

# PEL TEMA 2 SEMANA 5

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$$M = 2 \text{ g/mol}$$

$$\gamma = 1.35$$

$$\Gamma(\gamma) = 0.6761$$

$$c^* = 5500 \text{ m s}^{-1}$$

$$R_u = 8.314 \text{ J/mol K}$$

$$A_g = 1.2 \text{ cm}^2 = 0.0012 \text{ m}^2$$

$$R = 4157 \text{ J/kg K}$$

(condiciones tobera adaptada)

1.7 kg combustible / 5 segundos

$$\dot{m}_{\text{combustible}} = 0.34 \text{ kg s}^{-1}$$

$$V_s = 9075 \text{ m s}^{-1}$$

$$(a) \dot{m} = 0.34 \text{ kg s}^{-1} //$$

$$(b) p_c = \frac{c^* \dot{m}}{A_g} = 15.58 \text{ MPa} //$$

$$T_c = (c^* \Gamma(\gamma))^2 R^{-1} = 3326 \text{ K} //$$

$$(c) \dot{E} \approx \dot{m} V_s \approx 3085.5 \text{ N}$$

en tobera adaptada:

$$C_E = \frac{\dot{E}}{p_c A_g} = 1.65 //$$

$$I_{sp} \approx V_s \approx 9075 \text{ m s}^{-1} //$$

$$I_{sp} = 9075 \text{ m s}^{-1}$$

$$(d) G_E = (c^*)^2 I_{sp} = 1.65 //$$

$$(e) C_E = C_{E \text{ adapt}} = \Gamma(\gamma) \sqrt{\frac{2\gamma}{\gamma-1} \left[ 1 - \left( \frac{p_s}{p_c} \right)^{\frac{\gamma-1}{\gamma}} \right]}$$

$$\therefore \frac{p_s}{p_c} = 3.33 \cdot 10^{-3} //$$

$$(f) \varepsilon = \frac{A_s}{A_g} = \frac{\Gamma(\gamma)}{\left( \frac{p_s}{p_c} \right)^{1/\gamma} \sqrt{\frac{2\gamma}{\gamma-1} \left[ 1 - \left( \frac{p_s}{p_c} \right)^{\frac{\gamma-1}{\gamma}} \right]}} = 18.94 //$$

$$(g) C_E = \Gamma(\gamma) \sqrt{\frac{2\gamma}{\gamma-1} \left[ 1 - \left( \frac{p_s}{p_c} \right)^{\frac{\gamma-1}{\gamma}} \right]} + \varepsilon \left( \frac{p_s}{p_c} - \frac{p_{amb}^0}{p_c} \right)$$

with  $p_{amb} = 0$  en el vacío

$$\therefore C_E = 1.713$$

$$(h) I_{sp} = c^* C_E = 9421.5 \text{ m s}^{-1} //$$

$$(i) \text{ considerando } \Delta V = 6 \text{ km s}^{-1} = 6000 \text{ m s}^{-1}$$

$$\Delta V = I_{sp} \ln \left( \frac{M_0}{M_f} \right) \quad \therefore \frac{M_0}{M_f} = e^{\frac{\Delta V}{I_{sp}}} = 1.89 //$$

$$(j) M_0 = M_s + M_{cp} + M_p, \text{ con } M_s = 700 \text{ kg}; M_{cp} = 200 \text{ kg}$$

$$M_p = M_0 - M_s - M_{cp}$$

$$1.89 = \frac{M_s + M_{cp} + M_p}{M_s + M_{cp}} \Rightarrow M_p = 801 \text{ kg} //$$