

HW #6 - due 11/13 / Sun midnight

LCS → 1. $\langle BDCABA \rangle$
opt sub property $\langle ABCBDAB \rangle$
↑
bottom-up



Question 1.

we want to find a longest common sequence from these two. by using a table

How to use table?

Ex of solving a problem by structural property.

Question 1. Answers

- (1) allocate $m+1$ by $n+1$ matrix, where m and n are the lengths of the sequences.
- (2) all entries of the first row (for index 0), and all entries of the first column (for index 0) are filled with 0's.
- (3) starting from the second row (for index 1) fill in each entry in the row using the equation (15.9) of the textbook on page 395, which is

$$C[i, j] = \begin{cases} 0 & i = 0 \text{ or } j = 0 \\ C[i-1, j-1] + 1 & i, j > 0 \text{ and } x_i = y_j \\ \max(C[i, j-1], C[i-1, j]) & i, j > 0 \text{ and } x_i \neq y_j \end{cases}$$

which each entry is determined along the way, place a one of the following "marks" in the corresponding entry:

- if $x_i = y_j$ mark with "X"
- if $C[i-1, j] \geq C[i, j-1]$ mark with "A"
- else mark with "←"

(4) At the end of the construction, trace the "marks" starting from $C[m+1, n+1]$.

there are 3 possible marks recorded

a) # \rightarrow two letters are identical

b) "A" \rightarrow we need to look at the one right above the current entry

c) "←" \rightarrow we need to look at the one right next to the current entry (to the left)

table C

$i \backslash j$	0	1	2	3	4	5	6
		B	D	C	A	B	A
0	0	0	0	0	0	0	0
1	A	0	0	0	0	1	1
2	B	0	1	1	1	1	2
3	C	0	1	1	2	2	2
4	B	0	1	1	2	2	3
5	D	0	1	2	2	2	3
6	A	0	1	2	2	3	3
7	B	0	1	2	2	3	4

1. construction of the table C — order
 All in 1st row, and row, \vdots
2. trace the "marks" from $C[m, n]$
 $\rightarrow 4$ — in this example

Question 1

0/1 knapsack problem solve by Dynamic programming by using a table.
 n, v, w

		\$	lb
6	item 1	60	10
5	item 2	100	20
4	item 3	120	30
			60

DP \$/lb criteria 만 사용해서 item 1, 2 만 선택하여
item 3 을 사용하지 못한다. (GA X) 이렇게 table 을
사용해야 풀 수 있을 까?

Question 2 Answers

optimal value of the 0/1 knapsack problem.

Given n items and the weight for the knapsack w , allocate a table that consists of $n+1$ rows and $w+1$ columns.

let's call this table v .

All entries on the first row & columns are filled with 0's

Use the following equations to compute the value

$$v(i, w) = \max \left(v(i-1, w), v_i + v(i-1, w - w_i) \right) \quad \text{if } w_i \leq w$$

$$v(i-1, w) \quad \text{if } w_i > w$$

The optimal value will be in the entry $v[n+1, w+1]$.

$$W=10$$

$$v_1=1 \quad w_1=2$$

$$v_2=\underline{3} \quad w_2=3$$

$$v_3=5 \quad w_3=4$$

$$v_4=9 \quad w_4=7$$

0
↓

V

$v \backslash w$	0	1	2	3	4	5	6	7	8	9	10
0	0	0	0	0	0	0	0	0	0	0	0
1	0	0	1	1	1	1	1	1	1	1	1
2	0	0	1	3	3	4	4	4	4	4	4
3	0	0	1	3	5	5	6	8	8	9	9
4	0	0	1	3	5	5	6	9	9	10	12