



## Final Exam; Semester Review;

Computer Science 111  
Boston University  
Vahid Azadeh-Ranjbar, Ph.D.

### CS111 Final Exam

- Final exam: **Thursday, 12/19, 9:00 - 11:00 a.m.**
  - see the final-exam info sheet online
  - students with conflicts have been emailed the alternate exam info
- Bring:
  - A small index card that you obtain from us
  - your BU ID

## CS111 Final Exam

- Exam format:
  - Part I: multiple-choice

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- Exam format:
  - Part I: multiple-choice
  - Part II: several multi-part problems
    - some choice (3 out of 4, 4 out of 5, etc.)

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    - parts of this may require a bit more work

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  - Part III: multi-part problem that you must complete
    - parts of this may require a bit more work
- See website for more info, practice problems.

## CS111 Final Exam

### Part I:

- Tracing functions
- finding the outputs of a program
- Indexing, slicing, skip-slicing
- Mutable and immutable data
- 2D lists
- List comprehension
- Classes, objects & methods
- Dictionary
- Finite State Machine
- Circuits
- HMMM
- Efficiency and classifying algorithms

## CS111 Final Exam

### Part II and III:

- Object oriented programming
- Making functions:
  - ✓ Using loops
  - ✓ Using Recursion
  - ✓ Using List comprehensions
  - ✓ Using helper functions
  - ✓ Using any method
- Circuits
- Assembly (HMMM)
- Finite State Machine

## Extra Office Hours

I will hold extra office hours to help you for final exam:

- Thursday 12/12 at 3 – 5 PM
- Friday 12/13 at 3 – 5 PM
- Tuesday 12/17 at 2 – 4 PM

If you need to meet me out of office hours, please let me know by email ([vranjbar@bu.edu](mailto:vranjbar@bu.edu))

TFs and instructors will have office hours during study period.

## Some Review Problems

Tracing functions; mutable and immutable data

**What is printed by the following program?**

```
def mystery(a, b, c, i):
    if i < 2:
        a[i] += 2
    else:
        a = [1, 3]

a = [4, 6]
b = a[:]
c = b

mystery(c, a, b, 2)

print(a, b, c)
```

A. [4,6] [4,6] [4,6]  
B. [1,3] [4,6] [4,6]  
C. [4,6] [1,3] [4,6]  
D. [1,3] [1,3] [1,3]  
E. none of these

Tracing functions; mutable and immutable data

**What is printed by the following program?**

```
def mystery(a, b, c, i):
    if i < 2:
        a[i] += 2
    else:
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a = [4, 6]
b = a[:]
c = b

mystery(c, a, b, 2)

print(a, b, c)
```

A. [4,6] [4,6] [4,6]  
B. [1,3] [4,6] [4,6]  
C. [4,6] [1,3] [4,6]  
D. [1,3] [1,3] [1,3]  
E. none of these

## Tracing functions; mutable and immutable data

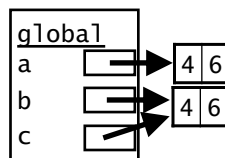
### What is printed by the following program?

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print(a, b, c)
```

before **mystery**

during **mystery**

after **mystery**



## Tracing functions; mutable and immutable data

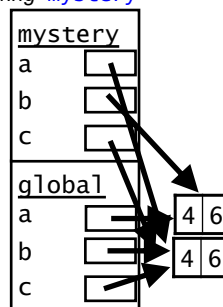
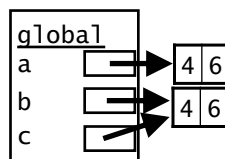
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before **mystery**

during **mystery**

after **mystery**

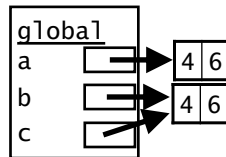


## Tracing functions; mutable and immutable data

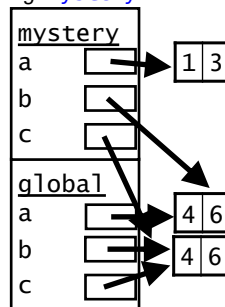
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mystery(c, a, b, 2)  
print(a, b, c)
```

before *mystery*



during *mystery*



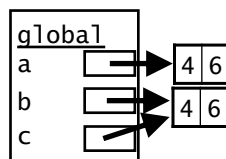
after *mystery*

## Tracing functions; mutable and immutable data

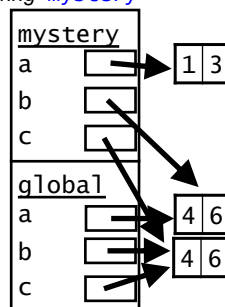
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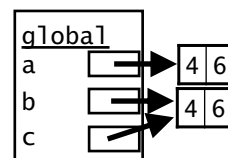
before *mystery*



during *mystery*



after *mystery*





### Dictionary What Is the Output?

```
d = {5: 18, 7: 12, 9: 21}
```

```
count = 0
for x in d:
    if x > 15:
        count = d[x]

print(count)
```

---

- A. 18
- B. 9
- C. 21
- D. 0
- E. none of these

### Dictionary What Is the Output?

```
d = {5: 18, 7: 12, 9: 21}
```

```
count = 0
for x in d: # x gets one key at a time!
    if x > 15:
        count = d[x]

print(count)
```

---

- A. 18
- B. 9
- C. 21
- D. 0
- E. none of these

### Dictionary What Is the Output?

```
d = {5: 18, 7: 12, 9: 21}

count = 0
for x in d: # x equals 5 then 7 then 9
    if x > 15:
        count = d[x]

print(count)
```

---

- A. 18
- B. 9
- C. 21
- D. 0
- E. none of these

### Dictionary What Is the Output?

```
d = {5: 18, 7: 12, 9: 21}

count = 0
for x in d: # 5, 7 and 9 are less than 15
    if x > 15:
        count = d[x]

print(count) # initial value of count = 0 will be printed.
```

---

- A. 18
- B. 9
- C. 21
- D. 0
- E. none of these

What is the output of this program?

```
from rectangle import *  
r1 = Rectangle(20, 30)  
r2 = Rectangle(25, 20)  
r3 = r2  
r2 = r1  
r1 = r3  
  
print(r1.width, r2.width, r3.width)
```

Rectangle

width	<input type="text"/>
height	<input type="text"/>

- A. 20 20 20
- B. 25 25 25
- C. 25 20 25
- D. 20 25 20
- E. 25 25 20
- F. none of these

What is the output of this program?

```
from rectangle import *  
r1 = Rectangle(20, 30)  
r2 = Rectangle(25, 20)  
r3 = r2  
r2 = r1  
r1 = r3  
  
print(r1.width, r2.width, r3.width)
```

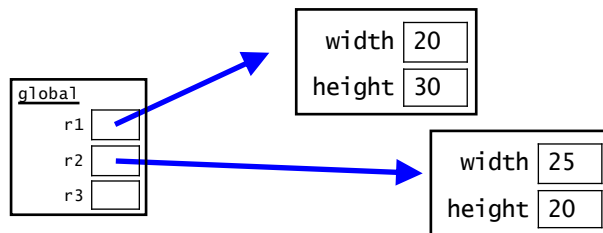
Rectangle

width	<input type="text"/>
height	<input type="text"/>

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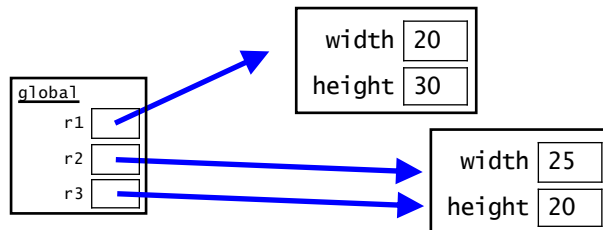
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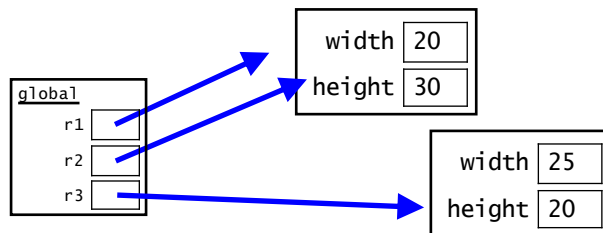
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r3 = r2  
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r1 = r3  
  
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What is the output of this program?

```
from rectangle import *           Rectangle
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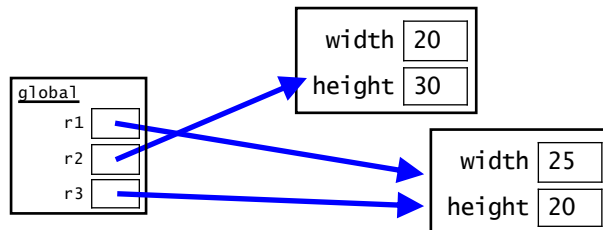
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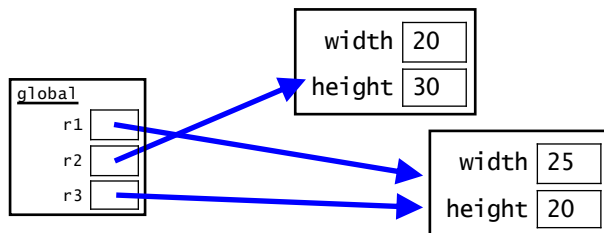
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from rectangle import *
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```



For the Inputs At Right,  
What Is the Output of this Program?

Screen 6 (1<sup>st</sup> input)  
8 (2<sup>nd</sup> input)

- A. 6
- B. 8
- C. 12
- D. 14
- E. none of these

0	read r1
1	read r2
2	copy r3 r1
3	sub r4 r2 r1
4	jeqz r4 12
5	nop
6	nop
7	nop
8	nop
9	addn r1 2
10	add r3 r3 r1
11	jumpn 3
12	write r3
13	halt

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r1	6
r2	8
r3	6
r4	2

0	read r1
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2	copy r3 r1
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For the Inputs At Right,  
What Is the Output of this Program?

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r1	8
r2	8
r3	6
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0	read r1
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What Is the Output of this Program?

Screen **6** (1<sup>st</sup> input)  
**10** (2<sup>nd</sup> input)

r1	8
r2	8
r3	14
r4	2

0	read r1
1	read r2
2	copy r3 r1
3	sub r4 r2 r1
4	jeqz r4 12
5	nop
6	nop
7	nop
8	nop
9	addn r1 1
10	add r3 r3 r1
11	jumpn 3
12	write r3
13	halt

For the Inputs At Right,  
What Is the Output of this Program?

Screen **6** (1<sup>st</sup> input)  
**10** (2<sup>nd</sup> input)

r1	8
r2	8
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r4	0

0	read r1
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For the Inputs At Right,  
What Is the Output of this Program?

Screen **6** (1<sup>st</sup> input)  
**10** (2<sup>nd</sup> input)  
**14** (output)

r1	8
r2	8
r3	14
r4	0

0	read r1
1	read r2
2	copy r3 r1
3	sub r4 r2 r1
4	jeqz r4 12
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9	addn r1 1
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### How Would You Complete This Function?

```
def longest_word(words):  
    """ returns the string that is the longest  
        word from the input list of words  
    """  
    scored_words = _____  
    bestpair = max(scored_words)  
    return _____
```

#### first blank

#### second blank

- |                                      |             |
|--------------------------------------|-------------|
| A. [[w, len(w)] for w in words]      | bestpair[0] |
| B. [[len(w), w] for w in words]      | bestpair[0] |
| C. [[w, len(w)] for w in words]      | bestpair[1] |
| D. [[len(w), w] for w in words]      | bestpair[1] |
| E. more than one of these would work |             |

### How Would You Complete This Function?

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def longest_word(words):  
    """ returns the string that is the longest  
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    """  
    scored_words = _____  
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    return _____
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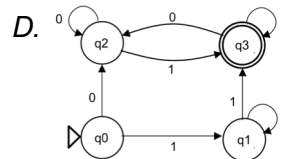
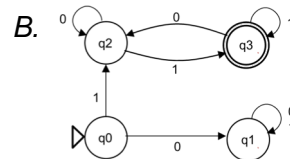
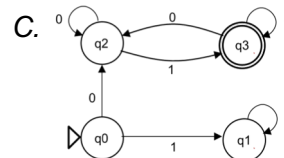
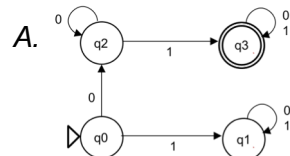
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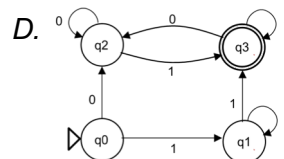
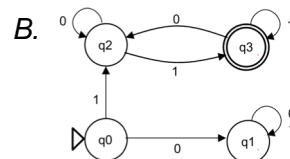
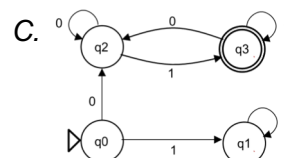
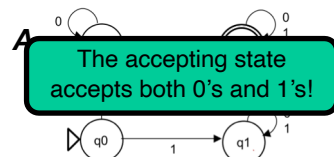
Which of these is the correct FSM?

- Construct a FSM accepting bit strings in which:
  - the **first** bit is 0
  - the **last** bit is 1



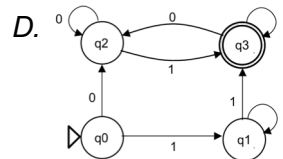
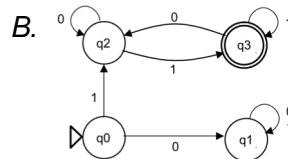
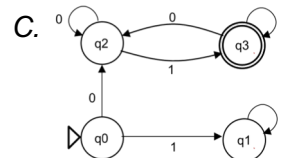
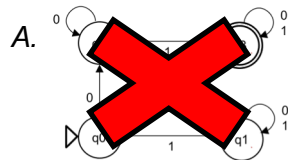
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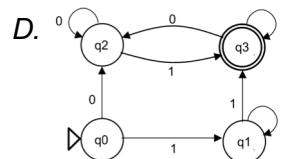
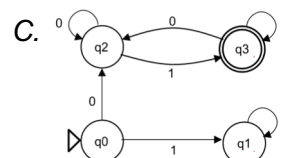
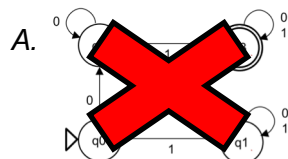
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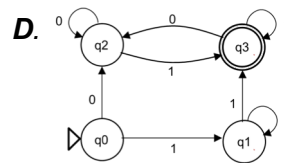
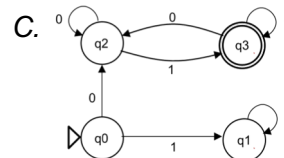
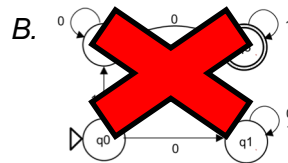
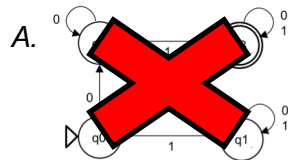
- Construct a FSM accepting bit strings in which:
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If first input is a zero it transitions into a non accepting state and stays there!

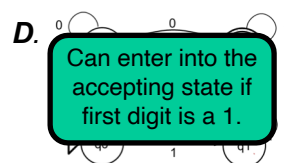
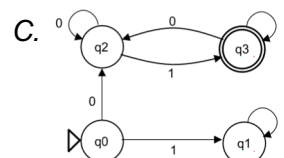
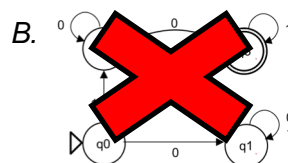
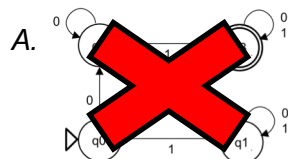
Which of these is the correct FSM?

- Construct a FSM accepting bit strings in which:
  - the **first** bit is 0
  - the **last** bit is 1



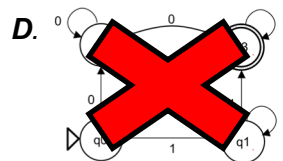
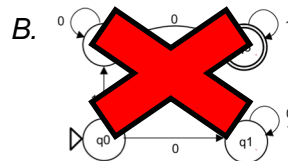
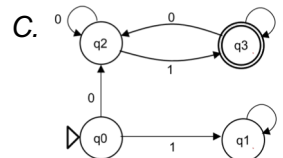
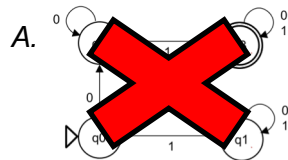
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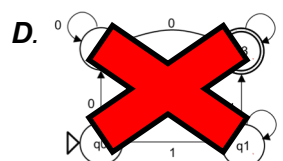
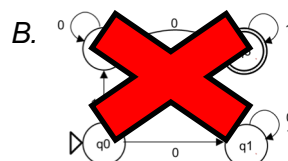
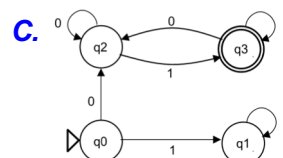
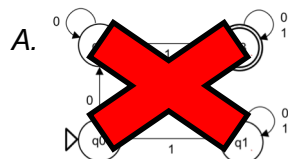
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## Algorithm Analysis

- Computer scientists characterize an algorithm's efficiency by specifying its *growth function*.
  - the function to which its running time is roughly proportional
- We've seen several different growth functions:
  - \_\_\_\_\_ # binary search
  - \_\_\_\_\_ # sequential/linear search
  - \_\_\_\_\_ # quicksort
  - \_\_\_\_\_ # selection sort
- Others include:
  - \_\_\_\_\_ # exponential growth
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  - $\log_2 n$  # binary search
  - $n$  # sequential/linear search
  - $n \log_2 n$  # quicksort
  - $n^2$  # selection sort
- Others include:
  - $c^n$  # exponential growth
  - $n!$  # factorial growth



- There are a 2 bits number (xy) and a 1 bit number (z).
- We want to add these numbers and return True if the addition is Even.
- Complete the Truth table and select the correct minterm expansion.

inputs			output
$\underline{x}$	$\underline{y}$	$\underline{z}$	
0	0	0	1

- A.  $yz + xz + xy$
- B.  $xyz + x\bar{y}\bar{z} + \bar{x}y\bar{z} + \bar{x}\bar{y}z$
- C.  $\bar{x}\bar{y}\bar{z} + \bar{x}y\bar{z} + x\bar{y}\bar{z} + xyz$
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- E. none of the above

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0	1	0	0 (integer 1)
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1	0	0	1 (integer 2)
1	0	1	0 (integer 3)
1	1	0	0 (integer 3)
1	1	1	1 (integer 4)

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