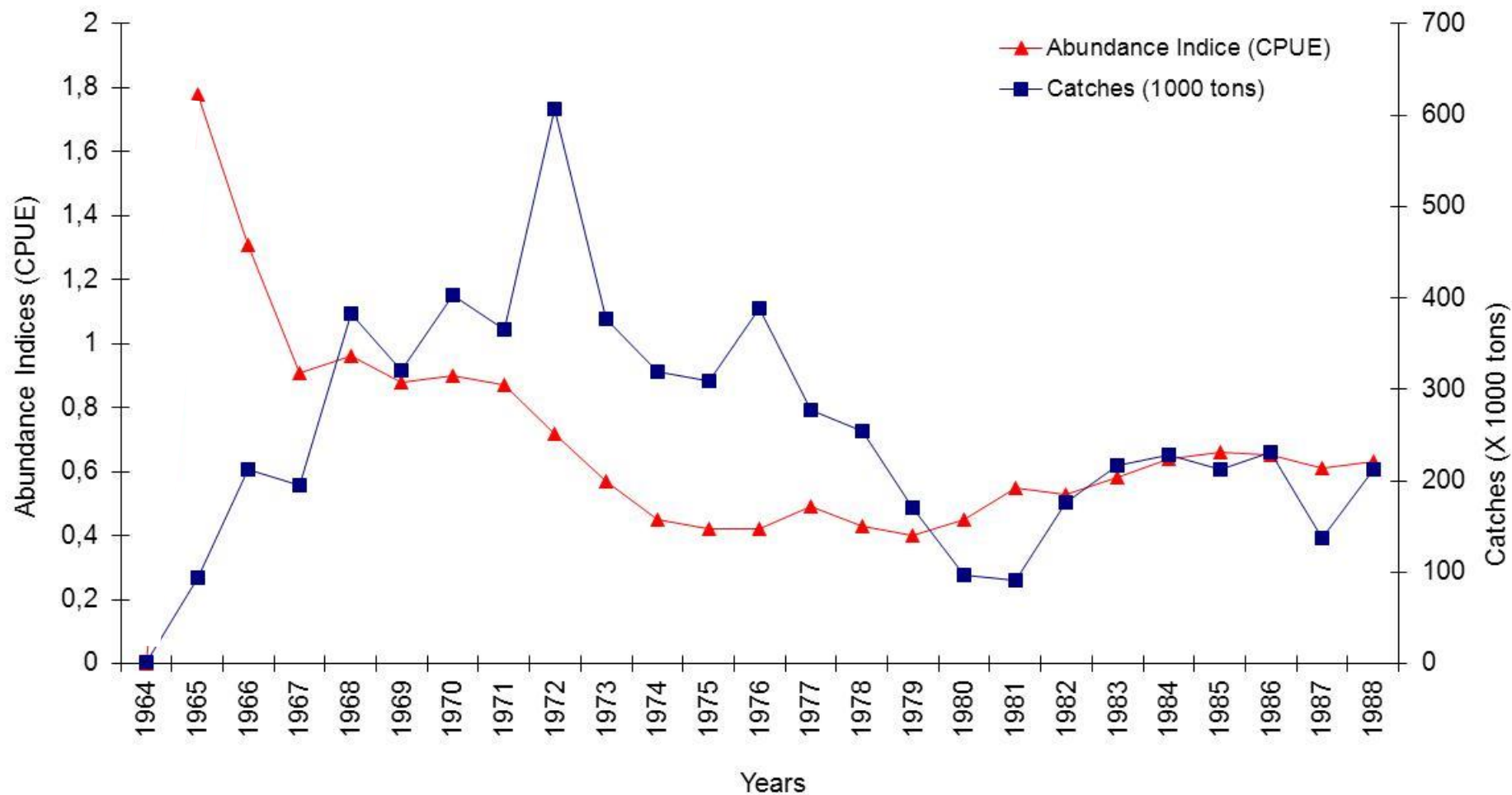
The International Commission for South East Atlantic Fisheries (ICSEAF) was formed in 1969.

A minimum mesh size of 110 cm was introduced in 1975.

From 1977 through 1989, the fishery is managed through annual TACs. Between 1980 and 1990, the average annual catch was reduced to about 325 000 tons.



Namibian Hake fishery - 1964-1988



Objectives

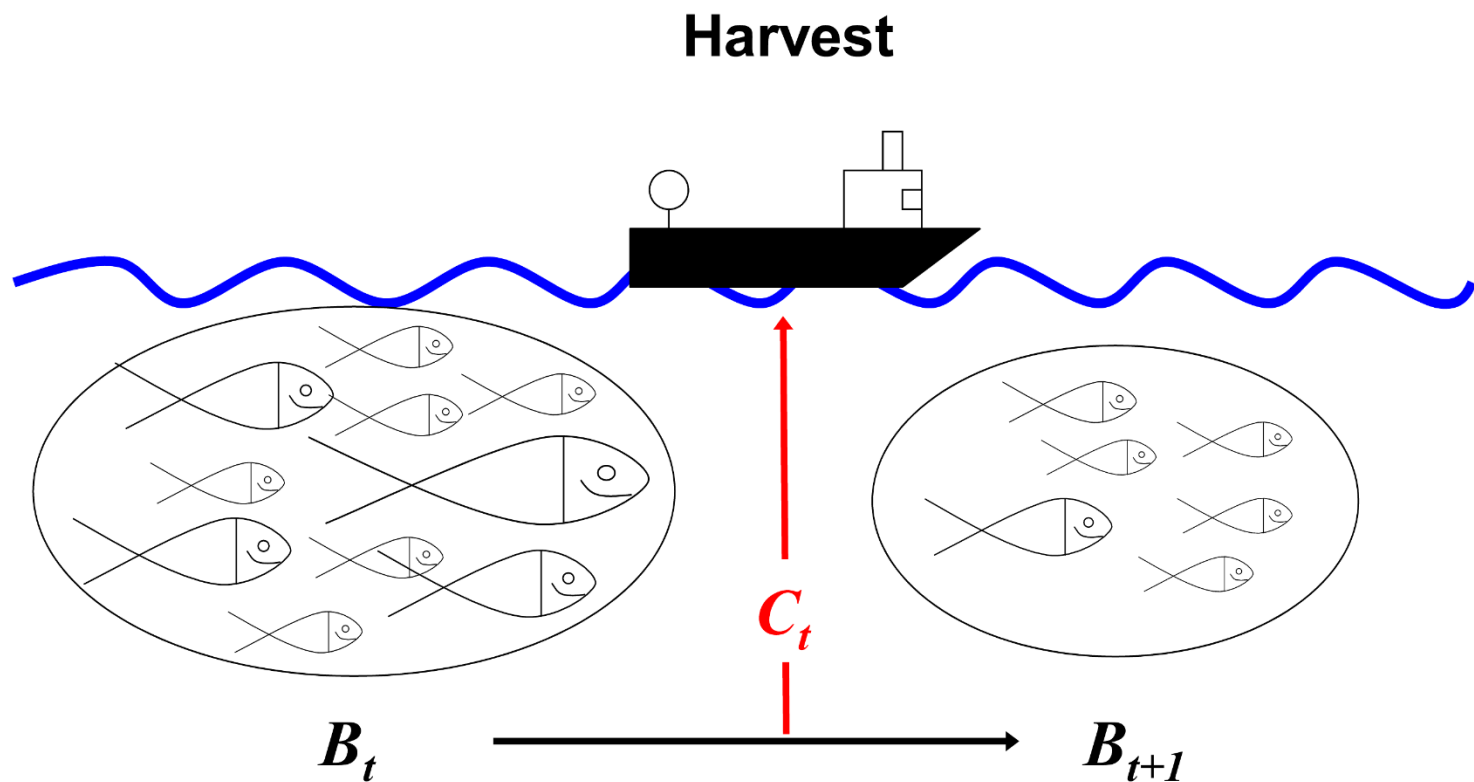
- **Assess fishery / stock status with regards to management reference points**
 - **Maximum Sustainable Yield (MSY)**
 - **Biomass at MSY ...**

(based on historical data)
- **Evaluate alternative management options (scenarios)**
- **All within a probabilistic rationale accounting for all sources of uncertainty**

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The Biomass production model

The Biomass production model



$$B_{t+1} = B_t + g(B_t) - C_t$$

The Biomass production model

A model to mimic the dynamic of the Biomass

A non-age-structured model (global model) used in practical stock assessments and fisheries management

Pro's of the surplus production model :

- Simple, parcimonious
- No need of detailed data (e.g. age –structured data)
- Quantity of interest for management are easily derived :
 - C_{MSY} : Captures at Maximum Sustainable Yield
 - B_{MSY} : Biomass level at MSY
 - F_{MSY} : Harvest rate at MSY
- Link with bio-economic modelling

The Biomass production model

$$\frac{dB(t)}{dt} = g(B(t), \theta) - C(B(t))$$

g = production function with parameters θ

C = captures (control). Generally $C = F \cdot B$

Difference model (discrete time)

Next biomass =

old biomass + recruitment - nat. mortality - captures

$$B(t+1) = B(t) + g(B(t), \theta) - C(t) \quad (\text{with } C(t) = F(t) \cdot B(t))$$

The Biomass production model

Production function g

Schaefer
$$\frac{dB(t)}{dt} = r \cdot B(t) \cdot \left(1 - \frac{B(t)}{K}\right) - C(t)$$

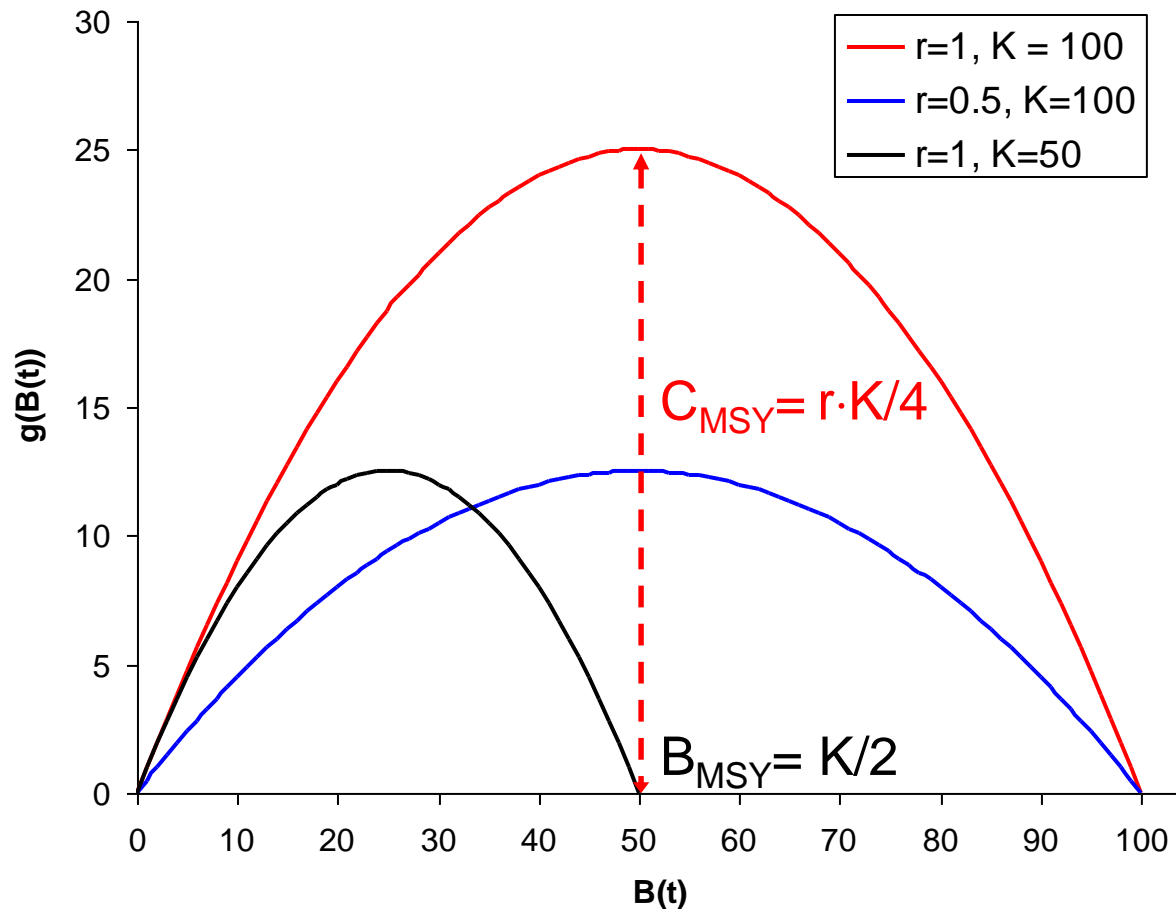
Fox
$$\frac{dB(t)}{dt} = r \cdot B(t) \cdot \left(1 - \frac{\log_e(B(t))}{\log_e(K)}\right) - C(t)$$

Pella-Tomlison
(general prod. model)
$$\frac{dB(t)}{dt} = r \cdot B(t) \cdot \left(1 - \left(\frac{B(t)}{K}\right)^{m-1}\right) - C(t)$$

Rk :
$$C(t) = q \cdot E \cdot B(t)$$

Reference points (for management)

Example : Schaefer



Deriving management reference points

Shaefer production model

$$B(t+1) = B(t) + g(B(t)) - C(t)$$

$$g(B(t)) = \rho \cdot B(t) \cdot \left(1 - \frac{1}{\kappa} \cdot B(t)\right)$$

Equilibrium state

$$B = B + g(B) - C \Rightarrow C = g(B)$$

MSY (maximum captures)

$$\left. \frac{\partial g(B)}{\partial B} \right|_{B_{MSY}} = 0$$

$$\frac{\partial g(B)}{\partial B} = \rho \cdot \left(1 - \frac{1}{\kappa} \cdot B\right) - \frac{\rho \cdot B}{\kappa} = \rho - 2 \cdot \frac{\rho \cdot B}{\kappa}$$

$$\left. \frac{\partial g(B)}{\partial B} \right|_{B_{MSY}} = 0 \Rightarrow B_{MSY} = \frac{\kappa}{2}$$

$$B_{MSY} = \frac{\kappa}{2}$$

$$C_{MSY} = \frac{\rho \cdot \kappa}{4}$$

$$F_{MSY} = \frac{C_{MSY}}{B_{MSY}} = \frac{\rho}{2}$$

Deriving management reference points

| | Modèle généralisé (m quelconque) | m=2 : Modèle de SCHAEFER | m=1 : Modèle exponentiel |
|-------------|--|-------------------------------|---|
| $B_0(E)$ | $K \left(1 - \frac{q}{r} E\right)^{\frac{1}{m-1}}$ | $K - \frac{q.K}{r} E$ | $K.e^{\left(-\frac{q.Ln(K)}{r} E\right)}$ |
| $U_0(E)$ | $q.K \left(1 - \frac{q}{r} E\right)^{\frac{1}{m-1}}$ | $q.K - \frac{q^2.K}{r} E$ | $q.K.e^{\left(-\frac{q.Ln(K)}{r} E\right)}$ |
| $Y_0(E)$ | $q.E.K \left(1 - \frac{q}{r} E\right)^{\frac{1}{m-1}}$ | $q.K.E - \frac{q^2.K}{r} E^2$ | $q.E.K.e^{\left(-\frac{q.Ln(K)}{r} E\right)}$ |
| E_r | $\frac{r}{q}$ | $\frac{r}{q}$ | ∞ |
| E_M | $\frac{r}{q} \cdot \frac{m-1}{m}$ | $\frac{r}{2.q}$ | $\frac{r}{q.Ln(K)}$ |
| $MSY : Y_M$ | $r.K \cdot \frac{m-1}{m^{\frac{m}{m-1}}}$ | $\frac{r.K}{4}$ | $\frac{r.K}{e.Ln(K)}$ |

Key assumptions

All parameters are constant over time

- Biological/ecological processes r, K
- Fisheries dependent process q
 - Explore the sensitivity of the results to change in q ?
 - See Cook et al. 2021 for an example of modelling change in fishing power

Cook, R., Acheampong, E., Aggrey-Fynn, J., & Heath, M. (2021). A fleet based surplus production model that accounts for increases in fishing power with application to two West African pelagic stocks. *Fisheries Research*, 243, 106048.

<https://doi.org/10.1016/j.fishres.2021.106048>