

# 1D Finite Element Analysis

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# Shortcoming of the classical (variational) Ritz method

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- Difficult to construct approximation functions
  - Especially in  $> 1$  dimension
  - No systematic way of choosing them

$$u \approx u_h = \sum_{j=1}^m c_j \phi_j \quad ???$$

# Finite Element Method overcomes this shortcoming

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- By...

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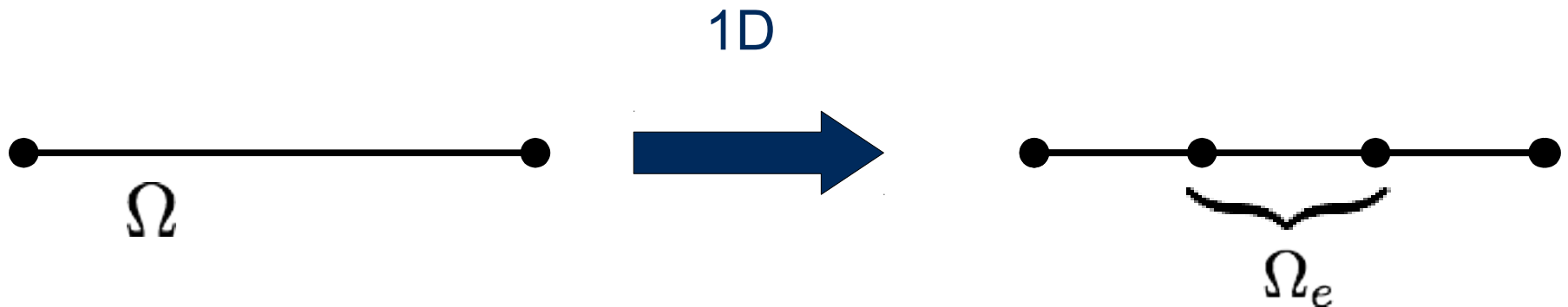
- By...

Return to day 1

# The Finite Element Method (FEM) in a nutshell

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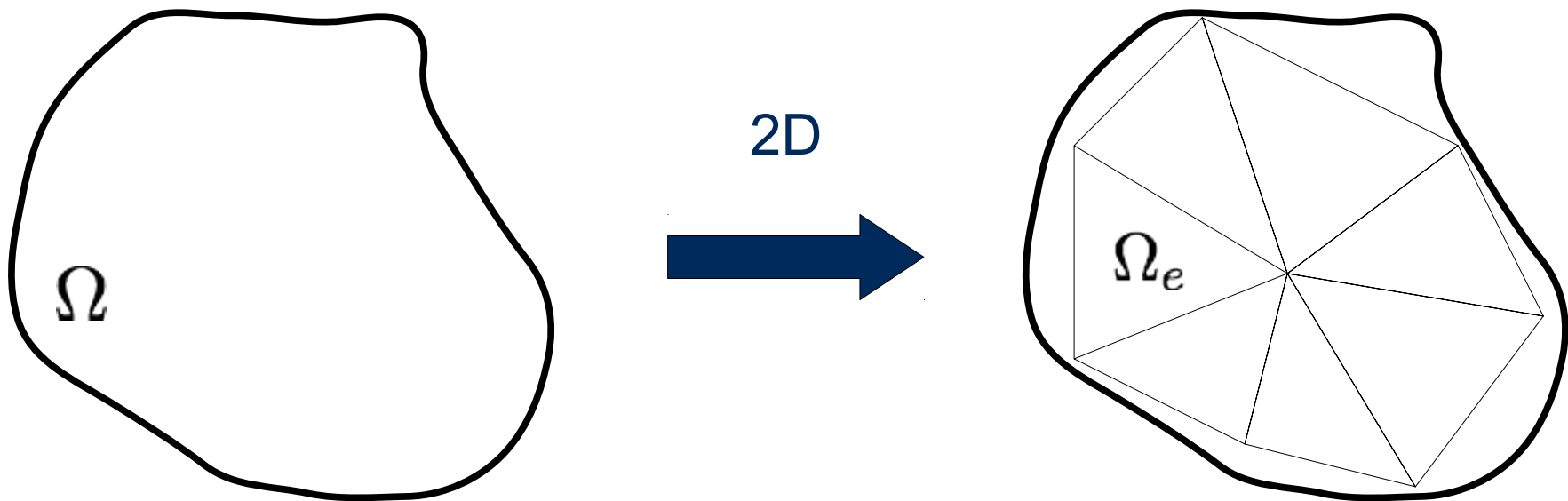
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  - The collection of finite elements is called the *finite element mesh*.



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- Over each finite element, the physical process is approximated by functions (polynomials or otherwise) and algebraic equations relating physical quantities at selective points, called **nodes**, are developed.

$$u \approx u_h = \sum_{j=1}^n u_j \psi_j$$

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  - The collection of finite elements is called the *finite element mesh*.
- Over each finite element, the physical process is approximated by functions (polynomials or otherwise) and algebraic equations relating physical quantities at selective points, called **nodes**, are developed.
- The element equations are *assembled* using continuity and/or “balance” of physical quantities and solved.



# Determining the interpolation (shape) functions

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- The approximate solution should be:
  - Continuous over the element and differentiable (required by weak form).
  - Complete.
  - Should be an interpolant of the nodal variables of interest.

# Determining the interpolation (shape) functions (cont.)

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- The interpolation (shape) functions are denoted by:

$$\psi_j \quad \text{or} \quad N_j$$

- For weak form derivation of element equations the interpolation functions must satisfy the essential boundary conditions (for admissibility).