

# SPRISS: Approximating Frequent k-mers by Sampling Reads, and Applications



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# Background

## Dataset $D$ of reads

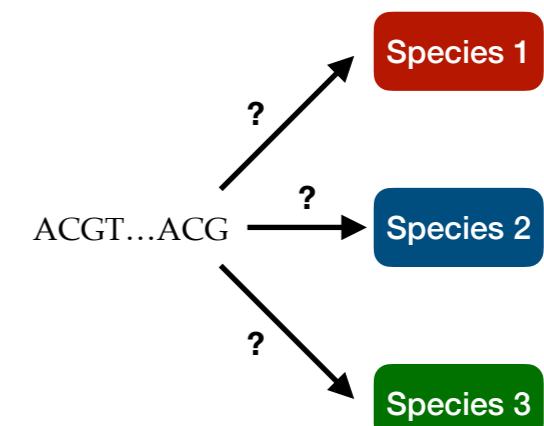
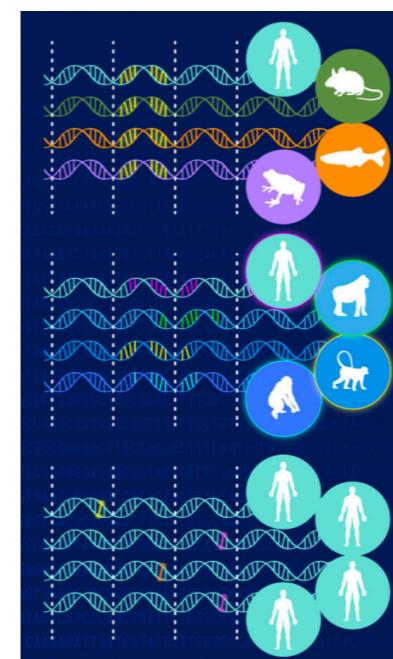
```
>seq1_RTW_read1  
ATCGACGTACGATGCACGCATGACG  
>seq1_RTW_read2  
ACGATGCATTGCATCGACTCGAATG  
>seq1_RTW_read3  
TTGCTAGTGTACCTGATGCATTGCA  
>seq1_RTW_read4  
CGACTCGAACATCGATGCATTGCATG  
>seq1_RTW_read5  
GTACCTGATTGCTAGTTGCATTGCA  
...
```

**$k$ -mer  $P$ :** substring of length  $k$  of a read

**frequency  $f_D(P)$  of  $P$  on  $D$**  = fraction of  $k$ -mers of  $D$  equal to  $P$

The **study of  $k$ -mers and their frequencies** from datasets of reads is a **crucial step** for:

- Comparison of metagenomic datasets;
- Read classification in metagenomics;
- Genome comparison;
- Error correction for genome assembly;
- ...



# Motivation

Exact  $k$ -mer counters exist 😊

**Jellyfish** (Marçais et al., 2011)

**BFCOUNTER** (Melsted and Pritchard, 2011)

**DSK** (Rizk et al., 2013)

**KAnalyze** (Audano and Vannberg, 2014)

**Turtle** (Roy et al., 2014)

**KMC** (Kokot et al., 2017)

**Squeakr** (Pandey et al., 2017)

...

→ counting all  $k$ -mers is computationally expensive on massive modern datasets 😞

For some applications:

- Comparisons of metagenomic datasets
- Discovery of discriminative k-mers



just frequent  $k$ -mers are of interest

# Motivation

**Frequent  $k$ -mer  $P$ :** given  $\theta \in (0,1]$ ,  $P$  appears in  $D$  with frequency  $f_D(P) \geq \theta$

**Def.**

**Frequent  $k$ -mer counting problem**

Given  $\theta$ , extract frequent  $k$ -mers (and their frequencies)  $FK(D, k, \theta)$  from  $D$

computationally expensive  
on massive modern datasets 😞



approximation methods

# State of the art

Frequent k-mers approximations with theoretical guarantees: relatively unexplored

**SAKEIMA** [Pellegrina, Pizzi, Vandin. RECOMB 2019 - JCB 2020]

- Approximations of frequent  $k$ -mers with guarantees by *sampling k-mers*
- Require to scan the entire dataset  $D$
- Needs to be reimplemented for more efficient exact  $k$ -mer counters  
(It is built on *Jellyfish*)



This work, **SPRISS**

- Approximations of frequent  $k$ -mers with guarantees by *sampling reads*
- Require to scan just a sample of reads of  $D$
- No need to reimplement it for more efficient exact  $k$ -mer counters



# Computational problem

## Computational problem

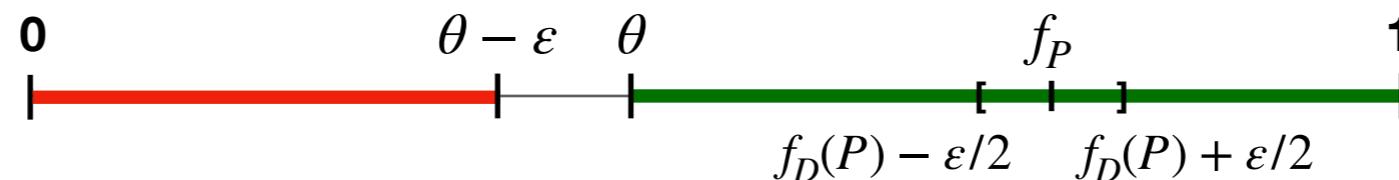
*Input:*  $D, k, \theta, \varepsilon, \delta$

*Output:*  $\varepsilon$ -approximation of frequent  $k$ -mers  $FK(D, k, \theta)$  with probability  $\geq 1 - \delta$

### Def.

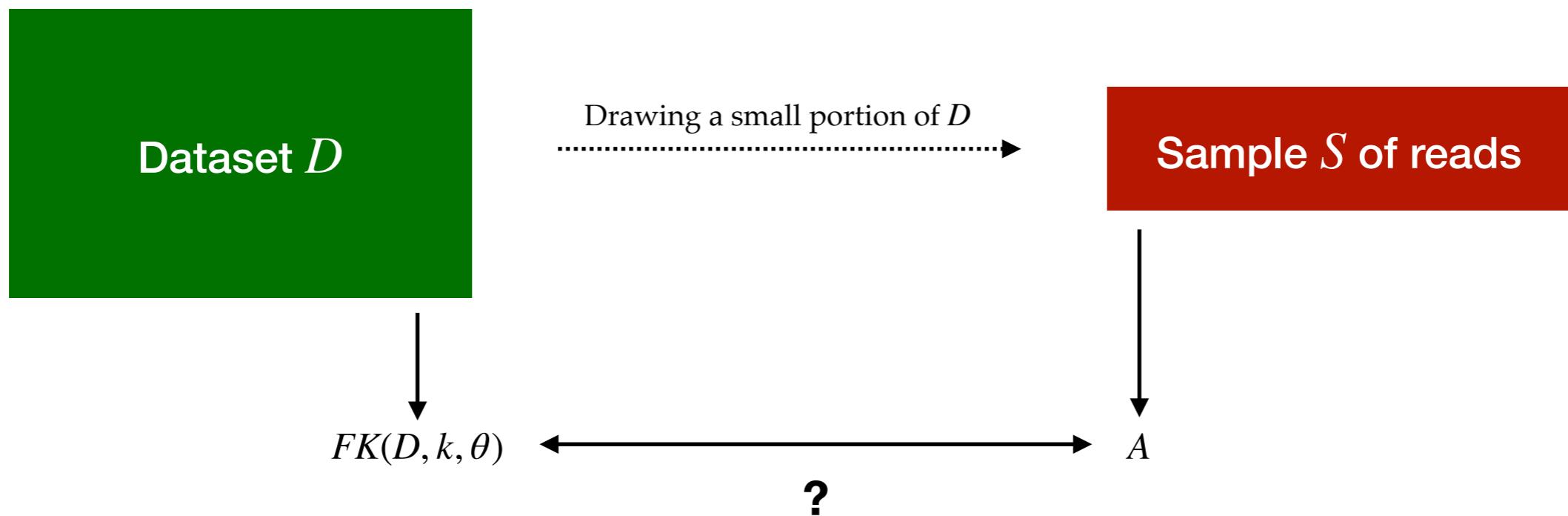
Given  $\varepsilon \in (0, \theta)$ , a set  $A = \{(P, f_P)\}$  is an  $\varepsilon$ -approximation of  $FK(D, k, \theta)$  if:

1.  $A$  contains no false negatives
2.  $A$  does not contain  $k$ -mers s.t.  $f_D(P) < \theta - \varepsilon$
3. All  $k$ -mers in  $A$  are s.t.  $|f_D(P) - f_P| \leq \varepsilon/2$



# SPRISS: main idea

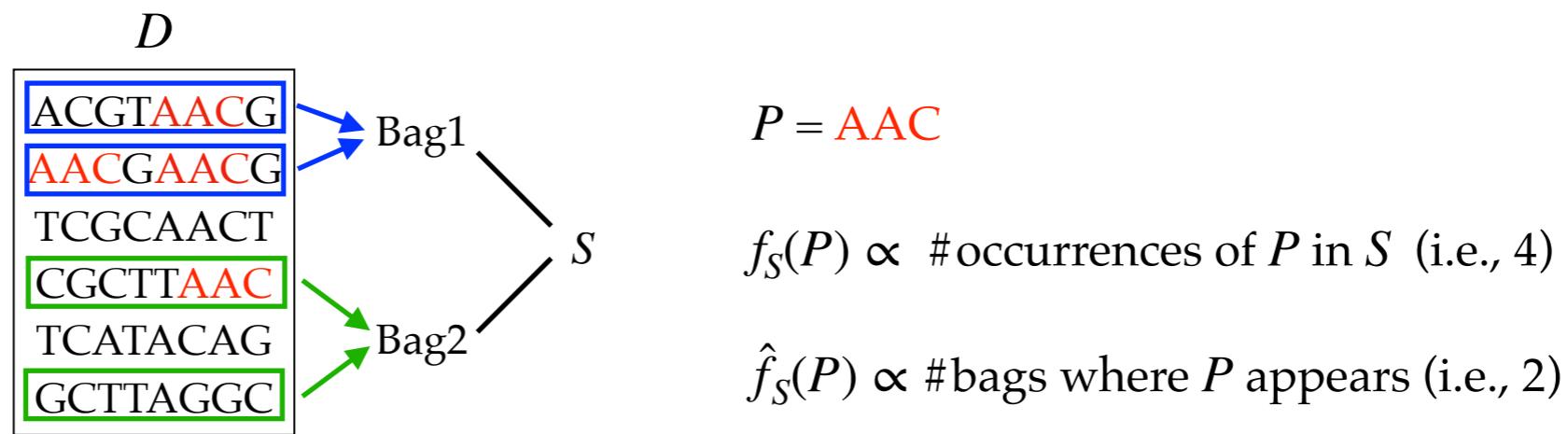
Approximation  $A$  of frequent  $k$ -mers  $FK(D, k, \theta)$  by analyzing a sample  $S$  of  $D$



## Challenges:

1. Find a rigorous relation between  $A$  and  $FK(D, k, \theta)$ .
2. Identify a sample size which is sufficient to guarantee good estimates from  $S$ .
3. Reads introduce dependencies among  $k$ -mers

**Sampling strategy:** sample  $S$  is a collection of  $m$  bags of  $\ell$  reads sampled independently and uniformly at random, with replacement, from  $D$



## Main steps:

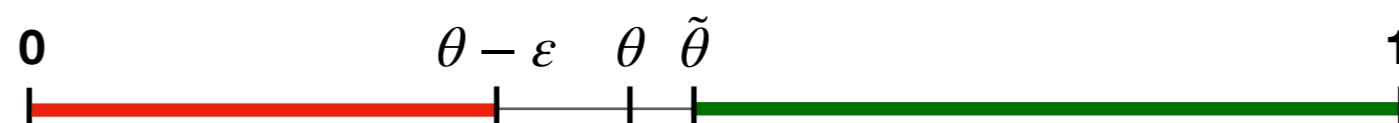
1. Compute sample  $S$
2. Compute  $f_S(P)$  and  $\hat{f}_S(P)$  using any exact k-mer counter
3. Output  $A = \{(P, f_S(P)) : \hat{f}_S(P) \geq \theta - \varepsilon/2\}$

# Main contribution

**Thm**

If  $m \geq \frac{2}{\varepsilon^2} \left( \frac{1}{\ell \ell_{D,k}} \right)^2 \left( \lfloor \log_2 \min(2\ell \ell_{\max, D, k}, \sigma^k) \rfloor + \ln \left( \frac{1}{\delta} \right) \right)$  then

$A = \{(P, f_S(P)) : \hat{f}_S(P) \geq \theta - \varepsilon/2\}$  is *almost* an  $\varepsilon$ -approximation  
of  $FK(D, k, \theta)$ , with probability  $\geq 1 - \delta$



**Proof:** based on the *pseudodimension*, a key tool from statistical learning theory, of k-mers

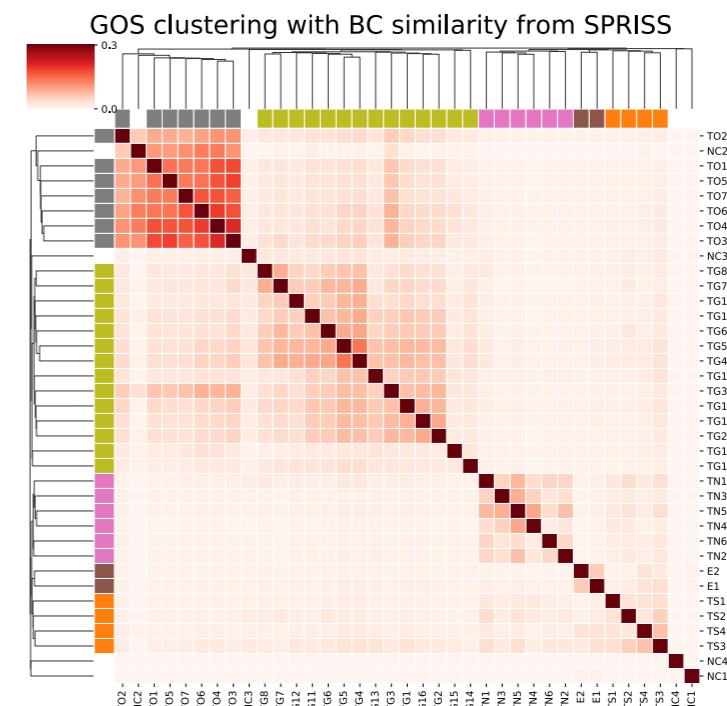
# Experimental results

**Implementation:** C++ (based on KMC exact counter)

**Machine:** 512 GB of RAM and 2 Intel(R) Xeon(R) CPU E5-2698 v3 @2.3GHz

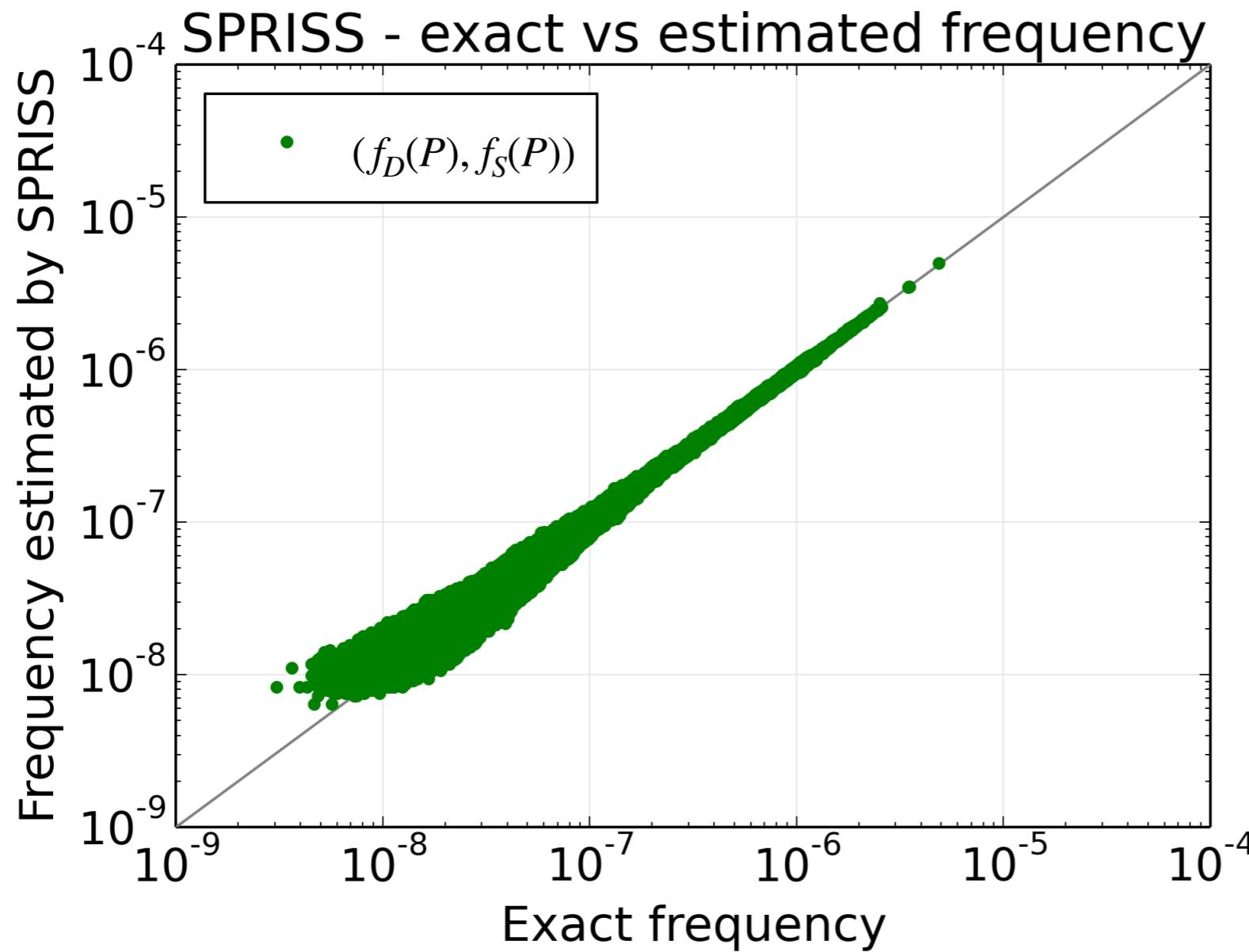
## Experimental results:

1. Accuracy of the estimates
  2. Resources
  3. Comparing metagenomic datasets
  4. Discriminative k-mers approximations



# Accuracy

6 large datasets from Human Microbiome Project (HMP) -  $\approx 10^8$  reads  
 $k = 31$



$$\theta = 2.5 \cdot 10^{-8}$$

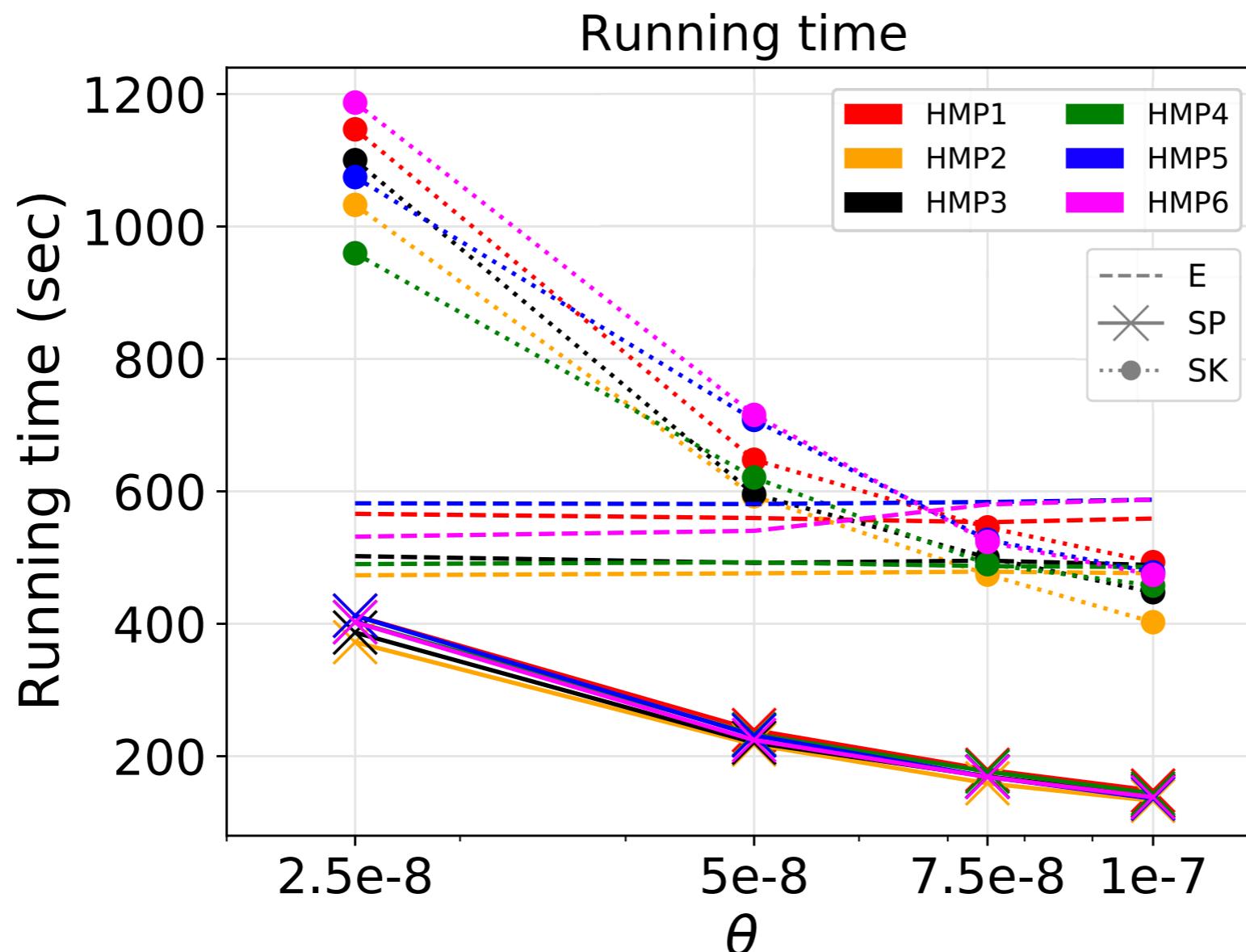
30% of  $D$  analyzed

# Resources

**SP** = SPRISS

**SK** = SAKEIMA (built on *Jellyfish*)

**E** = exact approach (KMC)

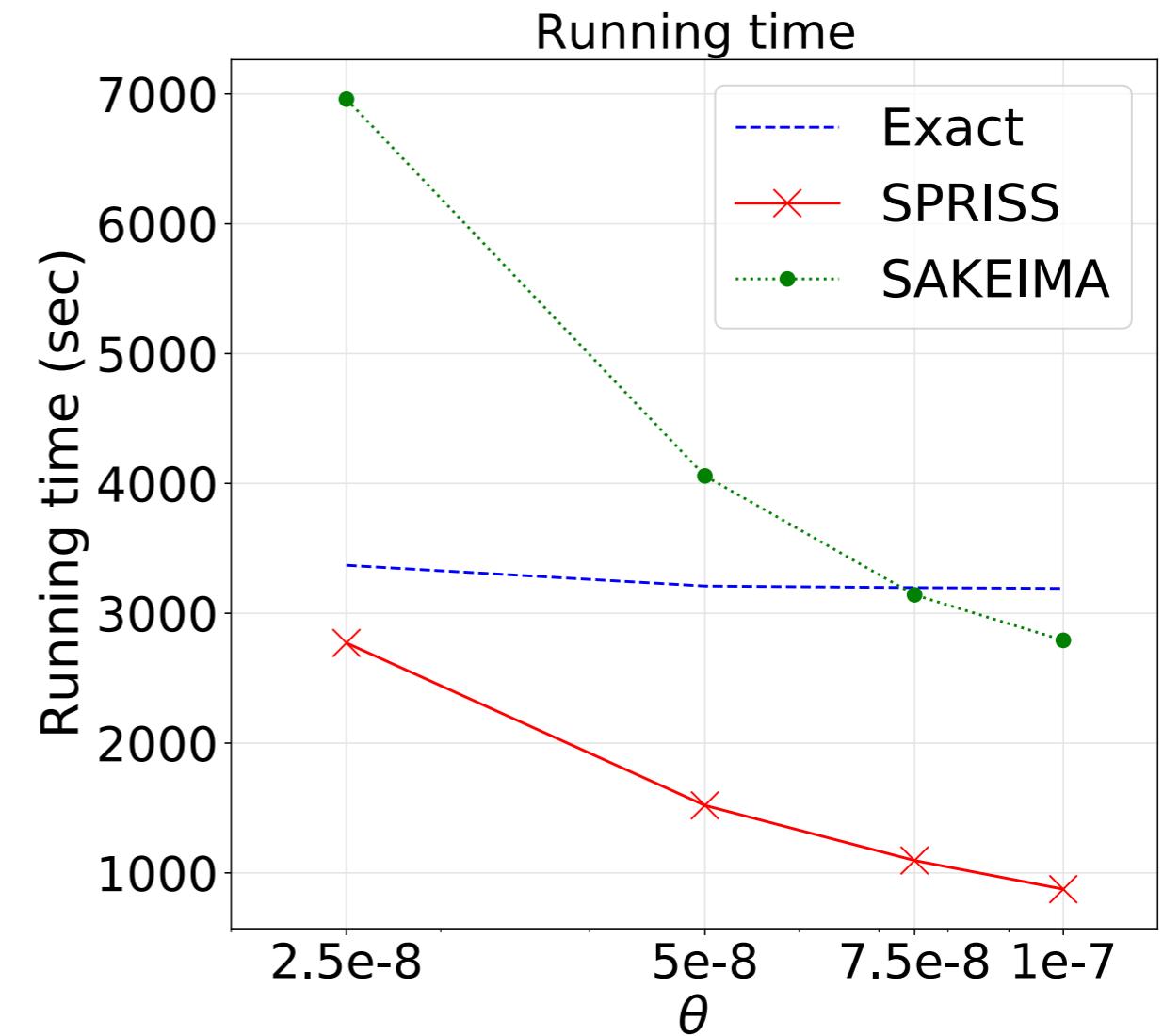
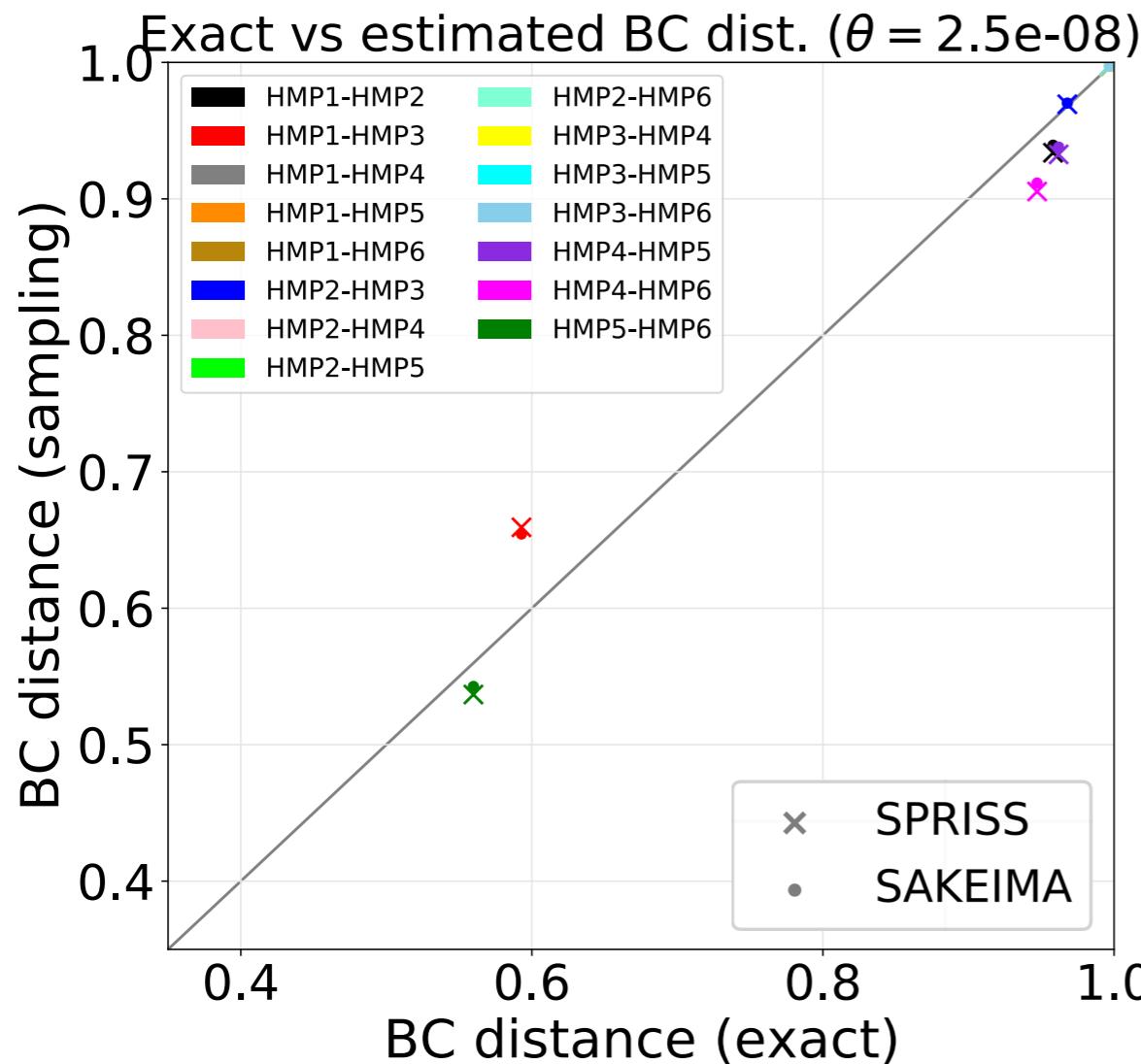


**SPRISS analyzes at most 34% of each dataset  $D$**

# Comparing metagenomic datasets

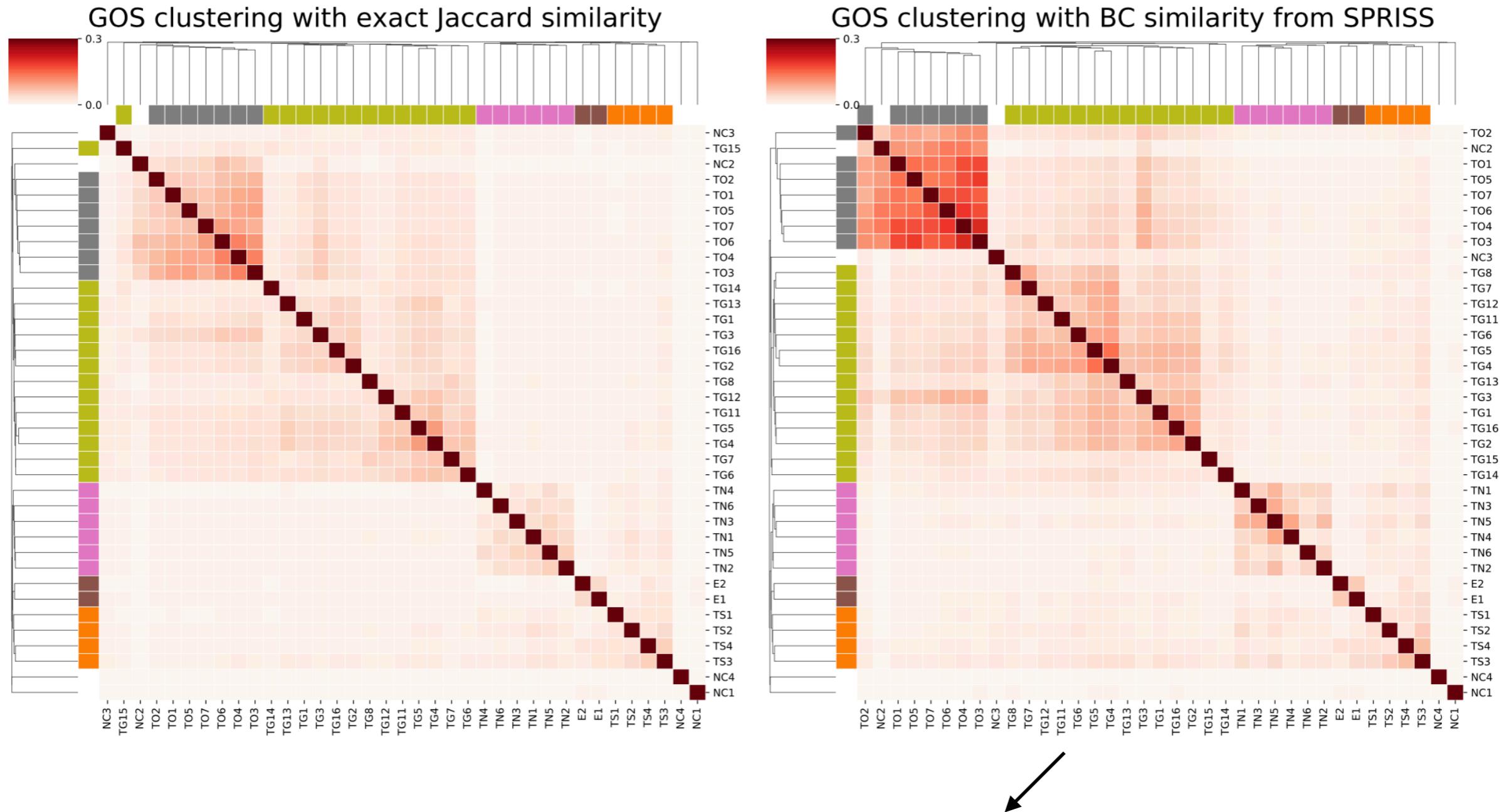
Bray-Curtis (BC) distance of  $D_1$  and  $D_2$  as a function of frequent  $k$ -mers

Estimation of BC by using approximations of  $FK(D_1, k, \theta)$  and  $FK(D_2, k, \theta)$



# Comparing metagenomic datasets

37 datasets from Global Ocean Sampling (GOS) Expedition -  $\approx 10^5$  reads  
 $k = 21$



Inside-vs-outside cluster signal increases of 50% using BC estimates  
SPRISS requires 40% of the time of exact BC approach

# Discriminative $k$ -mers

**Def.**

Given two datasets  $D_1$  and  $D_2$ , the  $D_1$ -discriminative  $k$ -mers are s.t.:

1.  $P \in FK(D_1, k, \theta)$ , and
2.  $f_{D_1}(P) \geq \rho f_{D_2}(P)$ ,  $\rho > 1$

$D_1$	$D_2$
ACGT <b>AAC</b> G	TTGACATG
<b>AAC</b> GAACG	GTCGTACG
CGCTT <b>AAC</b>	ATCCCGAG
TCATA <b>CAG</b>	CTGATCAA
GCTTAGGC	CCATACTC
TCGC <b>AACT</b>	ACTCATCG

$$P = \textcolor{red}{AAC}$$

Estimation of discriminative  $k$ -mers by using SPRISS's approximations

2 large datasets from (Liu et al., 2017) -  $\approx 4 \times 10^8$  reads,  $k = 31$ ,  $\rho = 2$

Using just 5% of reads of  $D_1$  and  $D_2$

- false negative rate is  $< 0.03$
- Running time gain: 90%



## Acknowledgements:



*Leonardo Pellegrina*



*Fabio Vandin*

## Fundings:



# Thanks for your attention! 😊



**SPRISS available at:**

<https://github.com/VandinLab/SPRISS>

<https://arxiv.org/abs/2101.07117>

**Recipe of SPRISS:**

3 ounces of Prosecco

2 ounces of Aperol

1 ounce of Club Soda

Garnish: orange slice

<https://www.liquor.com/recipes/aperol-spritz/>



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