

Assignment__1

21 September, 2019

Gasoline exercise

The unit of observation of the data is year-state. When I refer to gas prices or gas taxes, I measure them in real dollars per gallon with base 1987. When I talk about gas quantities, I am measuring them in gallons per capita in a given year-state.

a) Estimate the elasticity of supply of gasoline. Provide a confidence interval. Can you reject the hypothesis that the supply of gasoline is elastic?

In this part, our aim is to estimate $\epsilon_S = \frac{\partial Q_{jt}}{\partial P_{jt}^S} \frac{P_{jt}^S}{Q_{jt}}$. Where Q is the highway gasoline consumption per capita, P^S is the real price of gasoline excluding taxes, and j, t index state and year respectively. If we assume that the elasticity of supply is constant over time and across states, we are basically assuming that:

$$Q_{jt}^S(P_{jt}^S) = A_{jt} P_{jt}^{S\beta}$$

Where β is the elasticity of supply, and for some constant A_{jt} that we allow to change flexible by year, state (and also depending on covariates). Note that:

$$P^S = P^D - t$$

Namely that the producer price is the price paid by the consumers minus the total taxes (federal and state). With the data provided we can run a model like:

$$\ln(Q_{jt}^S) = \alpha + \beta \ln(P_{jt}^S) + X'_{jt}\gamma + \eta_j + \eta_t + \psi_{jt}^S$$

Where X'_{jt} is a vector of supply related controls, and where η_j and η_t are state and year fixed effects respectively. In this model β is a direct estimate of the price elasticity of supply. However, in order to estimate β consistently, we cannot rely on OLS using data from a perfectly competitive market. This is because, price and quantity are determined together through equating supply and demand (as we assumed a perfectly competitive market), and therefore the real price of gasoline excluding taxes P_{jt}^S is necessarily a function of the supply shocks ψ_{jt} . We can use two stage least squares but we need either a demand shifter that does not affect supplied quantity other than through the price change induced from the new demand curve, or exogenous variation (random or quasi-random changes) in some variable that is correlated with P_{jt}^S and that only causes changes on the quantities supplied through the change in P_{jt}^S that induces.

I choose to use as an instrument the logarithm of the total real gas tax (namely, the sum of the real gas charged by the state and federal government). I include as controls the logarithm of the real income per-capita, and the urbanization rate. In this case, I think that it is important to control for income because if for some units, income per-capita and gas prices are highly correlated (for example because a given state derives most of its income from the gas sector during the years on the data) we might think that a government trying to smooth private consumption will find it optimal to have a countercyclical tax policy in which taxes are raised when income (and gas prices) are high and in which taxes are lowered when they are low. In a case like this, controlling for income generates that the identifying variation for β comes from tax changes that occur within high income times and within low income times, which are unequivocally “more” random than those tax changes that occur irrespectively of the income level. Controlling for income would also be crucial in a case where the government changes taxes procyclically with income, or in any other case in which we

suspect that tax changes are responding to income changes. On the other hand, controlling for urbanization seems to be important for explaining quantity so including it as a control will increase precision.

Also, given that the data has a panel structure, for a given state the gas prices including taxes for two consecutive years are extremely correlated. Therefore, in order to identify β we can first difference the model above to get:

$$\ln(Q_{jt}^S) - \ln(Q_{jt-1}^S) = \beta(\ln(P_{jt}^S) - \ln(P_{jt-1}^S)) + (X'_{jt} - X'_{jt-1})\gamma + (\eta_t - \eta_{t-1}) + (\psi_{jt}^S - \psi_{jt-1}^S)$$

Where we can note that the constant and the state-fixed effects are not identified anymore, but we can still recover the β from the original model. This first-differenced model is the one that I will present results for.

Below, I first present the first stage regression output (omitting coefficients for the fixed effects).

```
##                      beta_fs  se_beta_fs  t_stat_fs
## instr                -0.10755768  0.020437629 -5.2627278
## fd_ln_realinc_percapita -0.01699463  0.049020633 -0.3466833
## fd_urbanization        -0.26978198  0.489659895 -0.5509579
## year_supply_1970       -0.03958184  0.005322857 -7.4362012
## [1] "F-stat of instruments in first stage is: 27.6963035833962"
```

The instrument is quite strong, as implied by the reported F-stat. The output of the second stage regression is below.

```
##                      beta      se_beta      t_stat
## endo_supply           0.47799096  0.174294964  2.742426
## fd_ln_realinc_percapita 0.32906581  0.044535764  7.388799
## fd_urbanization       -0.56880831  0.450533444 -1.262522
## year_supply_1970       0.05541277  0.008068089  6.868141
## [1] "The estimated supply elasticity is: 0.477990959926327"
## [1] "The 95% confidence interval is: [0.136372829868326, 0.819609089984328]"
```

A 95% confidence interval is constructed using:

$$CI(\beta) = [\beta - 1.96 * se(\beta), \beta + 1.96 * se(\beta)]$$

A 95% one-tailed t-test to see if we can reject supply elasticity being greater than 1 (so being elastic) is performed computing the following statistic:

$$t = \frac{\beta - 1}{se(\beta)}$$

```
df_supply_model <- iv_estimate_supply_model$df
t_test_supply_elastic = (supply_elasticity - 1)/supply_elasticity_se
critical_value_elastic_supply <- qt(p = 0.05, df = df_supply_model)

if (abs(t_test_supply_elastic) >= abs(critical_value_elastic_supply)) {
  print(paste("The t-stat is:", t_test_supply_elastic))
  print(paste("The critical value is:", critical_value_elastic_supply))
  print("We can reject the hypothesis that supply is elastic")
} else {
  print(paste("The t-stat is:", t_test_supply_elastic))
  print(paste("The critical value is:", critical_value_elastic_supply))
  print("We can't reject hypothesis that supply is elastic")
}
```

```
## [1] "The t-stat is: -2.99497488137029"
## [1] "The critical value is: -1.64580892731807"
## [1] "We can reject the hypothesis that supply is elastic"
```

As shown above we can reject that supply elasticity is elastic.

b) Estimate the elasticity of demand of gasoline. Provide a confidence interval. Can you reject the hypothesis that the demand of gasoline is elastic?

We proceed exactly as in part *a*), with the exception that now we use the price paid by the consumers P^D instead of the producer's price P^S . Our assumptions now mean that:

$$Q_{jt}^D(P_{jt}^S) = B_{jt}P_{jt}^{D\eta}$$

Where η is the elasticity of demand and for some constant B_{jt} that we allow to change flexible by year, state (and also the covariates explained in *a*)). We want to ran the following model:

$$\ln(Q_{jt}^D) = \omega + \eta \ln(P_{jt}^D) + X'_{jt} + \eta_j + \eta_t + \psi_{jt}^D$$

Were the controls are the same as in *a*). Again, first differencing the model as explained in *a*), we can obtain an estimate for η , the elasticity of demand.

Below, the first stage regression output (ommitting coefficients for the fixed effects).

```
##                beta_fs se_beta_fs  t_stat_fs
## instr                0.119568628 0.01498879  7.97720266
## fd_ln_realinc_percapita -0.003252058 0.03595133 -0.09045724
## fd_urbanization        -0.196781171 0.35911260 -0.54796510
## year_demand_1970       -0.031041207 0.00390374 -7.95165784
## [1] "F-stat of instruments in first stage is: 63.6357623006061"
```

The instrument is even stronger now, as implied by the reported F-stat. The output of the second stage regression is below.

```
##                beta    se_beta    t_stat
## endo_demand      -0.42997564 0.13639734 -3.152376
## fd_ln_realinc_percapita 0.31954423 0.03919855  8.151939
## fd_urbanization    -0.78237277 0.39227162 -1.994467
## year_demand_1970    0.02314605 0.00627316  3.689695
## [1] "The estimated demand elasticity is: -0.429975641592945"
## [1] "The 95% confidence interval is: [-0.697314428383888, -0.162636854802002]"
```

As in *a*) 95% confidence interval is constructed using:

$$CI(\eta) = [\eta - 1.96 * se(\eta), \eta + 1.96 * se(\eta)]$$

A 95% one-tailed t-test to see if we can reject demand elasticity being greater than -1 (so being elastic) is performed computing the following statistic:

$$t = \frac{\eta - 1}{se(\eta)}$$

```

df_demand_model <- iv_estimate_demand_model$df
t_test_demand_elastic = (demand_elasticity - 1)/demand_elasticity_se
critical_value_elastic_demand <- qt(p = 0.05, df = df_demand_model)

if (abs(t_test_demand_elastic) >= abs(critical_value_elastic_demand)) {
  print(paste("The t-stat is:", t_test_demand_elastic))
  print(paste("The critical value is:", critical_value_elastic_demand))
  print("Reject hypothesis that demand is elastic")
} else {
  print(paste("The t-stat is:", t_test_demand_elastic))
  print(paste("The critical value is:", critical_value_elastic_demand))
  print("Can't reject hypothesis that demand is elastic")
}

```

```

## [1] "The t-stat is: -10.4838968230745"
## [1] "The critical value is: -1.64580892731807"
## [1] "Reject hypothesis that demand is elastic"

```

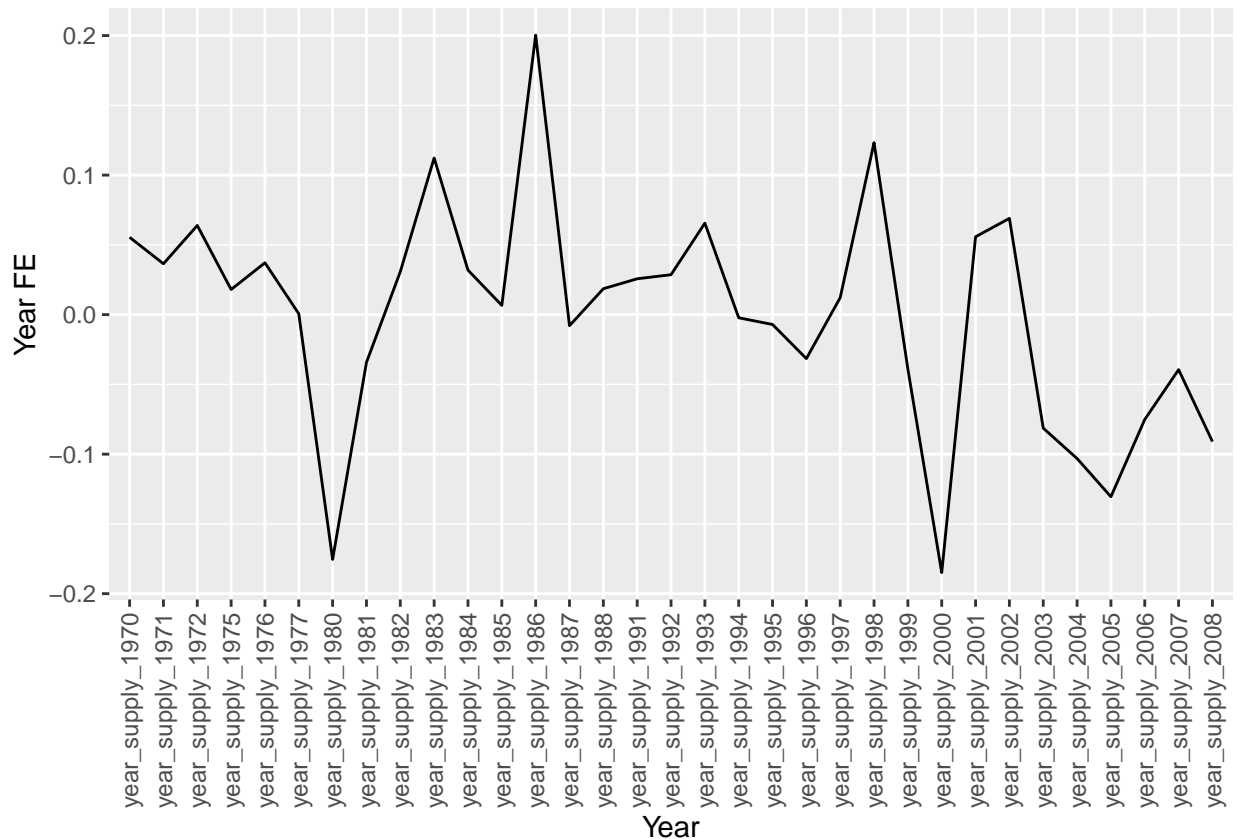
As shown above we can reject that demand elasticity is elastic.

c) A supply shock is a change from one year to the next in the amount of gasoline that would be supplied at a given price. According to your analysis, in what years did the US experience the most negative shock to the supply of gasoline? Why?

I plot the year fixed effects of the supply model in first differences that in the levels model corresponds to:

$$(\eta_t - \eta_{t-1})$$

which is exactly the change from one year to another in the amount of gasoline that would be supplied at a given price. Below the plot.



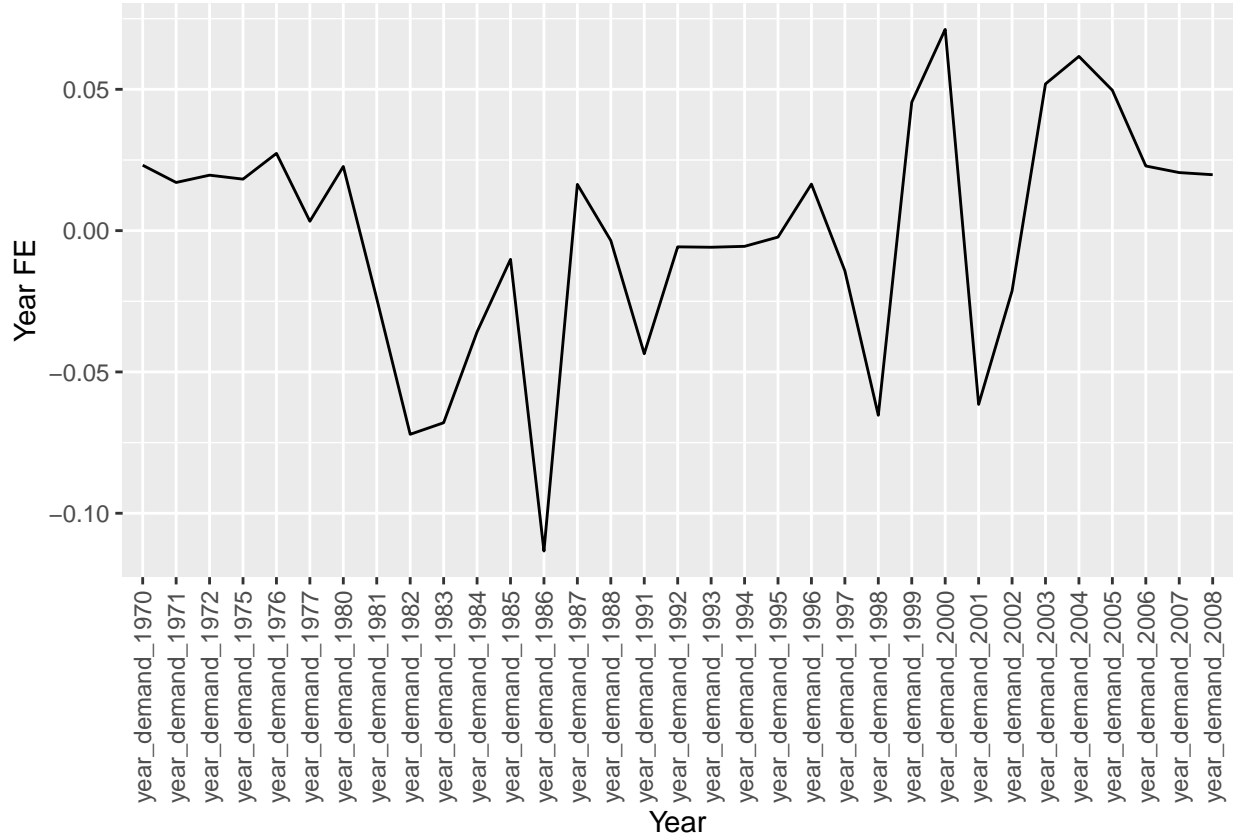
As shown above the most negative shock is in the year 2000, though the one in the year 1980 comes really close and corresponds to the 1979-1980 oil crisis, in which the price of oil increased a %100 in a few months. I am not sure what to make out of the year 2000 negative shock.

d) In what year after 2000 did the US experience the most negative shock to the supply of gasoline? Why?

It seems that the most negative shock after the year 2000 is in the year 2005. This is probably due to Hurricane Katrina, that occurred in August 2005, and according to Wikipedia it damaged or destroyed 30 oil platforms and caused the closure of nine refineries.

e) A demand shock is a change from one year to the next in the amount of gasoline that would be demanded at a given price. Examine the shocks to US gasoline demand over time as implied by your analysis. Is there any pattern that you can discern that explains when the shocks tend to be negative?

By the same reason expressed in c) I plot the year fixed effects from the demand model.



The negative shocks to demand seem to be correlated when times of economic crisis. For example, from July 1981 to November 1982 the US was in recession with the GDP contracting 2.7% coinciding with a very negative demand shock. The same is true for 1990 and 1991 when there was a short recession, and for the year 2001 when both the dot com bubble exploded and 9/11 happened. It is a little weird that the most negative demand shock happened in 1986, but clearly my model could be improved by controlling for other important variables.

f) Suppose that Rhode Island had declared a gasoline tax holiday in 2008, rebating the full value of all state and federal gasoline taxes. According to your analysis, what would have been the price of gasoline in that year? The quantity of gasoline?

As we assumed that the demand is isoelastic we have that for any given year-state:

$$Q_{jt}^D = A_{jt} P_{jt}^{D\eta}$$

and the same is true for the isoelastic supply:

$$Q_{jt}^S = B_{jt} P_{jt}^{S\beta}$$

Now, we can use the data from RI in 2008, to get the value of A and B. Note that:

$$A = \frac{Q^D}{P^{D\eta}}$$

and

$$B = \frac{Q^S}{P^{S\beta}}$$

Finally, we can equate the supply and demand equations and use the fact that $P^D = P^S$ without the tax so that we get the expression:

$$P^* = \frac{A}{B}^{\frac{1}{\beta-\eta}}$$

The new quantity can be recovered from plugging P^* in either the supply or demand equation. Below I implement this in code.

```
ri_2008_data <- gas_data %>%
  filter(state == "Rhode Island", year == 2008)

quantity <- as.numeric(ri_2008_data %>%
  mutate(quantity = exp(ln_q_percapita)) %>%
  select(quantity))
demand_constant <- as.numeric(ri_2008_data %>%
  mutate(demand_constant = (exp(ln_q_percapita))/(exp(ln_real_gas_p)^demand_elasticity)) %>%
  select(demand_constant))
supply_constant <- as.numeric(ri_2008_data %>%
  mutate(supply_constant = (exp(ln_q_percapita))/(exp(ln_real_gas_producer_p)^supply_elasticity)) %>%
  select(supply_constant))

price_producer <- as.numeric(ri_2008_data %>%
  mutate(price_producer = exp(ln_real_gas_producer_p)) %>%
  select(price_producer))
price_consumer <- as.numeric(ri_2008_data %>%
  mutate(price_consumer = exp(ln_real_gas_p)) %>%
  select(price_consumer))

total_tax <- price_consumer - price_producer
comp_price <- (demand_constant/supply_constant)^(1/(supply_elasticity - demand_elasticity))
new_quantity <- demand_constant*comp_price^demand_elasticity
print(paste("With tax the consumer price was: ", price_consumer))

## [1] "With tax the consumer price was:  1.6754617414248"
print(paste("With tax the producer price was: ", price_producer))

## [1] "With tax the producer price was:  1.42005276239642"
print(paste("With tax the quantity traded was: ", quantity))

## [1] "With tax the quantity traded was:  371.299443845952"
print(paste("Without the tax the competitive price is: ", comp_price))

## [1] "Without the tax the competitive price is:  1.53574896457545"
print(paste("Without the tax the quantity traded is: ", new_quantity))

## [1] "Without the tax the quantity traded is:  385.463730171299"
```

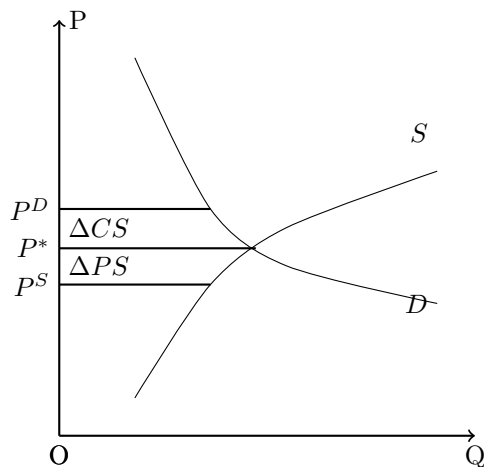


Figure 1: A tax holiday in RI: consumer and producer surplus gains.

```
if (round(new_quantity, digits = 3) ==
    round(supply_constant*comp_price^supply_elasticity,digits = 3)){
  print("Celebrate: we asserted that demand equals supply")
}else{
  print("Oops, demand does not equal supply")
}
```

```
## [1] "Celebrate: we asserted that demand equals supply"
```

g) What would have been the gain in consumer surplus, producer surplus, and total surplus from the tax holiday?

The gain in consumer surplus (ΔCS) and producer surplus (ΔPS) are given in the following figure:

The tax revenue that the government lost due to tax holiday is given by the rectangle marked in the following figure. Now note that the change in total surplus is given by the DWL as we have that:

$$\Delta TS = \Delta CS + \Delta PS + \Delta TR = DWL$$

In this particular case we can compute exactly the numbers and that I do in the code below:

```
demand <- function(x) {demand_constant*(x^(demand_elasticity))}
supply <- function(x) {supply_constant*(x^(supply_elasticity))}
change_cs <- integrate(demand, lower = comp_price, upper = price_consumer)$value
print(paste("The change in consumer surplus is :", change_cs))
```

```
## [1] "The change in consumer surplus is : 52.8442124270129"
```

```
change_ps <- integrate(supply, lower = price_producer, upper = comp_price)$value
print(paste("The change in producer surplus is :", change_ps))
```

```
## [1] "The change in producer surplus is : 43.7828953875963"
```

```
gov_loss <- -quantity*(price_consumer - price_producer)
print(paste("The change in tax revenue is :", gov_loss))
```

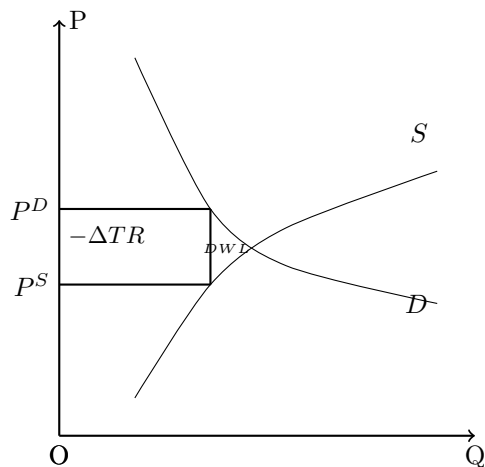



Figure 2: A tax holiday in RI: government loses tax revenue, DWL arises.

```
## [1] "The change in tax revenue is : -94.8332118665016"
change_ts <- change_cs + change_ps - gov_loss
print(paste("The change in total surplus is :", change_ps))

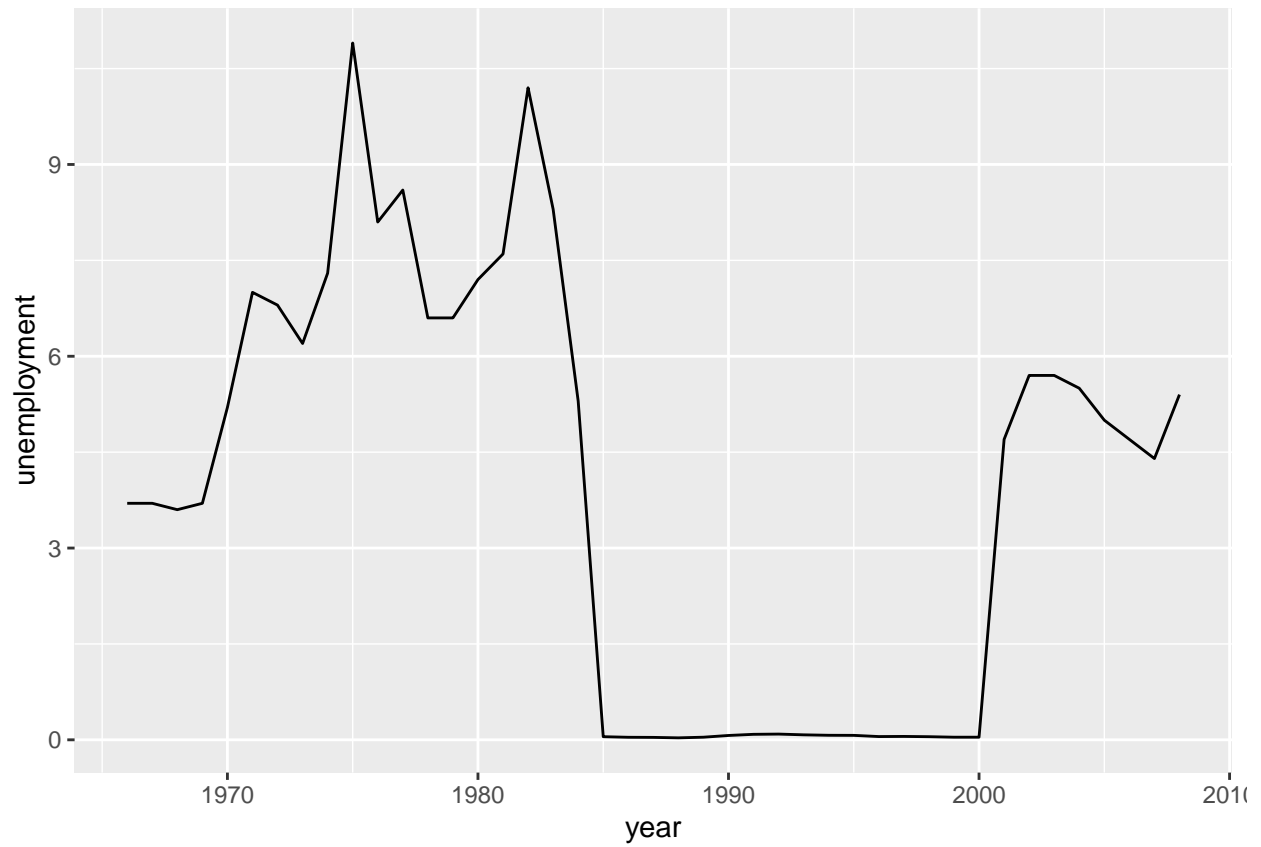
## [1] "The change in total surplus is : 43.7828953875963"
```

h) Suppose that Rhode Island had decided in 2008 to grant a monopoly concession to a single gasoline supplier (in addition to having a tax holiday). What would have been the price and quantity of gasoline in Rhode Island 2008?

The monopolist wouldn't be able to maximize profits, as the demand curve is isoelastic with an absolute value of the elasticity of demand that is smaller than 1. The monopolist could always increase price and make more profit, so the price that maximizes profits is infinity.

i) Plot the unemployment rate in Rhode Island over time. Do you notice anything odd about this series?

The original series looks like this:



However, if multiplying the weird years by 100 we get:

