

1st Year PhD Report

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**Using  $Z \rightarrow \tau\tau$  events to calculate tau ID scale factors using high  $p_T$  tau leptons**

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Diego Baron

Supervisor: Prof. Terry Wyatt

Examiner: Dr. Marco Gersabeck

University of Manchester  
Faculty of Science and Engineering  
School of Physics and Astronomy  
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**Supervisor**

Prof. Terry Wyatt

**Examiner**

Dr. Marco Gersabeck

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# 1. Introduction

The tau lepton has a proper decay length of  $87 \mu\text{m}$  [30]. For this reason, tau leptons usually decay before they can reach the innermost layer of the ATLAS detector. Thus, only the decay products of the tau leptons can be observed. The tau lepton mass of  $1.777 \text{ GeV}$  make this particle the only lepton that can decay into hadrons [30]. Tau decays can be either leptonically ( $\tau \rightarrow \nu_\tau \nu_l l$ ,  $l = e, \mu$ ) or semi-hadronically ( $\tau \rightarrow \nu_\tau \text{hadrons}$ ), the latter ones are commonly referred simply as hadronic tau decays ( $\tau_h$ ). Muons and electrons from leptonic tau decays do not have enough kinematical features that can make them distinguishable from prompt muons or electrons. In the case of hadronic tau decays, which represent approximately a branching fraction of 65%, the decay modes include one or three charged pions. Therefore, the signature of this decays are jets with one or three tracks, with a charge correlation and being more collimated than jets initiated from quark or gluon radiation.

For this reason, algorithms trained to identify true  $\tau_h$  and separating them from misidentified  $\tau_h$  candidates, originating from QCD processes, have been developed [15]. The most novel of these algorithms is a recurrent neural network (RNN) that uses track and calorimeter information in order to classify true and fake  $\tau_h$  candidates. The RNN is now used as the default tau identification criteria for the data recorded by the ATLAS experiment from 2015 to 2018 and has been used also in tau lepton triggers of 2018.

When the efficiency of the RNN algorithm is measured in data and simulation, a correction factor is derived and then applied to the simulation in order for the signal efficiency to agree between data and simulation. In this report, we summarize the progress that has been done during the first year of the PhD student Diego Baron. The work that he has been doing is aimed to measure the correction factors for tau identification in the high- $p_T$  regime using  $Z \rightarrow \tau_h \tau_{\text{lep}}$  events.

The report is structured as follows. Chapter 2 is a short review of the Standard Model and the physics of the tau lepton. Chapter 3 describes the ATLAS experiment and the tau reconstruction and identification. In Chapter 4 the analysis methodology and the event selection is presented. Some preliminary results and a discussion is presented in Chapter 5. Finally, in Chapter 6 conclusions and prospects are discussed.



## 2. The Standard Model and Lepton Universality Tests

This chapter begins with a short description of the Standard Model (SM), followed by a discussion about the Z boson production at the Large Hadron collider. Finally, a review of the tau lepton properties is presented. These include the nature of this particle, its interactions with the other SM particles, its main decay modes and the physics implications of the so called Lepton Universality (LU), one of the SM predictions.

### 2.1. The Standard Model

The Standard Model (SM) is a theory about the fundamental constituents of matter and the interactions between them. Four fundamental interactions are known: gravitational, electromagnetic, weak and strong interactions. The SM is based on the framework of Quantum Field Theory (QFT), in which particles are classified as *bosons* or *fermions*, which corresponds to particles with integer and half-integer spin respectively. Fermions form matter and they can interact with each other via the exchange of bosons, which are the force carriers. Three fundamental forces are described by the SM. The strong interaction is explained by a theory called quantum chromodynamics (QCD) [19] which relies on the principle of gauge invariance under the  $SU(3)_c$  group. The force carriers of the QCD are called *gluons*. The electromagnetic and weak interactions are unified in the SM and this theory is known as the electroweak (EW) theory [20, 27, 31]. In this sector of the SM the fields are invariant under  $SU(2)_L \times U(1)_Y$  group. The force carriers of the weak and electromagnetic interactions are the  $Z^0, W^\pm$  bosons and the *photon* ( $\gamma$ ) respectively. The gravitational interaction is not described by the SM.

Fermions in the SM are classified into *quarks* and *leptons* where the latter do not feel the strong interaction. There are 6 quarks grouped into 3 generations with increasing masses. Thus, the heavier generations can decay into the lighter ones. There are also 6 leptons grouped in 3 generations. Each generation is heavier than the previous one. There are 3 charged leptons: the electron ( $e$ ), the muon ( $\mu$ ) and the tau ( $\tau$ ); and their associated neutral partners, the *neutrinos* ( $\nu$ ). In order to give mass to the SM particles the Higgs mechanism was proposed in the 60's [23, 17, 22]. The Higgs boson is the particle responsible for this and is the only spin-0 particle in the SM. Fig.1 shows the SM particle content.

# Standard Model of Elementary Particles

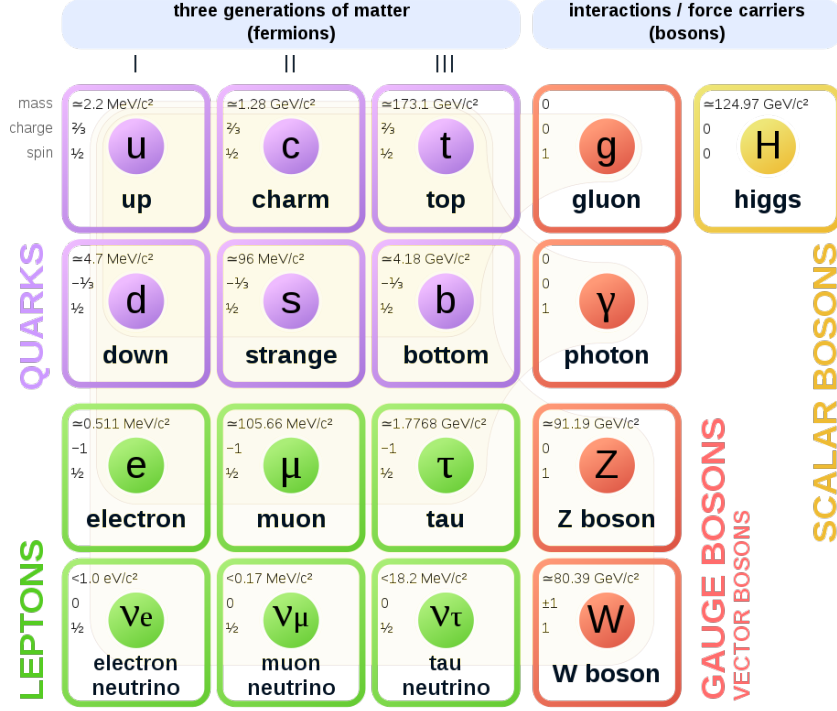


Figure 1.: The particle content of the Standard Model.

Decay mode	Branching fraction (%)
$e^+e^-$	$3.363 \pm 0.004$
$\mu^+\mu^-$	$3.366 \pm 0.007$
$\tau^+\tau^-$	$3.370 \pm 0.008$
Invisible	$20.00 \pm 0.06$
Hadrons	$69.91 \pm 0.06$

Table 1.: Z boson branching fractions.

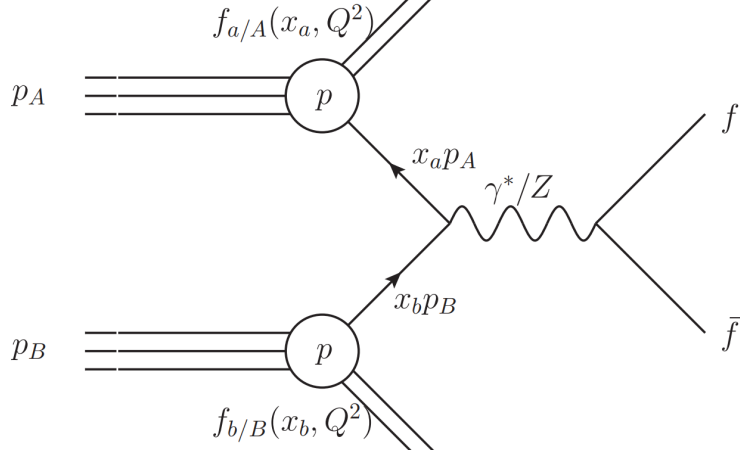
## 2.2. Z boson production at the LHC

Since the discovery of the Z boson at the UA1 and UA2 experiments [7, 8, 10, 9], it has been the subject of multiple measurements in proton-proton and electron-positron colliders. The Z boson mass  $m_Z = 91.1875 \pm 0.0021$  GeV and its decay width  $\Gamma_Z = 2.4952 \pm 0.0023$  GeV have been measured to outstanding precision [28]. The branching ratios of the Z boson are well known; they are presented in Table 1. In contrast to electron-positron colliders, the momentum of partons in proton-proton collisions is not precisely known. Thus, parton density functions (PDFs) are used to describe the proton structure in a phenomenological way. These functions are written as  $f_{a/A}(x, Q^2)$  and represent the probability density for a parton  $a$  to have a fraction  $x = \frac{p_a}{p_A}$  of the proton momentum  $p_A$ .  $Q$  is the energy scale of the scattering process. In this case, the cross

section of two protons going to a final state  $n$  will be

$$\sigma_{p_A p_B \rightarrow n} = \sum_q \int dz_a dx_b f_{a/A}(x_a, Q^2) f_{b/B}(x_b, Q^2) \times [\sigma_0 + \alpha_s \sigma_1 + \dots]_{ab \rightarrow n}. \quad (1)$$

The sum is made over all the partons.  $\sigma_0$  is the tree level parton-parton cross section and  $\sigma_1$  are the QCD corrections to first order. A diagram of the production of the Z boson in proton-proton collisions is shown in Fig.2. The main process contributing to Z boson production is the Drell-Yan



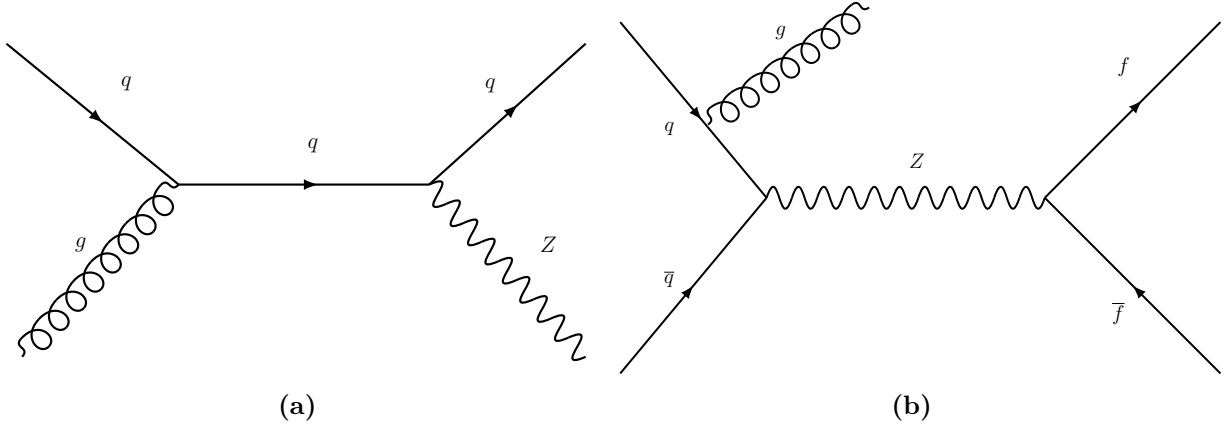
**Figure 2.:** Illustration of the production of a Z boson in pp collisions via quark-antiquark annihilation.

process, where a quark-antiquark ( $q\bar{q}$ ) pair annihilate, produce a Z boson and it subsequently decays into a pair of fermions. In this case, the transverse momentum ( $p_T$ ) of the Z boson comes from the intrinsic  $p_T$  of the partons. Nevertheless, this has been experimentally determined with a value of  $\langle k_T \rangle = 0.76$  GeV [16] and is not large enough to explain the measured Z boson  $p_T$  distribution that peaks at a few GeV and has a tail that extends at values  $p_T \gg m_Z$  [4, 5].

To explain this kinematic feature we have to look at the other ways the Z boson can be produced in  $pp$  collisions. First quark-gluon ( $qg$ ) scattering, where the Z boson recoils against the quark radiated in the final state, this process is illustrated in Fig.3a. In the other hand, we could also have a gluon being radiated before  $q\bar{q}$  annihilation takes place, having the Z boson recoiling against what is called *initial state radiation* (ISR), as is shown in Fig.3b. Partons generated in  $qg$  scattering and FSR pair with other quarks and gluons to form showers of *hadrons* (this showers are usually called jets) that are subsequently detected as energy deposits in the calorimeters of the particle detectors.

### 2.3. The Tau Lepton

The tau, is a spin- $\frac{1}{2}$  charged particle that belongs to the family of leptons. The first hints of the tau existence came from experiments conducted at the Stanford Linear Accelerator Center and



**Figure 3.:**  $q\bar{q}$  Z boson production with FSR (a) and  $q\bar{q}$  annihilation with gluon ISR (b).

Lawrence Berkeley National Laboratory [25]. They discovered 64 events of the form:

$$e^+ + e^- \rightarrow e^\pm + \mu^\mp + \geq 2 \text{ undetected particles}, \quad (2)$$

for which there was no conventional explanation at the time. Later on, it was discovered that these events came from the production of a pair of new particles, two taus that subsequently decayed into one electron, a muon and four neutrinos. Events like,

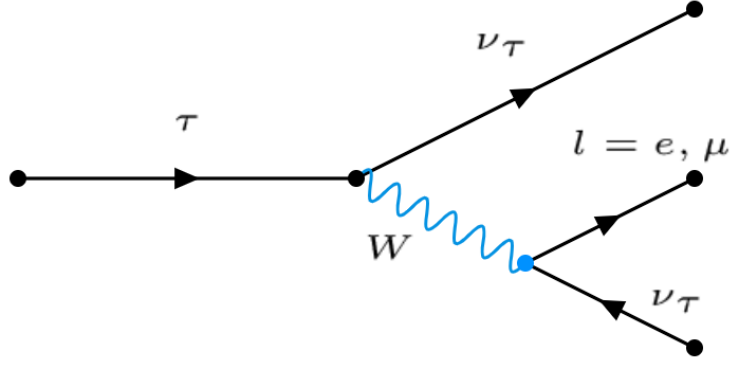
$$e^+ + e^- \rightarrow \tau^+ \tau^- \rightarrow e^\pm + \mu^\mp + 4\nu, \quad (3)$$

were later explored to derive tau mass and spin, confirming the existence of a third generation of leptons.

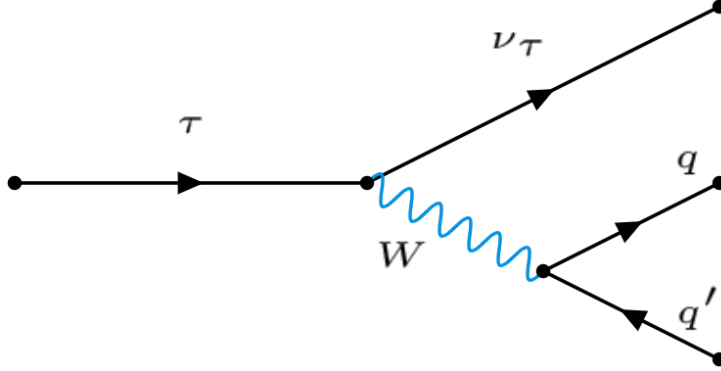
The tau has a mass of  $1776.86 \pm 0.12$  MeV [30], which allows it to decay not only into the other lighter lepton generations (*leptonic tau decays*), as shown on Fig.4 , but into hadrons. As we said on section 2.2 hadrons are particles made of quarks. All the decay channels of the tau containing hadrons in the final state are called *hadronic tau decays*. Strictly speaking this is a semi-hadronic decay mode because of the presence of the neutrino. Nonetheless, from now on we will refer to these processes with the commonly used term *hadronic tau decays*. An example of this decay mode is shown in Fig.5. Naively, if we were to estimate the branching fraction for hadronic and leptonic tau decay modes, defined as

$$\beta(\tau \rightarrow X\nu_\tau) = \frac{\Gamma(\tau \rightarrow X\nu_\tau)}{\Gamma_{\text{tot}}}. \quad (4)$$

Where  $X$  could be any number of leptons or hadrons and  $\Gamma_{\text{tot}}$  is the total decay width for the tau. We could argue that the contribution from the hadronic decays triples the contribution for one of the leptonic modes. This is because in any hadronic decay, we would have to count 3 different diagrams, like the one in Fig.5 because of the three colour possibility for the quarks.



**Figure 4.:** Tau leptonic decay mode. Tau lepton is kinematically allowed to decay into muons or electrons, note that in this decay mode two neutrinos of different flavour are produced.



**Figure 5.:** Tau hadronic decay mode. The tau lepton is kinematically allowed only to decay into hadrons containing up, down and strange quarks. This results on final states containing multiple pions or kaons [14].

Thus,

$$\beta(\tau \rightarrow l \nu_l \nu_\tau) \approx 20\% \quad l = e, \mu; \quad (5)$$

$$\beta(\tau \rightarrow X \nu_\tau) \approx 60\% \quad X = \text{hadrons} + \text{neutrinos}. \quad (6)$$

In fact, this naive estimation is not bad. Actual values for the leptonic branching ratios are [30]:

$$\beta(\tau \rightarrow e \nu_e \nu_\tau) = 17.82 \pm 0.04\% \quad (7)$$

$$\beta(\tau \rightarrow \mu \nu_\mu \nu_\tau) = 17.39 \pm 0.04\%. \quad (8)$$

The reason of the difference in the estimation is that in the case of the W decaying to quark pairs, there is a non-negligible contribution that comes of the mixing from quark pairs of different generations. In particular, in the tau decay we are talking about the contribution from up-strange quark couplings. This is the Cabibbo suppressed amplitude and it is proportional to the  $V_{us}$  component of the CKM matrix [13]. The small difference between the leptonic branching fractions is due to the mass difference between the muon and the electron.

On the other hand, the hadronic decays of the tau are more varied and can contain many more

Decay mode	Branching fraction
$\pi^\pm \nu_\tau$	11.1 %
$\pi^\pm \pi^0 \nu_\tau$	25.4%
$\pi^\pm \geq 2\pi^0 \nu_\tau$	9.1%
$3\pi^\pm \nu_\tau$	9.1%
$3\pi^\pm \geq 1\pi^0 \nu_\tau$	4.6%
others	5.5%

**Table 2.:** Branching fractions for hadronic tau decay modes [30].

particles in the final states. The vast majority of hadronic tau decays have charged or neutral pions in the final states, but more exotic decays including kaons also happen. Branching fractions for the most important tau hadronic decays are showed in Table 2.

## 2.4. Lepton Universality

The SM predicts that all charged leptons ( $e, \mu, \tau$ ) interact via the electromagnetic and weak forces and explains that these interactions can be seen as the interchange of *vector bosons*, the photon ( $\gamma$ ) and the W and Z bosons respectively. Specifically, in the SM the form of the interaction does not depend on the lepton generation. This feature of the SM is called *lepton universality* and it can be understood as that physical processes for electrons, muons and taus are almost identical copies of each other (although some small discrepancies arise from the fact that lepton masses).

For instance, tau leptonic decay widths present a great opportunity to test lepton universality hypothesis. If we start considering muon decay, at low energies we can consider this process to be a point like interaction well described by Fermi theory [18]. In this case, if we approximate the electron and neutrinos as being massless particles, a dimensionally correct expression for the width is of the form

$$\Gamma(\mu \rightarrow e + \nu_e + \nu_\mu) = K G_F^2 m_\mu^5, \quad (9)$$

where  $G_F = 1.1666 \times 10^{-5} \text{ GeV}^{-2}$  is the Fermi coupling constant and  $K$  is a constant that depends on the form of the interaction. If we assume that lepton universality holds, the respective widths for the tau leptonic decay modes, will have the form

$$\Gamma(\tau \rightarrow e + \nu_e + \nu_\tau) = K G_F^2 m_\tau^5, \quad (10)$$

$$\Gamma(\tau \rightarrow \mu + \nu_\mu + \nu_\tau) = \Gamma(\tau \rightarrow e + \nu_e + \nu_\tau), \quad (11)$$

which explains why to a good approximation leptonic branching fractions for tau decay are equal. Moreover, we can obtain a relation between tau and muon lifetimes. We know that,

$$\tau_l = \frac{1}{\Gamma_{\text{Tot}}} = \frac{\beta(l \rightarrow e \nu_e \nu_l)}{\Gamma(l \rightarrow e \nu_e \nu_l)}, \quad (12)$$

also that  $\beta(\mu \rightarrow e \nu_e \nu_\mu) = 1$  and taking into account eq.(7) we can take the ratio between eq.(12)



for  $l = \tau, \mu$  to obtain

$$\frac{\tau_\tau}{\tau_\mu} = \frac{\beta(\tau \rightarrow e \nu_e \nu_\tau)}{\beta(\mu \rightarrow e \nu_e \nu_\mu)} \left( \frac{m_\mu}{m_\tau} \right)^5 = (1.328 \pm 0.004) \times 10^{-7}. \quad (13)$$

This is consistent with the experimental lifetimes ratio of  $(1.3227 \pm 0.0005) \times 10^{-7}$  [24]. This agreement on lifetimes that differ on 7 orders of magnitude is a good proof that lepton universality holds on W decays at the tau mass scale.

Very precise tests of LU have been done by  $e^-e^+$  colliders (LEP1, SLC and LEP2). Measurements of the ratios between the leptonic decay widths of the Z boson have been performed and are consistent with the SM [28]:

$$\frac{\Gamma(Z \rightarrow \mu^+ \mu^-)}{\Gamma(Z \rightarrow e^+ e^-)} = 1.0009 \pm 0.0028, \quad (14)$$

$$\frac{\Gamma(Z \rightarrow \tau^+ \tau^-)}{\Gamma(Z \rightarrow e^+ e^-)} = 1.0019 \pm 0.0032. \quad (15)$$

LU has also been tested in W boson decays. A combination of measurements made by different experiments of the branching fractions between the first two families of leptons are consistent with SM predictions [26]:

$$\frac{\beta(W^- \rightarrow e^- \bar{\nu}_e)}{\beta(W^- \rightarrow \mu^- \bar{\nu}_\mu)} = 1.004 \pm 0.008. \quad (16)$$

But measurements including the third lepton family, apart from being less precise due to the more challenging reconstruction of the  $\tau$  lepton final states are in tension with SM [29]:

$$\frac{\Gamma(W^- \rightarrow \tau^- \bar{\nu}_\tau)}{\Gamma(W^- \rightarrow e^- \bar{\nu}_e)} = 1.063 \pm 0.027, \quad (17)$$

$$\frac{\Gamma(W^- \rightarrow \tau^- \bar{\nu}_\tau)}{\Gamma(W^- \rightarrow \mu^- \bar{\nu}_\mu)} = 1.070 \pm 0.026. \quad (18)$$

These results show that LU between the two first lepton family holds with a precision of 0.3% and 0.8% in Z and W decays respectively. Constraints between the third and the other two generations of leptons are of similar precision on Z boson decays (0.3%), but ten times worse for W boson decays (3%) and somewhat in tension with SM prediction. An example of this is a measurement exhibiting a tension of 2.6  $\sigma$  from the SM expectation [29]:

$$\frac{2\Gamma(W^- \rightarrow \tau^- \bar{\nu}_\tau)}{\Gamma(W^- \rightarrow e^- \bar{\nu}_e) + \Gamma(W^- \rightarrow \mu^- \bar{\nu}_\mu)} = 1.066 \pm 0.025. \quad (19)$$

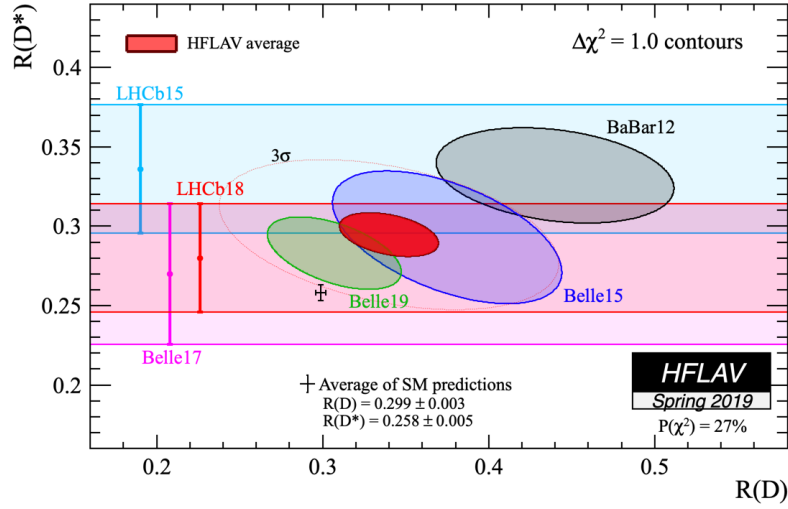
Furthermore, measurements from LHCb, BaBar and Belle experiments have shown consistent deviations from the SM predictions [12]. These experiments have independently measured a

deviation on  $\bar{B}$  meson semi-leptonic branching ratios, specifically:

$$R_D = \frac{\beta(\bar{B} \rightarrow D\tau^-\bar{\nu}_\tau)}{\beta(\bar{B} \rightarrow De^-\bar{\nu}_e)} \quad (20)$$

$$R_{D^*} = \frac{\beta(\bar{B} \rightarrow D^*\tau^-\bar{\nu}_\tau)}{\beta(\bar{B} \rightarrow D^*e^-\bar{\nu}_e)}. \quad (21)$$

The combined results for the different experiments are shown in Fig.6. These measurements represent a  $3.08\sigma$  deviation from the SM predictions, but even though they represent a hint of new physics, these results have to be taken with care since at this point it could be that statistical deviations are larger than expected. In this matters, future analysis from experiments like LHCb and Belle II with larger available datasets will be very important to untangle this situation.



**Figure 6.:** Combined results from BABAR, Belle and LHCb with  $1\text{-}\sigma$  contour. The average calculated by the Heavy Flavour Averaging Group [21] is compared with the SM predictions.

# 3. Tau Reconstruction and Identification in ATLAS

In this chapter, a review of the ATLAS detector at the Large Hadron Collider and a description of the reconstruction and identification of hadronic tau decays in ATLAS are presented.

## 3.1. The LHC and the ATLAS experiment

The Large Hadron Collider (LHC) is the largest particle accelerator currently operated by the European Organization for Nuclear Research (CERN). The LHC uses a 27 km tunnel where 2090, 15 m long, dipolar superconducting magnets bend the trajectories of two proton beams going in opposite directions. Each of the magnets is capable of producing a 8.33 T magnetic field and thus bending protons with an energy up to 7 TeV. The magnets are cooled down to 1.9 K in order to reach the superconducting state and the vacuum inside the beam pipes is of the order of  $10^{-9}$  mbar. During LHC Run II, proton beams were accelerated to an energy of 6.5 TeV and they were collided in 4 interaction points where the detector experiments are located.

One of these experiments is the ATLAS (A Toroidal LHC ApparatuS) detector. It is a multi-purpose particle detector, capable of discovering new physics but also to perform high precision SM measurements, a complete description of the ATLAS detector design can be found at [6]. ATLAS is a cylindrical detector composed by sub-detectors arranged in shells. The most inner layers are surrounded by a superconducting solenoid that generates a 2 T solenoidal magnetic field. ATLAS uses a right-handed coordinate system with its origin at the interaction point (IP) in the centre of the detector, the  $z$ -axis points along the beam pipe. The  $x$ -axis points towards the centre of the LHC ring and the  $y$ -axis in the vertical direction. The angle  $\phi$  is defined in the  $x - y$  plane and pseudorapidity is defined in terms of the polar angle  $\theta$  as  $\eta = -\log \tan(\theta/2)$ . The angular distance is measured in units of  $\Delta R \equiv \sqrt{(\Delta\phi)^2 + (\Delta\eta)^2}$ .

The most inner detector is responsible for track and vertex reconstruction and it consist of a silicon pixel, silicon microstrip and transition radiation tracking detectors. The system has a coverage of  $|\eta| < 2.5$ . The tracker system is followed by a lead/liquid-argon electromagnetic calorimeter (EC) and a steel/scintillator-tile hadron calorimeter (HC) that provide energy measurements with high granularity for electromagnetic showers and hadrons. The end-cap and forward EC and HC use LAr technology detectors and extend up to a  $|\eta| = 4.9$  region. The outermost detection system is a muon spectrometer that takes advantage of the bending power of a system of three air-core toroidal superconducting magnet systems.

## 3.2. Tau Reconstruction and Identification on the ATLAS detector

Leptonically decaying taus ( $\tau_{\text{lep}}$ ), may have a higher impact parameter and tend to have a softer  $p_T$  spectrum compared with prompt muons or electrons coming from W or Z boson decays. In principle, these variables are not sufficient to differentiate between  $\tau_{\text{lep}}$  and prompt muons or electrons. In the case of hadronically decaying taus ( $\tau_{\text{had}}$ ), as we will see, there are a lot more variables we could use to tag the presence of a  $\tau_h$ .

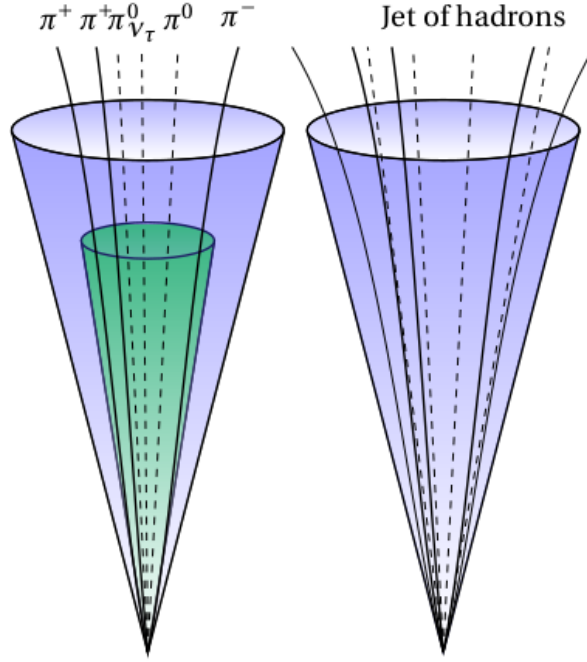
As we saw in section 2.3,  $\tau_h$  decays can be classified in 1-prong or 3-prong, depending on the number of charged particles in the decay. A detailed review of the reconstruction procedure for  $\tau_h$  is discussed on [2].  $\tau_h$  candidates are seeded by jets using the anti- $k_t$  algorithm [11] with a distance parameter of 0.4. Jets are required to have  $p_T > 10$  GeV and  $|\eta| < 2.5$ . Candidates between the barrel and forward calorimeter ( $1.37 < |\eta| < 1.52$ ) are excluded due to poor instrumentation in this region.

The axis of the seed jet is defined by the energy-weighted barycentre of all clusters of calorimeter cells, called *TopoClusters* [3]. The  $\tau_h$  vertex is defined as the vertex with the highest  $p_T$ -weighted fraction of all tracks with  $p_T > 0.5$  GeV within a cone of  $R = 0.2$  around the seed jet axis. Tracks within a cone of  $R = 0.4$  are classified with a set of boosted decision trees (BDTs) into core and isolation tracks, the number of core tracks defines the number of prongs. Candidates with neither one or three tracks are rejected. Additionally, the sum of the charge of the tracks is required to be  $\pm 1$ .

The tau reconstruction algorithm does not provide discrimination against jets that could mimic the signal of a  $\tau_h$  decay in the detector. Therefore, algorithms that perform this task have been developed. Previously, a BDT was used to discriminate jets against  $\tau_h$ . Recently, a recurrent neural network (RNN) classifier that provides improved performance compared with the BDTs is used [15].

The RNN makes use of a set of variables like:  $\tau_h$  track features, information about energy deposits on the calorimeters clusters and high level features like the mass of the  $\tau_h$  candidate tracks. These variables are used to exploit the differences in the shapes of the showers between  $\tau_h$  and jets. In general,  $\tau_h$  showers tend to be more collimated and to have fewer tracks than jets. A representation of this is shown in Fig.7.

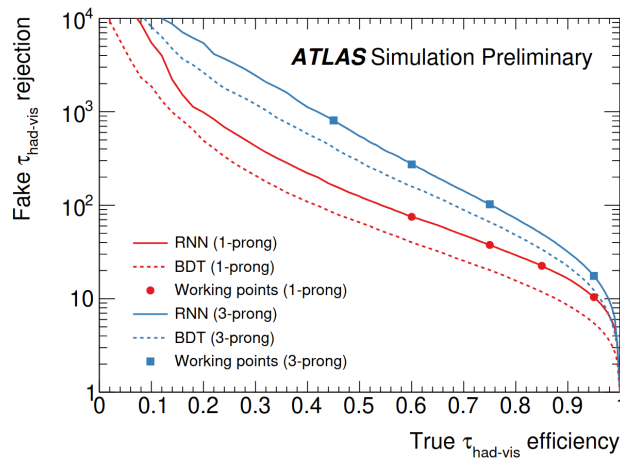
Separate algorithms are trained for 1-prong and 3-prongs. The final RNN score assigned to each event corresponds to the fraction of rejected true  $\tau_h$ , independent of  $p_T$  and number of interactions per bunch crossing (pileup). Four working points with increasing background rejection are defined to be used in physics analysis. The working points and background rejection factors are shown in Table 3. A plot comparing the true  $\tau_h$  selection efficiency versus the background rejection power for the RNN and BDT algorithm is shown in Fig.8, the performance of the RNN is better than the BDT classifier. Finally, the distribution for the RNN score for true and fake  $\tau_h$  is shown in Fig.9, for both 1-prong and 3-prong decays.



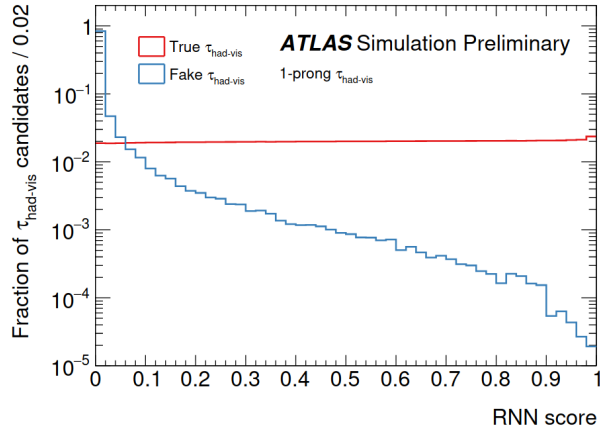
**Figure 7.:** Graphic representation that shows the main differences between a 3-prong  $\tau_h$  and a jet originated from quark or gluon radiation (QCD jets). Charged hadrons are shown as thick lines and dashed lines represent neutral particles. The green cone is drawn to depict how  $\tau_h$  product decays are more collimated.

Working point	Singal efficiency (%)		BG rejection BDT		BG rejection RNN	
	1-prong	3-prong	1-prong	3-prong	1-prong	3-prong
Tight	60	45	40	400	70	700
Medium	75	60	20	150	35	240
Loose	85	75	12	61	21	90
Very loose	95	95	5.3	11.2	9.9	16

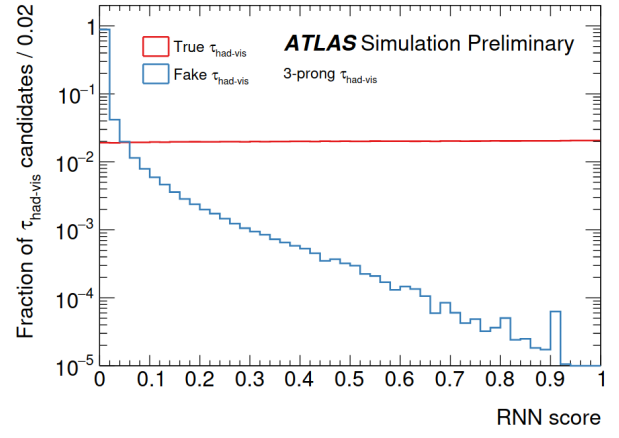
**Table 3.:** Working points with their corresponding true  $\tau_h$  selection efficiency and the background rejection factors [15]. The scores are shown for both RNN and BDT algorithms.



**Figure 8.:** Comparisson between the performance of BDT and RNN algorithms. Working points are shown as solid dots. Notice there is a trade off between true  $\tau_h$  efficiency and background rejection power. Taken from [15].



(a)



(b)

**Figure 9.:** Distribution of the RNN scores for true and fake  $\tau_h$  candidates for 1-prong (a) and 3-prong (b) cases. Taken from [15].

## 4. $Z \rightarrow \tau_h \tau_{lep}$ tag and probe study

This chapter describes the analysis methodology of using  $Z \rightarrow \tau\tau$  events to measure Monte Carlo correction factors for tau identification algorithms in the high- $p_T$  region.

As we saw in the previous section different working points are defined for RNN score relative to the efficiency of selecting true  $\tau_h$  candidates. When the efficiency of the working points is measured in data and simulation, a correction factor is derived and then applied to the simulation in order for the signal efficiency to agree between data and simulation [1]. Because of the top quark mass,  $t\bar{t}$  events are used as a source of high momentum taus for measuring correction factors on the high- $p_T$  bins. But as we already saw in section 2.4, Lepton universality may not hold in W decays. For that reason our study is aimed to use  $Z \rightarrow \tau\tau$  events for deriving and cross checking simulation correction factors in the high- $p_T$  region.

### 4.1. Signal events

The type of  $Z \rightarrow \tau\tau$  events we consider as signal for this study are when one the taus decays hadronically and the other leptonically, either into an electron or a muon ( $Z \rightarrow \tau\tau \rightarrow \tau_h + l = \mu, e$ ). Thus, our final states will include a  $\tau_h$  candidate and a lepton  $l = e, \mu$ . The presence of this lepton will be used as our tag. Generally, in  $Z \rightarrow \tau\tau$  events, the taus are produced back to back and their  $p_T$  spectrum does not go very high. One way to select events where the taus are boosted in the transverse plane is to look for events where the opening angle in the transverse plane between the taus ( $\Delta\phi(\tau_h, \tau_{lep})$ ) is more acute. For these events, the missing transverse momentum ( $\cancel{E}_T$ ) is assumed to come from the neutrinos produced in the decays of the tau leptons. Due to the fact that two neutrinos are produced in the leptonic decay mode we expect our events to have a larger  $\cancel{E}_T$  component along the  $\tau_{lep}$  direction.

We classify our events in two types of topologies. First, events where the  $\cancel{E}_T$  is inside the opening angle between the visible objects, in this kind of events we assume the missing energy is due to a pair of neutrinos flying in the same direction as the visible objects. This is shown in Fig.10a. In this case, we solve the following equation to obtain the momentum of the neutrinos:

$$\vec{p}_{T_{\nu_l}} + \vec{p}_{T_{\nu_h}} = \vec{\cancel{E}}_T, \quad (22)$$

given the following set of constraints (*collinear approximation*):

$$\phi(\nu_l) = \phi(l), \quad (23)$$

$$\phi(\nu_h) = \phi(\tau_h), \quad (24)$$

$$\eta(\nu_l) = \eta(l), \quad (25)$$

$$\eta(\nu_h) = \eta(\tau_h). \quad (26)$$

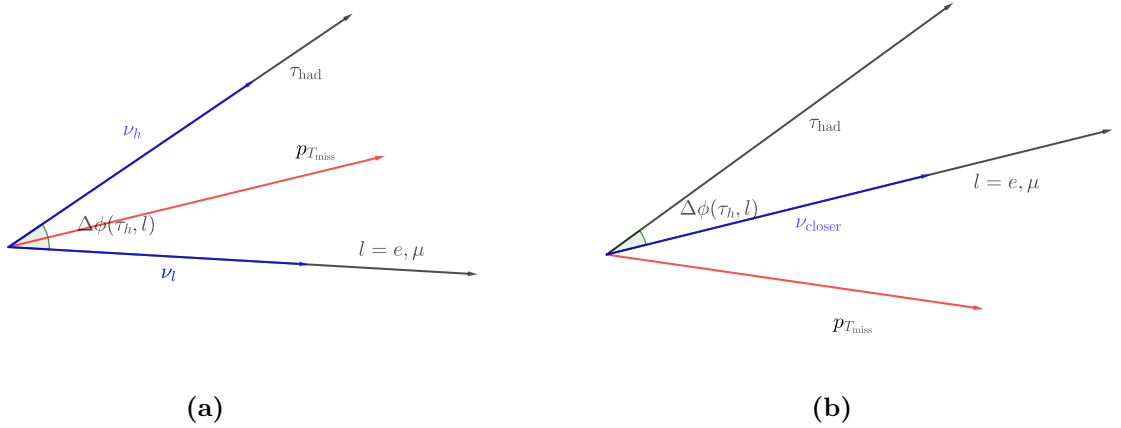
The second case is when the  $\cancel{E}_T$  is outside the angle formed by the visible objects, as is shown in Fig.10b. In this case the assumption is that only one neutrino is responsible for the majority of the  $\cancel{E}_T$ , a neutrino flying in the direction of the visible object that is closest to the  $\cancel{E}_T$ . We use the following equations to obtain the neutrino momentum:

$$p_{T\nu} = \cancel{E}_T \cos(\Delta\phi(\tau_{\text{closer}}, \cancel{E}_T)), \quad (27)$$

$$\phi(\nu) = \phi(\tau_{\text{closer}}), \quad (28)$$

$$\eta(\nu) = \eta(\tau_{\text{closer}}), \quad (29)$$

where  $\tau_{\text{closer}}$  stands for the visible object closest to the direction of the missing energy.



**Figure 10.:** The two different types of topologies that define signal events. On the right, when the missing energy is between the visible objects two neutrinos are assumed to be responsible for all the missing energy. On the left, only one neutrino is assumed to be flying on the direction of the visible object closest to the missing energy.

We define a variable called  $\Omega$  in order to classify our events in the different topologies already described. First we define:

$$\omega = \frac{\Delta\phi(\tau_{\text{close}}, \cancel{E}_T)}{\Delta\phi(\tau_h, \tau_{\text{lep}})}, \quad (30)$$

then,

- when  $\cancel{E}_T$  is inside the opening angle between the visible objects but closer to  $\tau_h$ :

$$\Omega = \omega, \quad (31)$$



- when  $\cancel{E}_T$  is still inside, but closer to  $\tau_{\text{lep}}$ :

$$\Omega = 1 - \omega. \quad (32)$$

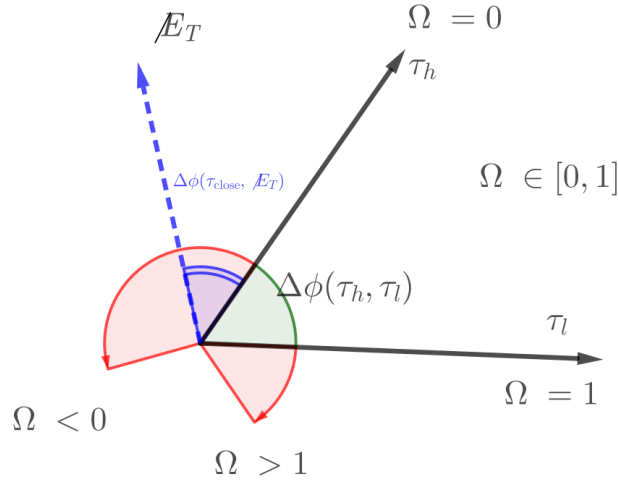
- If  $\cancel{E}_T$  is outside and closer to  $\tau_h$ :

$$\Omega = -\omega, \quad (33)$$

- and finally, if  $\cancel{E}_T$  is outside and closer to  $\tau_{\text{lep}}$ :

$$\Omega = \omega + 1. \quad (34)$$

Thus,  $\Omega$  is a continuous variable that give us information on the topology of the event. When  $\cancel{E}_T$  is inside the visible system it has values in the interval  $[0,1]$ . Exactly 0 when  $\cancel{E}_T$  is in the  $\tau_h$  direction and 1 when is on the  $\tau_{\text{lep}}$  direction.  $\Omega$  has negative values when  $\cancel{E}_T$  is outside and closer to the  $\tau_h$  candidate and has positive and values greater than 1 when is outside and closer to the  $\tau_{\text{lep}}$ . A diagram describing the  $\Omega$  values is shown in Fig.11. As we will see later the event



**Figure 11.:** Graphical representation of the different values of  $\Omega$  depending on the region where the  $\cancel{E}_T$  is located in the event.

classification into this two different type of topologies will allow us to reconstruct and exploit kinematical variables as the invariant mass of the di-tau system, the Z boson transverse momentum ( $Z_{p_T}$ ) and the angular distribution of the objects in the event.

## 4.2. Monte Carlo and Data Samples

The data used for this study has been recorded during the Run-II of the LHC. It corresponds to the 2015-2018 data taking period, the total integrated luminosity corresponds to  $139.2 \text{ fb}^{-1}$  of proton-proton collisions at a centre-of-mass energy of  $\sqrt{s} = 13 \text{ TeV}$ .

Process	Event Generator
$Z \rightarrow \tau\tau$	Powheg+Pythia8 and Sherpa
$Z \rightarrow ee$	Powheg+Pythia8
$Z \rightarrow \mu\mu$	Powheg+Pythia8
$W \rightarrow l\nu_l$	Powheg+Pythia8
$t\bar{t}$	Powheg+Pythia8
Single $t$	Powheg+Pythia8
Diboson	Powheg+Pythia8

**Table 4.:** List of MC event generators used.

Monte Carlo (MC) samples are used for signal and background simulation. For  $Z \rightarrow \tau\tau$  events two MC samples are used, Powheg+Pythia8 and Sherpa. For the rest of the samples Powheg+Pythia8 is used. Table 4 shows the MC generators used for each process.

### 4.3. Event Selection

In order to select  $Z \rightarrow \tau_h \tau_{lep}$  events, our basic selection includes events with exactly one  $\tau_h$  candidate and one lepton, a muon or an electron. The  $\tau_h$  and lepton pair need to have opposite charge. As we said, the presence of the lepton will be used as our tag, thus, a lepton trigger is required to be fired with an online requirement on the  $p_T(\mu) \geq 20$  ( $p_T(e) \geq 24$ ) GeV for 2015 data taking period. For 2016-2018 the requirement is  $p_T(\mu, e) \geq 26$  GeV. The muons are required to pass a *medium* ID requirement and the electron has to pass a *tight* ID filter. Additionally, both muons and electrons have to pass an offline  $p_T$  requirement to be greater than 27 GeV. Finally, the opening angle between the two visible objects  $\Delta\phi(\tau_h, l) \leq 2\pi/3$ .

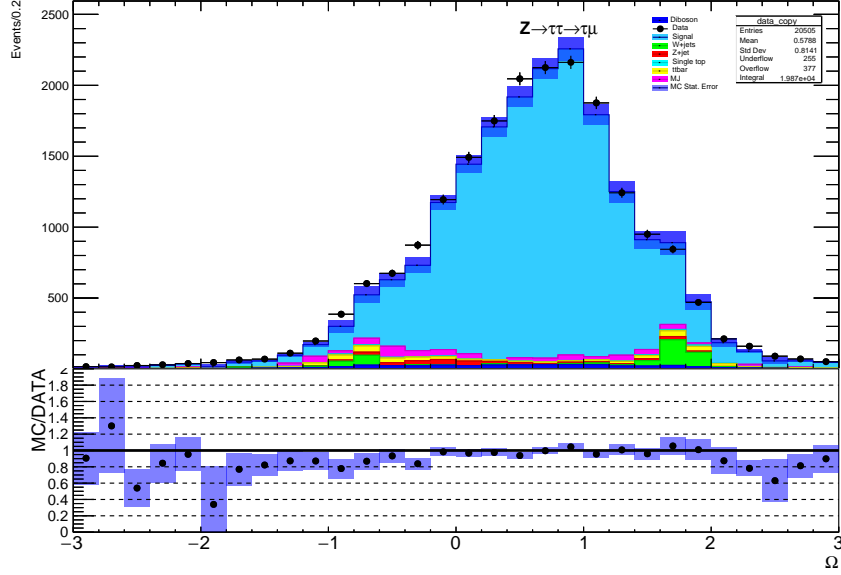
Events containing b-jets are vetoed in order to reject  $t\bar{t}$  events. Also an isolation criterion is required to be passed by the leptons: for the muon (electron), the scalar sum of the  $p_T$  of the tracks within a cone of  $\Delta R = 0.3(0.2)$  of the muon (electron) must be less than 0.06 times the muon (electron)  $p_T$ . Additionally, for the electron, the sum of the calorimeter cluster energy in a cone of size  $\Delta R = 0.2$  must be 0.06 times the electron  $p_T$ . As we said in section 4.1, we expect signal events to peak around  $\Omega = 1$ , thus we select events where  $\Omega \in (0, 1.4)$ . Fig.12 shows the  $\Omega$  distribution for  $Z \rightarrow \tau_h \mu$  final state. Additionally, a cut on the reconstructed invariant mass ( $m_{reco}$ ) of the event is made, the cut aims to pick events where the invariant mass is around the Z boson mass ( $70 \leq m_{reco} \leq 110$  GeV). The invariant mass of the final states is calculated depending on the event topology. For events where  $\Omega \in [0, 1]$  (*in between events*),

$$m_{reco}^2 = (q_l + q_{\tau_h} + q_{\nu_l} + q_{\nu_{\tau_h}})^2. \quad (35)$$

When the  $\cancel{E}_T$  is outside (*outside events*),

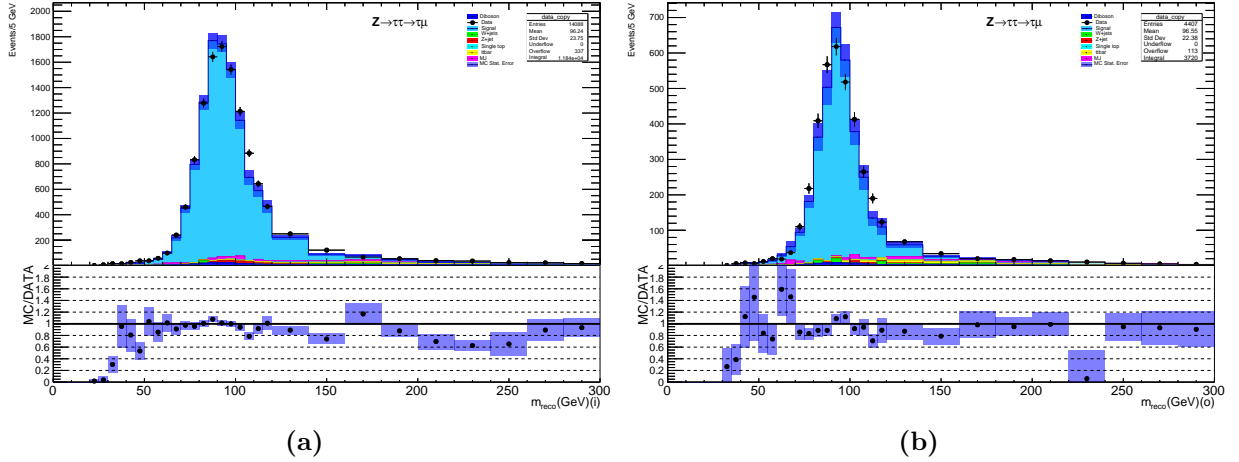
$$(m_{reco} - 5)^2 = (q_l + q_{\tau_h} + q_{\nu})^2. \quad (36)$$

The RHS of Eq. (35) and Eq. (39) are vector sums, where  $q$  represents the four-momentum of each



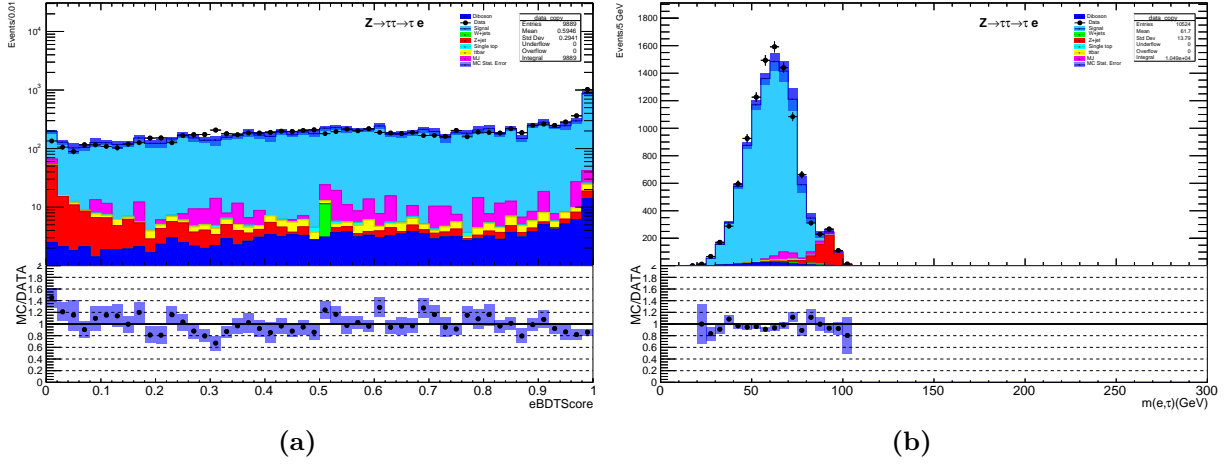
**Figure 12.:** Distribution of  $\Omega$  for  $Z \rightarrow \tau_h \mu$  final state. All the other cuts have been applied apart from the one being plotted.

particle. In the latter case we manually add 5 GeV to maintain our cuts consistent, since in this region the  $Z$  mass is underestimated. Fig.13 shows the distribution of  $m_{\text{reco}}$  for the in between and outside  $Z \rightarrow \tau_h \mu$  events.

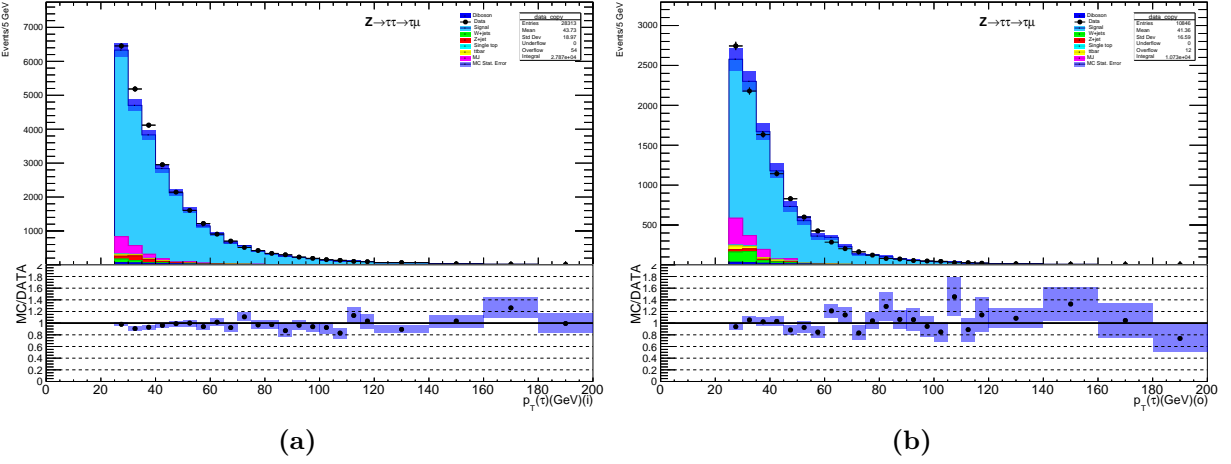


**Figure 13.:**  $m_{\text{reco}}$  distribution for the in between region (a) and the outside region (b). All the other cuts have been applied apart from the one being plotted.

In addition, for the  $Z \rightarrow \tau_h e$  final state, we add two cuts aimed to reject events where the  $\tau_h$  candidate is faked by an electron. First to reject  $Z \rightarrow ee$  events, a requirement on the invariant mass of the electron and  $\tau_h$  candidate is made,  $m(e, \tau_h) < 80$  GeV. Then, we also make use of an ID algorithm trained to discriminate electrons from real  $\tau_h$ . In our case,  $\text{eBDTScore} \geq 0.06$ . The distributions for this variables are shown in Fig.14. Finally, in order to measure the tau ID scale factors on the high- $p_T$  region we select events where  $p_T(\tau_h) \geq 45$  GeV. The  $p_T$  distributions for  $\tau_h$  candidates are shown in Fig.15 for the in between and outside regions.



**Figure 14.:** Distribution of the variables used for rejecting  $\tau_h$  fakes coming from electrons. On the right  $m(e, \tau_h)$  distribution (a) and on the left the eBDTScore distribution (b). All the other cuts have been applied apart from the one being plotted.



**Figure 15.:**  $p_T(\tau_h)$  distribution for the in between (a) and outside (b) regions. All the other cuts have been applied apart from the one being plotted.

#### 4.4. Multi Jet Background Estimation

As we said previously,  $\tau_h$  candidates are seeded by jets, thus, QCD events represent a source of background. Nonetheless, we do not have MC simulations for this processes as compared with the EW interactions shown in Table 4. For this reason, we use a *data driven method* to estimate multi jet (MJ) background. For that purpose, we choose a variable that in principle we suppose is uncorrelated with the shape of the MJ background. For our study, this variable is the relative sign between the charges of the  $\tau_h$  and the lepton. Thus, this defines two regions: the same sign (SS) region where  $q(\tau_h) = q(l)$  and the opposite sign region where  $q(\tau_h) = -q(l)$ . Our estimate of MJ background for the SS region is obtained subtracting signal and electroweak backgrounds (EWBG) simulated contributions, basically:

$$\text{MJBG}_{\text{SS}} = \text{Dat}_{\text{SS}} - \text{Signal}_{\text{SS}} - \text{EWBG}_{\text{SS}}, \quad (37)$$

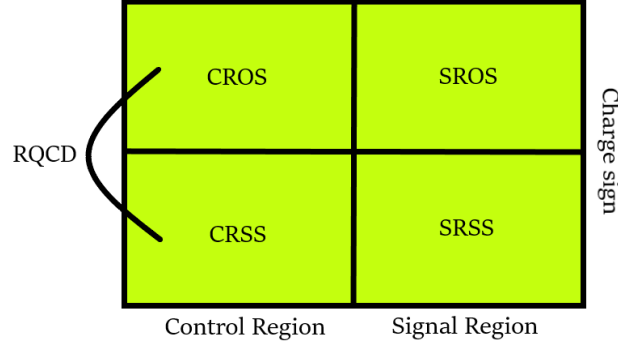
To study the residual charge correlation, we define a control region (CR) where the MJ background is enhanced. This region is defined by events that fail either the lepton isolation criteria or the  $\tau_h$  ID requirement of  $\text{tauRNNScore} > 0.4$  (0.55) for 1-prong (3-prong)  $\tau_h$  candidates and have the same other kinematic features of the signal region (SR) described in section 4.3. A diagram showing the four regions just defined is shown in Fig.16. Now, if charge correlation is the same in SR and CR, we have:

$$\frac{\text{MJBG}_{\text{SROS}}}{\text{MJBG}_{\text{SRSS}}} = \frac{\text{MJBG}_{\text{CROS}}}{\text{MJBG}_{\text{CRSS}}}, \quad (38)$$

then,

$$\text{MJBG}_{\text{SROS}} = \text{MJBG}_{\text{SRSS}} \times \text{RQCD} \quad (39)$$

where  $\text{RQCD} \equiv \frac{\text{MJBG}_{\text{CROS}}}{\text{MJBG}_{\text{CRSS}}}$ . So, Eq. (39) gives the estimation of MJ background on the signal region (SROS).



**Figure 16.:** Diagram showing the regions defined to estimate MJ background contribution in the SROS region. This data-driven method is also known as ABCD method.



## 5. Results

In this section we present the preliminary results of the performance of the  $\tau_h$  identification algorithm using  $\int \mathcal{L} dt = 139.2 \text{ fb}^{-1}$  of data recorded between 2015 and 2018. The correction factors are applied to simulation in order to match the efficiency observed in data. These correction factors are defined as the ratio between the efficiency measured in data and in simulation. For the present report, we present the value of the correction factors for *Tight* ID working point for  $\tau_h$  candidates with  $p_T$  above 45 GeV.

### 5.1. $\mu\tau$ Final state

We define the simulation correction factor as

$$C_{\text{Tight-ID}} = \frac{\mathcal{E}_{\text{Data}}}{\mathcal{E}_{\text{MC}}}. \quad (40)$$

The value obtained for the final state that contains one muon and a  $\tau_h$  candidate is

All the distributions of the relevant cuts for selecting our signal events after applying all the other cuts are shown in Appendix A.

### 5.2. $e\tau$ Final state

The value obtained for  $C_{\text{Tight-ID}}$  in the final state that contains one electron and a  $\tau_h$  candidate is

All the distributions of the relevant cuts for selecting our signal events after applying all the other cuts are shown in Appendix A.

### 5.3. Discussion





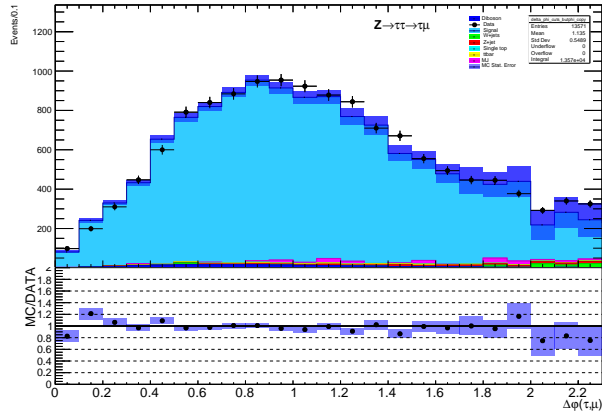
## 6. Conclusions and prospects



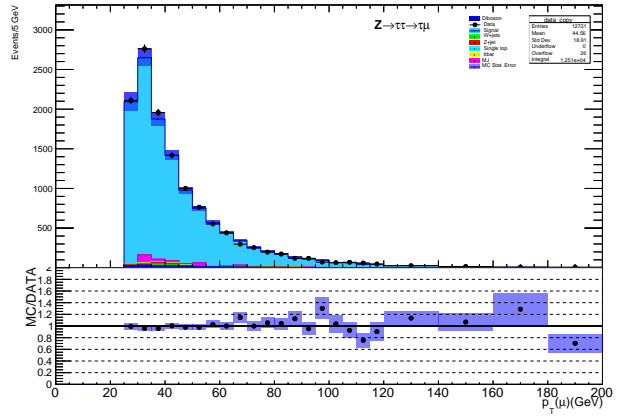
## A. Appendices

### A.1. $Z \rightarrow \tau_h \mu$ final state distributions

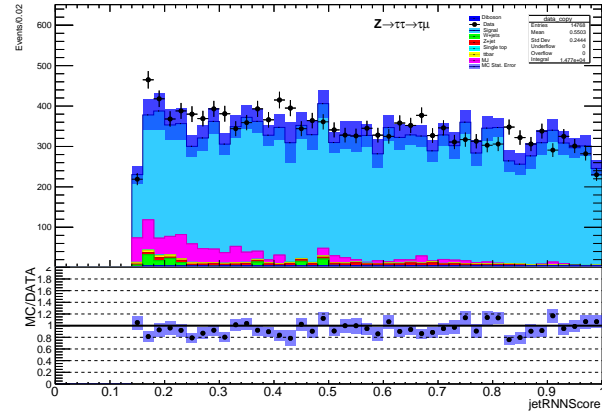
## A.2. $Z \rightarrow \tau_h e$ final state distributions



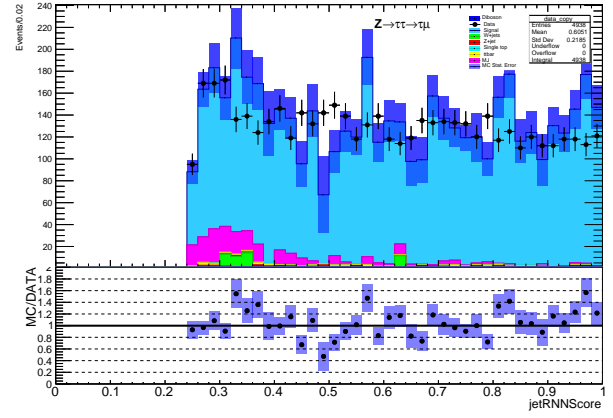
(a)



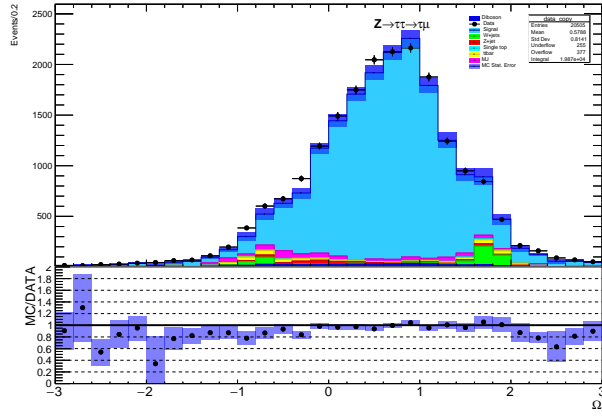
(b)



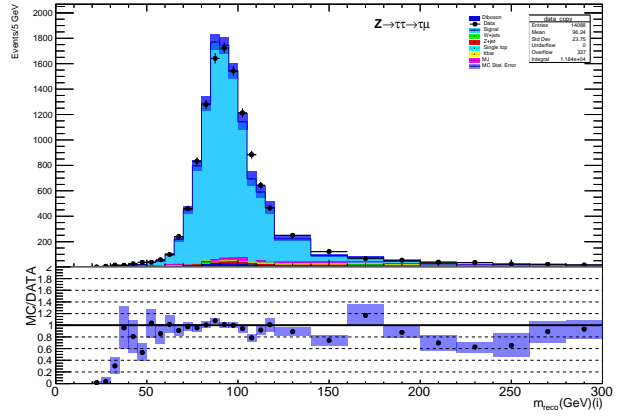
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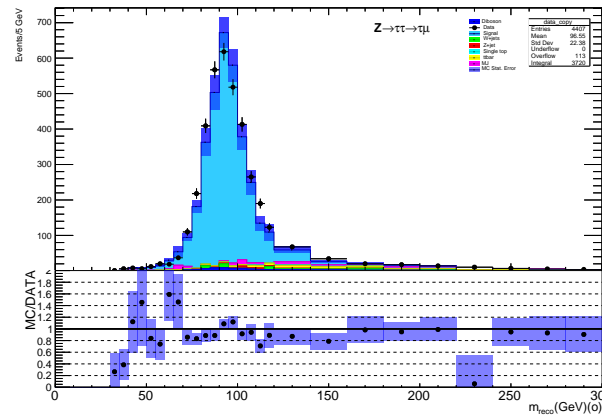
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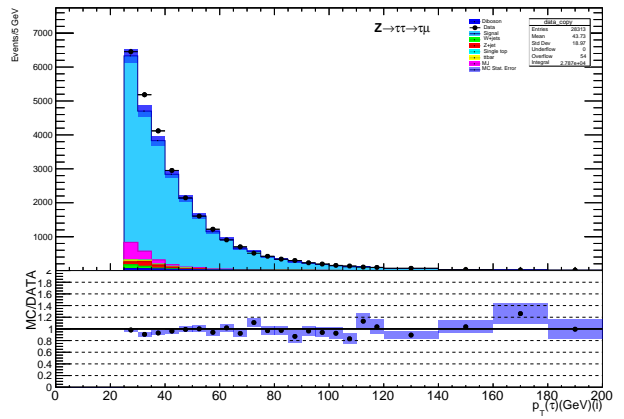
(e)



(f)



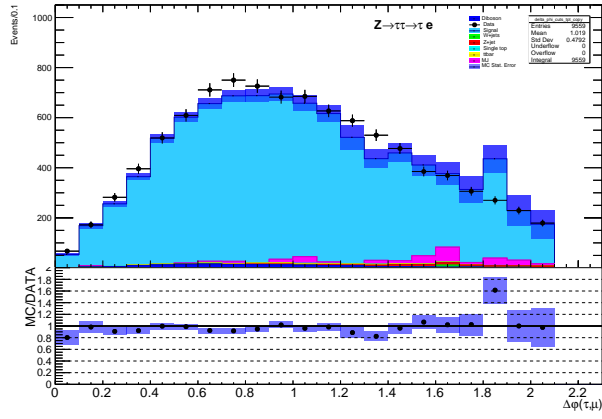
(g)



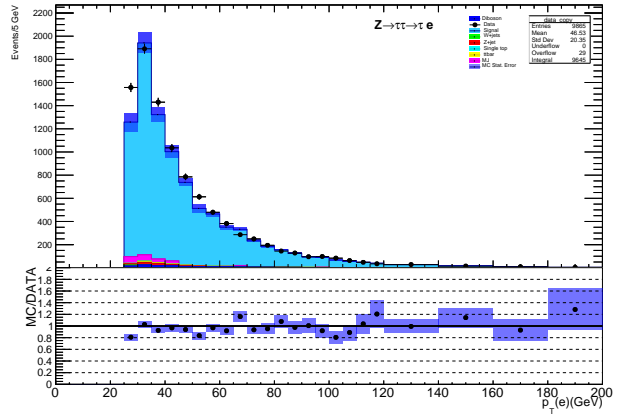
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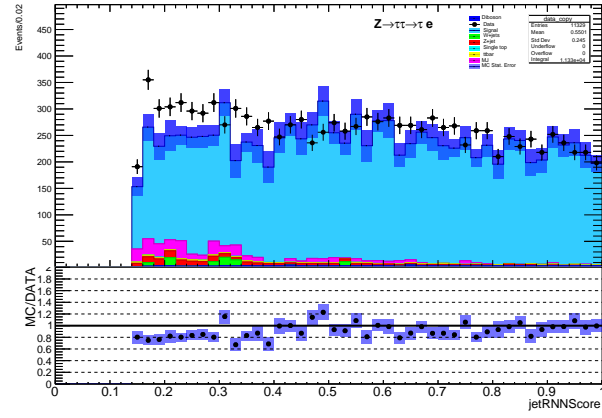
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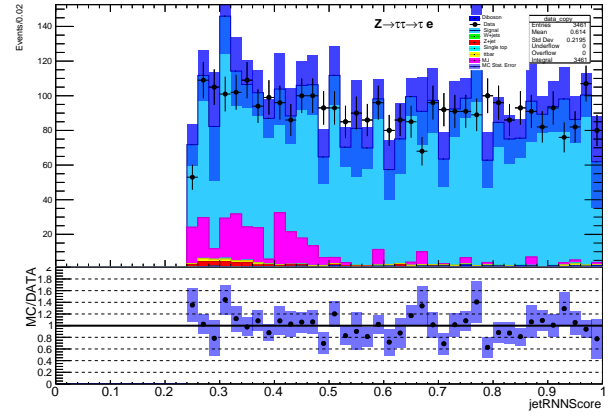
(a)



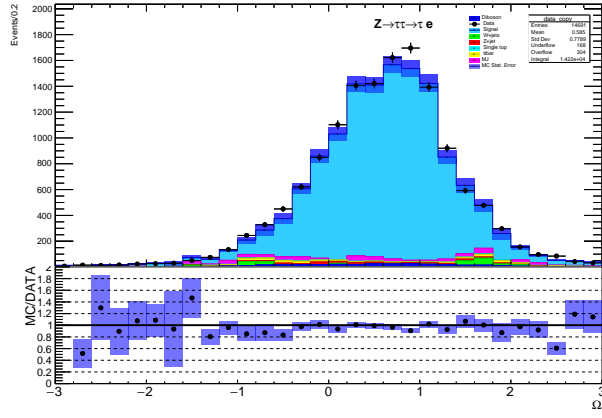
(b)



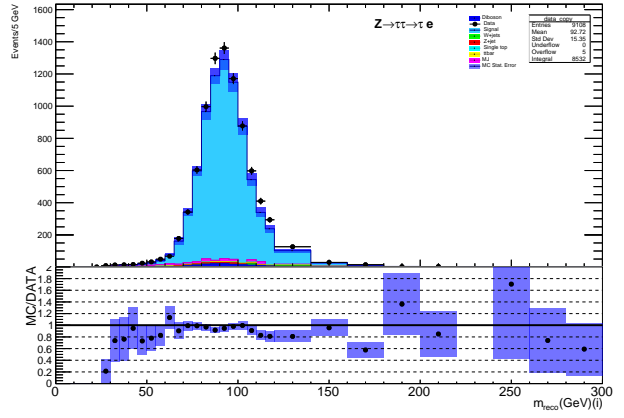
(c)



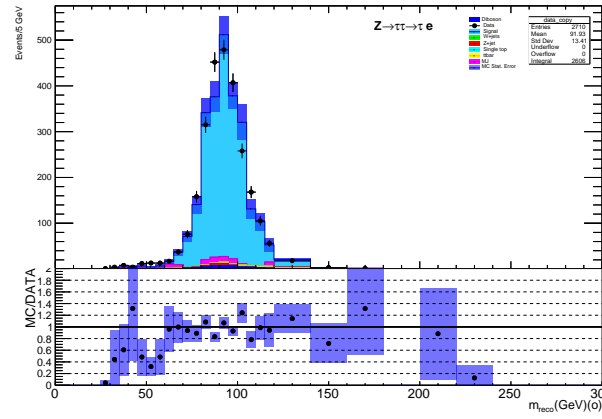
(d)



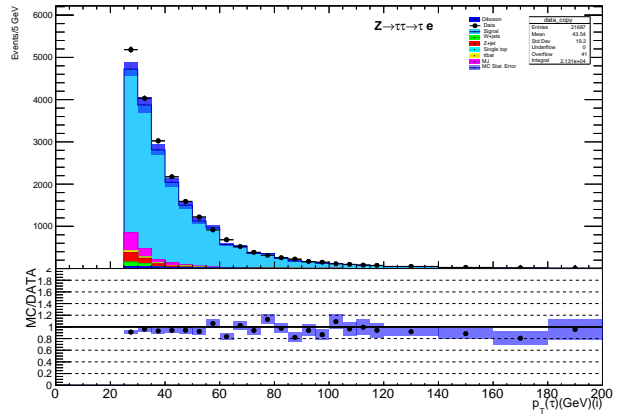
(e)



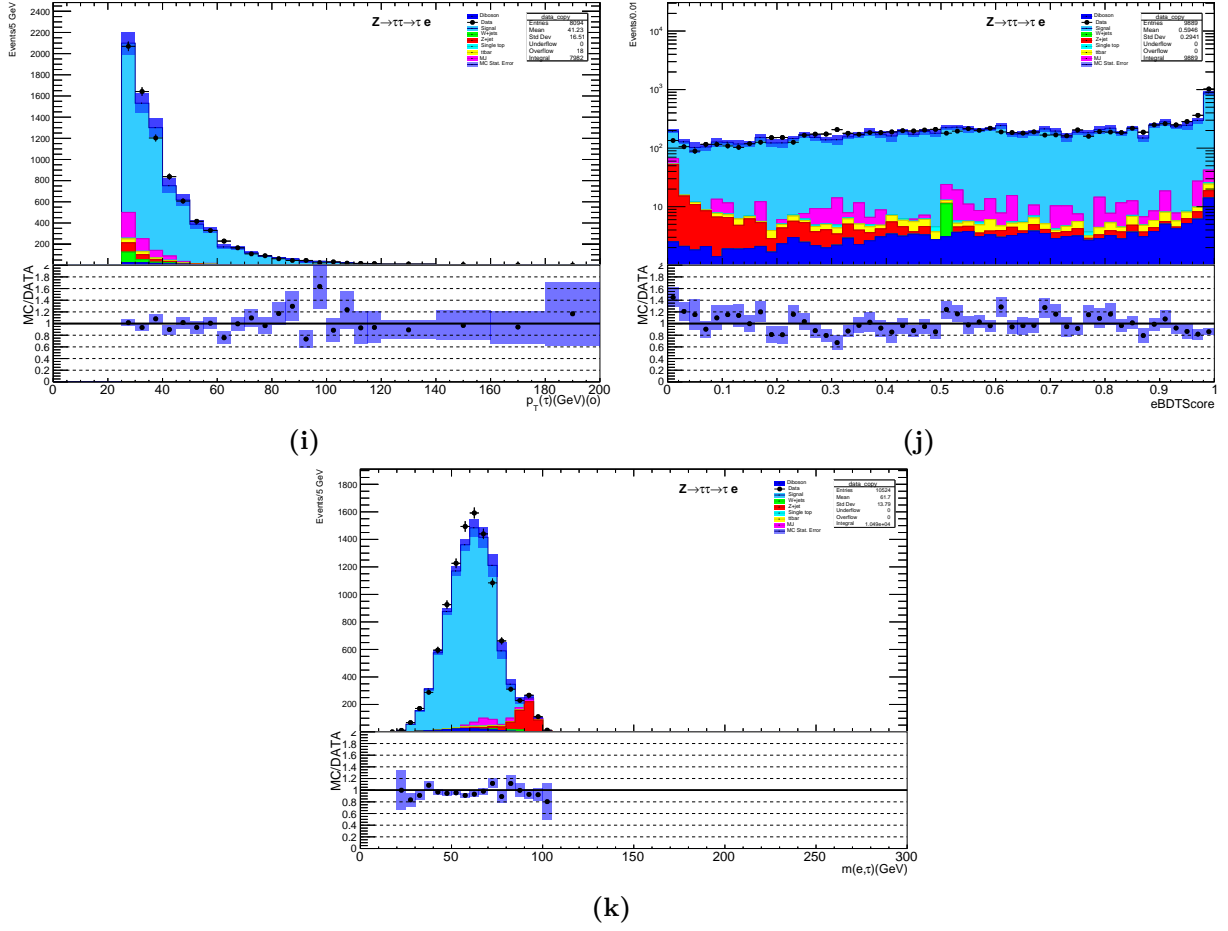
(f)



(g)



(h)



**Figure 18.:**  $m_{\text{reco}}$  distribution for the in between region (a) and the outside region (b). All the other cuts have been applied apart from the one being plotted.



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