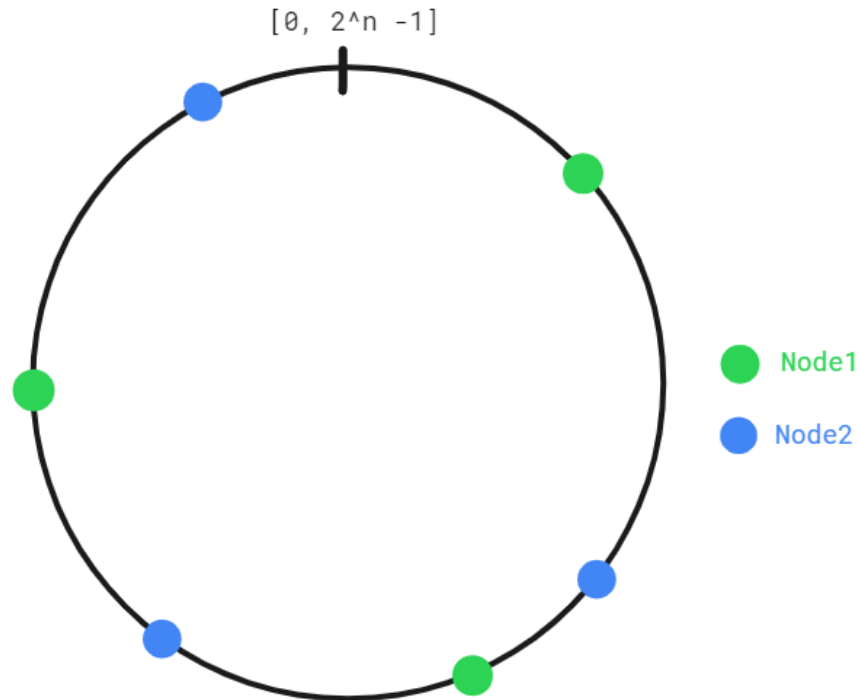


# Consistent Hashing

## Server Node

1. Treat Hash function as a cycle.
2. Each Server is assigned as **multiple Nodes uniformly**.

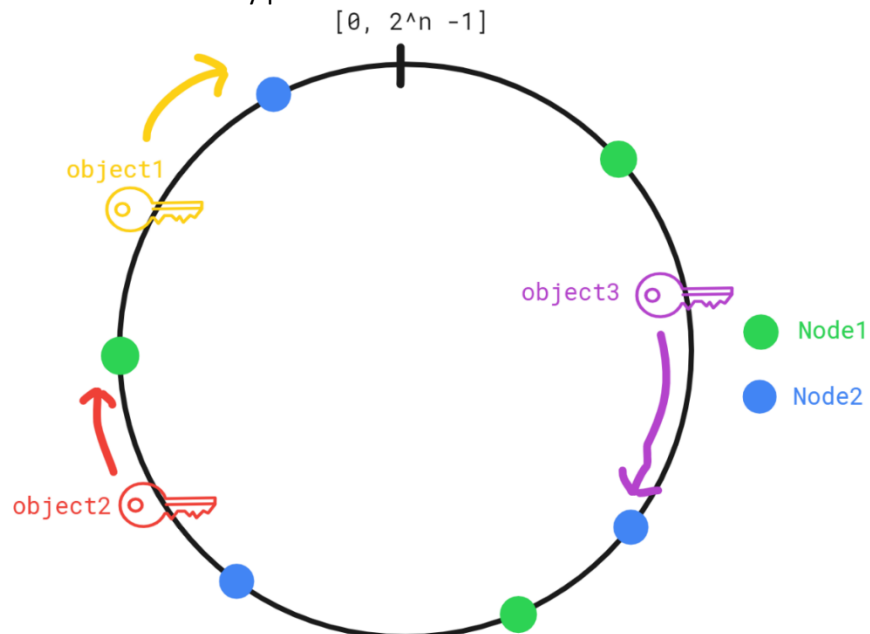


## Object hashing

Compute object's **index by key** in circle, and find **closest clockwise Node** to store.

$$\text{index} = \text{hash\_function}(\text{key})$$

When search Object, pointer search from key point to find closet clockwise Node.

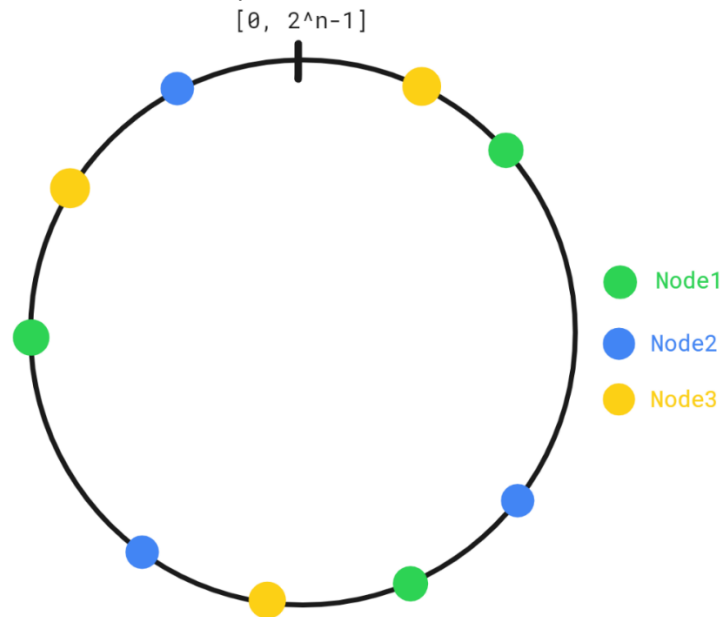


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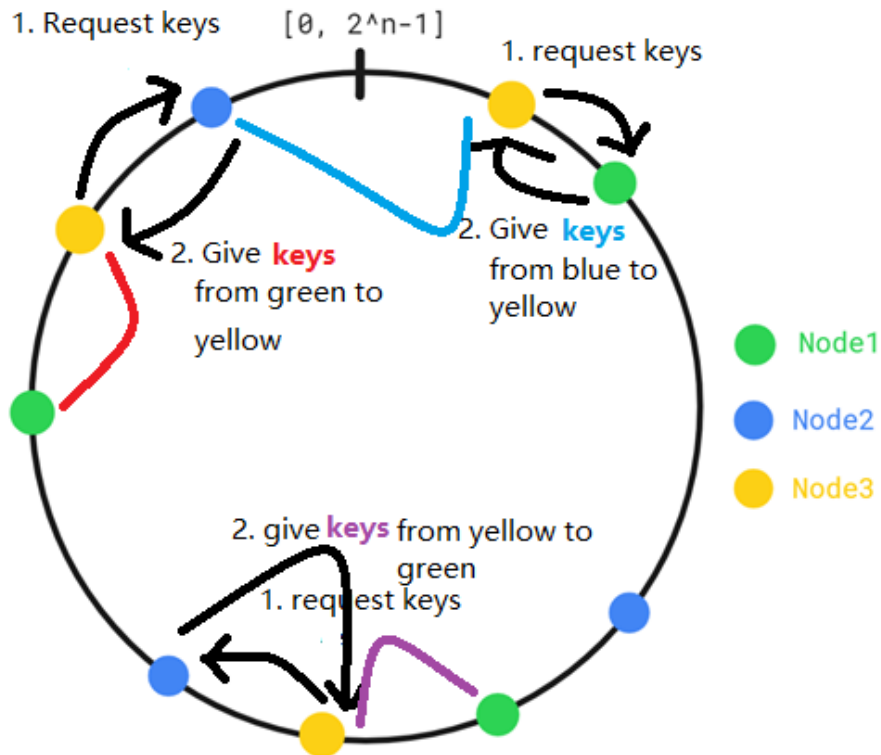
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## Add a Node

1. Assign multiple nodes to new server uniformly.



2. Each new Node require **next clockwise node** for the object keys from previous Node to new node.



Time complexity:

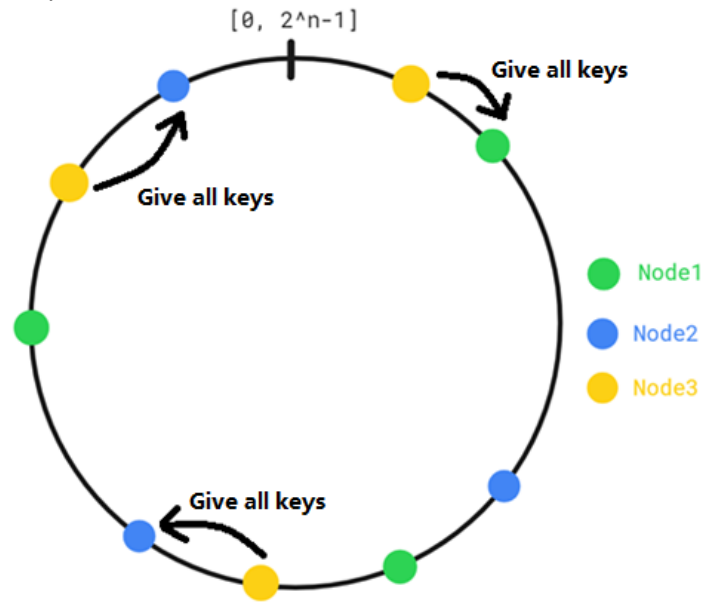
$$O\left(\frac{K}{N} + \log(N)\right), K \text{ is total } k \text{ numbers; } N \text{ is total Node numbers.}$$

**Note:**  $\log(N)$  for binary search for next Node.  $O(k/n)$  for moving keys.

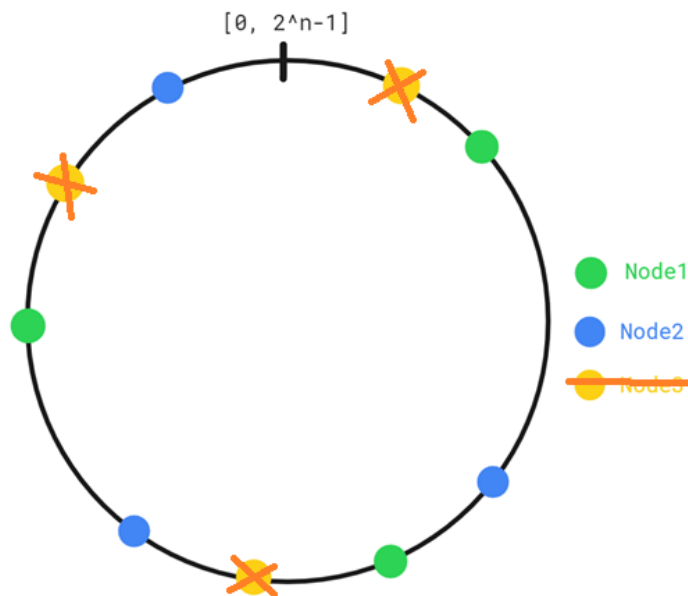
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## Remove a node

1. The removed node gives all keys to next clockwise node.



2. Remove the Node.



**Note:**  $\log(N)$  for binary search for next Node.  $O(k/n)$  for moving keys.

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## Complexity and advantage

### Advantage

1. No matter removes or add a Node, it ensures that keys are uniformly distributed.
2. When keys are in transferring, the traffic load is balanced in each server.

### Complexity

Asymptotic time complexities for N nodes (or slots) and K keys.

Note:  $\log(N)$  due to find closet Node via **binary search**.

Consistent hashing	
add a node	$O(K/N + \log(N))$
remove a node	$O(K/N + \log(N))$
add a key	$O(\log(N))$
remove a key	$O(\log(N))$