#### Assignment

 $Diego\ Uriarte$ 

September 09, 2018

#### 1 Conceptual questions on static demand and cost estimation

### 1.1 Explain in words why price is endogenous in Berry's framework in discrete choice models?

The price is endogenous because of the unobservable product characteristics ( $\xi_j$ ). The consumer does observe these characteristics but not the econometrician (there are not in the dataset). The endogeneity occurs because the unobservable characteristics of the cars (that the consumers do observe) is obviously correlated with the price. For that reason, in the equation:

$$\ln(s_j) - \ln(s_0) = x_j \times \beta - \alpha \times p_j + \xi_j$$

A higher  $\xi_j$  will cause a higher  $p_j$  (because firms are in a Bertrand price competition), all else equal.

#### 1.2 Explain in words why within-group share is endogenous in discrete choice models?

The within-group is endogenous because is correlated with the unobservable product characteristics  $(\xi_j)$ . For instance, if the share of Mercedes Benz automobiles goes down (maybe because there is an increase in their prices), we would expect that the share of BMW cars goes up by much more than the share of Nissan cars. This would be because both Mercedes and BMW share characteristics that appeal to the same costumers.

### 1.3 Derive marginal costs for single-product firms for Berry's nested logit model, given data and estimated parameters.

First, profit for firm j are given by:

$$\pi_j(\mathbf{p}, z, \xi, \omega_j, \theta) = p_j M s_j(x, \xi, p, \theta_d) - C_j(q_j, w_j, \omega_j, \gamma)$$

Where, p are prices, x, w observed characteristics,  $\xi$  and  $\omega$  unobserved characteristics,  $\theta_d$  demand parameter, M is total market size.

Since firms are price setters, and if we assume that there is an interior equilibrium, the FOC are:

$$p_j = c_j + s_j / |\partial s_j / \partial p_j|$$

Also, using the chain rule  $(\frac{\partial s_j}{\partial \delta_j} \frac{\partial \delta_j}{\partial p_j} = \frac{\partial s_j}{\partial p_j})$ , and using the definition of  $\delta_j$  to differentiate  $\frac{\partial \delta_j}{\partial p_j} = -\alpha$  we get:

$$-\alpha \frac{\partial s_j}{\partial \delta_j} = \frac{\partial s_j}{\partial p_j}$$

Also, we assume that the marginal cost is linear in the unobservable cost term  $\omega_j$ , we get  $c_j = \bar{c}(q_j, w_j, \gamma) + \omega_j$ . Replacing in the FOC:

$$p_j = \bar{c_j} + \frac{1}{\alpha} [s_j/|\partial s_j/\partial \delta_j|] + \omega_j$$

Using the market share equation for the logit model, we get:

$$\partial \int_{j} / \partial \delta_{j} = \frac{1}{1 - \sigma} s_{j} [1 - \sigma s_{j/g} - (1 - \sigma) s_{j}]$$

Finally, replacing in the previous expression:

$$p_{j} = \bar{c_{j}} + \frac{1-\sigma}{\alpha}/[1-\sigma s_{j/g}^{-} - (1-\sigma)s_{j}] + \omega_{j}$$

Since the parameters have been estimated, we can determine average marginal cost from the previous expression. These derivation was taken from Berry (1994).

### 1.4 What are two useful source of instruments for discrete choice models? Explain.

One possibility is to use price variation across cities or regions as cost shifters. These are a valid instrument if the marginal costs are correlated across cities, but not the unobservable product characteristics ( $\xi_j$ ). That is to say that the price of a good in city j is correlated with the marginal cost in city j, that is correlated with the marginal cost in city i. But  $\xi_i$  and  $\xi_j$  are not correlated.

For the automobile sector, changes in fuel prices generate cost variation. The consumer is interested in how long can she travel with 1\$ of fuel (miles per dollar), but for the car maker, increase the miles per gallon for a given model is costly. For that reason, fuel prices variation can be used as cost shifter, however they may not be that strong.

### 1.5 What are two reasons to estimate the supply side models along with the demand side of discrete choice models? Explain.

Only estimating the demand side is consistent with the endogeneity of prices and with equilibrium results, however, by adding the supply side we can get better or more precise estimates of the parameters. Another reason to incorporate supply side models and solve for the equilibrium is that we can test with type of competitive model fits best the data. As Miller and Weinberg (2017) used this approach to reject the hypothesis that there was a Nash-Bertrand equilibrium between two brewing company after their merge.

### 1.6 What are the advantages of using a random coefficients model, à la BLP, instead of a nested logit model?

IV estimator for the nested logit model is just a special case of the BLP model, where  $\xi_j$  is linear in the parameters. The advantage of BLP is that it allows for non-linear relation between  $\xi_j$  and the parameters, by recovering the function numerically. Another advantage is that BLP added equilibrium behavior to the models, and as it was discussed in the previous question, it can improve the accuracy of the parameters and allows us to test for market behavior.

- 2 Computational questions on static demand and cost estimation (40 points)
- 2.1 Collapse the data to the product / market level and drop the outside good for each market as observations, creating an "outside good share" variable for each inside good choice. Report summary statistics on market shares and outside good share by plan number. Report the number of observations.

First, we explore the dataset

#### head(data)

```
## # A tibble: 6 x 11
     individual market plan num_plans choice price
                                                           xsi x_constant
##
                  <int> <int>
                                   <int>
                                           <int> <dbl>
                                                        <dbl>
                                                                    <int>
## 1
                                       5
                                               0 0
                      1
                             0
                                                       0
                                                                         0
## 2
                                       5
                                               1 1.09
                                                       0.631
                                                                         1
                             2
                                       5
## 3
               1
                                               0 1.32 0.921
                      1
                                                                         1
## 4
               1
                             3
                                       5
                                               0 0.876 0.0309
                      1
                                                                         1
                                       5
## 5
              1
                      1
                             4
                                               0 0.908 0.0125
                                                                         1
                             0
                                       5
                                               0 0
                      1
     ... with 3 more variables: x_coinsurance <dbl>, x_deductible <dbl>,
       x_oopmax <dbl>
```

There are 89801 persons in the dataset, 100 markets, each with different plans. We are given information about the plan chosen by each individual (choice variable), as well as the price, and the observable characteristic in each plan (x\_constant, x\_coinsurance, x\_deductible, x\_oopmax). It is important to note that plan x in market i is not the same as plan x in market j. The value xsi represents the unobservable characteristics, and as such, they will only be used at the end as benchmark for our regression results.

We are asked to collapse the data to the market level. The first 10 values of the collapsed dataset are showed. The complete dataset transformation can be found in the replication file.

```
## # A tibble: 10 x 11
##
  # Groups:
               market [3]
##
      market plan
                     s 0
                             s_j s_j_given_g price
                                                        xsi x constant
##
       <int> <int> <dbl>
                          <dbl>
                                       <dbl> <dbl>
                                                      <db1>
                                                                  <dbl>
##
    1
           1
                 1 0.352 0.183
                                      0.283 1.09
                                                     0.631
                                                                      1
##
    2
           1
                 2 0.352 0.300
                                      0.463 1.32
                                                                      1
                                                     0.921
##
   3
           1
                 3 0.352 0.0679
                                      0.105 0.876
                                                    0.0309
                                                                      1
##
   4
           1
                 4 0.352 0.0970
                                      0.150 0.908
                                                     0.0125
                                                                      1
           2
##
    5
                 1 0.349 0.101
                                      0.155 0.932
                                                     0.237
                                                                      1
##
    6
           2
                 2 0.349 0.0166
                                      0.0256 0.814 -0.650
                                                                      1
           2
   7
                 3 0.349 0.264
                                      0.406
                                             1.21
                                                     0.681
                                                                      1
           2
##
    8
                 4 0.349 0.256
                                      0.393
                                             1.23
                                                     0.657
                                                                      1
##
           2
                 5 0.349 0.0135
                                      0.0208 0.813 -0.738
                                                                      1
## 10
           3
                                      0.536 1.34
                 1 0.549 0.242
                                                     0.0325
## # ... with 3 more variables: x_coinsurance <dbl>, x_deductible <dbl>,
       x_oopmax <dbl>
```

 $s_0$  is the outside share for each market,  $s_j$  is the share within market for a given plan,  $s_j$  given g is the within market share.

Now, we find the summary statistic by plan number:

	plan: $1 (N = 100)$	plan: $2 (N = 100)$	plan: $3 (N = 66)$	plan: $4 (N = 39)$	plan: $5 (N = 20)$	
price						
min	0.812888	0.814086	0.805460	0.813620	0.807153	
max	2.13393	2.47220	1.83560	1.29913	1.47126	
mean (sd)	$1.19 \pm 0.29$	$1.19 \pm 0.33$	$1.08 \pm 0.25$	$0.96 \pm 0.13$	$0.95 \pm 0.17$	
xsi						
min	-1.059690	-1.048210	-1.054930	-1.114970	-0.954659	
max	1.394570	1.413610	1.462110	0.708806	0.688833	
mean (sd)	$0.05 \pm 0.41$	$0.02 \pm 0.51$	$-0.02 \pm 0.52$	$-0.12 \pm 0.42$	$-0.13 \pm 0.47$	
x_coinsurance						
min	0.812888	0.814086	0.805460	0.813620	0.807153	
max	2.13393	2.47220	1.83560	1.29913	1.47126	
mean (sd)	$1.19 \pm 0.29$	$1.19 \pm 0.33$	$1.08 \pm 0.25$	$0.96 \pm 0.13$	$0.95 \pm 0.17$	
x_deductible						
min	0.812888	0.814086	0.805460	0.813620	0.807153	
max	2.13393	2.47220	1.83560	1.29913	1.47126	
mean (sd)	$1.19 \pm 0.29$	$1.19 \pm 0.33$	$1.08 \pm 0.25$	$0.96 \pm 0.13$	$0.95 \pm 0.17$	
x_oopmax						
min	0.812888	0.814086	0.805460	0.813620	0.807153	
max	2.13393	2.47220	1.83560	1.29913	1.47126	
mean (sd)	$1.19 \pm 0.29$	$1.19 \pm 0.33$	$1.08 \pm 0.25$	$0.96 \pm 0.13$	$0.95 \pm 0.17$	

# 2.2 Construct as instruments the within-group sum of every characteristic. Report summary statistics on your instruments, with the Stata "summarize" command or analog in the software that you use

First, we add a column to the table with the within-group sum of every characteristic (z1, z2, z3). However, following Berry (1994), we will also try with the within-group sum of the characteristics without the plan j. We call these three instruments (z11, z22, z33). Here, we report the summary statistics

```
data_with_instruments <- collapsed_data %>% group_by(market) %>%
  summarise(z1 = sum(x_coinsurance), z2 = sum(x_deductible), z3 = sum(x_oopmax)) %>%
  right_join(collapsed_data, by = "market") %>%
  select(market, plan:x_oopmax, z1:z3) %>%
  mutate(z11 = z1 - x_coinsurance, z22 = z2 - x_deductible, z33 = z3 - x_deductible)

data_with_instruments %>% select(z1, z2, z3, z11, z22, z33) %>% describe(skew = FALSE, quant=c(.25,.75))
```

	vars	n	mean	sd	min	max	range	se	Q0.25	Q0.75
z1	1	325	0.9462760	0.3608348	0.0686351	1.562735	1.494100	0.0200155	0.6664640	1.2334426
z2	2	325	0.9877420	0.4141706	0.2497498	1.935549	1.685799	0.0229741	0.6735020	1.2356470
z3	3	325	0.9178204	0.3912168	0.0908578	1.757930	1.667072	0.0217008	0.6338763	1.3016240
z11	4	325	0.6853273	0.3465371	0.0025128	1.507379	1.504866	0.0192224	0.4157900	0.9761845
z22	5	325	0.7164153	0.3895531	0.0037613	1.754211	1.750450	0.0216085	0.4177920	0.9933539
z33	6	325	0.6464937	0.4161860	-0.2394983	1.602361	1.841860	0.0230858	0.3584879	0.9571203

	T			
Summary Statistics	N = 325			
z1				
min	0.0686351			
median (IQR)	0.93 (0.67, 1.23)			
mean (sd)	$0.95 \pm 0.36$			
max	1.562735			
<b>z</b> 2				
min	0.2497498			
median (IQR)	$0.95 \ (0.67, 1.24)$			
mean (sd)	$0.99 \pm 0.41$			
max	1.935549			
<b>z</b> 3				
min	0.09085784			
median (IQR)	0.89 (0.63, 1.30)			
mean (sd)	$0.92 \pm 0.39$			
max	1.75793			
z11				
min	0.00251275			
median (IQR)	0.68 (0.42, 0.98)			
mean (sd)	$0.69 \pm 0.35$			
max	1.507379			
z22				
min	0.00376132			
median (IQR)	0.69 (0.42, 0.99)			
mean (sd)	$0.72 \pm 0.39$			
max	1.754211			
<b>z33</b>				
min	-0.2394983			
median (IQR)	0.64 (0.36, 0.96)			
mean (sd)	$0.65 \pm 0.42$			
max	1.602361			
	I .			

## 2.3 Estimate a nested logit model using Berry's method, not instrumenting for within-group share or price. Report your results.

Now, we estimate the nested logit model. The model is as follows:

## lm(formula = ln\_sj\_minus\_s0 ~ x\_coinsurance + x\_deductible +

x\_oopmax + price + ln\_sj\_g, data = transformed\_data)

##

##

## Residuals:

```
\ln(s_i) - \ln(s_0) = \beta_0 + \beta_1 x_{coinsurance} + \beta_2 x_{deductible} + \beta_3 x_{oopmax} - \alpha p_i + \sigma \ln(s_{i/q}) + \xi_i
```

```
Median
                 1Q
## -0.98191 -0.25049 0.02532 0.24990 0.81439
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
                -0.11916 0.17393 -0.685
                                            0.4938
## (Intercept)
                           0.14029 -1.888
## x coinsurance -0.26490
                                            0.0599 .
## x_deductible -0.20614
                           0.13369 - 1.542
                                            0.1241
## x_oopmax
                 0.20636
                           0.13156
                                    1.569
                                             0.1177
## price
                 0.10443
                           0.10094
                                    1.035
                                             0.3016
                                             <2e-16 ***
## ln_sj_g
                 0.80387
                           0.03125 25.727
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.3388 on 319 degrees of freedom
## Multiple R-squared: 0.8435, Adjusted R-squared: 0.8411
## F-statistic:
                 344 on 5 and 319 DF, p-value: < 2.2e-16
```

2.4 Estimate a nested logit model using Berry's method, instrumenting for within-group share but not price. Report your results.

```
##
## Call:
## ivreg(formula = ln_sj_minus_s0 ~ x_coinsurance + x_deductible +
##
      x_{oopmax} + price + ln_{sj_g} \mid . - ln_{sj_g} + z1 + z2 + z3,
##
      data = transformed_data)
##
## Residuals:
      Min
               1Q Median
                              3Q
                                    Max
## -3.0257 -0.2556 0.1309 0.4060 1.1356
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
               ## x_coinsurance -0.02080
                           0.25583 -0.081
                                            0.9352
## x_deductible -0.28211
                           0.23870 -1.182
                                            0.2381
                                   2.482
## x_oopmax
                0.62764
                           0.25283
                                            0.0136 *
## price
                2.11343
                           0.48744
                                   4.336 1.95e-05 ***
## ln_sj_g
               -0.01853
                           0.19364 -0.096
                                            0.9238
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.6033 on 319 degrees of freedom
## Multiple R-Squared: 0.5038, Adjusted R-squared: 0.496
## Wald test: 66.71 on 5 and 319 DF, p-value: < 2.2e-16
```

2.5 Estimate a nested logit model using Berry's method, instrumenting for within-group share and price. Report your results. Does it appear that price was endogenous? How are you making this judgment?

```
reg3 <- ivreg(data = transformed data,
      formula = ln_sj_minus_s0 ~ x_coinsurance + x_deductible + x_oopmax + price + ln_sj_g | . - price
summary(reg3)
##
## Call:
## ivreg(formula = ln_sj_minus_s0 ~ x_coinsurance + x_deductible +
       x_{oopmax} + price + ln_sj_g \mid . - price - ln_sj_g + z1 + z2 +
##
       z3, data = transformed_data)
##
## Residuals:
##
       Min
                  1Q
                      Median
                                    30
  -1.11665 -0.35187 -0.08585 0.26870
                                       2.65404
##
## Coefficients:
##
                Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                 2.54694
                          1.83910
                                      1.385 0.16706
## x_coinsurance -0.95821
                            0.34676 -2.763 0.00605 **
## x_deductible -0.49901
                            0.23739
                                     -2.102
                                             0.03633 *
## x_oopmax
                 0.06652
                            0.28436
                                       0.234
                                              0.81518
## price
                -1.83602
                            1.12769
                                     -1.628
                                            0.10449
## ln_sj_g
                 0.93102
                            0.30934
                                       3.010 0.00282 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5829 on 319 degrees of freedom
## Multiple R-Squared: 0.5368, Adjusted R-squared: 0.5295
## Wald test: 12.43 on 5 and 319 DF, p-value: 4.953e-11
```

We observe that when we don't use instruments for price nor withing group share, the price coefficient is positive (0.1044329) which would indicate that an increase in price increases the market share of the plan. Controlling for within group share does not disappear this effect since the price coefficient for the second regression is 2.1134273. However, controlling for price does make the price coefficient negative, which intuitively makes sense since from the model we are quite sure that price is correlated with  $\xi_i$ .

In addition, using as instruments for each plan k the within sum characteristic for values different than k  $(z_{11} = \sum_{i \neq k} x_i)$ , provides the same estimates:

```
z22 + z33, data = transformed_data)
##
##
## Residuals:
##
       Min
                  1Q
                       Median
                                    30
                                             Max
##
  -1.11665 -0.35187 -0.08585
                               0.26870
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  2.54694
                             1.83910
                                       1.385
                                              0.16706
## x_coinsurance -0.95821
                             0.34676
                                      -2.763
                                              0.00605 **
## x_deductible
                -0.49901
                             0.23739
                                      -2.102
                                              0.03633 *
## x_oopmax
                  0.06652
                             0.28436
                                       0.234
                                              0.81518
## price
                 -1.83602
                             1.12769
                                      -1.628
                                              0.10449
## ln_sj_g
                  0.93102
                             0.30934
                                       3.010
                                              0.00282 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 0.5829 on 319 degrees of freedom
## Multiple R-Squared: 0.5368, Adjusted R-squared: 0.5295
## Wald test: 12.43 on 5 and 319 DF, p-value: 4.953e-11
```

#### transformed\_data

```
## # A tibble: 325 x 19
                             s_j s_j_given_g price
                                                         xsi x_constant
##
      market plan
                      s_0
##
                                        <dbl> <dbl>
                                                                  <dbl>
       <int> <int> <dbl>
                           <dbl>
                                                      <dbl>
##
   1
           1
                  1 0.352 0.183
                                       0.283 1.09
                                                      0.631
                                                                      1
##
           1
                  2 0.352 0.300
                                       0.463 1.32
                                                      0.921
                                                                       1
##
    3
           1
                 3 0.352 0.0679
                                       0.105 0.876
                                                     0.0309
                                                                       1
    4
##
           1
                  4 0.352 0.0970
                                       0.150 0.908
                                                     0.0125
                                                                       1
##
    5
           2
                 1 0.349 0.101
                                       0.155 0.932
                                                     0.237
                                                                       1
           2
##
    6
                 2 0.349 0.0166
                                       0.0256 \ 0.814 \ -0.650
                                                                       1
##
    7
           2
                                       0.406 1.21
                 3 0.349 0.264
                                                      0.681
                                                                       1
##
    8
           2
                  4 0.349 0.256
                                       0.393 1.23
                                                      0.657
                                                                       1
##
    9
           2
                  5 0.349 0.0135
                                       0.0208 0.813 -0.738
                                                                       1
##
   10
           3
                  1 0.549 0.242
                                       0.536 1.34
                                                      0.0325
##
   # ... with 315 more rows, and 11 more variables: x_coinsurance <dbl>,
       x_deductible <dbl>, x_oopmax <dbl>, z1 <dbl>, z2 <dbl>, z3 <dbl>,
## #
       z11 <dbl>, z22 <dbl>, z33 <dbl>, ln_sj_minus_s0 <dbl>, ln_sj_g <dbl>
```

- 3 Conceptual questions on applications of discrete choice models to antitrust (20 points)
- 3.1 How did Prof. Nevo argue that the nested logit model was a useful demand model, in the Aetna/Humana merger case? (Please read the judge's decision in this case that is on the syllabus.)

Prof. Nevo used the CMS data on Medicare Advantage plan enrollments, that also included seniors who chose Original Medicare Options. The nested logit was useful in this context because it allows us to test whether, an to what degree, a senior might prefer "a Medicare Advantage plan because it is a Medicare Advantage plan" (United States District Court for the District of Columbia (2017)). The key parameter in the model

is the nesting parameter, that indicates the strength of this preference and it can have values between 0 and 1.

Nevo found that 70% of users of one of the Medicare Advantage plans would change to another Medicare Advantage plan (nesting parameter of 0.65). Nevo considered this to be an conservative estimated since the data showed that around 80% of seniors change a Medicare Advantage Plan of another Medicare Advantage Plan. Using this model, we was able to prove that an hypothetical profit-maximizing monopolist could profitably increase prices in any county.

One turning point for the judge to accept Nevo's econometric evidence was that he used the defendant nesting parameters (that were much lower that his) and the lowest parameter he could find the literature, and still found that the Medicare Advantage passed the SSNIP test of 5% or 10%, that is, an hypothetical monopolist in that market could profitably increase prices in more than 5%.

3.2 How would you would perform a hypothetical monopolist test for your estimated model of insurance demand? Explain with words and equations.

#### References

Berry, Steven T. 1994. "Estimating Discrete-Choice Models of Product Differentiation." *The RAND Journal of Economics*. JSTOR, 242–62.

Miller, Nathan H, and Matthew C Weinberg. 2017. "Understanding the Price Effects of the Millercoors Joint Venture." *Econometrica* 85 (6). Wiley Online Library: 1763–91.

United States District Court for the District of Columbia. 2017. "United States et al. v. AETNA INC et al." https://www.justice.gov/opa/press-release/file/930361/download.