

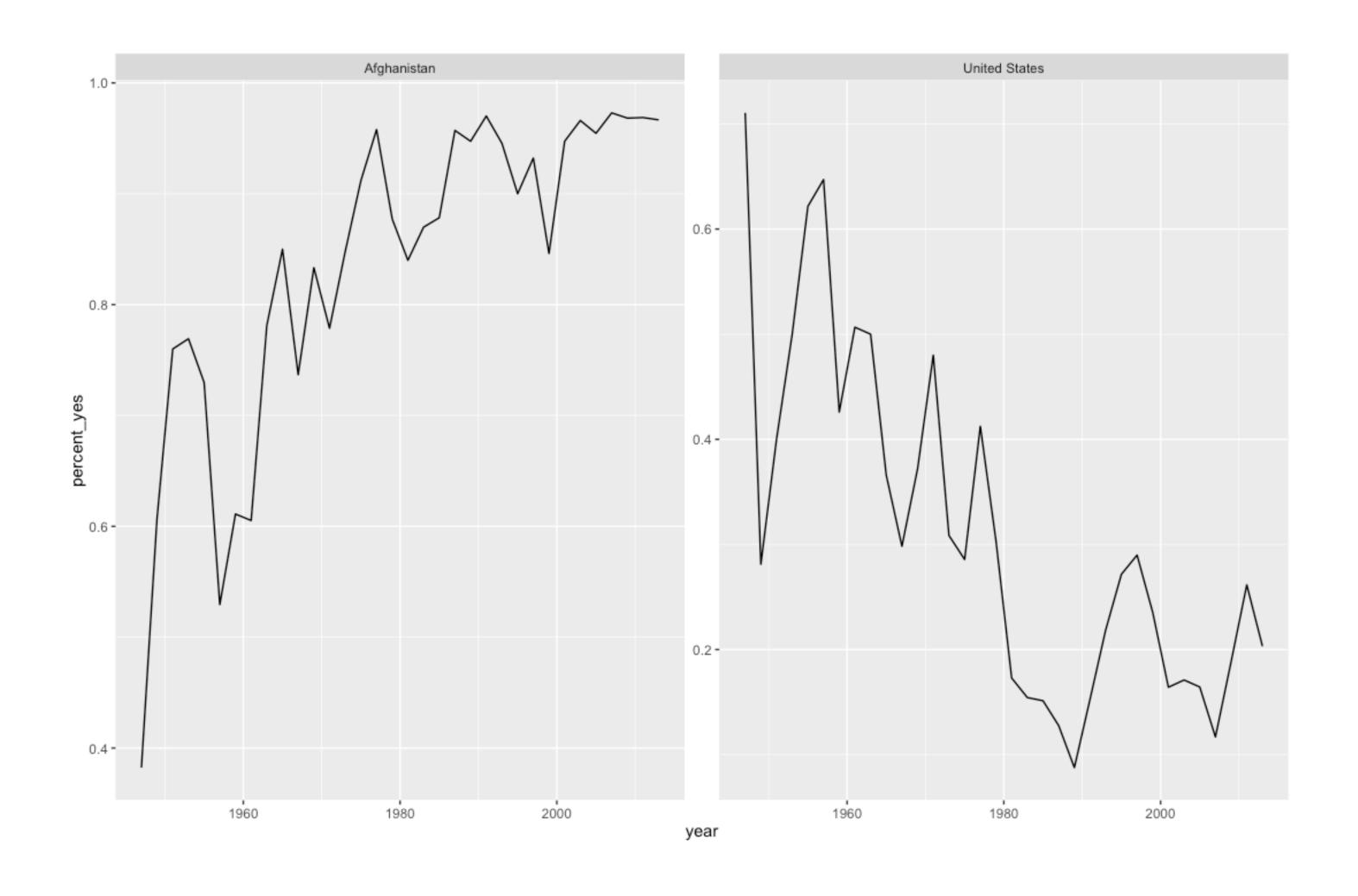


# Linear regression





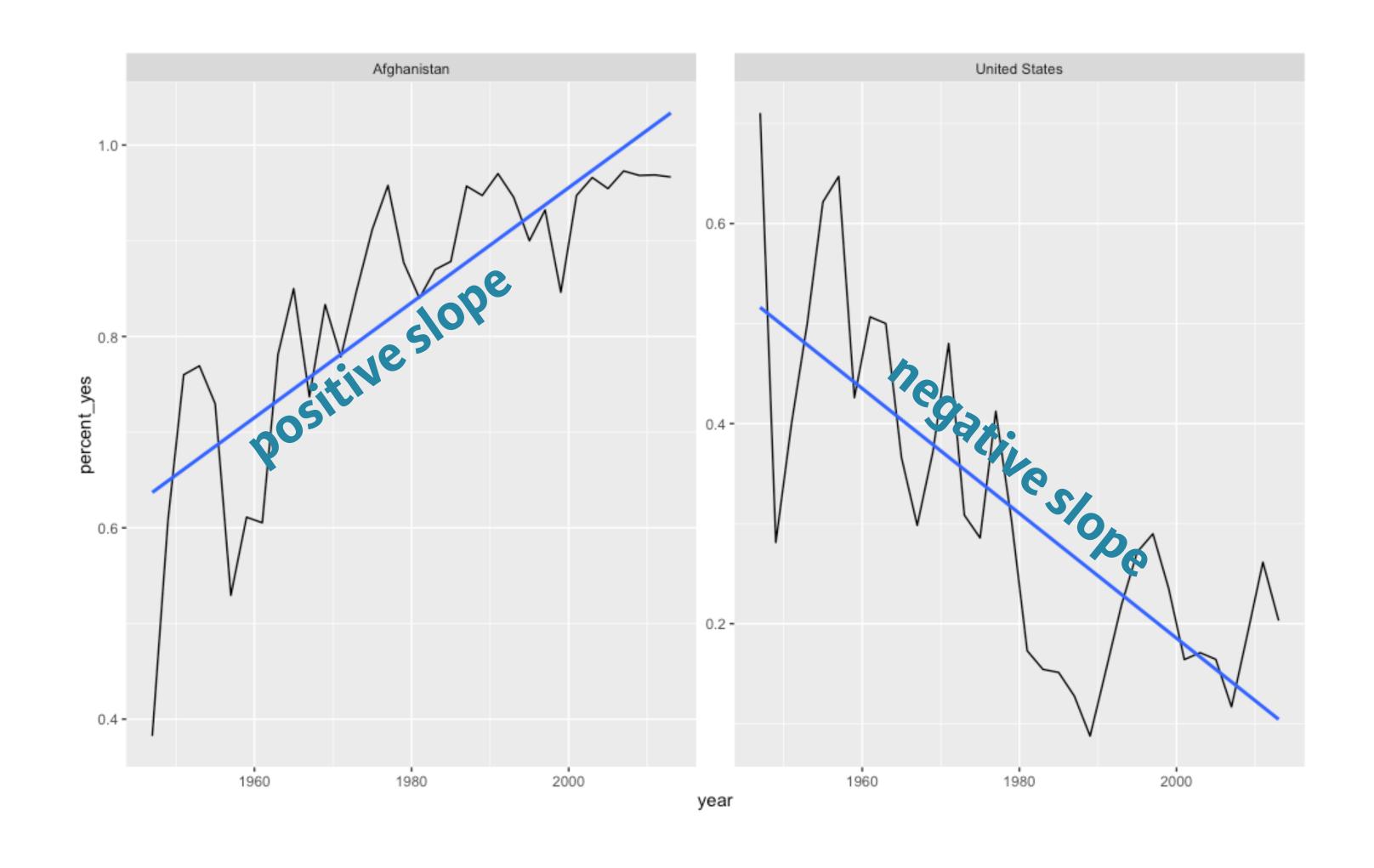
# Quantifying trends







## Linear regression







## Fitting model to Afghanistan

```
> afghanistan <- by_year_country %>%
    filter(country == "Afghanistan")
> afghanistan
# A tibble: 34 \times 4
        country total percent_yes
   year
   <dbl> <chr> <int>
                                <dbl>
   1947 Afghanistan 34 0.3823529
   1949 Afghanistan
                     51
                            0.6078431
   1951 Afghanistan
                       25
                           0.7600000
   1953 Afghanistan
                       26
                            0.7692308
   1955 Afghanistan
                       37
                            0.7297297
   1957 Afghanistan
                       34
                            0.5294118
   1959 Afghanistan
                            0.6111111
   1961 Afghanistan
                            0.6052632
    1963 Afghanistan
                       32
                            0.7812500
   1965 Afghanistan
                            0.8500000
 ... with 24 more rows
```

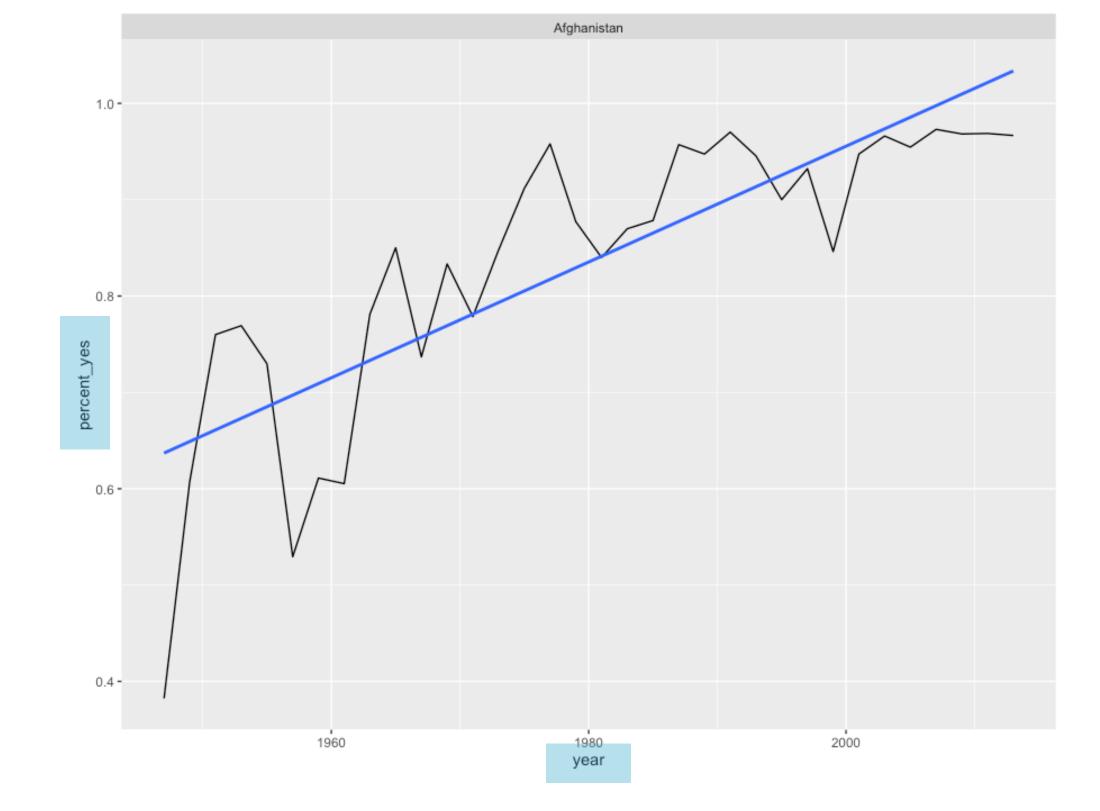
dependent variable



## Fitting model to Afghanistan

explained by

> model <- lm(percent\_yes ~ year, data = afghanistan)</pre>



independent variable





## Fitting model to Afghanistan

```
> summary(model)
Call:
lm(formula = percent_yes ~ year, data = afghanistan)
Residuals:
             1Q Median 3Q
     Min
                                            Max
-0.254667 -0.038650 -0.001945 0.057110 0.140596
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.106e+01 1.471e+00 -7.523 1.44e-08 ***
            6.009e-03 7.426e-04 8.092 3.06e-09 ***
year
                                     3e-09 = .00000003
            6e-03 = .006
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.08497 on 32 degrees of freedom
Multiple R-squared: 0.6717, Adjusted R-squared: 0.6615
F-statistic: 65.48 on 1 and 32 DF, p-value: 3.065e-09
```



Visualization can surprise you, but it doesn't scale well. Modeling scales well, but it can't surprise you.

-Hadley Wickham





# Let's practice!





# Tidying models with broom



## A model fit is a "messy" object

```
> summary(model)
Call:
lm(formula = percent_yes ~ year, data = afghanistan)
Residuals:
     Min
            1Q Median 3Q
                                            Max
-0.254667 -0.038650 -0.001945 0.057110 0.140596
Coefficients:
             Estimate Std. Error t value Pr(>|t|)
(Intercept) -1.106e+01 1.471e+00 -7.523 1.44e-08 ***
            6.009e-03 7.426e-04 8.092 3.06e-09 ***
year
Signif. codes:
               0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
Residual standard error: 0.08497 on 32 degrees of freedom
Multiple R-squared: 0.6717, Adjusted R-squared: 0.6615
F-statistic: 65.48 on 1 and 32 DF, p-value: 3.065e-09
```





#### Models are difficult to combine

```
> model1 <- lm(percent_yes ~ year, data = afghanistan)
> model2 <- lm(percent_yes ~ year, data = united_states)
> model3 <- lm(percent_yes ~ year, data = canada)</pre>
```





#### broom turns a model into a data frame



### Tidy models can be combined

```
> model1 <- lm(percent_yes ~ year, data = afghanistan)</pre>
> model2 <- lm(percent_yes ~ year, data = united_states)</pre>
> tidy(model1)
        term estimate std.error statistic
                                                      p.value
1 (Intercept) -11.063084650 1.4705189228 -7.523252 1.444892e-08
               0.006009299 0.0007426499 8.091698 3.064797e-09
        year
> tidy(model2)
        term estimate std.error statistic
                                                     p.value
1 (Intercept) 12.664145512 1.8379742715 6.890274 8.477089e-08
        year -0.006239305 0.0009282243 -6.721764 1.366904e-07
> bind_rows(tidy(model1), tidy(model2))
                  estimate std.error statistic
                                                      p.value
        term
1 (Intercept) -11.063084650 1.4705189228 -7.523252 1.444892e-08
     year 0.006009299 0.0007426499 8.091698 3.064797e-09
3 (Intercept) 12.664145512 1.8379742715 6.890274 8.477089e-08
        year -0.006239305 0.0009282243 -6.721764 1.366904e-07
```





# Let's practice!





# Nesting for multiple models





### One model for each country







## Start with one row per country

```
> by_year_country
# A tibble: 4,744 × 4
                                 country total percent_yes
    year
                                   <chr> <int>
   <dbl>
                                                      <dbl>
                             Afghanistan
    1947
                                            34 0.3823529
                               Argentina
                                            38
                                                 0.5789474
    1947
                               Australia
3
                                            38
                                                 0.5526316
    1947
                                 Belarus
                                            38
    1947
                                                 0.5000000
                                 Belgium
                                            38
    1947
                                                 0.6052632
    1947 Bolivia, Plurinational State of
                                            37
                                                 0.5945946
                                  Brazil
    1947
                                            38
                                                 0.6578947
                                  Canada
                                            38
    1947
                                                 0.6052632
8
                                   Chile
                                            38
                                                 0.6578947
    1947
                                Colombia
                                            35
    1947
                                                 0.5428571
  ... with 4,734 more rows
```





#### nest() turns it into one row per country

```
> library(tidyr)
> by_year_country %>%
    nest(-country) -country means "nest all except country"
# A tibble: 200 × 2
                              country
                                                     data
                                <chr>
                                                   t>
                                                           Contains the "nested"
                         Afghanistan <tibble [34 × 3]>
                                                          year, total, percent_yes data
                           Argentina <tibble [34 × 3]> forjust Afghanistan
                           Australia <tibble [34 × 3]>
3
                              Belarus <tibble [34 × 3]>
                              Belgium <tibble [34 × 3]>
5
   Bolivia, Plurinational State of <tibble [34 × 3]>
                               Brazil <tibble [34 × 3]>
                               Canada <tibble [34 × 3]>
8
                                Chile <tibble [34 × 3]>
9
                            Colombia <tibble [34 \times 3]>
  ... with 190 more rows
```

```
# A tibble: 34 × 3
   year total percent_yes
                     <dbl>
   1947
                0.3823529
                0.6078431
   1951
                0.7600000
   1953
                0.7692308
   1955
                0.7297297
   1957
                0.5294118
                0.6111111
   1961
                0.6052632
                0.7812500
           40 0.8500000
# ... with 24 more rows
```



### unnest() does the opposite

```
> by_year_country %>%
    nest(country) %>%
    unnest(data)
# A tibble: 4,744 × 4
    year total percent_yes
                                   country
   <dbl> <int>
                     <dbl>
                                     <chr>
    1947
                              Afghanistan
            34
                 0.3823529
                                 Argentina
    1947
            38
                 0.5789474
                 0.5789474 United Kingdom
            38
3
    1947
                                 Australia
            38
                 0.5526316
    1947
                                   Belarus
5
    1947
            38
                 0.5000000
            38
    1947
                 0.5000000
6
                                     Egypt
                              South Africa
    1947
            38
                 0.5000000
            38
                                Yugoslavia
    1947
                 0.5000000
                                   Belgium
            38
9
                 0.6052632
    1947
            38
                                    Canada
   1947
                 0.6052632
```





# Let's practice!





# Fitting multiple models



#### nest() turns data into one row per country

```
> library(tidyr)
> by_year_country %>%
    nest(-country)
# A tibble: 200 × 2
                                                               # A tibble: 34 × 3
                                                                 year total percent_yes
                               country
                                                        data
                                                                         0.3823529
                                  <chr>
                                                      0.6078431
                                                                        0.7600000
                           Afghanistan <tibble [34 × 3]>
                                                                 1953 26 0.7692308
                                                                 1955 37 0.7297297
                             Argentina <tibble [34 × 3]>
                                                                1957 34 0.5294118
                                                                 1959 54 0.6111111
                             Australia <tibble [34 × 3]>
3
                                                                 1961
                                                                      76 0.6052632
                                                                         0.7812500
                               Belarus <tibble [34 × 3]>
                                                                        0.8500000
                                                               # ... with 24 more rows
                               Belgium <tibble [34 × 3]>
5
   Bolivia, Plurinational State of <tibble [34 × 3]>
                                 Brazil <tibble [34 × 3]>
                                 Canada <tibble [34 × 3]>
8
                                  Chile <tibble [34 × 3]>
9
                              Colombia <tibble [34 \times 3]>
  ... with 190 more rows
```





#### map () applies an operation to each item in a list

```
> v <- list(1, 2, 3)
> map(v, ~ . * 10)
[[1]]
[1] 10

[[2]]
[1] 20

[[3]]
[1] 30
```





#### map () fits a model to each dataset

```
> library(purrr)
> by_year_country %>%
    nest(-country) %>%
    mutate(models = map(data, ~ lm(percent_yes ~ year, .)))
# A tibble: 200 × 3
                                                        models
                           country
                                                 data
                                                        t>
                             <chr>
                                               <list>
                       Afghanistan <tibble [34 × 3]> <S3: lm>
                         Argentina <tibble [34 × 3]> <S3: lm>
                         Australia <tibble [34 × 3]> <S3: lm>
                           Belarus <tibble [34 × 3]> <S3: lm>
4
                           Belgium <tibble [34 × 3] > <S3: lm>
5
   Bolivia, Plurinational State of <tibble [34 × 3]> <S3: lm>
                            Brazil <tibble [34 × 3]> <S3: lm>
                            Canada <tibble [34 × 3]> <S3: lm>
                             Chile <tibble [34 \times 3] > (S3: lm)
                          Colombia <tibble [34 × 3]> <S3: lm>
10
# ... with 190 more rows
```





p.value

#### tidy turns each model into a data frame

```
> by_year_country %>%
                                                                                                                                                                                                                             > tidy(model1)
             nest(-country) %>%
                                                                                                                                                                                                                                                                                                            std.error statistic
                                                                                                                                                                                                                                                                              estimate
                                                                                                                                                                                                                                                    term
                                                                                                                                                                                                                             1 (Intercept) -11.063084650 1.4705189228 -7.523252 1.444892e-08
             mutate(models = map(data, ~ lm(percent_yes ~ year, .))) %>%
                                                                                                                                                                                                                                                                     0.006009299 0.0007426499 8.091698 3.064797e-09
             mutate(tidied = map(models, tidy))
# A tibble: 200 × 4
                                                                                                                                                            data models
                                                                                                                                                                                                                                                             tidied
                                                                                          country
                                                                                                                                                         t> <list>
                                                                                                                                                                                                                                                              st>
                                                                                                 <chr>
                                                                            Afghanistan <tibble [34 × 3]> <S3: lm> <data.frame [2 × 5]>
                                                                                   Argentina <tibble [34 × 3]> <S3: lm> <data.frame [2 × 5]>
                                                                                   Australia <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] > (S3: lm) < data.frame [2 \
                                                                                          Belarus <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] > lm
                                                                                          Belgium <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] >
          Bolivia, Plurinational State of <tibble [34 \times 3] \times (S3: lm) \times (data.frame [2 \times 5] \times (lm))
                                                                                              Brazil <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] >
                                                                                             Canada <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] >
                                                                                                Chile <tibble [34 \times 3] <S3: lm> <data.frame [2 \times 5] >
                                                                                      Colombia <tibble [34 \times 3] > (S3: lm) < data.frame <math>[2 \times 5] > (S3: lm) 
10
                   with 190 more rows
```





#### unnest() combines the tidied models

```
> by_year_country %>%
   nest(-country) %>%
   mutate(models = map(data, ~ lm(percent_yes ~ year, .))) %>%
   mutate(tidied = map(models, tidy)) %>%
   unnest(tidied)
# A tibble: 399 × 6
                                                                    p.value
      country
                     term
                               estimate
                                          std.error statistic
        <chr>
                    <chr>
                                  <dbl>
                                               <dbl>
                                                         <dbl>
                                                                      <dbl>
   Afghanistan (Intercept) -11.063084650 1.4705189228 -7.523252 1.444892e-08
                     year 0.006009299 0.0007426499 8.091698 3.064797e-09
  Afghanistan
    Argentina (Intercept)
                           -9.464512565 2.1008982371 -4.504984 8.322481e-05
    Argentina
                            0.005148829 0.0010610076 4.852773 3.047078e-05
                     year
    Australia (Intercept)
                           -4.545492536 2.1479916283 -2.116159 4.220387e-02
    Australia
                            0.002567161 0.0010847910 2.366503 2.417617e-02
                     year
      Belarus (Intercept)
                           -7.000692717 1.5024232546 -4.659601 5.329950e-05
      Belarus
                            0.003907557 0.0007587624 5.149908 1.284924e-05
                     year
      Belgium (Intercept)
                           -5.845534016 1.5153390521 -3.857575 5.216573e-04
      Belgium
                            0.003203234 0.0007652852 4.185673 2.072981e-04
                     year
# ... with 389 more rows
```





# Let's practice!





# Working with many tidy models



### We have a model for each country

```
> country_coefficients
# A tibble: 399 × 6
                               estimate
                                          std.error statistic
       country
                      term
                                                                     p.value
         <chr>
                     <chr>
                                   <dbl>
                                                <dbl>
                                                          <dbl>
                                                                       <dbl>
   Afghanistan (Intercept) -11.063084650 1.4705189228 -7.523252 1.444892e-08
   Afghanistan
                             0.006009299 0.0007426499 8.091698 3.064797e-09
                      year
                            -9.464512565 2.1008982371 -4.504984 8.322481e-05
     Argentina (Intercept)
     Argentina
                             0.005148829 0.0010610076 4.852773 3.047078e-05
                      year
    Australia (Intercept)
                            -4.545492536 2.1479916283 -2.116159 4.220387e-02
     Australia
                             0.002567161 0.0010847910 2.366503 2.417617e-02
                      year
                            -7.000692717 1.5024232546 -4.659601 5.329950e-05
       Belarus (Intercept)
       Belarus
                             0.003907557 0.0007587624 5.149908 1.284924e-05
                      year
                            -5.845534016 1.5153390521 -3.857575 5.216573e-04
       Belgium (Intercept)
       Belgium
                             0.003203234 0.0007652852 4.185673 2.072981e-04
                      year
     with 389 more rows
```



## Filter for the year term (slope)

```
> country_coefficients %>%
    filter(term == "year")
# A tibble: 199 × 6
                                                      std.error statistic
                                                                                p.value
                                           estimate
                          country term
                                              <dbl>
                                                           <dbl>
                                                                     <dbl>
                                                                                  <dbl>
                            <chr> <chr>
                      Afghanistan year 0.006009299 0.0007426499 8.091698 3.064797e-09
                        Argentina year 0.005148829 0.0010610076
                                                                  4.852773 3.047078e-05
                        Australia year 0.002567161 0.0010847910 2.366503 2.417617e-02
                                  year 0.003907557 0.0007587624 5.149908 1.284924e-05
                          Belgium year 0.003203234 0.0007652852
                                                                  4.185673 2.072981e-04
   Bolivia, Plurinational State of
                                   year 0.005802864 0.0009657515
                                                                  6.008651 1.058595e-06
                                   year 0.006107151 0.0008167736 7.477164 1.641169e-08
                                  year 0.001515867 0.0009552118 1.586943 1.223590e-01
                           Canada
                                   year 0.006775560 0.0008220463
                                                                  8.242310 2.045608e-09
                                  year 0.006157755 0.0009645084
10
                         Colombia
                                                                  6.384346 3.584226e-07
  ... with 189 more rows
```

Multiple hypothesis correction because some p-values will be less than .05 by chance



## Filtered by adjusted p-value

```
> country_coefficients %>%
   filter(term == "year") %>%
   filter(p.adjust(p.value) < .05)</pre>
# A tibble: 61 × 6
                          country term
                                           estimate
                                                      std.error statistic
                                                                                p.value
                            <chr> <chr>
                                              <dbl>
                                                           <dbl>
                                                                     <dbl>
                                                                                  <dbl>
                      Afghanistan year 0.006009299 0.0007426499 8.091698 3.064797e-09
                        Argentina year 0.005148829 0.0010610076 4.852773 3.047078e-05
                          Belarus year 0.003907557 0.0007587624 5.149908 1.284924e-05
                          Belgium year 0.003203234 0.0007652852 4.185673 2.072981e-04
   Bolivia, Plurinational State of
                                  year 0.005802864 0.0009657515 6.008651 1.058595e-06
                           Brazil year 0.006107151 0.0008167736 7.477164 1.641169e-08
                            Chile year 0.006775560 0.0008220463 8.242310 2.045608e-09
                         Colombia
                                   year 0.006157755 0.0009645084
                                                                  6.384346 3.584226e-07
                       Costa Rica year 0.006539273 0.0008119113 8.054171 3.391094e-09
                                  year 0.004610867 0.0007205029
10
                                                                  6.399512 3.431579e-07
```





# Let's practice!