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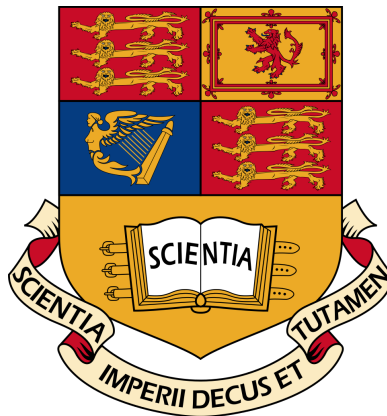
INDIVIDUAL PROJECT REPORT

DEPARTMENT OF COMPUTING

Business Management Processes: Verifying their Compliance with Security and Business Rules

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Abstract

TODO

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Chapter 1

Introduction

Chapter 2

Background

2.1 Workflows

Business management processes can be represented as a workflow of tasks, where each of these tasks produce a certain output for the next task to be realised. These tasks are assigned in the workflow as a sequence, where in order to perform the next task, the current task must be completed. However, in order to start a task, it must meet all the constraints within workflow. However, in a large business, making sure that all the constraints are met in a workflow can become a large problem as the more tasks are added to a workflow. Workflows are modeled as directed acyclic graphs [1], where there are no directed cycles. The vertices are tasks in the workflow and the directed edges connecting to each task vertex is the execution order.

An example of a business workflow is given in Figure 2.1a with nine tasks that need to be allocated:

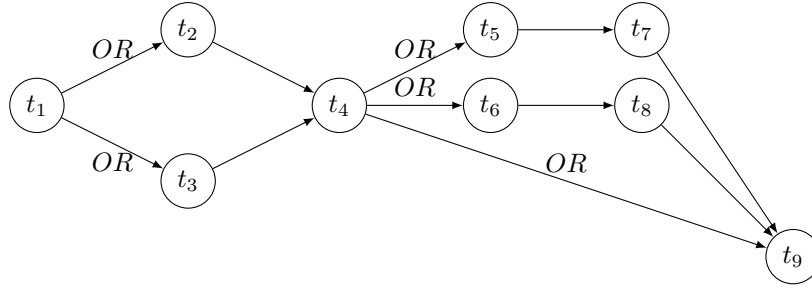
- A user in the business receives the order from a customer.
- They then pass it onto another user depending on the two possible sizes of the order and are given different prices accordingly.
- Someone then needs to approve and authorise the price for checkout.
- Then a discount may be provided depending on the current total cost of the order.
- Finally, the sale is approved and the new total is returned back to the customer.

However, the order of execution in Figure 2.1a is affected by how the graph is forked. These forks are represented as constraints or rules within a business which may prevent tasks being executed such as a government restriction on business logic. The fork at t_1 is an OR-fork showing that either t_2 or t_3 can be executed. Depending on whether t_2 or t_3 can be executed, determines whether t_4 can then be executed afterwards and affects the whole execution of the workflow.

2.2 Tasks

In business management processes, users have to be allocated tasks for an execution to occur. These tasks are represented as vertices in the graph as t_n . The tasks in the example workflow given in Figure 2.1a are listed in Table 2.1b.

If users cannot be allocated to these tasks, then there is no way in which the task can be executed. Therefore it is not executed and the workflow becomes unsatisfiable.



(a) Ordered business workflow with nine tasks

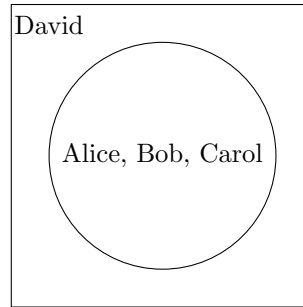
Task Number	Task
t_1	Receive order from customer
t_2	Give total of large sale
t_3	Give total of small sale
t_4	Approve and authorise checkout
t_5	Give 10% discount
t_6	Give 20% discount
t_7	Give new total of sale
t_8	Give new total of sale
t_9	Approve and return new total

(b) Table of tasks

Figure 2.1: Business management process workflow

2.3 Users

A user belongs to the set of users who can be allocated to tasks in order to execute them. However, there are possible allocation constraints which refrain particular users from executing these tasks. In the example given below, Alice, Bob and Carol are users specified in the domain of the workflow, but David is not.



2.4 Business and Security Rules

Business and security rules are used to prevent fraud and follow business compliance rules. For example, in some cases, different users are needed to execute a certain set of tasks to perhaps prevent fraud or erroneous activities in a workflow. In Figure 2.1 some constraints about which users in the business can execute these tasks are added below:

- Whomever is allocated task t_1 to receive the order from customers and pass them onto the relevant user, but cannot be allocated and execute t_2 and t_3 , but can be allocated other tasks within the workflow besides t_2 and t_3 .
- Whomever is allocated task t_2 to give a total of a large sale cannot be the same user that is allocated t_3 who gives a total of a small sale. Therefore whomever is allocated t_3 cannot be allocated to t_2 .

With the additional constraints to the workflow it may be satisfiable given that there are enough users. But there may be other constraints that can make this workflow unsatisfiable. For example, if there are not enough users to be allocated to ensure that some of the tasks do not have the same user. So a valid workflow is a satisfied workflow if there can be users allocated tasks in the workflow that do not break the constraints within the given model.

2.5 Satisfiability Modulo Theories (SMT)

Satisfiability Modulo Theories (SMT) [2] check the satisfiability of logical formulas over given theories. It helps to determine whether there is a solution in a formula which expresses a constraint. It is one of the fundamental problems in the area of computer science to check boolean satisfiability over logical domains and the completeness and incompleteness of logical theories and complexity theory.

SMT is similar to Boolean or Propositional Satisfiability Problem (SAT) [3], where the problem is to determine if there exists a determination that satisfies the boolean formula. But SAT ranges only over binary predicates which are predicated that only take in two arguments in their formula. Whereas SMT covers non-binary predicates with types and sorts. This project will focus on SMT rather than SAT as we can use non-binary predicates provided by SMT to define and solve some of these constraints.

2.6 Z3

Z3 [4] is a SMT solver developed by Microsoft Research. It is used to integrate several decision procedures and verify the satisfiability of logical formulas over given theories. The theories our case, is the workflow model. There are many features of Z3 which will come in useful including:

- Uninterpreted functions - where a theory has an empty set of sentences. An example of this can be an axiom, where the satisfiability of the axiom depends on whether the uninterpreted function can be evaluated to true.
- Linear arithmetic
- Bitvectors, arrays, datatypes
- Quantifiers
- Satisfiability core
- Returns a model

There were many other SMT solvers considered but did not include certain built in theories and features such as:

- Yices [5] - it has almost all features of Z3 but doesn't have quantifiers, which is needed to define general rules to satisfy a formula in the domain.
- CVC4 [6] - Similar features of Z3 including quantifiers not included in Yices. But typically with CVC4, it is not very scalable. It is intended to run with small finite models, but realistically, business processes can be huge within large organisations.
- MathSAT 5 [7] - It is lacking a lot of features in Z3, especially the quantifiers.

2.6.1 Basics

A simple example is illustrated in Figure 2.2 shows how some simple first order predicate logic in Figure 2.2a can be expressed in Z3 SMT solver in Figure 2.2b.

- To define constants in Z3, in this case x and y , we can declare them as constants using the keyword (`declare-const x Int`) where x is the name of the constant and the type of x is an Integer.

- Z3 uses assertions to add constraints to the solver as a keyword `assert`.
- `(check-sat)` (line 5) is a call to Z3 to check if the theory is satisfiable. It returns `sat` if the theory is satisfiable and `unsat` if the theory is unsatisfiable.
- `(get-model)` (line 6) is a call to Z3 to return an interpretation of the theory which makes all the formulas defined in the Z3 stack true. If the theory returns false, no model able to be retrieved.

In the example below, $x > 10$ is given as an assertion (`assert(> x 10)`) and $y \times 10 \geq x$ is given the assertion (`assert (>= (* y 10) x)`). When this is run in Z3, a result is returned. `(check-sat)` returns as `sat` which means that this theory is satisfiable.

What we can see also, is that Z3 gives back an appropriate model as a result that satisfies these constraints with $x = 11$ and $y = 2$. This is true as if we put $x = 11$ and $y = 2$ back into the constraints, $11 > 10$ and $20 \geq 11$.

$$\begin{aligned} x &> 10 \\ y \times 10 &\geq x \end{aligned}$$

(a) Simple predicate logic using logic symbols

```
1 (declare-const x Int)
2 (declare-const y Int)
3 (assert (> x 10))
4 (assert (>= (* y 10) x))
5 (check-sat)
6 (get-model)
```

(b) Simple predicate logic in Z3

```
sat
(model
  (define-fun y () Int
    2)
  (define-fun x () Int
    11)
)
```

(c) Z3 Result

Figure 2.2: Simple predicate logic

2.6.2 Functions

Z3 also has uninterpreted functions where unlike most programming languages where functions have side effects, may never return a value or raise or throw exceptions, Z3 functions have no side effects since they are in classical first order logic and are total. Everything in Z3 is a function, including constants as they don't take in arguments.

- `(declare-fun f (Int) Int)` - We declare a function f which takes in an integer as its parameter and returns an integer

In Figure 2.3, a function `f` has been declared which takes an integer as input, and returns an integer. Since this is an uninterpreted function, Z3 does not know what this function does. But we can add some constraints, so when we apply the function to the integer, it ensures that the interpretation is consistent within the theory and constraints.

In Figure 2.3b, there are two assertions (`assert (= (f x) x)`) which represents $f(x) = x$ and (`assert (> (f y) (f x))`) as $f(y) > f(x)$. The result that Z3 returns in Figure refZ3 Result with functions has still kept the values of `x` and `y` as it is the same as Figure 2.2. But for function f , it takes in an integer as we have specified in our function declaration as `(x!1 Int)` which means that the first variable has a

type `Int` (integer). It returns an integer which is consistent and the type integer is interpreted. Looking at the model returned in Figure 2.3c, we can see that `x` and `textttf` are both interpreted as a function as well as `textttf`. It interprets `f` to take in an integer, the `ite` stands for if-then-else. So we can read the definition of `f` as if `x!1` is equal to 20, then return 20, else if `x!1` is equal to 2, then return 2 else, return 21. Else, return 20. So for the case that `x` is put into the function `f`, then `x!1 = 20`, then the value of the function is 20, else if `y` is put into the function, then `x!1 = 2`, then the value of the function is 21. If any other input is put in, then it will return 20.

Z3 also includes built in arithmetic functions such as `=`, `-`, `+`, `×`, `div`, `mod`, `≥`, `≤`, `>`, `<`, `not` that support integer and real constants.

$$\begin{aligned} x &> 10 \\ y \times 10 &\geq x \\ f(x) &= x \\ f(y) &> f(x) \end{aligned}$$

(a) Predicate logic with functions

```
1 (declare-const x Int)
2 (declare-const y Int)
3 (assert (> x 10))
4 (assert (>= (* y 10) x))
5 (declare-fun f (Int) Int)
6 (assert (= (f x) x))
7 (assert (> (f y) (f x)))
8 (check-sat)
9 (get-model)
```

(b) Z3 with functions

```
sat
(model
  (define-fun y () Int
    2)
  (define-fun x () Int
    20)
  (define-fun f ((x!1 Int)) Int
    (ite (= x!1 20) 20
      (ite (= x!1 2) 21
        20)))
)
```

(c) Z3 Result with functions

Figure 2.3: Predicate Logic with Functions

2.6.3 Stack

Z3 has a stack implementation, where constraints and formulas can be pushed onto and popped off the stack using the commands `(push)` and `(pop)` which pushes and pops constraints off the stack respectively. These commands can be used to check the satisfiability of some rules or definitions. When the solver stack is pushed, the state of the solver is saved. When the stack is popped, any rules and assertions declared between that pop and the corresponding push on the stack is removed from the stack, and the interpretation is reverted back to its previous state before the push.

In Figure 2.5, the theory is satisfied before the push. However, when the stack is pushed and an assertion is added which violates the constraints already in the current frame which is $x < 2$, but $x > 2$ has been pushed onto the stack frame previously, the model becomes unsatisfied. Since the constraint $x < 2$ was

between a push-pop frame, it can be popped off the stack and the model is returned back to its previous state on the stack.

```

1 (declare-const x Int)
2 (declare-const y Int)
3 (declare-fun f (Int) Int)
4 (assert (> x 2))
5 (assert (< y 2))
6 (assert (= (f x) (f y)))
7 (check-sat)
8 (get-model)
9 (push)
10 (assert (< x 2))
11 (check-sat)
12 (pop)
13 (check-sat)
14 (get-model)

```

(a) Z3 with stack

```

sat
(model
  (define-fun y () Int
    0)
  (define-fun x () Int
    3)
  (define-fun f ((x!1 Int)) Int
    (ite (= x!1 3) 1
      (ite (= x!1 0) 1
        1)))
)
unsat
sat
(model
  (define-fun y () Int
    0)
  (define-fun x () Int
    3)
  (define-fun f ((x!1 Int)) Int
    (ite (= x!1 3) 1
      (ite (= x!1 0) 1
        1)))
)

```

(b) Z3 Result with stack

Figure 2.4: Predicate Logic with stack

2.6.4 Sorts

When a constant is defined, they are declared as a type which is a sort in Z3. For example, integers, reals and booleans are declared, they are a pre-defined sort in Z3.

- `(define-sort t1 Task)` - the command defines a new symbol with the type Task.

2.6.5 Quantifiers

One of the reasons why we chose Z3 as the back end constraint solver was because it is able to have quantifiable logic such as the universal quantifier which is interpreted as “for all” \forall . The universal quantifier asserts that all predicates within the scope of the quantifier must be true of every value of the predicate. In Z3, they are represented as:

- `(assert (forall ((x Int)) (x > 0)))` which in first order predicate logic is $\forall x : (x > 0)$. So for all integers, they must be greater than zero.

2.6.6 Satisfiability and Validity

Validity

A formula f is valid if f always evaluates to true for any assignment to an appropriate value.

Satisfiability

A formula f is satisfiable if there is some assignment to an appropriate value to the function where f evaluates to true.

As we mentioned previously, Z3 SMT Solver gives back the satisfiability of the interpretation. It has three states when the `(check-sat)` command is called:

- **sat** - satisfied model, a model can be returned. We give an example of a satisfied formula in Figure 2.5a.
- **unsat** - unsatisfied model - a model cannot be returned. We give an example of an unsatisfied formula in Figure 2.5b.
- **unknown** - when Z3 does not know whether a formula is satisfiable or not. We give an example of an unknown result in Figure 2.5c.

What is good about whether a formula is satisfiable is that it is about finding a solution under a set of constraints.

```
1 (declare-const x Int)
2 (assert (> x 10))
3 (assert (< x 100))
4 (check-sat)
5 (get-model)
```

(a) Z3 with satisfied core

```
1 (declare-const a Int)
2 (assert (> a 10))
3 (assert (< a 10))
4 (check-sat)
5 (get-model)
```

(b) Z3 with unsatisfied core

```
1 (declare-const a Int)
2 (assert (> a 10))
3 (assert (< a 10))
4 (check-sat)
5 (get-model)
```

(c) Z3 with unknown

Figure 2.5: Predicate Logic with stack

Chapter 3

Theory of Business Rules

3.1 Business Management Workflows

There are many rules and restrictions within business management workflows in order to prevent fraud, and a matter of authorisation and following regulation. Each rule is different, and therefore will have different axioms that follow. We will talk about the rules that have been implemented in the application.

3.2 Tasks and Users

Firstly, tasks and users need to be defined in the application in order to define the basic workflow domain. These are defined in Z3 as sorts where they define the types task and user respectively:

- `(declare-sort Task)`
- `(declare-sort User)`

Then each task and user in the domain are able to be defined after the sort has been defined:

```
1 (declare-sort Task)
2 (declare-sort User)
3 (declare-const alice User)
4 (declare-const bob User)
5 (declare-const price_large_order Task)
6 (declare-const price_small_order Task)
```

We have now declared a user called “alice” and another user “bob” in the user domain, as well as defining two tasks in the task domain “receive_large_order” and “recieve_small_order”.

3.3 User Allocation

The most basic constraint in a workflow is that the tasks can only be executed if they have been allocated a user. Obviously, if there was not a user in the domain able to be allocated to a task, no one is able to execute and complete the task for the workflow to progress.

In Z3, we define user allocation as a function, which takes in a task, and returns a user:

- `(declare-fun alloc_user (Task) User)`

3.4 Separation of Duty

Separation of duties [8] is where users need to be different in order to complete a set of tasks. This is implemented usually implemented in order to avoid conflicts of interests that may cause fraud by an

individual or break some rules within a business. This restricts and reduces powers of individuals within a business where there could be a chance of collusion happening.

This is where a user who is allocated a task t , must also be a different user to who is allocated task t if these tasks are bound as knowledge from task t must not be used in order to execute task t . It may be that separation of duties cannot use their knowledge to participate in certain tasks.

This is easy to spot within a workflow diagram giving in Figure 3.2. We give a scenario that there are three users in the domain: Alice, Bob and Carol. The separation of duties are as follows: the user who is allocated the task of receiving the order and authorising the payment at checkout and cannot not handle any form of pricing the order. Whereas whichever user handles pricing of large orders cannot be the same user that handles pricing of small orders. The same users are not authorised to be allocated the tasks of creating and authorising orders, otherwise they could create fake orders or authorise orders with incorrect prices which may benefit themselves. It is also the case that large orders and small order prices should not be affected by each other, otherwise they could affect the final price or cause some sort of price fixing.

The main rules we will focus on Figure 3.1a is between lines 14-18. As seen, we must give a rule that whichever user is allocated a certain task cannot be the same (not equal) as which ever user is allocated the other task which is defined in the separation of duty. The resulting model in Figure 3.1b shows that this is in fact satisfiable under the given separation of duty constraints and the model is consistent with the description. The allocation is as follows:

- Task `price_large_order` is allocated to user Alice.
- Task `price_small_order` is allocated to user Bob.
- Tasks `receive_order` and `checkout` are both allocated to user Carol

```

1 (declare-sort Task)
2 (declare-sort User)
3
4 (declare-fun alloc_user (Task) User)
5
6 (declare-const alice User)
7 (declare-const bob User)
8 (declare-const carol User)
9 (declare-const receive_order Task)
10 (declare-const price_large_order Task)
11 (declare-const price_small_order Task)
12 (declare-const checkout Task)
13
14 (assert (not (= (alloc_user price_large_order) (alloc_user
    price_small_order))))
15 (assert (not (= (alloc_user price_large_order) (alloc_user checkout))))
16 (assert (not (= (alloc_user checkout) (alloc_user price_small_order))))
17 (assert (not (= (alloc_user price_large_order) (alloc_user
    receive_order))))
18 (assert (not (= (alloc_user receive_order) (alloc_user
    price_small_order))))
19
20 (assert (forall ((u User)) (or(= u alice)(= u bob)(= u carol))))
21
22 (check-sat)
23 (get-model)

```

(a) Z3 Separation of Duty

```

sat
(model
  ;; universe for Task:
  ;;   Task!val!2 Task!val!3 Task!val!0 Task!val!1
  ;;   _____
  ;; definitions for universe elements:
  (declare-fun Task!val!2 () Task)
  (declare-fun Task!val!3 () Task)
  (declare-fun Task!val!0 () Task)
  (declare-fun Task!val!1 () Task)
  ;; universe for User:
  ;;   User!val!2 User!val!0 User!val!1
  ;;   _____
  ;; definitions for universe elements:
  (declare-fun User!val!2 () User)
  (declare-fun User!val!0 () User)
  (declare-fun User!val!1 () User)
  ;; cardinality constraint:
  (forall ((x User)) (or (= x User!val!2) (= x User!val!0) (= x User!val!1)))
  ;; _____
  (define-fun price_small_order () Task
    Task!val!1)
  (define-fun checkout () Task
    Task!val!2)
  (define-fun receive_order () Task
    Task!val!3)
  (define-fun bob () User
    User!val!1)
  (define-fun carol () User
    User!val!2)
  (define-fun price_large_order () Task
    Task!val!0)
  (define-fun alice () User
    User!val!0)
  (define-fun alloc_user ((x!1 Task)) User
    (ite (= x!1 Task!val!0) User!val!0
      (ite (= x!1 Task!val!1) User!val!1
        (ite (= x!1 Task!val!2) User!val!2))))
)

```

(b) Z3 result for separation of duty

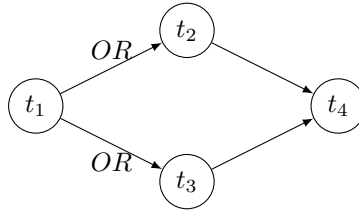


Figure 3.2: Part of the example workflow

3.5 Binding of Duty

Binding of duties [9] is where a user who is allocated a task t , must also be the same user who is allocated task t if these tasks are bound as knowledge from task t must be used in order to execute task t . It may be that binding of duties is needed as the user who is allocated these tasks have the required knowledge in order to execute both.

Given Figure 3.2, who ever is allocated the task of receiving an order has to price the order, regardless of whether it is a large or small order as they may be authorised to do so.

As seen in Figure 3.3a, the rule is specified between lines 14-17. Whichever user is allocated task `price_large_order` has to be the same (equal to) whichever user is allocated task `price_small_order`. This matches the definition of binding of duties.

Looking at the result produced in Figure 3.4b, this is satisfiable for the given constraints and is consistent to the user input and is complete:

- Task checkout is allocated to user Alice
- All other tasks (`receive_order`, `price_large_order`, `price_small_order`) are all allocated to user Carol. Which matches the users need for binding of duties.

```
1 (declare-sort Task)
2 (declare-sort User)
3
4 (declare-fun alloc_user (Task) User)
5
6 (declare-const alice User)
7 (declare-const bob User)
8 (declare-const carol User)
9 (declare-const receive_order Task)
10 (declare-const price_large_order Task)
11 (declare-const price_small_order Task)
12 (declare-const checkout Task)
13
14 (assert (not (= (alloc_user price_large_order) (alloc_user checkout))))
15 (assert (not (= (alloc_user checkout) (alloc_user price_small_order))))
16 (assert (= (alloc_user price_large_order) (alloc_user receive_order)))
17 (assert (= (alloc_user receive_order) (alloc_user price_small_order)))
18
19 (assert (forall ((u User)) (or(= u alice)(= u bob)(= u carol))))
20
21 (check-sat)
22 (get-model)
```

(a) Z3 Binding of Duty


```

sat
(model
  ;; universe for Task:
  ;;   Task!val!2 Task!val!3 Task!val!0 Task!val!1
  ;;   -----
  ;; definitions for universe elements:
  (declare-fun Task!val!2 () Task)
  (declare-fun Task!val!3 () Task)
  (declare-fun Task!val!0 () Task)
  (declare-fun Task!val!1 () Task)
  ;; cardinality constraint:
  (forall ((x Task))
    (or (= x Task!val!2)
        (= x Task!val!3)
        (= x Task!val!0)
        (= x Task!val!1)))

  ;;   -----
  ;; universe for User:
  ;;   User!val!0 User!val!1
  ;;   -----
  ;; definitions for universe elements:
  (declare-fun User!val!0 () User)
  (declare-fun User!val!1 () User)
  ;; cardinality constraint:
  (forall ((x User)) (or (= x User!val!0) (= x User!val!1)))

  ;;   -----
  (define-fun price_small_order () Task
    Task!val!2)
  (define-fun checkout () Task
    Task!val!1)
  (define-fun receive_order () Task
    Task!val!3)
  (define-fun carol () User
    User!val!1)
  (define-fun bob () User
    User!val!0)
  (define-fun price_large_order () Task
    Task!val!0)
  (define-fun alice () User
    User!val!0)
  (define-fun alloc_user ((x!1 Task)) User
    (ite (= x!1 Task!val!1) User!val!0
          User!val!1))
)

```

(b) Z3 result for binding of duty

3.6 Seniority

In most businesses and corporations, there are different levels of seniority based on their positions in the company. Different seniority levels allow users to execute different tasks. For example, a confidential task maybe worked on by a less senior member of a department, but have to be authorised by a more senior member as they may have more experience or the appropriate training.

An example of seniority allocation is given in Figure 3.5. As we can see, whoever is allocated $t1$ must be

the same user as whoever is allocated to task t_4 as they will have the same level of seniority, the same user will have the same seniority. It does not make sense from a business perspective that the allocation needs to be different users of the same seniority as the trust and experience levels are the same. Also in the figure, whoever is assigned to t_1 has to be more senior than whoever is assigned to t_2 and t_3 . This also means that the users assigned to t_2 and t_3 have to be less senior than the user allocated to t_1 . The tasks t_2 and t_3 cannot have users of the same seniority, so therefore the users allocated to those tasks must not be the same.

We can declare a new function for seniority which takes two users as parameters and returns a boolean whether the users are senior to each other:

```
(declare-fun seniority (User User) Bool)
```

Given the example below, u is senior to u' .

```
(assert (seniority (u u')))
```

The different types of seniority explained above are:

- t has to be allocated a user that is more senior than the user allocated for t' ($t > t'$): `(assert (seniority (alloc_user t) (alloc_user t')))`
- t has to be allocated a user that is less senior than the user allocated for t' ($t < t'$): `(assert (seniority (alloc_user t') (alloc_user t)))`
- t has to be allocated a user that is the same seniority as t ($t = t'$): `(assert (= (alloc_user t) (alloc_user t')))`
- t has to be allocated a user that is not the same seniority as t' ($t \neq t'$): `(assert (not (= (alloc_user t) (alloc_user t'))))`

We give a scenario in Figure 3.4a where whoever is allocated `receive_order` has to be less senior than whoever is allocated `checkout` task. Also, `price_large_order` and `price_small_order` have to have the same seniority as each other as they are both tasks that can be executed with the same skill. However, whoever is allocated `receive_order` must also be less senior than the pricing tasks. This can be expressed in Z3 as in lines 22-26:

```

1 (declare-sort Task)
2 (declare-sort User)
3
4 (declare-fun seniority (User User) Bool)
5
6 (declare-fun alloc_user (Task) User)
7 (declare-fun duration (Task) Real)
8
9 (assert (forall ((u User))(not (seniority u u))))
10
11 (declare-const carol User)
12 (declare-const bob User)
13 (declare-const alice User)
14 (declare-const checkout Task)
15 (declare-const price_small_order Task)
16 (declare-const price_large_order Task)
17 (declare-const receive_order Task)
18
19 (assert (seniority bob carol))
20 (assert (seniority alice bob))
21 (assert (seniority alice carol))
22 (assert (seniority (alloc_user checkout) (alloc_user receive_order)))
23 (assert (seniority (alloc_user price_small_order) (alloc_user
    receive_order)))
24 (assert (seniority (alloc_user price_large_order) (alloc_user
    receive_order)))
25 (assert (seniority (alloc_user checkout) (alloc_user receive_order)))
26 (assert (forall ((u User)) (or(= u carol)(= u bob)(= u alice))))
27
28 (check-sat)
29 (get-model)

```

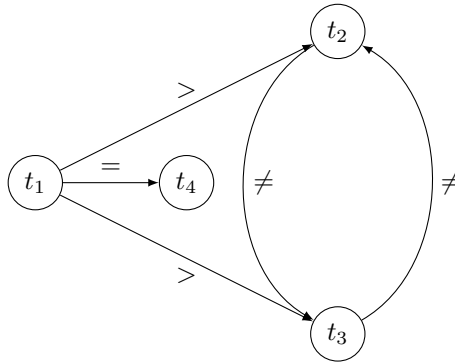
(a) Z3 Seniority

```

sat
(model
;; universe for User:
;;   User!val!2 User!val!1 User!val!0
;;
;; definitions for universe elements:
(declare-fun User!val!2 () User)
(declare-fun User!val!1 () User)
(declare-fun User!val!0 () User)
;; cardinality constraint:
(forall ((x User)) (or (= x User!val!2) (= x User!val!1) (= x User!val!0)))
;;
;; universe for Task:
;;   Task!val!0 Task!val!1 Task!val!2 Task!val!3
;;
;; definitions for universe elements:
(declare-fun Task!val!0 () Task)
(declare-fun Task!val!1 () Task)
(declare-fun Task!val!2 () Task)
(declare-fun Task!val!3 () Task)
;; cardinality constraint:
(forall ((x Task))
(or (= x Task!val!0)
(= x Task!val!1)
(= x Task!val!2)
(= x Task!val!3)))
;;
(define-fun receive_order () Task
Task!val!1)
(define-fun checkout () Task
Task!val!0)
(define-fun carol () User
User!val!1)
(define-fun bob () User
User!val!0)
(define-fun price_small_order () Task
Task!val!2)
(define-fun price_large_order () Task
Task!val!3)
(define-fun alice () User
User!val!2)
(define-fun seniority!16 ((x!1 User) (x!2 User)) Bool
(ite (and (= x!1 User!val!1) (= x!2 User!val!1)) false
(ite (and (= x!1 User!val!0) (= x!2 User!val!0)) false
(ite (and (= x!1 User!val!2) (= x!2 User!val!2)) false
true))))
(define-fun k!14 ((x!1 User)) User
(ite (= x!1 User!val!1) User!val!1
(ite (= x!1 User!val!0) User!val!0
User!val!2)))
(define-fun seniority ((x!1 User) (x!2 User)) Bool
(seniority!16 (k!14 x!1) (k!14 x!2)))
(define-fun alloc_user ((x!1 Task)) User
(ite (= x!1 Task!val!0) User!val!0
(ite (= x!1 Task!val!1) User!val!1
User!val!2)))
)

```

(b) Z3 result for binding of duty



Symbol	Seniority
=	Users can be allocated this task with the same rank
≠	Different ranked users
>	$t_x > t_y$ User who takes on t_x is more senior than t_y
<	$t_x < t_y$ User who takes on t_x is less senior than t_y

Figure 3.5: Seniority Relationships with tasks

3.7 Worst Time Completion

In business, it is useful to find the worst time completion in a workflow as some task executions are not helping to optimise the total workflow duration. The aim is to then find the worst time to completion after setting rules and constraints. Users usually have finite time to execute a task and in business, there are deadline to be met. This can be established if tasks have an estimate worst time duration, the longest time it could take to execute this task. We will define a function for the duration of a task and each task will have a duration listed:

- `(declare-fun duration (Task) Real)`
- `(assert (= (duration t) 60))`

Task `t` has a worst time duration of sixty minutes to execute. Since in Z3, they do not have a time unit, the user can decide what the real value can be, i.e. minutes, hours.

3.8 Temporal Order of Task Execution

Temporal order of task execution is when tasks need to be executed in a certain order. We can easily represent this in the workflow as a directed graph, where the edges are directed to tasks (vertices) which is to be executed next. This rule is important to model in business management processes because some tasks cannot be executed before another and some tasks may be dependant on another to be executed. In Figure 3.2, it has directional arrows between vertices to represent the temporal order of task execution. For example, we cannot price orders if we have not received orders. Similarly, we cannot proceed to checkout if no pricing has been handled on the orders. We can model temporal order of task execution in Z3 where task `t` is executed before `t'` as:

- `(declare-fun before (Task Task) Bool)`
- `(assert (before t t'))`

3.9 Task Execution (and, or, exclusive-or)

Another constraint we are going to explore is which tasks are actually executed. In some workflows some tasks are not necessarily needed to be executed. Given in Figure 3.2 we can create a fork at task `receive_order` and determine which pricing task is next to be executed. We can have three different types of forking:

- And - All tasks in the forking have to be executed, we cannot choose which tasks to execute.
- Or - One or more tasks in the forking have to be executed, we cannot choose to execute none.
- Exclusive or - One and only one tasks can be executed.

3.10 Authorised User Allocation

In a business process, we can choose the authorise particular users to execute a task explicitly. This is similar to RBAC [10] where a system restricts access to authorised users in a domain. Authorisation is usually assigned to them by their roles. We have not implemented roles in the set of workflow constraints, but rather just users who are only allowed by input. If there are more than one users authorised to execute a task, then we can use Z3 to choose which user to execute the task:

- `(assert (or (= (alloc_user receive_order) alice) (= (alloc_user receive_order) bob)))`

So either users Alice or Bob can be allocated the task of receiving the order to be executed and only them.

Chapter 4

Implementation

Chapter 5

Evaluation

Chapter 6

Conclusion

Chapter 7

Appendix A: How to Use

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