



Bookmarks



Bookmark

► Introduction

▼ 1. Probability and Inference

Introduction to Probability (Week 1)

Exercises due Sep 21, 2016 at 21:00 UTC

Probability Spaces and Events (Week 1)

Exercises due Sep 21, 2016 at 21:00 UTC

Random Variables (Week 1)

Exercises due Sep 21, 2016 at 21:00 UTC

Jointly Distributed Random Variables (Week 2)

Exercises due Sep 28, 2016 at 21:00 UTC

Conditioning on Events (Week 2)

Exercises due Sep 28, 2016 at 21:00 UTC

Homework 1 (Week 2)

Homework due Sep 28, 2016 at 21:00 UTC

Inference with Bayes' Theorem for Random Variables (Week 3)

Exercises due Oct 05, 2016 at 21:00 UTC

Independence Structure (Week 3)

Exercises due Oct 05, 2016 at 21:00 UTC

Homework 2 (Week 3)

1. Probability and Inference > Inference with Bayes' Theorem for Random Variables (Week 3) > Maximum A Posteriori (MAP) Estimation

MAXIMUM A POSTERIORI (MAP) ESTIMATION


For a hidden random variable \mathbf{X} that we are inferring, and given observation $\mathbf{Y} = \mathbf{y}$, we have been talking about computing the posterior distribution $p_{\mathbf{X}|\mathbf{Y}}(\cdot|\mathbf{y})$ using Bayes' rule. The posterior is a distribution for what we are inferring. Often times, we want to report which particular value of \mathbf{X} actually achieves the highest posterior probability, i.e., the most probable value \mathbf{x} that \mathbf{X} can take on given that we have observed $\mathbf{Y} = \mathbf{y}$.

The value that \mathbf{X} can take on that maximizes the posterior distribution is called the *maximum a posteriori* (MAP) estimate of \mathbf{X} given $\mathbf{Y} = \mathbf{y}$. We denote the MAP estimate by $\hat{\mathbf{x}}_{\text{MAP}}(\mathbf{y})$, where we make it clear that it depends on what the observed \mathbf{y} is. Mathematically, we write

$$\hat{\mathbf{x}}_{\text{MAP}}(\mathbf{y}) = \arg \max_{\mathbf{x}} p_{\mathbf{X}|\mathbf{Y}}(\mathbf{x}|\mathbf{y}).$$


Note that if we didn't include the "arg" before the "max", then we would just be finding the highest posterior probability rather than which value—or "argument"— \mathbf{x} actually achieves the highest posterior probability.

In general, there could be ties, i.e., multiple values that \mathbf{X} can take on are able to achieve the best possible posterior probability.

Homework due Oct 05,
2016 at 21:00 UTC 

**Notation Summary
(Up Through Week
3)**

**Mini-project 1:
Movie
Recommendations
(Week 3)**

Mini-projects due Oct
12, 2016 at 21:00 UTC 

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