

Filters

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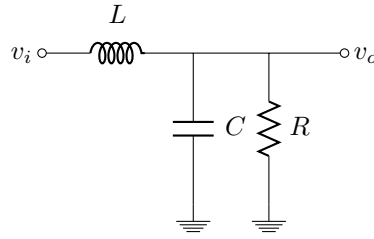
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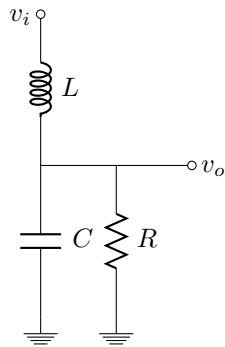
1 Filters

1.1 LC filter

LC filter loaded with R transfer function



In the voltage-divider form:



$$V_o = V_i \frac{Z_{R//C}}{Z_L + Z_{R//C}}$$

Butterworth filter. Maximum flatness filter. The normalized Butterworth polynomials can be used to determine the transfer function for any low-pass filter cut-off frequency ω_c , as follows

$$H(s) = \frac{G_0}{B_n(a)}$$

where $a = \frac{s}{\omega_c}$.

To four decimal places, Butterworth polynomials are (expressed in quadratic factors)

Order	Polynomial $B_n(s)$
1	$(s + 1)$
2	$s^2 + 1.4142s + 1$
3	$(s + 1)(s^2 + s + 1)$
4	$(s^2 + 0.7654s + 1)(s^2 + 1.8478s + 1)$
5	$(s + 1)(s^2 + 0.6180s + 1)(s^2 + 1.6180s + 1)$
6	$(s^2 + 0.5176s + 1)(s^2 + 1.4142s + 1)(s^2 + 1.9319s + 1)$
7	$(s + 1)(s^2 + 0.4450s + 1)(s^2 + 1.2470s + 1)(s^2 + 1.8019s + 1)$
8	$(s^2 + 0.3902s + 1)(s^2 + 1.1111s + 1)(s^2 + 1.6629s + 1)(s^2 + 1.9616s + 1)$

From [Butterworth filter, Wikipedia](#)

- two frequencies which ratio is 1:10 are separate by a decade
- two frequencies which ratio is 1:2 are separate by a octave
- 1 decade is 3.33 octaves