

Assembly Language: Loops Revisited; Functions

Computer Science 111
Boston University

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*based in part on notes from the CS-for-All curriculum
developed at Harvey Mudd College*

Computing Factorial in Assembly

- Given an input of x , compute the factorial of x ($x!$)
- We could do it recursively in Assembly
- But we'll hold off on that! Instead, we'll use a loop.

Computing Factorial in Assembly (cont.)

- Begin by planning out how the registers will be used:
 - r1 will hold the input, and gradually count down to 0
 - r2 will gradually *accumulate* the result

• For example:

<u>r1</u>	<u>r2</u>
5	5
4	20
3	60
2	120
1	120
0	done!

- How does r1 change each time?
What about r2?

Computing Factorial in Assembly (cont.)

- Begin by planning out how the registers will be used:
 - r1 will hold the input, and gradually count down to 0
 - r2 will gradually *accumulate* the result

• For example:

<u>r1</u>	<u>r2</u>
5	5
4	20
3	60
2	120
1	120
0	done!

- How does r1 change each time? $r1 = r1 - 1$
What about r2? $r2 = r2 * r1$
- What should r2's initial value be?

Computing Factorial in Assembly (cont.)

- Begin by planning out how the registers will be used:
 - r1 will hold the input, and gradually count down to 0
 - r2 will gradually *accumulate* the result

For example:

<u>r1</u>	<u>r2</u>
	1
5	5
4	20
3	60
2	120
1	120
0	done!

- How does r1 change each time? $r1 = r1 - 1$
What about r2? $r2 = r2 * r1$
- What should r2's initial value be? **1**

Factorial Using a Loop

Screen

5 (input)

CPU

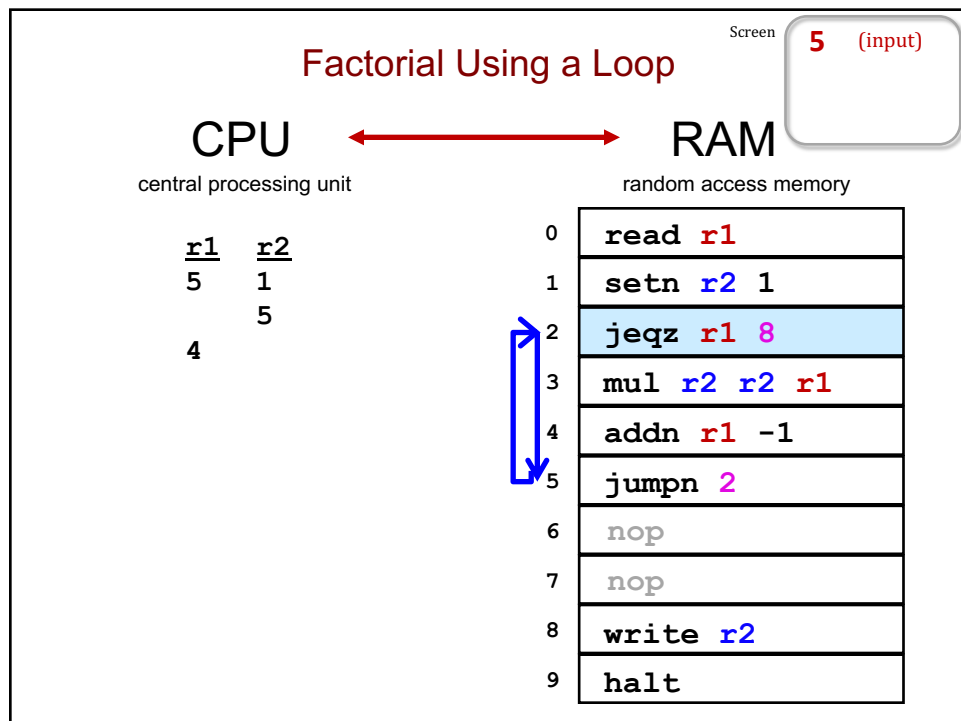
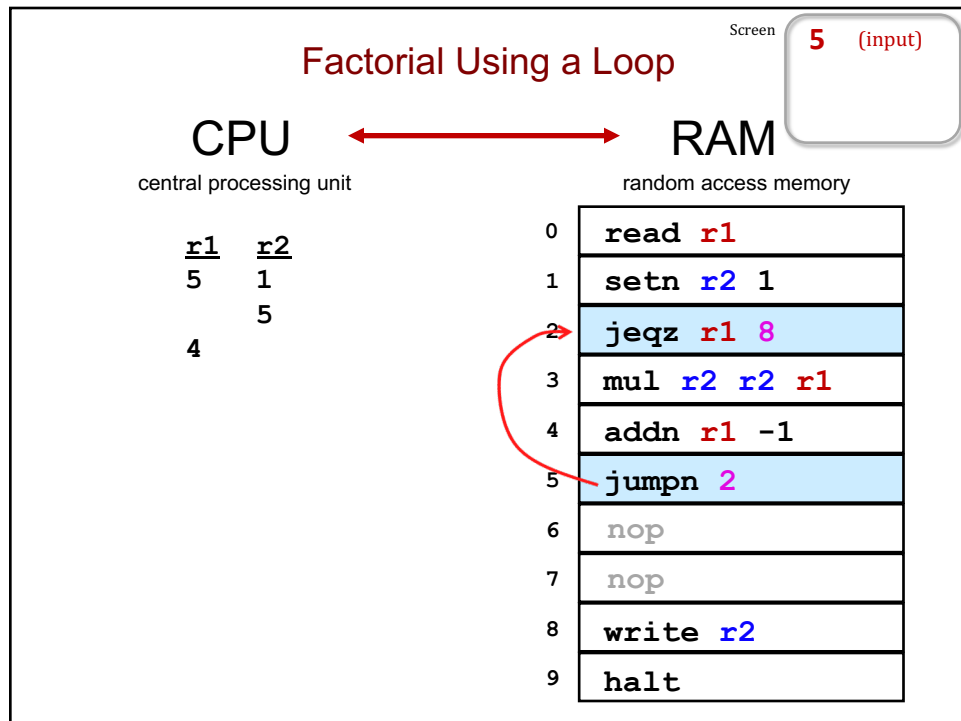
central processing unit

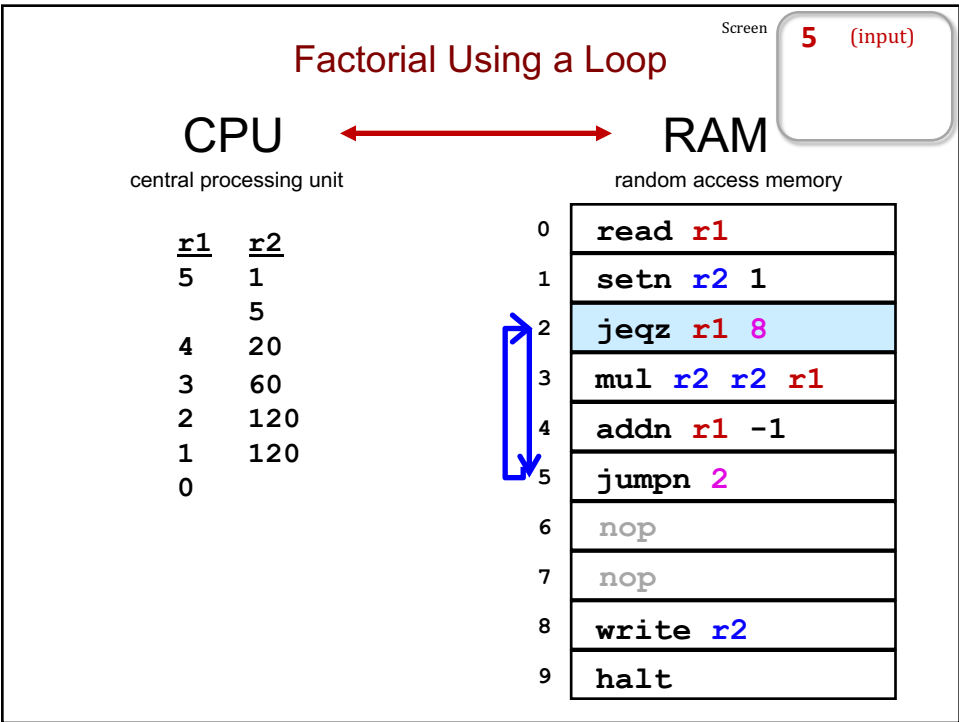
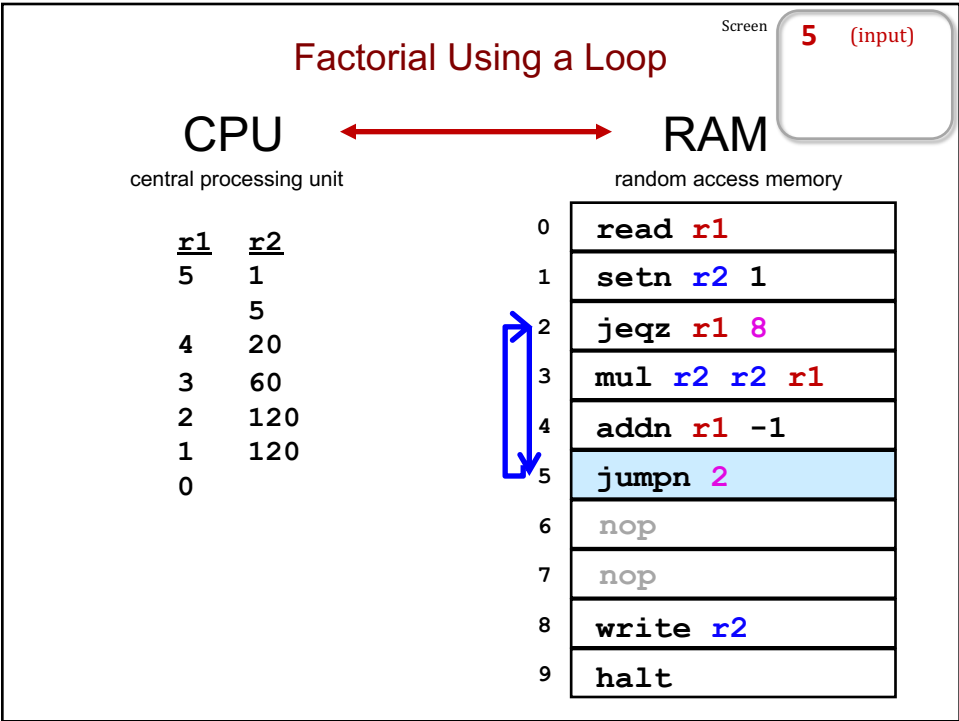
<u>r1</u>	<u>r2</u>
5	1
	5
4	

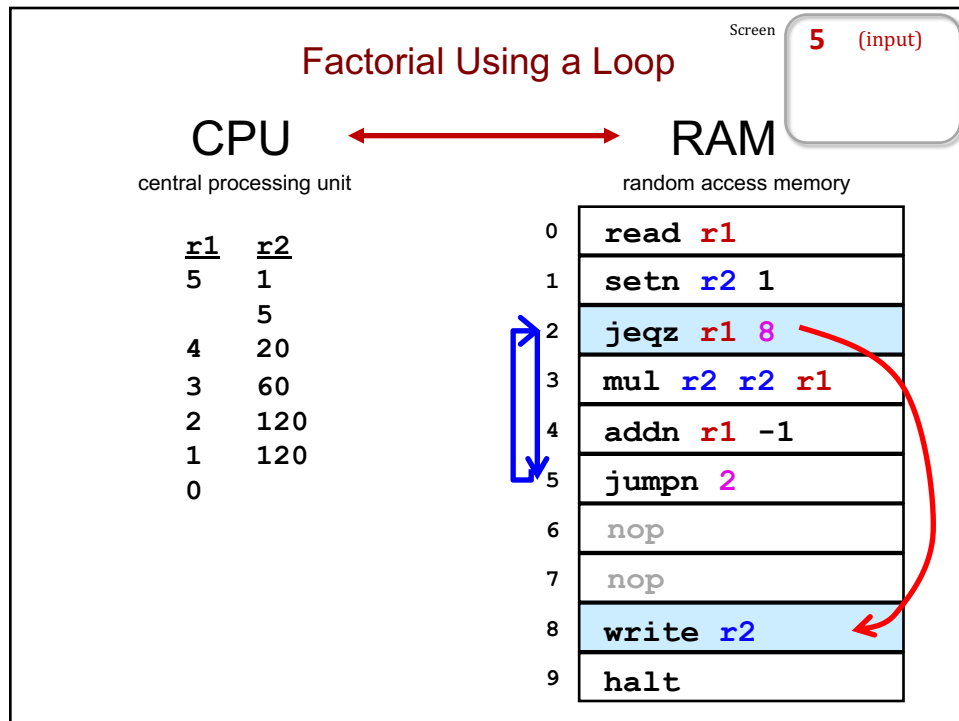
RAM

random access memory

0	read r1
1	setn r2 1
2	jeqz r1 8
3	mul r2 r2 r1
4	addn r1 -1
5	jumpn 2
6	nop
7	nop
8	write r2
9	halt







From Python...

Consider this Python program:

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

- foo(x) takes a number x and returns x*(x - 1)

```
>>> foo(5)  
20  
  
>>> foo(7)  
42
```
- the program:
 - gets a number from the user
 - calls foo(), passing in that number
 - prints the return value

From Python to Assembly

Consider this Python program:

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

Here's the assembly version:

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- Lines 0-3 correspond to the Python code from the global scope.
- Lines 4-7 correspond to the function foo.

From Python to Assembly

Consider this Python program:

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

Here's the assembly version:

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- Use registers for the variables:
 - **r1** for x (the user's input), which is also used by the function
 - **r13** for y (the function's return value)

Making a Function Call in Assembly

Consider this Python program:

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

Here's the assembly version:

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- In assembly, function calls do **not** explicitly pass in any inputs.
- Rather, we put the inputs into registers **before** the call.
 - there's only one set of registers, so the function can get the inputs from the registers

Making a Function Call in Assembly (cont.)

- To call a function in Hmmm, we use a **call** instruction:

call rX L

↑ ↑
the line number
where the function begins

any register from r1-r15;
used to store the line number
of the instruction *after* the call

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- The register used by **call** is referred to as the *return address* register.
 - stores the *return address* – the memory address that we will return to after the function completes

Returning From a Function in Assembly

Consider this Python program:

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

Here's the assembly version:

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- In assembly, we do **not** explicitly return a value.
- Rather, we put the return value into a register.
 - there's only one set of registers, so the return value can be obtained from the register

Returning From a Function in Assembly (cont.)

- To return from a function in Hmmm, we use a **call** instruction:

jumpr rX



any register from r1-r15;
the return address register --
the same one used by **call**!

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

- **jumpr** performs an *indirect* jump.
 - it jumps to the line number stored in the specified register -- the return address that was stored there by **call**

Calling and Returning: call and jumpr

Screen **7** (input)

r1 7

r13

r14 2
return address register

*the **return address** –
the line # of the instruction
after the call*

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Calling and Returning: call and jumpr

Screen **7** (input)

r1 6

r13 7

r14 2
return address register

equivalent to:

$$\begin{aligned} \mathbf{r13} &= \mathbf{r13} * \mathbf{r1} \\ 7 &* 6 \\ 42 \end{aligned}$$

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Calling and Returning: call and jumpr

Screen **7** (input)

r1 6

r13 42

r14 2
return address register

equivalent to:

$$\text{r13} = \text{r13} * \text{r1}$$

$$42 = 42 * 6$$

$$42 = 252$$

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Calling and Returning: call and jumpr

Screen **7** (input)

r1 6

r13 42

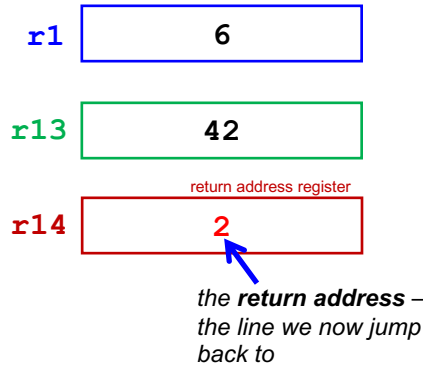
r14 2
return address register

*the **return address** –
the line we now jump
back to*

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Calling and Returning: call and jumpr

Screen **7** (input)

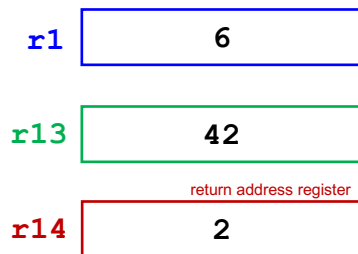


0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Calling and Returning: call and jumpr

Screen **7** (input)

42 (output)



0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

Why Do We Need call and jumpr?

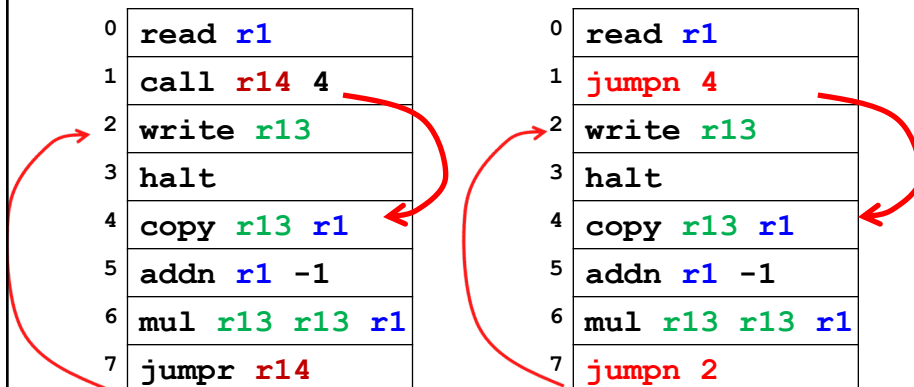
0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14



Why Do We Need call and jumpr?

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpr r14

0	read r1
1	jumpn 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jumpn 2




Unconditional jumps (**jumpn**) could be used in place of **call/jumpr** here, because we only call the function once.

Why Do We Need call and jumpr?

0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14

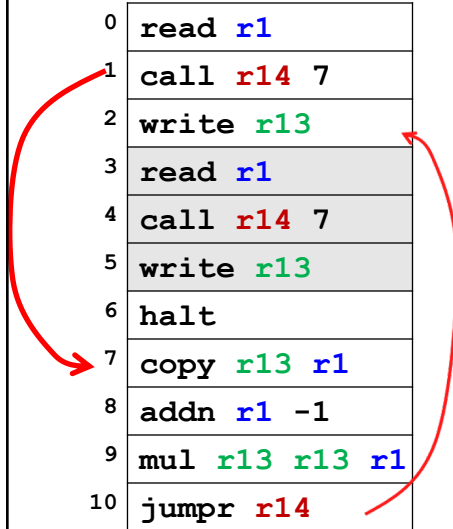
Why Do We Need call and jumpr?

0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14



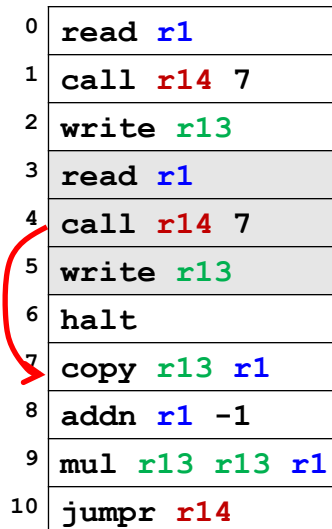
Why Do We Need call and jumpr?

0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14



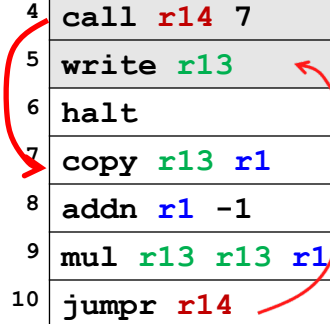
Why Do We Need call and jumpr?

0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14



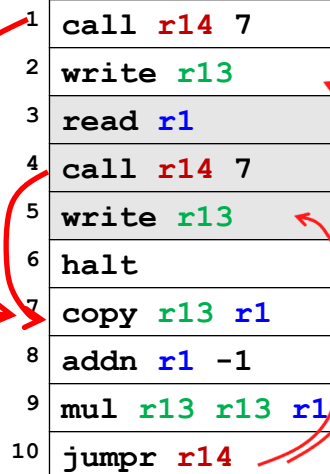
Why Do We Need call and jumpr?

0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14

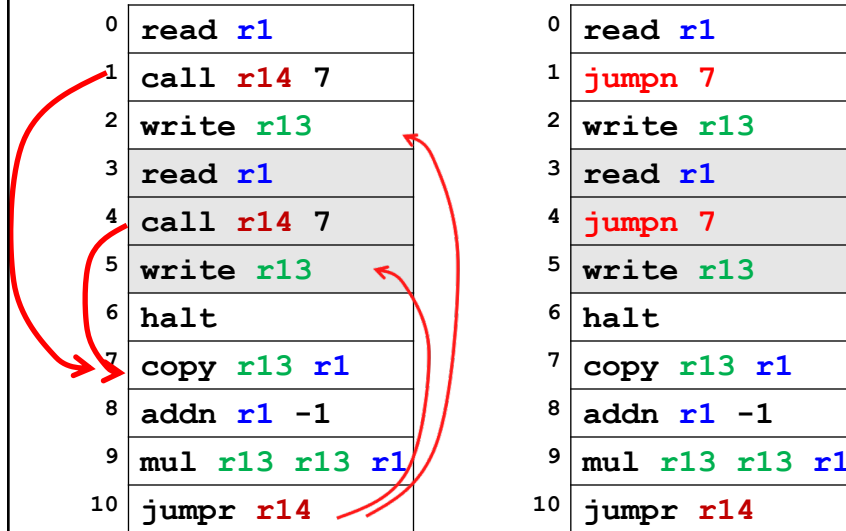


Why Do We Need call and jumpr?

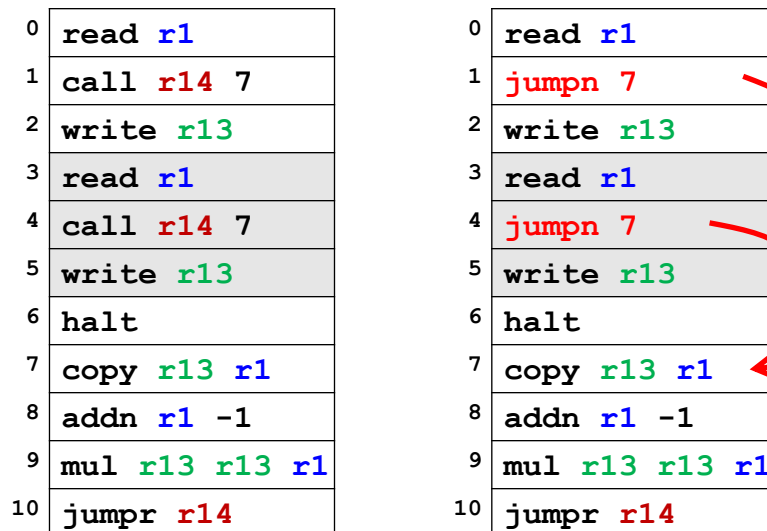
0	read r1
1	call r14 7
2	write r13
3	read r1
4	call r14 7
5	write r13
6	halt
7	copy r13 r1
8	addn r1 -1
9	mul r13 r13 r1
10	jumpr r14



Why Do We Need call and jumpr?



Why Do We Need call and jumpr?



Why Do We Need call and jump?

0	read r1	0	read r1
1	call r14 7	1	jumpn 7
2	write r13	2	write r13
3	read r1	3	read r1
4	call r14 7	4	jumpn 7
5	write r13	5	write r13
6	halt	6	halt
7	copy r13 r1	7	copy r13 r1
8	addn r1 -1	8	addn r1 -1
9	mul r13 r13 r1	9	mul r13 r13 r1
10	jumpn r14	10	jumpn ???

Diagram illustrating the need for call and jump instructions. The left table shows a sequence of instructions where a function is called twice (lines 1 and 4). The right table shows the same sequence, but with the jump instruction at line 10 replaced by a placeholder '???' and a red arrow pointing to the first 'jumpn 7' instruction (line 4), indicating the need to know the return address.

Why Do We Need call and jump?

0	read r1	0	read r1
1	call r14 7	1	jumpn 7
2	write r13	2	write r13
3	read r1	3	read r1
4	call r14 7	4	jumpn 7
5	write r13	5	write r13
6	halt	6	halt
7	copy r13 r1	7	copy r13 r1
8	addn r1 -1	8	addn r1 -1
9	mul r13 r13 r1	9	mul r13 r13 r1
10	jumpn r14	10	jumpn ???

Diagram illustrating the need for call and jump instructions. The left table shows a sequence of instructions where a function is called twice (lines 1 and 4). The right table shows the same sequence, but with the jump instruction at line 10 replaced by a placeholder '???' and a red arrow pointing to the first 'jumpn 7' instruction (line 4), indicating the need to know the return address.

Here, we call the function twice, so we need call/jump so that line 10 will know whether to go back to line 2 or 5.

For the inputs at right, what are the final values of r13 and r14?

Screen 4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8	3
D.	4	5
E.	8	5

- Which lines make up the function?
- What Python function is this?

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

For the inputs at right, what are the final values of r13 and r14?

Screen 4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8	3
D.	4	5
E.	8	5

- Which lines make up the function?
- What Python function is this?

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

return address:
where to go after
the function is done

For the inputs at right, what are the final values of r13 and r14?

Screen 4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8 ← <i>return value</i>	3 ← <i>return address: where to go after the function is done</i>
D.	4	5
E.	8	5

- Which lines make up the function?
- What Python function is this?

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

For the inputs at right, what are the final values of r13 and r14?

Screen 4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8 ← <i>return value</i>	3 ← <i>return address: where to go after the function is done</i>
D.	4	5
E.	8	5

- Which lines make up the function?
- What Python function is this?

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

For the inputs at right, what are the final values of r13 and r14?

Screen
4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8	3
D.	4	5
E.	8	5

← return value

← return address:
where to go after
the function is done

- Which lines make up the function?
lines 5-10
- What Python function is this?

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

For the inputs at right, what are the final values of r13 and r14?

Screen
4 (1st input)
8 (2nd input)

	<u>r13</u>	<u>r14</u>
A.	8	2
B.	4	3
C.	8	3
D.	4	5
E.	8	5

← return value

← return address:
where to go after
the function is done

- Which lines make up the function?
lines 5-10
- What Python function is this?
max()

0	read r1
1	read r2
2	call r14 5
3	write r13
4	halt
5	sub r3 r1 r2
6	jltz r3 9
7	copy r13 r1
8	jumpr r14
9	copy r13 r2
10	jumpr r14

The Need for the Stack

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
print(y)
```

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1
6	mul r13 r13 r1
7	jump r14

The Need for the Stack

```
def foo(x):  
    y = x*(x-1)  
    return y  
  
x = int(input())  
y = foo(x)  
y = y + x  
print(y)
```

0	read r1
1	call r14 4
2	write r13
3	halt
4	copy r13 r1
5	addn r1 -1

What if we add this line?

We want to add the user's input **x** to the function's return value **y** before printing **y**.

The Need for the Stack

```
def foo(x):
    y = x*(x-1)
    return y

x = int(input())
y = foo(x)
y = y + x
print(y)
```

0	read r1	
1	call r14 4	
1.5	add r13 r13 r1	← <i>doesn't work!</i>
2	write r13	
3	halt	
4	copy r13 r1	
5	addn r1 -1	← the user's input gets changed
6	mul r13 r13 r1	
7	jump r14	

- There's only one set of registers – shared by all lines of code!
 - in line 5, the function changes the value of **r1**
 - line 1.5 gets the changed value

Solution: Store Things on the Stack

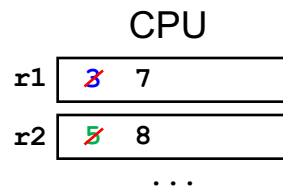
CPU	
r1	3
r2	5
...	

- Before calling a function, **store** on the stack any register values the function may overwrite.

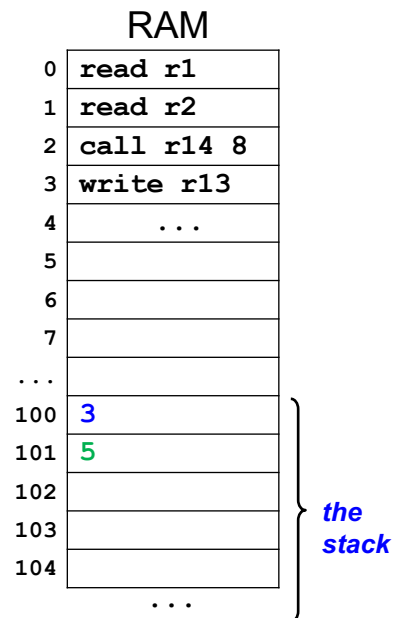
RAM	
0	read r1
1	read r2
2	call r14 8
3	write r13
4	...
5	
6	
7	
...	
100	3
101	5
102	
103	
104	
...	

the stack

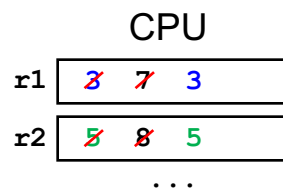
Solution: Store Things on the Stack



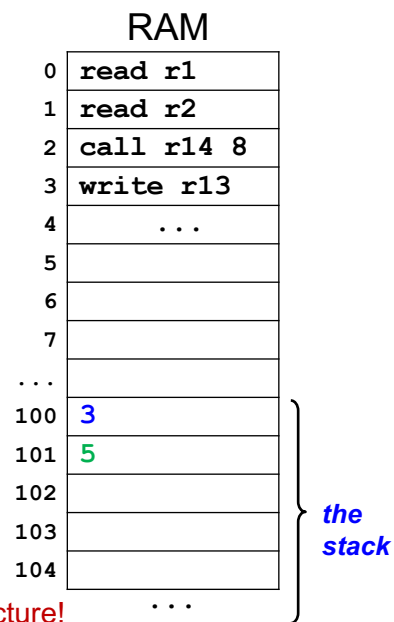
- Before calling a function, **store** on the stack any register values the function may overwrite.
- Call the function and let it modify the registers as needed.



Solution: Store Things on the Stack



- Before calling a function, **store** on the stack any register values the function may overwrite.
- Call the function and let it modify the registers as needed.
- After the function returns, **load** the values from the stack back into the registers.



- We'll see how to do this in the next lecture!