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In [1]: using Distributions
using Gadfly
using Interact
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In [2]: set_default_plot_size(25cm, 12cm)
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In [4]: @manipulate for samples in 10:50:1000, observations in 10:100:1000,  $\beta_0$  in 0:10,  $\beta_1$  in 0:0.1:1,  $u_\mu$  in -5:5,  $u_\sigma$  in 1:5

# Create lists for values of  $\beta_0$  and  $\beta_1$ 
 $\beta_0\_hat$  = []
 $\beta_1\_hat$  = []

# Collect values of  $\beta$  among different samples
for sample in 1:1:samples

    ## Initial
    x_values = rand(Uniform(0,100),observations)
    u = rand(Normal( $u_\mu$ ,  $u_\sigma$ ),observations)
    y_values =  $\beta_0$  +  $\beta_1$  * x_values + u

    ## Classical Linear Regression
    X = [ones(x_values) x_values]
     $\beta$  = inv(X'*X)*X'*y_values

    ## Save values
    push!( $\beta_0\_hat$ ,  $\beta[1]$ )
    push!( $\beta_1\_hat$ ,  $\beta[2]$ )

end

# Plot

## Example values
x_values = rand(Uniform(0,100),observations)
u = rand(Normal( $u_\mu$ ,  $u_\sigma$ ),observations)
y_values =  $\beta_0$  +  $\beta_1$  * x_values + u
X = [ones(x_values) x_values]
 $\beta$  = inv(X'*X)*X'*y_values

# CLR graph
graph_CLR = plot(
    layer(x=x_values, y=y_values, Geom.point, order=1),
    layer(x=x_values, y=X* $\beta$ , Geom.line, order=2, Theme(default_color=colorant"black", line_width=1pt)),
    Guide.XLabel("Values of x"),
    Guide.YLabel("Values of y"),
    Guide.Title("Classical Linear Regression"),
    Coord.Cartesian(xmin=0,xmax=100,ymin=0,ymax=100, fixed=true)
)

# Distribtuion of  $\beta_1$ 
graph_ $\beta$  = plot(
    layer(x= $\beta_1\_hat$ , Geom.histogram(bincount=50), order=1),
    layer(xintercept= $\beta_1$ , Geom.vline(color="black", style=[1mm], size=[.5mm]), order=3),
    Guide.XLabel("Estimates of  $\beta_1$ "),
    Guide.YLabel("Number of Observations"),
    Guide.Title("Distribution of  $\beta_1$ ")
)

hstack(graph_CLR, graph_ $\beta$ )

end
```

samples

observations

β_0

β_1

u_μ

u_σ

Out[4]:

