# R Assignment 3 - SuperLearner

#### Introduction to Causal Inference

Write-up: Please answer all questions and include relevant R code. You are encouraged to discuss the assignment in groups, but should not copy code or interpretations verbatim. You need to bring your own completed assignment to class.

#### 1 Background Story

Given the success of our previous studies, we have been hired by lead NGOs to build a prediction model for community-level severe acute malnutrition. The outcome of interest Y is the average mid-upper arm circumference (MUAC) of children aged 6-59 months in each community. In this age range, a MUAC less than 110 mm indicates severe acute malnutrition. (Other indicators of severe acute malnutrition include visible severe wasting, nutritional edema, and a standardized weight for height lower than 3 standard deviations from the median.)





Figure 1: http://www.doctorswithoutborders.co.nz/education/activities/braceletoflife/index.html

We have data on the following community-level predictor variables:

- W1 community's access to potable water (1-yes; 0-no)
- W2 whether the community is located in a stable region (1-yes; 0-no)
- W3 a measure of the community's socio-economic status (on a scale from 0-5)
- W4 the proportion of children visiting a health center in the last year for common childhood illnesses (e.g. diarrhea and pneumonia)
- W5 the number of health facilities or therapeutic feeding centers in a community (min=1, max=4)

Let  $W = \{W1, W2, W3, W4\}$  be the set of predictors.

# 2 Import and explore the data set RAssign3.csv.

- 1. Use the read.csv function to import the data set and assign it to data frame ObsData.
- 2. Use the names, tail and summary functions to explore the data.
- 3. Use the nrow function to count the number of communities in the data set. Assign this number as n.

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#### 3 Code discrete SuperLearner to select the estimator with the lowest cross-validated risk

The first step of the Super Learner algorithm (and more generally loss-based learning) is to define the target parameter  $\bar{Q}_0(W) = E_0(Y|W)$  as the minimizer of the expectation of a loss function:

$$\bar{Q}_0(W) = argmin_{\bar{Q}} E_0[L(O,\bar{Q})]$$

Since the outcome is continuous and the target parameter is the conditional mean of the outcome Y given the covariates W = (W1, W2, W3, W4, W5), we will use the L2 loss function:

$$L(O, \bar{Q}) = (Y - \bar{Q}(W))^2$$

The expectation of the loss function is called the *risk*. The second step is to define a library of candidate estimators. Suppose that before beginning the analysis you talked to subject matter experts and came up with the following candidate estimators for the conditional expectation of MUAC, given the covariates:

$$\bar{Q}_{n}^{a}(W) = \beta_{0} + \beta_{1}W1 + \beta_{2}W2 + \beta_{3}\sin(W3) + \beta_{4}W4^{2}$$

$$\bar{Q}_{n}^{b}(W) = \beta_{0} + \beta_{1}W1 + \beta_{2}W2 + \beta_{3}W4 + \beta_{4}\cos(W5)$$

$$\bar{Q}_{n}^{c}(W) = \beta_{0} + \beta_{1}W2 + \beta_{2}W3 + \beta_{3}W5 + \beta_{4}W2^{*}W5 + \beta_{5}W4^{2} + \beta_{6}\cos(W5)$$

$$\bar{Q}_{n}^{d}(W) = \beta_{0} + \beta_{1}W1 + \beta_{2}W2 + \beta_{3}W5 + \beta_{4}W1^{*}W2 + \beta_{5}W1^{*}W5 + \beta_{6}W2^{*}W5 + \beta_{7}W1^{*}W2^{*}W5$$

Therefore, our library consists of four parametric models, denoted with the superscripts a-d. We will choose the candidate estimator with the smallest cross-validated risk estimate. In other words, we are going to select the estimator with the lowest cross-validated mean squared prediction error.

- 1. Briefly discuss the motivation for using discrete SuperLearner (a.k.a. the cross-validation selector).
- 2. Create the following transformed variables and add them to data frame ObsData.
  - > sinW3<- sin(ObsData\$W3)</pre>
  - > W4sq <- ObsData\$W4\*ObsData\$W4</pre>
  - > cosW5 <- cos(ObsData\$W5)</pre>
- 3. Split the data into V = 20 folds. With n = 5000 observations total, we want n/20 = 250 observations in each fold. Create the vector Fold and add it to the data frame ObsData.
- 4. Create an empty matrix CV.risk with 20 rows and 4 columns for each algorithm, evaluated at each fold.
- 5. Use a for loop to fit each estimator on the training set (19/20 of the data); predict the expected MUAC for the communities in the validation set (1/20 of the data), and evaluate the cross-validated risk.
  - (a) Since each fold needs to serve as the training set, have the for loop run from V is 1 to 20. First, the observations in Fold = 1 will serve as the validation set and other 4750 observations as the training set. Then the observations in Fold = 2 will be the validation set and the other 4750 observations as the training set... Finally, the observations in Fold = 20 will be the validation set and the other 4750 observations as the training set.
  - (b) Create the validation set as a data frame valid, consisting of observations with Fold equal to V.
  - (c) Create the training set as a data frame train, consisting of observations with Fold not equal to V.
  - (d) Use glm to fit each algorithm on the training set. Be sure to specify data=train.

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(e) For each algorithm, predict the average MUAC for each community in the validation set. Be sure to specify the type='response' and newdata=valid.

- (f) Estimate the cross-validated risk for each algorithm with the L2 loss function. Take the mean of the squared differences between the observed outcomes Y in the validation set and the predicted outcomes. Assign the cross-validated risks as a row in the matrix CV.risk.
- 6. Select the algorithm with the lowest average cross-validated risk. Hint: use the colMeans function.
- 7. Fit the chosen algorithm on all the data.
- 8. Can we do better?

# 4 Use the SuperLearner package to build the best combination of algorithms.

- 1. Load the SuperLearner package with the library function and set the seed to 252.
- 2. Use the source function to load script file Rassign3.Fa2012.Wrappers.R, which includes the wrapper functions for the *a priori*-specified parametric regressions.
- 3. Specify the algorithms to be included in SuperLearner's library. Create a vector SL.library of the following algorithms:

```
> SL.library<- c('SL.glm.EstA', 'SL.glm.EstB', 'SL.glm.EstC', 'SL.glm.EstD',
+ 'SL.ridge','SL.rpartPrune', 'SL.polymars', 'SL.mean')</pre>
```

Here, we are expanding the library in two ways: (1) by including these new algorithms, and (2) by searching for the best convex combination of algorithms.

Bonus: Very briefly describe the algorithms corresponding to SL.ridge, SL.rpartPrune, SL.polymars and SL.mean.

- 4. Create data frame X with the predictor variables. Include the original predictor variables and the transformed variables.
- 5. Run the SuperLearner function. Be sure to specify the outcome Y, the predictors X and the library SL.library. Also include cvControl=list(V=20) in order to get 20-fold cross-validation.
- 6. Explain the output to relevant policy makers and stake-holders. What do the columns Risk and Coef mean? Are the cross-validated risks from SuperLearner close to those obtained by your code?

# 5 Implement CV.SuperLearner

- 1. Explain why we need CV. SuperLearner.
- 2. Run CV.SuperLearner. Again be sure to specify the outcome Y, predictors X, library SL.library, folds V=20 and cvControl=list(V=20). This might take a couple minutes.

```
> CV.SL.out<- CV.SuperLearner(Y=ObsData$Y, X=X, SL.library=SL.library, V=20,
+ cvControl=list(V=20))</pre>
```

This function is partitioning the data into  $V^*=20$  folds, running the whole SuperLearner algorithm in each training set (19/20 of the data), evaluating the performance on the corresponding validation set (1/20 of the data), and rotating through the folds. Each training set will itself be partitioned into V=20 folds in order to run SuperLearner.

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3. Explore the output. For example, if the output object from CV.SuperLearner was CV.SL.out, run the following code.

```
> # summary of the output of CV.SuperLearner
> summary(CV.SL.out)
> #
> # returns the output for each call to SuperLearner
> CV.SL.out$AllSL
> #
> # condensed version of the output from CV.SL.out$AllSL with only the coefficients
> # for each SuperLearner run
> CV.SL.out$coef
> #
> # returns the algorithm with lowest CV risk (discrete SuperLearner) at each step.
> CV.SL.out$whichDiscrete
```

Only include the output from the summary function in your write-up, but comment on the other output.

### 6 Bonus! -Completely Optional

- 1. Try adding more algorithms to the SuperLearner library.
- 2. Try writing your own wrapper function. The following code will give you a template.

```
> SL.template

function (Y, X, newX, family, obsWeights, id, ...)
{
    if (family$family == "gaussian") {
      }
    if (family$family == "binomial") {
      }
    pred <- numeric()
    fit <- vector("list", length = 0)
      class(fit) <- c("SL.template")
      out <- list(pred = pred, fit = fit)
      return(out)
}
</pre>

<environment: namespace:SuperLearner>
```