# Multilingual Knowledge-Based Question Answering

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**Abstract.** The desire for knowledge is one of the most important characteristics of humans. Since knowledge graphs store knowledge in a graph structure rather than plain text, logical query can be applied to obtain implicit information, which is a more efficient and effective way. Many researchers published approaches for converting English natural language questions to SPARQL queries, which are used to query Wikidata and DBpedia. However, multilingual question answering systems so far perform well on English, but not on other languages, especially on languages with missing training data. In this paper, we develop a knowledge-graph multilingual question-answering system using the mt5 model from google, a pre-trained transformer model, which supports 101 languages. Our system treats SPARQL queries as another language and converts natural language questions to SPARQL queries. We explore zero-shot along with different fine-tuning strategies to reach the best performance. Our experiment results show the state-of-the-art performance of the system not only on English, but also on other languages for QALD-9-plus dataset.

Keywords: Transformers · KGQA · Wikidata

## 1 Introduction

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The remainder of the paper starts with a presentation of related work (Sect. 3). It is followed by a presentation of hints on LATEX (??). Finally, a conclusion is drawn and outlook on future work is made (Sect. 6).

## 2 Backgroud Knowledge

- 2.1 Language Model
- 2.2 Feature-based Approach
- 2.3 Transformer-based Approach
- 2.4 Knowledge Graph
- 3 Related Work

## Language model

In Natural Language Processing (NLP), a probability distribution of words is defined as a Language model. Based on previous tokens and task, a language model predicts the next token continuously to generate a sequence. There are various approaches in language model. In feature-based approaches, linguistic features are extracted to understand a text. In transformer-based approaches, self-attention plays an significant part.

## Feature-based Approach

Feature-based approaches, e.g. parsing, POS tagging and Term Frequency-Inverse Document Frequency, embed input text into a numerical representation by analysing linguistic features, which are essential for computer to understand languages. POS tagging assigns part-of-speech or grammatical tagging to each word in a text with e.g. nouns, verbs, adjectives and more. Term Frequency-Inverse Document Frequency (TF-IDF) weights a word based on how often it appears in a text and how many documents include it. If a word appears rarely, it contains more information, therefore has a higher weight and vice versa.

Depending on the task, features are extracted from different aspects. Frequently, these features are combined with transformer-based approach to achieve better performance.

### Transformer-based Approach

Transformers is another popular approach in Natural Language Processing using self-attention. A model is pre-trained in unsupervised or semi-supervised manner on a large data set. For downstream tasks, the pre-trained model only needs to be fine-tuned on a few data for a short time, which saves a lot of time and compute resources. In 2017, Vaswani et al. introduced the first Transformers [32], which allows all input tokens to be processed in parallel via self-attention. In recent years, many transformer models are presented based on this paper, including new pre-training methods, different architectures, etc.

Bidirectional Encoder Representations from Transformers [7], referred to as BERT, is an encoder-based transformer, which is pre-trained with two tasks: masked language model and next sentence prediction on BooksCorpus [38] and English Wikipedia datasets. mBERT [6] is a variant of BERT which is pre-trained on 104 languages with Wikipedia data. After fine-tuning, it could be used for multilingual tasks e.g. translation. Rebalanced multilingual BERT (RemBert) [4] improves mBERT by reducing input embedding and enlarging output embedding, which shows that tweaking parameters is important in transformers and can lead to state-of-the-art performance.

GPT-2 [25] is a decoder only transformer, which functions like a language model: given all previous tokens to predict the next token. GPT-2 is pre-trained in unsupervised manner with 40 GB WebText and can be used for tasks, including question answering, summarization, and translation, even without fine-tuning.

Compare to BERT and GPT-2, Text-To-Text Transfer Transformer (T5) [26] combines encoder and decoder to convert NLP tasks into a text-to-text format. It is pre-trained on multi-tasking unsupervised and supervised. In unsupervised training, a BERT style approach is applied, namely mask tokens and predict next sentence. In supervised training, prefixes are given in input texts to define the tasks to be done. Thus, pre-trained T5 model can process several tasks well via adding the specific prefix to the text, e.g. "cola sentence: ..."for Sentence acceptability judgment (CoLA [34]), "summarize: ..."for summarization, "mrpc sentence1: ... sentence2: ..."for Paraphrasing/sentence similarity (MRPC [9]), and more. Xue et al. [35] released mT5 which utilizes the methodology as T5 for 101 languages. mT5 is trained on multilingual Colossal Clean Crawled Corpus (mC4) unsupervisedly, therefore, if must be fine-tuned and prefixes are not necessary, unless a multi-task fine-tuning is required. Similar to T5 model, BART [15] is also a sequence-to-sequence model, which consists of a encoder and a decoder and pre-trained with a combination of span masking and sentence shuffling objectives.

mBART [16] is a cross-lingual version of BART, pre-trained with denoising full texts in 25 languages. In multilingual transformers, XLM [13], XLM-RoBERTa [5] also achieves state-of-the-art performance and support 100 languages. Both of them optimize BERT architecture and pre-trained on 100 languages.

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MARGE [14] provides another pre-training approach, reconstruct a document in one language by retrieving documents in other languages. MARGE model supports 26 languages and performs well even merely pre-training.

## Knowledge Graph

In contrast to many information in the Internet are stored in plain text, Knowledge graphs manages in a structural fashion. Relations between entities connects them together as edges in a graph, so that knowledge is linked instead of a lot of isolated island and implicit knowledge can be simply retrieved. Wikidata [33] is currently the largest knowledge graph, which contains about 100 Million instances in over 400 languages. It can be applied in e.g. enriching informations for applications, deriving new insights from stated data, etc.

DBpedia [1] consists of structured infobox information extracted from Wikipedia. It contains about 900 million triples by January 2021 and provides free APIs for online accessing and querying.

YAGO [29] is also one of the large knowledge graph, which combines information from Wikidata with WordNet [10]. In the newest YAGO 4 [20], they combine Wikidata with more user-friendly taxonomy from schema.org [11] while containing more than 64 million entities and 2 billion facts.

NELL [3] is short for Never-Ending Language Learner developed by Carlson et al., which performs a reading task and a learning task each day to extract information from Internet while learning to categorise noun phrases and find relations to pairs of noun phrases. NELLs expands itself rapidly, for example, it contains more than 242,000 new facts after running it 67 days.

OpenCyc [17] is a subset of Cyc knowledge base, a knowledge graph with about forty years history. OpenCyc contains 239,000 concepts in its 4.0 version, accessible via a interpreter on Linux and Microsoft Windows. However, it is not available after 2017.

conceptnet [28] represents facts in sentences in knowledge graph with terms and assertions, including knowledge from Open Mind Common Sense (OMCS), Wiktionary, Open Multilingual WordNet [2], etc. There are roughly 34 million statements in conceptnet and 304 language are supported in total, 10 of them have core support.

Wikidata, DBpedia and YAGO have SPARQL endpoint while NELL and conceptnet doesn't support SPARQL query. OpenCyc is currently not accessible. Wikidata has the most language supports in these knowledge graphs. Moreover, entities and relations are represented and stored with ids in Wikidata while these are all represented explicitly in DBpedia.

## Knowledge Graph Question Answering (KGQA)

KGQA-Leaderboard [23] is a open source platform to record and compare scores of QA systems for different datasets. Presently, SGPT [27] is leading in English QALD-9 [31] dataset and QAnswer in the multilingual QALD-9-PLUS [22] dataset.

SGPT [27] combines feature-based approach and transformer-based approach. Linguistic features, e.g. POS-tag, dependency relation embedding, are extracted from the question, then fed into transformer encoders, lastly GPT-2 generates a SPARQL query. This approach avoids high cost of templates and provides deeper understanding of questions using linguistic features.

To et al. [30] derived a Linguistic Term Question Answering (LingTeQA), in which a natural language question is analysed with dependency tree and converted to a question template, then a SPARQL template is retrieved from pre-generated template set to create SPARQL query.

qaSQP [36] is proposed by Zheng et al. Instead of detecting the template to use for a question, they use a structural query pattern framework: build a sketch of the query, then extend entities according to the question and lastly add constraints defined in the question.

Panchbhai et al. [18] used a completely different approach. They consider SPARQL as another language and use Neural Machine Translation to transform natural language questions to SPARQL queries. A Neural SPARQL Machine is built to process the Sequence-to-Sequence task, including three components, namely generator, learner and interpreter.

## Multilingual KGQA

To the best of our knowledge, there are only a few researches focusing on multilingual KGQA.

Veyseh [24] proposed a four-stage cross-lingual approach: keyword extraction, keyword classification, entity linking and ontology type extraction and answer extraction using unified semantic representation of concepts, which is evaluated on Persian and Spanish.

Hakimov et al. also used semantic parsing mapping natural language input into logical form and developed AMUSE [12], which works for English, German ans Spanish.

Platypus [19] is presented by Tanon et al., integrating two analyzers: grammatical and template-based analyzer, for queuing Wikidata in 3 languages.

Diefenbach et al. [8] provided an approach over the Semantic Web, which works on 5 knowledge-graphs with 5 different languages.

Recently, transformer-based approach is applied to multilingual KGQA.

Zhou et al. [37] derived an approach using zero-shot transfer setting, given only a high-resource language (e.g. English) and exploit unsupervised bilingual lexicon induction (BLI) to generate augmented training data. The effectiveness is proved by their experiment in 11 zero-resource languages.

Perevalov et al. [21] experience with machine translation to extend supported languages of existing multilingual KGQA systems. They demonstrate that translated to English provides the best performance in most cases and machine translation quality only has small or moderate positive correlation with the question answering score.

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- 4 Approach
- 5 Experiments
- 5.1 Knowledge Graph and Dataset
- 5.2 Experimental Settings
- 5.3 Results
- 5.4 Analysis

## 6 Conclusion and Outlook

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