

Performance Analysis for Downlink Transmission in Multi-Connectivity Cellular V2X Networks

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Abstract—With the ever-increasing number of connected vehicles in the fifth-generation mobile communication networks (5G) and beyond 5G (B5G), ensuring the reliability and high-speed demand of cellular vehicle-to-everything (C-V2X) communication in scenarios where vehicles are moving at high speeds poses a significant challenge. Recently, multi-connectivity technology has become a promising network access paradigm for improving network performance and reliability for C-V2X in the 5G and B5G era. To this end, this paper proposes an analytical framework for the performance of downlink in multi-connectivity C-V2X networks. Specifically, by modeling the vehicles and base stations as one-dimensional Poisson point processes, we first derive and analyze the joint distance distribution of multi-connectivity. Then through leveraging the tools of stochastic geometry, the coverage probability and spectral efficiency are obtained based on the previous results for general multi-connectivity cases in C-V2X. Additionally, we evaluate the effect of path loss exponent and the density of downlink base station on system performance indicators. We demonstrate through extensive Monte Carlo simulations that multi-connectivity technology can effectively enhance network performance in C-V2X. Our findings have important implications for the research and application of multi-connectivity C-V2X in the 5G and B5G era.

Index Terms—C-V2X, multi-connectivity, coverage probability, spectral efficiency, stochastic geometry.

I. INTRODUCTION

WITH the evolution of the fifth-generation mobile communication networks (5G) and beyond 5G (B5G), reliable and high-performance wireless communication systems have become essential to fully exploit the potential of intelligent transportation systems (ITS) [1]–[3]. Cellular vehicle-to-everything (C-V2X) has emerged as a promising technology that utilizes the existing cellular network infrastructure and spectrum to provide efficient and reliable communication between vehicles (V2V), as well as between vehicles and

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other network entities such as base stations (BS), roadside units, pedestrians, and cloud servers (V2I) [4]. This technology aims to enhance the efficiency and safety of vehicular traffic while enabling various applications such as collision avoidance, traffic management, cooperative driving, platooning, and autonomous driving, that require high-speed and low-latency communication in ITS [5], [6]. However, as the number of connected vehicles continues to increase, C-V2X is rapidly developing towards ultra-dense, which poses challenges such as interference management, security, and energy efficiency, and require further research and development to enable reliable and efficient vehicular communication. C-V2X also faces significant challenges due to the high-speed mobility and dynamic topology of vehicles, which may cause rapid fluctuations in the quality of wireless links, frequent handovers, and increased signaling overhead. These challenges are severely impacting the communication performance and influence the quality of experience (QoE) and quality of service (QoS) of ITS applications.

In recent years, multi-connectivity technology has attracted significant attention to address these aforementioned challenges [7]. Multi-connectivity enables a vehicle to establish multiple simultaneous connections with different BSs using various radio access technologies (RATs), access points (APs), or channels, thus taking advantage of the diversity and availability of wireless resources in the cellular network [3]. The multi-connectivity technology, as compared to the traditional point-to-point communication, offers substantial advantages in terms of various communication performance metrics, e.g., enhanced reliability [8], improved coverage [9], and enabled seamless mobility and handover [10]. Through accessing multiple BSs, vehicles can switch between available connections without disrupting ongoing communication, providing uninterrupted connectivity even when moving across network boundaries or transiting under different coverage of networks. In addition, based on the specific requirements of the application or user preferences, multi-connectivity is capable of offering flexibility for choosing the most suitable network connections and providing better spectral efficiency by dynamic adaptation to changing network conditions [11]. Thus, applying multi-connectivity to C-V2X is of remarkable significance for improving communication performance and makes it more suitable for ITS applications.

In the context of multi-connectivity in C-V2X, coverage probability and spectral efficiency are two important performance metrics for evaluating wireless communication system performance [9]. However, establishing a comprehensive ana-

lytical framework with regard to these performance metrics is challenging and holds significant academic importance. following a spatial point process [12], [13]. System modeling and analytical performance evaluation based on stochastic geometry have proven to be a powerful method for monitoring the effects of important system parameters as well as optimizing system configurations, all without the need for computationally expensive and resource-intensive computer simulations [14]. Moreover, there is a research gap in the analysis of uplink and downlink performance for multi-connectivity C-V2X communication. While most of the existing studies primarily focused on the uplink transmission and performance optimization [9], [15], the downlink transmission based on an analytical framework has not been sufficiently explored. This is a significant limitation since downlink transmission plays a crucial role in supporting various ITS applications that rely on receiving downlink information from infrastructures. Therefore, conducting in-depth studies on the downlink performance of multi-connectivity C-V2X communication is substantial for filling this existing gap and ensuring a holistic analysis of the system's capabilities for supporting diverse ITS applications.

Therefore, this paper considers multi-connectivity as an effective solution to resolve the challenges faced by C-V2X communication, aiming to enhance the communication performance for ITS applications. A feasible analytical framework for downlink transmission in multi-connectivity C-V2X networks is proposed by modeling the vehicles and downlink base stations (DBSs) as one-dimensional (1-D) Poisson point processes (PPPs), the tools of stochastic geometry are used to derive crucial performance indicators, including joint distance distribution, coverage probability, and spectral efficiency. The key contributions of this paper are summarized below:

- We present a novel multi-connectivity performance analytical framework for C-V2X, which enables the evaluation of network performance in the 5G/B5G era. This framework provides a foundation for further research and potential performance improvement of multi-connectivity technology in C-V2X systems.
- We derive precise expressions of coverage probability and spectral efficiency for general multi-connectivity cases in C-V2X based on the joint distance distribution. We also provide important insights into the design and optimization of C-V2X networks by analyzing the effect of path loss exponent and DBS density on system performance indicators.
- We conduct comprehensive Monte Carlo simulations to confirm the effectiveness of the presented multi-connectivity performance analytical framework, which shows that multi-connectivity technology can significantly improve network performance in C-V2X. This finding has important implications for the practical applications of multi-connectivity C-V2X in the 5G/B5G era.

The subsequent sections of this paper are structured as follows. We briefly introduce the existing research works related to our work in Section II. Section III presents the proposed framework for analyzing multi-connectivity perfor-

mance. Section IV conducts a performance analysis of the system, including the joint distance distribution, coverage probability and spectral efficiency. In Section V, the simulation setup and results obtained from extensive Monte Carlo simulations are presented, providing verification of the proposed framework and evaluation of the system performance. Section VI presents the concluding remarks of this paper.

II. RELATED WORK

The adoption of C-V2X has emerged as a critical network paradigm for enabling vehicular communication with other vehicles and the infrastructure, offering diversified safety and efficiency applications for ITS [16]. However, despite of its significant potential, the implementation of C-V2X communication is confronted with numerous challenges, such as high mobility, dynamic topology, heterogeneous network, and stringent QoS requirements [12]. In high-speed C-V2X scenarios, single connectivity with just one base station frequently leads to handover issues [7], [9], resulting in a rapid decline in communication speed and reliability, thus no longer meeting C-V2X's QoS requirements. In recent years, multi-connectivity has been considered to be a promising technology to tackle these challenges in C-V2X through enhancing reliability, reducing latency, and boosting overall network performance.

With multiple BSs access, multi-connectivity supports seamless mobility and handover between different BS coverage. Exploiting simultaneous connections, multi-connectivity offers considerable availability for the improvement of spectral efficiency [17]. A number of studies have investigated the potential benefits of applying multi-connectivity in C-V2X and wireless networks. Numerous studies have delved into the potential advantages of implementing multi-connectivity within C-V2X and wireless networks. These investigations cover various aspects, ranging from resource optimization in C-V2X multi-connectivity to performance analyses in wireless networks.

In the context of C-V2X, some studies concentrate on optimizing communication resources. Rabitsch *et al.* [8] explored multi-connectivity algorithms tailored to meet the stringent requirements for communication availability and latency in V2I networks. Lu *et al.* [7] introduced a novel approach to reduce duplication rates in DBSs in fully-decoupled C-V2X networks. They achieved this by formulating and solving optimization problems using Lyapunov stochastic optimization techniques to help vehicles select access BSs for multi-connectivity and optimize bandwidth resources to meet user communication requirements. Kousaridas *et al.* [18] analyzed multi-connectivity management in a Manhattan model for V2X communication.

Other studies aim to evaluate the performance of multi-connectivity in both wireless networks and C-V2X scenarios. Moltchanov *et al.* [19] provided a closed-form upper bound on the probability density function (PDF) for multi-connectivity, shedding light on its statistical characteristics. Weedage *et al.* [3] scrutinized the downlink performance of multi-connectivity in wireless networks. Wu *et al.* [9] proposed a multi-connectivity scheme for uplink C-V2X communica-

tions, deriving precise expressions for the outage probability using stochastic geometry tools.

Numerous performance metrics have been employed in research works that explore the application of multi-connectivity technology in cellular communication scenarios. In 5G and beyond 5G networks, Sylla *et al.* [20] provided a comparable cellular communication analysis for multi-connectivity. Pupiles *et al.* [2] focused on the multi-connectivity architectures and protocols for 5G network and they described the different network entities and protocol layers involved in multi-connectivity, such as multi-connectivity coordinator, multi-connectivity agent, multi-connectivity manager and packet data. Petrov *et al.* [21] studied the dynamic characteristics of multi-connectivity technology, whereas Giordani *et al.* [22] investigated its application in 5G mmWave cellular networks.

In this paper, we mainly focus on the performance indicator of coverage probability and spectral efficiency based on distance distribution. Coverage probability and spectral efficiency are two of the most important metrics that hold significance for evaluating the wireless networks. Firstly, coverage probability determines the reliability of C-V2X communication in different geographical areas and network densities [13]. By leveraging multi-connectivity technology, the coverage probability can be improved and the risk of communication interruptions can be reduced. With multiple connections simultaneously receiving and transmitting data, even if one connection encounters interruption issues, the others can maintain communication, thereby enhancing overall coverage probability. Secondly, spectral efficiency is extremely crucial for the transmission capacity of C-V2X. C-V2X communication involves handling a substantial amount of traffic-related information, including vehicle sensor data and traffic management instructions [23]. Additional spectrum resources can be utilized in parallel or through multiplexing, thus improving spectral efficiency to support higher data transmission rates and faster response times through multi-connectivity [24]. Further improvements in coverage probability and spectral efficiency can be achieved by optimizing load balancing and resource allocation among the connections. Research in this area is of paramount importance to achieve efficient and reliable C-V2X communication, providing a more robust and efficient foundation for critical applications such as real-time vehicle communication, traffic management, and vehicular safety in ITS.

To obtain the exact analytical expression of performance metrics for multi-connectivity in C-V2X, leveraging the tools of stochastic geometry is regarded as an efficient approach and it has been increasingly popular in recent years for the performance analysis in multi-connectivity scenarios. For instance, Molchanov *et al.* [19] were among the pioneers in deriving the PDF for multi-connectivity, laying essential groundwork for further investigations. Building upon this foundation, Kibria *et al.* [25] assessed the viability of employing dual connectivity and coordinated multiple points (CoMP) transmission in wireless communication systems, expanding the scope of multi-connectivity applications.

Moreover, the utilization of stochastic geometry in various multi-connectivity scenarios has witnessed extensive exploration. Shafie *et al.* [24] explored multi-connectivity in in-

door communication systems using ultra-wideband terahertz (THz) technology, focusing on average ergodic capacity and connectivity likelihood. Chen *et al.* [12] employed coordinated multipoint techniques to enhance spectral efficiency, while Giordani *et al.* [22] and Kamble *et al.* [26] aimed to optimize the Signal-to-Interference-Plus-Noise Ratio (SINR) and outage probability in single-frequency networks. Weedage *et al.* [3] delved into the analysis of channel capacity and outage probability in wireless networks' downlink scenarios.

III. SYSTEM MODEL

When analyzing the overall performance of a multi-connectivity C-V2X network, a specific vehicle is considered as a typical analysis object. Therefore, the multiple roads model can still be simplified and analyzed as a single road situation. Moreover, it has been proven that the single road model can effectively reflect the performance of multi-connectivity in C-V2X [7], [9]. Therefore, to investigate the downlink multi-connectivity in C-V2X scenario, we introduce a simplified 1-D system model in this paper. A coordination scheme called Single Frequency Networks (SFN) as in [27] are leveraged for spectrum allocation. SFN enables the transmission of incoherent joint signals on the same radio resources in frequency and time, which requires BSs to coordinate when creating signals and to strictly synchronize their timing. Our focus in this paper is on the intra-frequency multi-connectivity, which requires simultaneous transmission of multiple DBSs operating at the same carrier frequency to the same vehicle. This is an important issue to address in the C-V2X scenario, where high data rates and reliable communication are need for safety-critical applications. The following of this section introduces the channel model, association policy, interference model, and performance metrics utilized in this study. Table I lists the key symbols used throughout this paper.

A. Modeling of C-V2X Network

Fig. 1 shows the downlink multi-connectivity scenario in C-V2X networks. The vehicles are randomly distributed on an urban freeway segment, and the DBSs are densely distributed along the road. To simplify the analysis, we make the assumption that both the DBSs and vehicles utilize a single antenna, and denote the height difference between the antenna of the DBS and the vehicle as h .

For the tractability of the downlink performance analysis, we consider a 1-D scenario on a road including vehicles, DBSs, and interference DBSs as shown in Fig. 1, as in [6], [9]. From a statistical perspective, the spatial distributions of vehicles and DBSs conform to 1-D PPP distributions [13], and we use the 1-D PPPs φ_V, φ_D with density λ_v, λ_d to denote the locations of vehicles and DBSs on the road, respectively, where φ_V, φ_D can be expressed as

$$\varphi_j \triangleq \{x_{i,j} \in R^2 : i \in \mathbb{N}_+\}, j = \{V, D\}.$$

All of the vehicles and DBSs are distributed along a road with length l . As per Slivnyak's theorem, the distribution of point processes remains unchanged even after adding a node at the origin [28], and in order not to lose generality and eliminate

TABLE I
A LIST OF MAJOR SYMBOLS

Notation	Description
$\lambda; x_i$	The density of the vehicles and DBSs on a 1-D road; The distance of i th nearest DBS to the typical vehicle.
$P_d; \alpha_d$	The transmit power of DBS; The downlink path loss exponent parameter.
$g_d; \chi_d$	The channel gain between the DBS and vehicle; The Nakagami-m fading gain.
$\tau_D; \mu$	The spectral efficiency of downlink; The mean of exponential function.
$\omega_d; \delta_d^2$	The mean of the logarithm of χ_d ; The variance of the logarithm of χ_d .
φ_V, φ_D	The Poisson point processes of vehicles and DBSs.
$\varphi_D^t; t$	The DBSs set after being executed random displacement; The predetermined threshold t of coverage probability.
$\varphi_c; \Theta_d^d$	The collaborative DBS set of multi-connectivity; The interference DBS set of multi-connectivity.
$I_d; \sigma_d^2$	The received interference of the typical vehicle; The noise of channel.
$\mathbb{E}(\cdot)$	The expectation of a random variable.
$\mathbb{P}(\cdot)$	The probability of a random variable.
$F(\cdot)$	The cumulative distribution function of a random variable.
$f(\cdot)$	The probability density function of a random variable.
$\zeta_I(\cdot)$	The Laplace transform of interference I .
$\Gamma(\cdot)$	The gamma distribution function of a random variable.

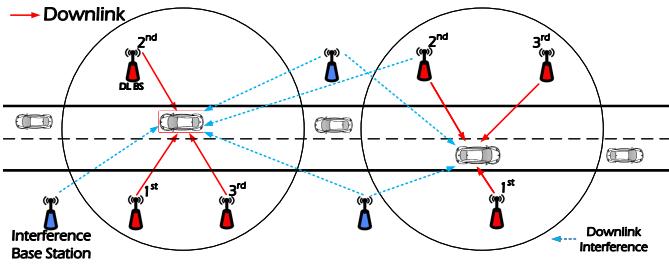


Fig. 1. An example of a practical 1-D scenario for downlink transmission in multi-connectivity C-V2X is illustrated. In this scenario, the target vehicle receives messages from the three closest DBSs, while transmissions from DBSs located beyond the collaboration distance can lead to interference to the target vehicle.

segmentation due to boundary effects, we place the typical vehicle at the origin $v_o = (0, 0)$, i.e. which represents the center of the road [9].

In relation to the formation of virtual cells, we assume that each vehicle is connected to the n nearest DBSs on a Euclidean plane. The 1-D distance between the typical vehicle v_o with the i -th ($i \leq n$) DBS is r_i , thus the actual distance x_i between the transmit antenna of DBS to receive antenna of the typical vehicle is

$$x_i = \sqrt{r_i^2 + h^2}. \quad (1)$$

We adopt a common power-law pathloss and Rayleigh fading model with a decay rate of $x^{-\alpha_d}$, where x denotes the distance between the DBS and the typical vehicle. The downlink pathloss exponent parameter is denoted as α_d ($\alpha_d > 2$). g_d is used to denote the power gain of Rayleigh fading and it is modeled by an exponential distribution with a mean of $1/\mu$. Therefore, we have $g_d \sim \exp(\mu)$. The distribution function of g_d is

$$f(g_d) = \mu e^{-\mu g_d}. \quad (2)$$

Furthermore, we use random variable χ_d to model the effects of shadowing between the DBS and the typical vehicle in the downlink, and χ_d follows a log-normal distribution given by $10\log_{10}\chi_d \sim \mathcal{N}(\omega_d, \delta_d^2)$, where ω_d represents the mean of the logarithm of χ_d (i.e., the geometric mean of χ_d), while δ_d^2

represents the variance of the logarithm of χ_d [29]. Hence, the received signal power of the typical vehicle from the i -th DBS in the downlink is [30]

$$P_{r,v}(x_i) = P_d g_d \chi_d x_i^{-\alpha_d}, \quad i \in \varphi_D, \quad (3)$$

where P_d is the transmitting power of the DBS and assumed to be the same for all DBSs.

B. Association policy

The typical vehicle is assumed to be connected to n nearest DBSs by measuring all the receiving power from the nearby DBSs, finding the DBSs with the maximum receiving power (MRP) in turn [9]. Since the received power $P_{r,v}$ is not exponentially distributed for the modeling of the shadow fading [16], the lemma of random displacement theorem is considered to solve this issue [31]. Thus, $P_{r,v}(x_i) = P_d g_d \chi_d x_i^{-\alpha_d}$ can be transformed to $P_{r,v}(y_i) = P_d g_d y_i^{-\alpha_d}$, where $y_i = \chi_d^{-\frac{1}{\alpha_d}} x_i$. The 1-D PPP transformed converges to a 1-D homogeneous PPP and the intensity λ_d is transformed to $E[\chi_d^{-\frac{1}{\alpha_d}}] \lambda_d$, and the intensity of the 2-D PPP is $E[\chi_d^{-\frac{2}{\alpha_d}}] \lambda_d$ after executing the procedure of random displacement [13]. Specifically, $E[\chi_d^{-\frac{1}{\alpha_d}}] \lambda$ can be calculated as

$$\mathbb{E}[\chi_d^{-\frac{1}{\alpha_d}}] \lambda_d = \exp\left(\frac{\omega_d \ln 10}{10\alpha_d} + \frac{1}{2}\left(\frac{\sigma_d \ln 10}{10\alpha_d}\right)^2\right) \lambda_d. \quad (4)$$

Then we use 1-D PPP φ_D^t to denote the transformed set of DBS and $\lambda_D = E[\chi_d^{-\frac{1}{\alpha_d}}] \lambda_d$ denotes the transformed DBS intensity. To facilitate performance analysis in the following sections, we use the symbol $\varphi_D^{t,d}$ to denote the set of distances between the DBSs and the typical vehicle,

$$\varphi_D^{t,d} = \{x_1, x_2, \dots, x_i\}, \quad i \in \mathbb{N}_+, \quad (5)$$

where x_i denotes the distance between the typical vehicle v_o and the i -th nearest DBS $\in \varphi_D^t$. Thus the candidate serving

DBSs is changed to the n nearest DBSs $\in \varphi_D^t$ in turn, and this can be expressed as

$$x_i = \arg \max_{x_i \in \varphi_D^{t,d} \setminus \varphi_c^d} x_i^{-\alpha_d}, i > m \quad (6)$$

where we use $\varphi_c^d = \{x_1, x_2, \dots, x_m\}$ to denote the set of the distances between the connected collaborative DBSs and the typical vehicle v_o at the origin, m is the number of DBSs that the typical vehicle has already connected to, and $x_i, i \in \{m+1, m+2, \dots\}$ denotes the distance between the DBS outside φ_c^d and the typical vehicle. Let φ_c to denote the set of the connected collaborative DBSs. This means that to expand the set φ_c , we need to find the nearest DBS among DBSs in $\varphi_D^t \setminus \varphi_c$.

C. Interference

In the collaboration DBSs set φ_c , all DBSs will transmit the control and data signals simultaneously on the same subband [7]. Since the signal components of the DBSs are within the cyclic prefix, the resulting multi-connectivity SINR experienced by the typical vehicle v_o in the downlink is defined as follows:

$$\text{SINR}_D = \frac{\sum_{i \in \varphi_c} P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2}, \quad (7)$$

where $\sum_{i \in \varphi_c} P_d g_d x_i^{-\alpha_d}$ represents the sum of received signal power from the DBSs in φ_c . We use σ_d^2 to denote the power of the additive white Gaussian noise (AWGN) [14]. I_D is the power of aggregate interference from the DBSs outside of φ_c and I_D can be expressed as

$$I_D = \sum_{i \in \{\varphi_D^t \setminus \varphi_c\}} P_d g_d x_i^{-\alpha_d}. \quad (8)$$

D. Performance Metrics

In order to enable advanced C-V2X applications such as automated driving applications and stream media [4], [16], it is crucial to ensure that the downlink transmission is both reliable and capable of transmitting data at a high rate. This is important not only from the perspective of a single vehicle but also from the perspective of the whole C-V2X network. To this end, this paper conducts an analytical evaluation of two performance metrics, i.e. coverage probability and spectral efficiency as follows.

- The coverage probability of the typical vehicle v_o in downlink, is defined as the probability that the received SINR outperforms a predetermined threshold t [32]. It can be expressed as

$$\mathbb{P}_{cov}(t) = \mathbb{P}(\text{SINR}_D > t). \quad (9)$$

It can also be calculated as the proportion of vehicles that have the received SINR_D above a threshold t , i.e., establish a successful connection with the DBSs in φ_c ,

among all vehicles in the simulation scenario. Since the cumulative distribution function (CDF) of SINR_D is $\mathbb{P}_{cov}(t) = \mathbb{P}(\text{SINR}_D < t)$, the coverage probability can also be expressed as the complementary cumulative distribution function (CCDF) of the SINR_D at the typical vehicle from the DBSs.

- The spectral efficiency of the typical vehicle v_o is the amount of data transmitted per unit of bandwidth [33]. According to the Shannon Theory, the spectral efficiency of the downlink is

$$\tau_D = \mathbb{E}[\ln(1 + \text{SINR}_D)], \quad (10)$$

where $\mathbb{E}(\cdot)$ is the expectation function. The spectral efficiency describes the likelihood of a wireless communication system achieving a specific information amount within a certain time period and space range during actual use [23]. It can help evaluate the performance of C-V2X in a multi-connectivity environment and determine whether system optimization or adjustments are needed [33].

IV. PERFORMANCE ANALYSIS

We first derive the expression for the joint distance distribution from x_1 to x_n in this section. To optimize system configurations without the need for time-consuming computer simulations, we leverage the stochastic geometry. Specifically, by using the tools provided by stochastic geometry, we utilize the results obtained from previous sections to derive the coverage probability and spectral efficiency of C-V2X in a multi-connectivity scenario.

A. The joint distance distribution of the typical vehicle to n service DBSs

Since the typical vehicle is connected to the n nearest DBSs in multi-connectivity, no other DBSs are closer than distance x_n . And it also means that all interference DBSs are farther than x_n . The above definition can be expressed by $f(x_1, x_2, \dots, x_n)$, and we call it joint distance distribution for x_1, x_2, \dots, x_n .

Lemma 1. *The joint distance distribution of the typical vehicle to its service DBSs in set φ_c from x_1 to x_n is*

$$f(x_1, x_2, \dots, x_n) = (2\lambda_D)^n e^{-2\lambda_D x_n}, \quad (11)$$

where x_n denotes the distance between the typical vehicle and the n -th closest DBS in φ_c .

Proof: The null probability of a PPP in an area A is $e^{-\lambda A}$, where $A = 2\lambda x$ in 1-D PPP and $A = \pi x^2$ in 2-D PPP, thus the CCDF of x_1 is [14]

$$\begin{aligned} \mathbb{P}[x > x_1] &= \mathbb{P}[\text{no DBS closer than } x_1] \\ &= e^{-2\lambda_D x_1}. \end{aligned} \quad (12)$$

Because the $CDF = 1 - CCDF$, the CDF of x_1 is

$$F(x_1) = 1 - e^{-2\lambda_D x_1}. \quad (13)$$

Since the PDF $f(x) = \frac{\partial F(x)}{\partial x}$ [28], the PDF of x_1 is

$$f(x_1) = 2\lambda_D e^{-2\lambda_D x_1}. \quad (14)$$

According to the definition of Section 3.3 in [34], let $f(x_2|x_1)$ denote the probability that the 2nd closest DBS is at x_2 given that the closest one is at the distance of x_1 . Thus the probability of having no DBSs between the distances x_1 and x_2 can be calculated as follows

$$f(x_2|x_1) = 2\lambda_D e^{-2\lambda_D(x_2-x_1)}. \quad (15)$$

According to the conditional probability Bayes theorem [35], $f(x_2, x_1)$ denotes the joint distance distribution to the two nearest distances, i.e., the probability of having at least one point in $x_2 + \Delta x$, where Δx is an infinitesimal quantity, is

$$f(x_1, x_2) = f(x_2|x_1) f(x_1) = (2\lambda_D)^2 e^{-2\lambda_D x_2}. \quad (16)$$

By following the similar procedures in Eq. (15) and Eq. (16), the joint distance distribution $f(x_1, x_2 \dots x_n)$ from x_1 to x_n is

$$f(x_1, x_2, \dots, x_n) = (2\lambda_D)^n e^{-2\lambda_D x_n}. \quad (17)$$

■

To compare the joint distance distribution $f(x_1, x_2, \dots, x_n)$ and the PDF of x_n , we provide the PDF of x_n in Eq. (18) as

$$f(x_n) = \frac{(2\lambda_b x_n)^n}{x_n \Gamma(n)} e^{-2\lambda_b x_n}, \quad (18)$$

where $\Gamma(n) = (n - 1)!$ when n is a positive integer.

B. Coverage Probability

A general expression for the coverage probability of multi-connectivity in C-V2X is calculated in this subsection.

Theorem 1. A vehicle is considered to be within the coverage area if its $SINR_D$ value from the nearest base station exceeds a certain threshold value t . On the other hand, if the $SINR_D$ falls below t , the vehicle is dropped from the network. Thus, the coverage probability of downlink for multi-connectivity C-V2X is

$$\begin{aligned} & \mathbb{P}(SINR_D > t) \\ &= \int_{0 < x_1 < x_2 < \dots < x_m < \infty} \zeta_{I_D}(j) \exp \left(-\frac{\mu t \sigma_d^2}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \times \\ & \quad f(x_1, x_2, \dots, x_m) dx_1 dx_2 \dots dx_m, \end{aligned} \quad (19)$$

where $j = \frac{\mu t}{\sum_{i=1}^m P_d x_i^{-\alpha_d}}$, m is the number of cooperating DBSs in the cooperative set, $\zeta_{I_D}(j)$ is the Laplace transform of random variable interference I_D evaluated at j and $\zeta_{I_D}(j)$ is

$$\zeta_{I_D}(j) = \exp \left[-2\lambda_D \int_{x_m}^{\infty} 1 - \frac{\mu}{j P_d x_i^{-\alpha_d} + \mu} dx_i \right]. \quad (20)$$

Proof: The proof of coverage probability in the downlink is

$$\begin{aligned} & \mathbb{P}(SINR_D > t) \\ & \stackrel{(a)}{=} \mathbb{P} \left(\frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} > t \right) \\ &= \mathbb{P} \left(g_d > \frac{t(I_D + \sigma_d^2)}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \\ & \stackrel{(b)}{=} \mathbb{E}_{x_i, I_D} \left[\exp \left(-\frac{\mu t (I_D + \sigma_d^2)}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \right] \\ & \stackrel{(c)}{=} \mathbb{E}_{x_i} \left[\exp \left(-\frac{\mu t \sigma_d^2}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \zeta_{I_D}(j) \right] \\ &= \int_{0 < x_1 < x_2 < \dots < x_m < \infty} \zeta_{I_D}(j) \exp \left(-\frac{\mu t \sigma_d^2}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \times \\ & \quad f(x_1, x_2, \dots, x_m) dx_1 dx_2 \dots dx_m, \end{aligned} \quad (21)$$

where (a) is obtained by substituting the expression of $SINR_D$ in Eq. (7). (b) is obtained by finding the CCDF of g_d which is exponentially distributed with parameter μ . $\zeta_{I_D}(j)$ is the Laplace transform of interference I_D in (c), and $j = \frac{\mu t}{\sum_{i=1}^m P_d x_i^{-\alpha_d}}$. Based on the definition of the Laplace transform, the derivation of $\zeta_{I_D}(j)$ is

$$\begin{aligned} \zeta_{I_D}(j) &= \mathbb{E}_{I_D} [e^{-j I_D}] \\ &\stackrel{(a)}{=} \mathbb{E}_{I_D} \left[\exp \left(-j \sum_{i \in \varphi_D^t \setminus \varphi_c} P_d g_d x_i^{-\alpha_d} \right) \right] \\ &\stackrel{(b)}{=} \mathbb{E}_{\Theta_I^d \setminus \{g_d\}} \left[\prod_{i \in \Theta_I^d} e^{-j P_d g_d x_i^{-\alpha_d}} \right] \\ &\stackrel{(c)}{=} \exp \left[-2\lambda_D \int_{x_m}^{\infty} 1 - \mathbb{E}_{g_d} [\exp(-j P_d g_d x_i^{-\alpha_d})] dx_i \right] \\ &\stackrel{(d)}{=} \exp \left[-2\lambda_D \int_{x_m}^{\infty} 1 - \frac{\mu}{j P_d x_i^{-\alpha_d} + \mu} dx_i \right], \end{aligned} \quad (22)$$

where we use $\Theta_I^d = \varphi_D^t \setminus \varphi_c$ to denote the interference DBSs, interference I_D can be obtained in Eq. (8). (b) is obtained by finding the CCDF of g_d which is exponentially distributed with parameter μ . (c) is derived from the probability generating functional (PGFL) of the PPP [36], i.e.,

$$\mathbb{E} \left(\prod f(x) \right) = \exp \left(-\lambda \int_{R^2} (1 - f(x)) dx \right). \quad (23)$$

$\mathbb{E}_{g_d} [\exp(-jP_d g_d x_i^{-\alpha_d})]$ in (d) can be derived as

$$\begin{aligned} & \mathbb{E}_{g_d} [\exp(-jP_d g_d x_i^{-\alpha_d})] \\ &= \int_0^\infty e^{-jP_d g_d x_i^{-\alpha_d}} \mu e^{-\mu g_d} dg_d \\ &= -\frac{\mu e^{-j(P_d x_i^{-\alpha_d} + \mu) g_d}}{j P_d x_i^{-\alpha_d} + \mu} \Big|_0^\infty \\ &= \frac{\mu}{j P_d x_i^{-\alpha_d} + \mu}. \end{aligned} \quad (24)$$

Since the farthest cooperation DBS is at a distance of x_m , the integration limits are from x_m to ∞ in (d). \blacksquare

C. Spectral efficiency

This subsection derives the expression of spectral efficiency for the downlink by using the tools of stochastic geometry for C-V2X in multi-connectivity. We computed the spectral efficiency in units of *nats/s/Hz* ($1 \text{ bit} = \ln(2) = 0.693 \text{ nats}$) for the typical vehicle.

Theorem 2. *The spectral efficiency of the downlink in multi-connectivity C-V2X is*

$$\tau_D = \int_{0 < x_1 < x_2 < \dots < x_m < \infty} f(x_1, x_2, \dots, x_m) \times \mathbb{E} [\ln(1 + \text{SINR}_D)] dx_1 dx_2 \dots dx_m, \quad (25)$$

where m is the number of cooperating DBSs. $\mathbb{E} [\ln(1 + \text{SINR}_D)]$ is

$$\mathbb{E} [\ln(1 + \text{SINR}_D)] = \int_{t>0} P \left[\ln \left(1 + \frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} \right) > t \right] dt, \quad (26)$$

where

$$\begin{aligned} & \mathbb{P} \left[\ln \left(1 + \frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} \right) > t \right] \\ &= \exp \left(-\frac{\beta \sigma_d^2}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \zeta_{I_D}(j), \end{aligned} \quad (27)$$

where $\beta = \mu(e^t - 1)$ and $j = \frac{\beta}{\sum_{i=1}^m P_d x_i^{-\alpha_d}}$. $\zeta_{I_D}(j)$ is the Laplace transform of interference I_D , and $\zeta_{I_D}(j)$ is the same as in Eq. (22),

$$\zeta_{I_D}(j) = \exp \left[-2\lambda_D \int_{x_m}^\infty \left(1 - \frac{\mu}{j P_d x_i^{-\alpha_d} + \mu} \right) dx_i \right]. \quad (28)$$

Proof: The proof of spectral efficiency of downlink is

$$\begin{aligned} \tau_D &= \mathbb{E} [\ln(1 + \text{SINR}_D)] \\ &= \int_{0 < x_1 < x_2 < \dots < x_m < \infty} f(x_1, x_2, \dots, x_m) \times \\ &\quad \mathbb{E} \left[\ln \left(1 + \frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} \right) \right] dx_1 dx_2 \dots dx_m \\ &\stackrel{(a)}{=} \int_{0 < x_1 < x_2 < \dots < x_m < \infty} f(x_1, x_2, \dots, x_m) \times \\ &\quad \int_{t>0} \mathbb{P} \left[\ln \left(1 + \frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} \right) > t \right] dt dx_1 dx_2 \dots dx_m, \end{aligned} \quad (29)$$

where t is the predetermined threshold. As a positive random variable X is considered, it follows that $\mathbb{E}(X)$ can be calculated as $\int_0^\infty \mathbb{P}(X > t) dt$ [14], thus the $\mathbb{E} [\ln(1 + \text{SINR}_D)]$ can be calculated in (a). Furthermore, $\mathbb{P} \left[\ln \left(1 + \sum_{i=1}^m P_d g_d x_i^{-\alpha_d} / (I_D + \sigma_d^2) \right) > t \right]$ is

$$\begin{aligned} & \mathbb{P} \left[\ln \left(1 + \frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} \right) > t \right] \\ &\stackrel{(a)}{=} \mathbb{P} \left(\frac{\sum_{i=1}^m P_d g_d x_i^{-\alpha_d}}{I_D + \sigma_d^2} > e^t - 1 \right) \\ &\stackrel{(b)}{=} \mathbb{E}_{g_d} \left[g_d > \frac{(e^t - 1)(I_D + \sigma_d^2)}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right] \\ &\stackrel{(c)}{=} \mathbb{E}_{I_D} \left[\exp \left(-\frac{\mu(e^t - 1)(I_D + \sigma_d^2)}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \right] \\ &\stackrel{(d)}{=} \exp \left(-\frac{\beta \sigma_d^2}{\sum_{i=1}^m P_d x_i^{-\alpha_d}} \right) \zeta_{I_D}(j), \end{aligned} \quad (30)$$

where (a) first solves the logarithm, then calculate the expectation of the channel gain g_d in (b), and g_d follows the exponential distribution with mean $1/\mu$ in (c). Since some variables have nothing to do with I_D , they can be treated as constants and remain unchanged in (d). For the simplicity of the formula, we use $\beta = \mu(e^t - 1)$ and $j = \frac{\beta}{\sum_{i=1}^m P_d x_i^{-\alpha_d}}$. The Laplace transform ζ_{I_D} is the same with Eq. (22) and is omitted here. \blacksquare

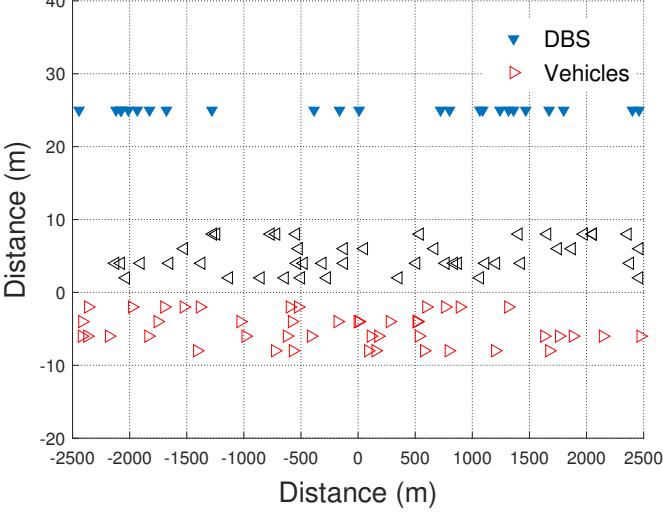


Fig. 2. Simulation scenario of multi-connectivity in C-V2X.

D. Special case: Single-connectivity

In order to compare the performance with multi-connectivity in C-V2X, this subsection focuses on the calculation of the coverage probability and spectral efficiency in a cellular single-connectivity scenario, which represents the most basic approach. In this scenario, the typical vehicle associates with the cellular base station (CBS) with the MRP.

As the single-connectivity is a special case of multi-connectivity, we model the similar channel model as in multi-connectivity scenario, and use λ_C to denote the transformed intensity λ_c of CBS ϱ_C^t after executing the procedures of random displacement, and $\lambda_C > \lambda_D$. As the CBS are distributed along the road following a 1-D PPP, the PDF of distance distribution is

$$f(x) = 2\lambda_C e^{-2\lambda_C x}, \quad (31)$$

where x is the distance between the nearest CBS and the typical vehicle.

The coverage probability of the downlink in cellular single-connectivity is

$$\mathbb{P}_{cov}(SINR_c^D > t) = \int_0^\infty 2\lambda_C e^{-\mu t \sigma_d^2 x^{\alpha_d} / P_d} e^{-2\lambda_C x} \zeta_{I_d^c}(j) dx, \quad (32)$$

where $j = \mu t x^{\alpha_d} / P_d$, the $SINR_c^D$ is

$$SINR_c^D = \frac{P_d g_d x_i^{-\alpha_d}}{I_d^c + \sigma_d^2}, \quad (33)$$

where the interference I_d^c is

$$I_d^c = \sum_{i \in \varrho_C^t} P_d g_d x_i^{-\alpha_d}. \quad (34)$$

The Laplace transform of I_d^c is

$$\zeta_{I_d^c}(j) = \exp \left[-2\lambda_C \int_x^\infty 1 - \frac{\mu}{j P_d x_i^{-\alpha_d} + \mu} dx_i \right]. \quad (35)$$

Proof: Given the similarity in the proof to that of Theorem 1, we omit the specific steps here. ■

The spectral efficiency of cellular single-connectivity for downlink is

$$\tau_c^D = \int_0^\infty f(x) E[\ln(1 + SINR_c^D) > t] dx, \quad (36)$$

where

$$\mathbb{E}[\ln(1 + SINR_c^D) > t] = \int_0^\infty e^{-\frac{\mu(e^t - 1)x^{\alpha_d}\sigma_d^2}{P_d}} \zeta_{I_d^c}(j) dt, \quad (37)$$

where $j = \mu(e^t - 1)x^{\alpha_d}/P_d$, the $\zeta_{I_d^c}(j)$ is

$$\begin{aligned} \zeta_{I_d^c}(j) = \\ \exp \left[-2\lambda_D \int_x^\infty \left(1 - \frac{\mu}{(e^t - 1)x^{\alpha_d}x_i^{-\alpha_d} + \mu} \right) dx_i \right] S \end{aligned} \quad (38)$$

Proof: The proof of spectral efficiency of downlink for cellular single-connectivity is similar to Theorem 2, the specific steps are omitted here. ■

Simulation 1: Simulation for multi-connectivity in C-V2X

Input: simulation number n , road length l , threshold t , DBS density λ_d , vehicle density λ_v ;

Output: Coverage probability CP , spectral efficiency τ_D ;

- 1 Initialize $\tau_o \leftarrow \mathbf{0}_{n \times \lambda_v l}$, $\mathbf{P} \leftarrow \mathbf{0}_{n \times \lambda_v l}$, $CP_n \leftarrow \mathbf{0}_{1 \times n}$, $\tau_n \leftarrow \mathbf{0}_{1 \times n}$
- 2 **for** $i = 1; i \leq n; i++$ **do**
- 3 Generate the locations \mathbf{m} , \mathbf{V} of DBSs and vehicles following 1-D PPP, respectively;
- 4 **for** $v = 1; v \leq \lambda_v l; v++$ **do**
- 5 Select collaborative DBSs according to Eq. (6);
- 6 Calculate $SINR_D$ of DL according to Eq. (7);
- 7 $\tau_o(i, v) = \ln(1 + SINR_D)$, $\mathbf{P}(i, v) = SINR_D$;
- 8 **end**
- 9 $CP_n(i) = \sum_{i=1}^{\lambda_v l} (\mathbf{P}(i, :) > t) / (\lambda_v l)$;
- 10 $\tau_n(i) = \sum_{i=1}^{\lambda_v l} \tau_o(i, :) / (\lambda_v l)$;
- 11 **end**
- 12 Return $\tau_D = \sum_{i=1}^n \tau_n(i) / n$, $CP = \sum_{i=1}^n CP_n(i) / n$;

V. NUMERICAL AND SIMULATION RESULTS

A two-tier communication scenario on a straight urban freeway is considered in this section. The length of the freeway is set as 30 km. The specific simulation scenario is shown in Fig. 2. We first verify the proposed theoretical derivation in previous sections over 10,000 Monte Carlo simulations of the DBSs and vehicles following 1-D PPPs. The detailed steps of the simulation are in Simulation 1. We use ‘Cellu 1’, ‘Conn 2’, and ‘Conn 3’ to abbreviate single-connectivity, dual-connectivity, and triple-connectivity, respectively, in the legends of the figures. According to [37]–[39], Table II summarizes the system simulation parameters employed in this paper.

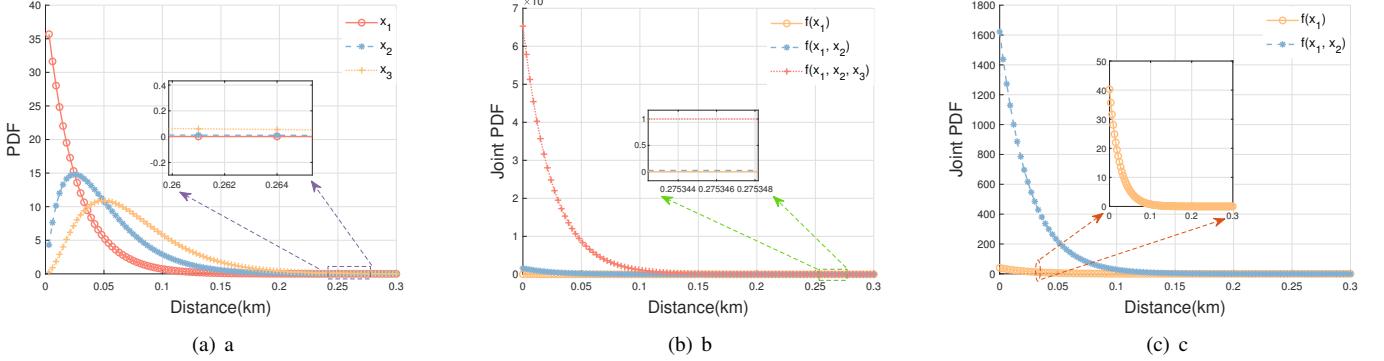


Fig. 3. The distance distributions $f(x_i)$ and joint distance distribution $f(x_1, x_2, \dots, x_m)$ under different distances. (a) Distance distribution for nearest distances x_1, x_2 and x_3 . (b) The joint distance distribution of $f(x_1), f(x_1, x_2)$ and $f(x_1, x_2, x_3)$. (c) Since $f(x_1)$ and $f(x_1, x_2)$ is much smaller than $f(x_1, x_2, x_3)$, the two functions are highlighted here.

TABLE II
MAIN PARAMETERS

Channel Parameters	Value
DBS transmitting power P_d (dBm)	23
Pathloss exponent for downlink α_d	$2.1 \sim 6$
Noise power σ_d^2 (dBm)	-96
Mean of log-normal shadowing gain (dB)	0
Std of shadowing gain for MBS (dB)	2
Simulation parameters	Value
The length of road (km)	30
The number of iteration	10,000
Density of vehicle on road λ_v (nodes/km)	20
Density of DBS λ_d (nodes/km)	$0.05 \sim 5.7$
Threshold (dB)	$0 \sim 40$

A. Joint distance distribution

Fig. 3(a) shows the distance distribution of x_1, x_2 , and x_3 . We can see that the peak is gradually moving away from the origin from x_1 to x_3 . Fig. 3(b) and Fig. 3(c) depict the joint distance distribution for $f(x_1, x_2)$ and $f(x_1, x_2, x_3)$. We can see that the peak of $f(x_1, x_2, x_3)$ is closest to the origin, followed by $f(x_1, x_2)$, and the furthest is $f(x_1)$. Compared with distance distributions in Fig. 3(a), the peak of joint distance distribution has a huge boost. The closer the distance between the peak and the origin, the better the performance. It can be observed that in single-connectivity, $f(x_1)$ exhibits better performance. Compared to a single-connectivity, a greater number of DBSs connections in multi-connectivity lead to a more significant performance improvement.

B. Coverage probability

The coverage probability variation of downlink with threshold t is illustrated in Fig. 4. It is apparent that the simulation values closely match the theoretical values, which further verifies the validity of the theoretical derivation results. The density of BS λ_c in single-connectivity is set as 3 nodes/km, and the density λ_d of DBSs in multi-connectivity is set as 6 nodes/km. Though $\lambda_c > \lambda_d$, we can see that the dual-connectivity and triple-connectivity still have a greater coverage probability than single-connectivity. This suggests that multi-connectivity performs better than cellular single-

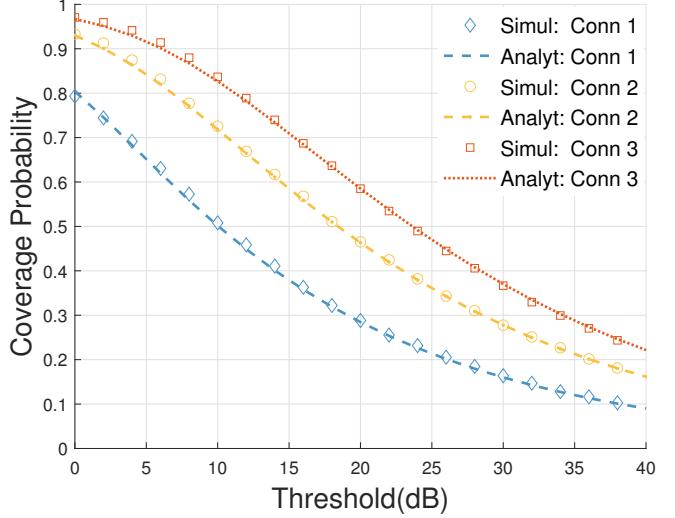


Fig. 4. Coverage probability variation with threshold t ($t \in [0, 40]$) ($\lambda_d = 3$ nodes/km, $\lambda_c = 6$ nodes/km).

connectivity in C-V2X and multi-connectivity enhances the coverage area of communications.

Fig. 5 illustrates the coverage probability as a function of path loss exponent α_d . It can be seen that the Monte Carlo simulation data and analytical data fit well. Considering the dense deployment of DBSs in the simulation, vehicles are in an interference-limited state. At this moment, the interference power will decrease in accordance with the increase of α_d , which in turn lead to a promotion of SINR. Therefore, the coverage probability will be improved even if the channel gain decrease.

For a better investigation of the impact of path loss exponent α_d on the coverage probability under different densities of DBSs, we plot Fig. 6 in a dual-connectivity scenario. As shown in Fig. 6, when the density of DBSs is in a dense deployment, the system is an interference-limited network. The distance between the signal DBSs $\in \varphi_c$ and the interference DBSs is close to the typical vehicle, so the increase of α_d leads to a greater impact on the interference signal power, resulting

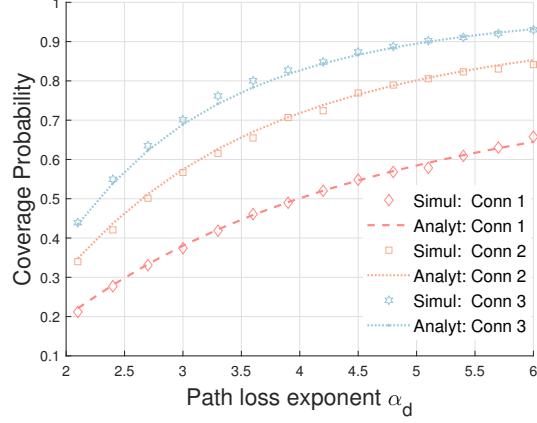


Fig. 5. The effect of path loss exponent on coverage probability($\alpha_d \in [2.1, 6]$).

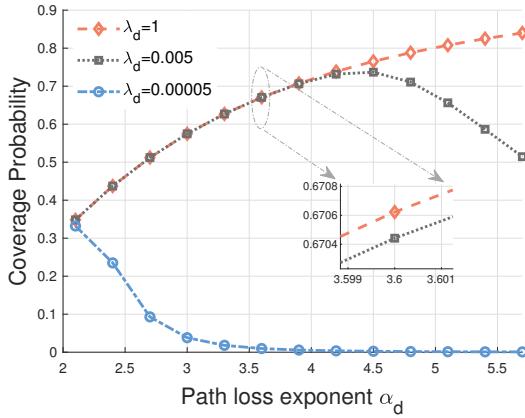


Fig. 6. Coverage probability of dual-connectivity varies with different path loss exponent in different densities of DBSs α_d (2.1 ~ 5.7).

in an increase in the coverage probability. However, when the density is low enough, the system can be considered as a noise-limited network. Both the signal DBSs and the interference DBSs are far away from the typical vehicle, so the increase of α_d has a greater impact on the receiving signal power, leading to a continuous decrease in the coverage probability. When the density λ_d is at an appropriate size, such as $\lambda_d = 0.005 \text{ nodes/km}$, the coverage probability first increases and then decreases with the increase of α_d .

The coverage probability of all cases decreases as the threshold t increases, while the difference between single-connectivity and multi-connectivity first increases and then decreases in Fig. 7. This is mainly because the coverage probability is respectively high and low at small and large thresholds, respectively. Only when the threshold value is in the middle range, the difference in coverage probability is large, and the advantage of applying multi-connectivity is also demonstrated. It can be observed that increasing the number of connected DBSs does not result in a proportional increase in the coverage probability gain. Hence, at a particular threshold, there exists a balance tradeoff between the number of corporation DBSs that are connected and the associated

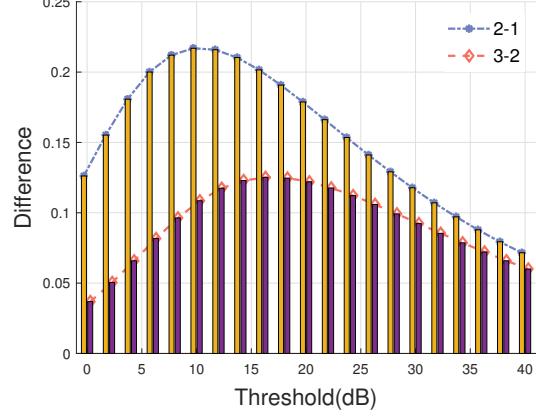


Fig. 7. Coverage probability differences variation with threshold t ($0 \sim 40 \text{ dB}$).

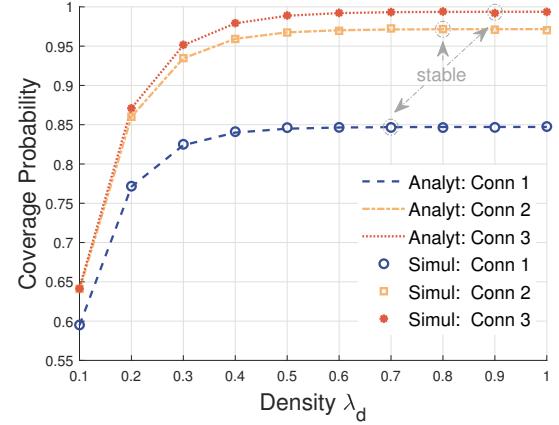


Fig. 8. Coverage probability variation with base station density λ_d ($0.1 \sim 1$ nodes/km).

cost.

As shown in Fig. 8, the coverage probability varies with the density λ_d of DBSs. The coverage probability goes up first and then stays relatively constant for both cellular single-connectivity and multi-connectivity when the density λ_d increases. It can also be seen that the growth rate of multi-connection is faster than that of single-connection, and it also reaches a stable point later. At the same time, it can be seen that the coverage probability does not increase significantly when comparing triple-connectivity to dual-connectivity. Therefore, increasing the number of cooperative BSs can improve communication coverage area, but it may also incur high costs. By observing the horizontal axis, it can be noted that the change in DBS density λ_d is relatively small in magnitude. This implies that the coverage probability is sensitive to changes in λ_d , and suggests that simply increasing λ_d does not necessarily lead to an improvement in coverage probability.

C. Spectral efficiency

The spectral efficiency varies with the path loss exponent α_d is illustrated in Fig. 9. The simulation data is represented

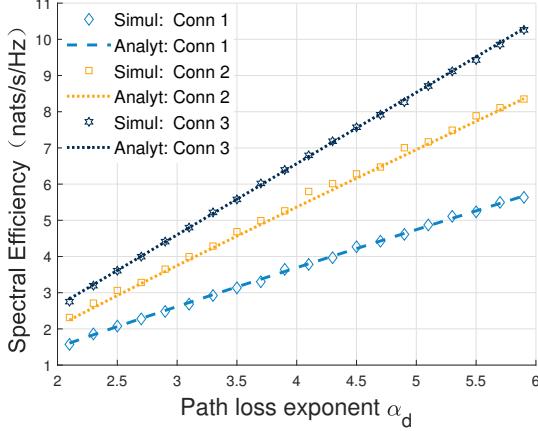


Fig. 9. Spectral efficiency variation with the path loss exponent α_d (2.1 ~ 5.9).

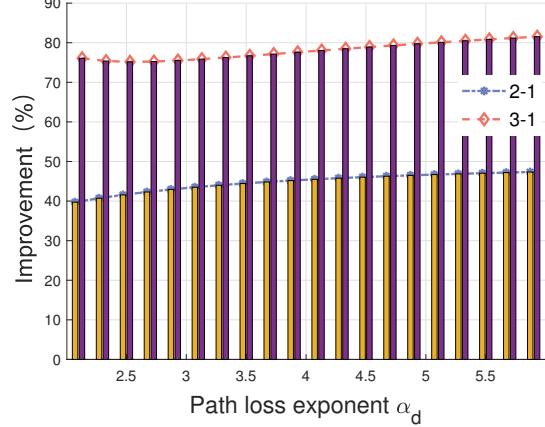


Fig. 11. Spectral efficiency percentage increase of multi-connectivity compared to single-connectivity.

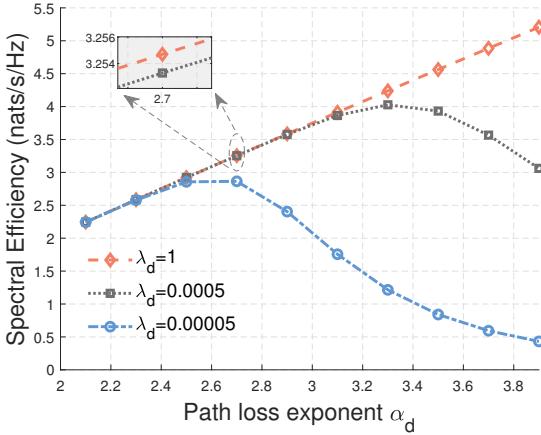


Fig. 10. Spectral efficiency of dual-connectivity varies with different path loss exponent in different densities of DBSs α_d (2.1 ~ 3.9).

by the points and the theoretical data is represented by the dashed line in Fig. 9. We can observe that the simulation data matches the theoretical data well, demonstrating the correctness of the theoretical derivation. The increase of path loss exponent leads to a gradual increase in spectral efficiency and an approximately linear relationship. The reason is that, as the dense deployment of DBSs, vehicles are in a interference-limited state, with the increase of path loss exponent α_d , the interference signals weaken more than the signals transmitted by the cooperative BSs, resulting in an increase in SINR and consequently spectral efficiency. It appears that there exists a close-to-linear relationship between the path loss exponent α_d , mainly because after dividing the received signal power $\sum_{i \in \varphi_c} P_d g_d x_i^{-\alpha_d}$ into the denominator of Eq. (9), since the thermal noise is much smaller than the received signal and thus $\sigma_d^2 / \sum_{i \in \varphi_c} P_d g_d x_i^{-\alpha_d} \approx 0$, then after logarithmic calculation, it approximates to a linear relationship. Fig. 12 depicts the spectral efficiency of dual-connectivity as a function of α_d in different densities of DBSs. Since the spectral efficiency is mainly affected by SINR, it can be seen that the trend of

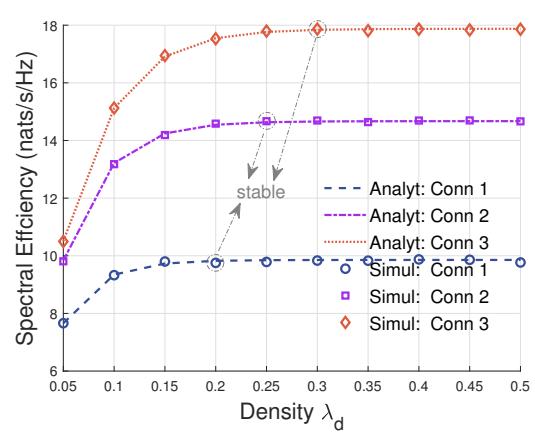


Fig. 12. Spectral efficiency as a function of base station density λ_d (0.05 ~ 0.5 nodes/km).

spectral efficiency is similar to that of coverage probability in Fig. 6 when the DBSs layout changes from extremely dense to extremely sparse.

Fig. 11 plots the spectral efficiency improvements between the multi-connectivity and single-connectivity. It can be observed that the application of multi-connectivity technology greatly improves the spectral efficiency in C-V2X. The improvement achieved by dual-connectivity can reach up to 40%, and that achieved by triple-connectivity can increase to more than 75%. With the increase of path loss exponent α_d , the performance improvement of spectral efficiency does not increase significantly. This indicates that multi-connectivity technology has a stable performance gain.

Fig. 12 illustrates the spectral efficiency varies with the DBS density λ_d . With the increase of λ_d , the spectral efficiency first improves and then remains stable. Moreover, the improvement of multi-connectivity is greater than that of single-connectivity, and the stable point is also further back. This means that multi-connectivity has a larger range of performance improvement. Similar to Fig. 8, adding too many DBSs does not continuously improve spectral efficiency. Additionally, it can be observed

that the stable point of spectral efficiency arrives earlier than the stable point of coverage probability. Thus, when increasing the density of DBSs λ_d , it is necessary to comprehensively consider the demands between spectral efficiency and coverage probability.

VI. CONCLUSION

This paper has demonstrated the potential of enhancing network performance in C-V2X by using the proposed multi-connectivity performance analysis framework. By analyzing performance indicators such as coverage probability and spectral efficiency in the downlink, this paper has provided insights into the effect of path loss exponent and the density of DBS on the system performance indicators. The extensive Monte Carlo simulations have effectively validated the proposed framework and demonstrated the effectiveness of multi-connectivity technology in enhancing the performance of C-V2X networks. The results of this paper have important implications for the research and practical applications of multi-connectivity C-V2X in the 5G and B5G era, and further investigations are warranted to explore the full potential of this technology for next-generation communication systems.

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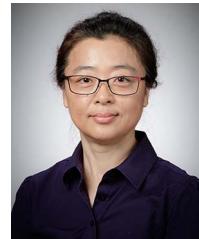
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