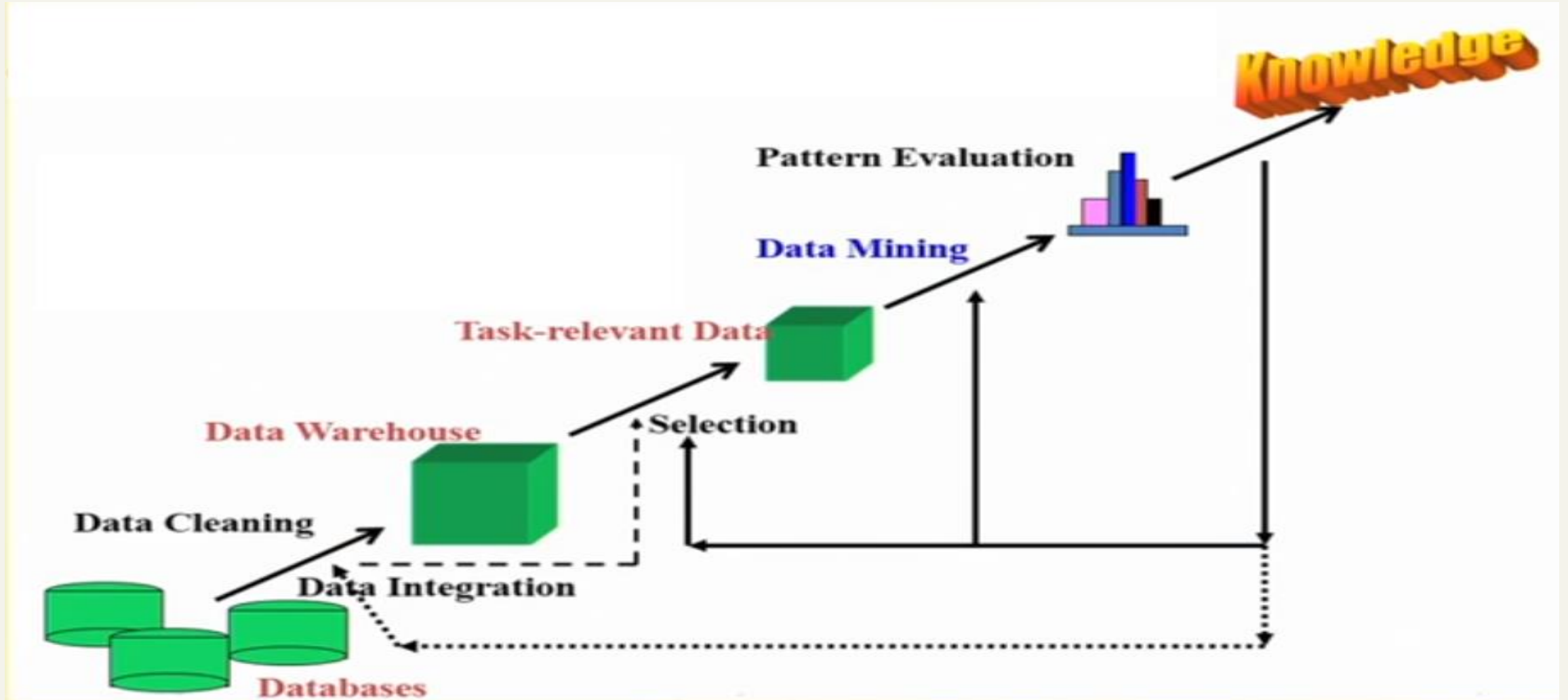


# Data Pre-processing

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# Knowledge Discovery in Data: Process



# What is Data?

- a collection of number assigned as value to quantitative variable and/ or characters assigned as value to qualitative variables, or
- collection of records and their attributes
- An attribute is a characteristic of an object
  - Example: Colours of yes, temperature, etc.
  - Attribute is also known as variable, feature, characteristics, fields, etc.
- A collection of attributes describe an object
  - Object is also known as record, point, case, sample, entity or instances

| Attributes |        |                |                |       |
|------------|--------|----------------|----------------|-------|
| Tid        | Refund | Marital Status | Taxable Income | Cheat |
| 1          | Yes    | Single         | 125K           | No    |
| 2          | No     | Married        | 100K           | No    |
| 3          | No     | Single         | 70K            | No    |
| 4          | Yes    | Married        | 120K           | No    |
| 5          | No     | Divorced       | 95K            | Yes   |
| 6          | No     | Married        | 60K            | No    |
| 7          | Yes    | Divorced       | 220K           | No    |
| 8          | No     | Single         | 85K            | Yes   |
| 9          | No     | Married        | 75K            | No    |
| 10         | No     | Single         | 90K            | Yes   |

# Types of Attributes

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- Nominal
  - Used to assign individual cases to categories
  - Example: eye colour, ID number, Zip code, etc
- Ordinal
  - Used to rank order cases
  - Example: ranking (eg. movie on scale of 1-10), height (tall, medium, short), grades
- Interval
  - Example: Calendar dates, longitude, latitude
- Ratio
  - Same as interval variable but they have a “true zero”
  - Example: time, length, population, age

# Properties of Attribute values

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- The type of an attributes depends on which of the following properties it possess:
  - Distinctness:  $= \neq$
  - Order:  $< >$
  - Addition:  $+ -$
  - Multiplication:  $* /$
- Nominal: Distinctness
- Ordinal: Distinctness, Order
- Interval: Distinctness, Order, Addition
- Ratio: all 4 properties

# Discrete and Continuous Attributes

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## ■ Discrete Attribute

- Has only a finite or countable infinite set of values
- Examples: zip codes, counts, or the set of words in a collection of documents
- Often represented as integer variables.
- Note: Binary attributes are special cases of discrete attributes

## ■ Continuous Attribute

- Has real numbers as attribute values
- Examples: temperature, height, or weight.
- Practically, real values can only be measured and represented using a finite number of digits.
- Continuous attributes are typically represented as floating-point variable

# Type of data sets

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- Record Data
  - Data Matrix
  - Transaction data
- Graph Data
  - World wide web
  - Molecular structure
- Ordered
  - Spatial data
  - Temporal data
  - Sequential data
  - Genetic sequence data

# Record Data

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- Data that consists of a collection of records, each of which consists of fixed set of attributes

| <i>Tid</i> | Refund | Marital Status | Taxable Income | Cheat |
|------------|--------|----------------|----------------|-------|
| 1          | Yes    | Single         | 125K           | No    |
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# Data Matrix

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- If data objects have the same fixed set of numeric attributes, then the data objects can be thought of as points in a multidimensional space, where each dimension represents a distinct attribute
- Such data set can be represented by an  $m$  by  $n$  matrix, where there are  $m$  rows, one for each object, and  $n$  columns, one for each attribute

# Data Matrix Example for Documents

- Each document becomes a `term' vector,
  - each term is a component (attribute) of the vector,
  - the value of each component is the number of times the corresponding term occurs in the document.

|            | team | coach | play | ball | score | game | win | lost | timeout | season |
|------------|------|-------|------|------|-------|------|-----|------|---------|--------|
| Document 1 | 3    | 0     | 5    | 0    | 2     | 6    | 0   | 2    | 0       | 2      |
| Document 2 | 0    | 7     | 0    | 2    | 1     | 0    | 0   | 3    | 0       | 0      |
| Document 3 | 0    | 1     | 0    | 0    | 1     | 2    | 2   | 0    | 3       | 0      |

# Transaction Data

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- A typical type of record data, then
  - Each record (transaction) involves a set of items

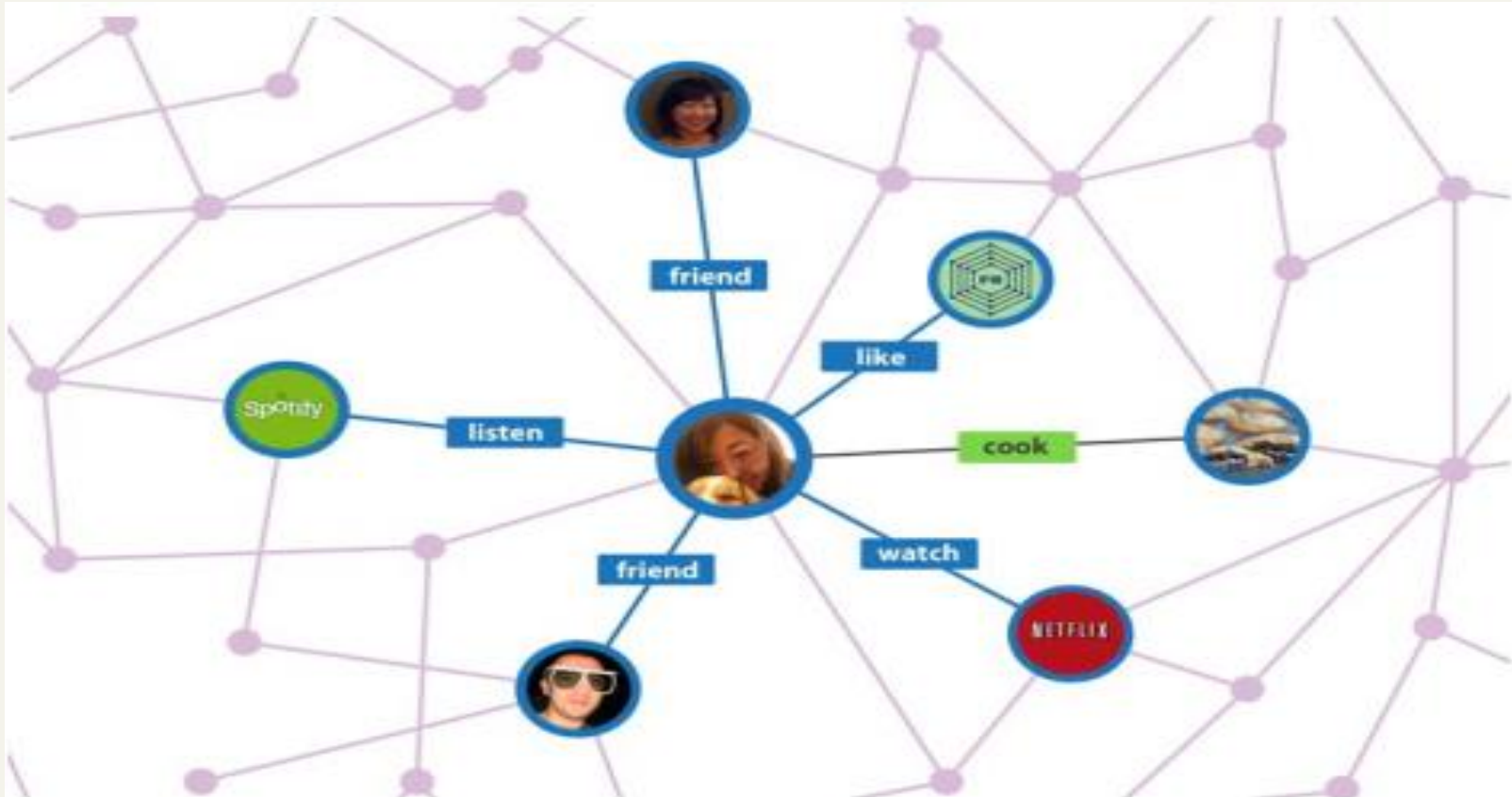
| <i>TID</i> | <i>Items</i>              |
|------------|---------------------------|
| 1          | Bread, Coke, Milk         |
| 2          | Beer, Bread               |
| 3          | Beer, Coke, Diaper, Milk  |
| 4          | Beer, Bread, Diaper, Milk |
| 5          | Coke, Diaper, Milk        |

**Market-Basket Dataset**

# Graph data

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Example: Facebook graph and HTML links



# Ordered data

- Genetic sequence data

| Species | Alignment of Amino Acid Sequences of $\beta$ -globin |            |             |            |            |            |
|---------|--|------------|-------------|------------|------------|------------|
| Human   | 1  | VHLTPEEKSA | VTALWGKLVNV | DEVGGEALGR | LLVVYPWTQR | FFESFGDLST |
| Monkey  | 1  | VHLTPEEKNA | VTTLWGKLVNV | DEVGGEALGR | LLLVYPWTQR | FFESFGDLSS |
| Gibbon  | 1  | VHLTPEEKSA | VTALWGKLVNV | DEVGGEALGR | LLVVYPWTQR | FFESFGDLST |
| Human   | 51   | PDAVMGNPKV | KAHGKKVLGA  | FSDGLAHLDN | LKGTFAQLSE | LHCDKLHVDP |
| Monkey  | 51   | PDAVMGNPKV | KAHGKKVLGA  | FSDGLNHLDN | LKGTFAQLSE | LHCDKLHVDP |
| Gibbon  | 51   | PDAVMGNPKV | KAHGKKVLGA  | FSDGLAHLDN | LKGTFAQLSE | LHCDKLHVDP |
| Human   | 101  | ENFRLLGNVL | VCVLAHHFGK  | EFTPPVQAAY | QKVVAGVANA | LAHKYH     |
| Monkey  | 101  | ENFKLLGNVL | VCVLAHHFGK  | EFTPQVQAAY | QKVVAGVANA | LAHKYH     |
| Gibbon  | 101  | ENFRLLGNVL | VCVLAHHFGK  | EFTPQVQAAY | QKVVAGVANA | LAHKYH     |

# Data Quality

- What kind of data quality problems?
- How can we detect the problem with the data?
- What can we do about these problem?
- Examples of data quality problems:
  - Missing values
  - Noise and outliers
  - Duplicate data

A mistake or a millionaire?

Missing values

Inconsistent duplicate entries

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| 5          | No     | Divorced       | 10000K         | Yes   |
| 6          | No     | NULL           | 60K            | No    |
| 7          | Yes    | Divorced       | 220K           | NULL  |
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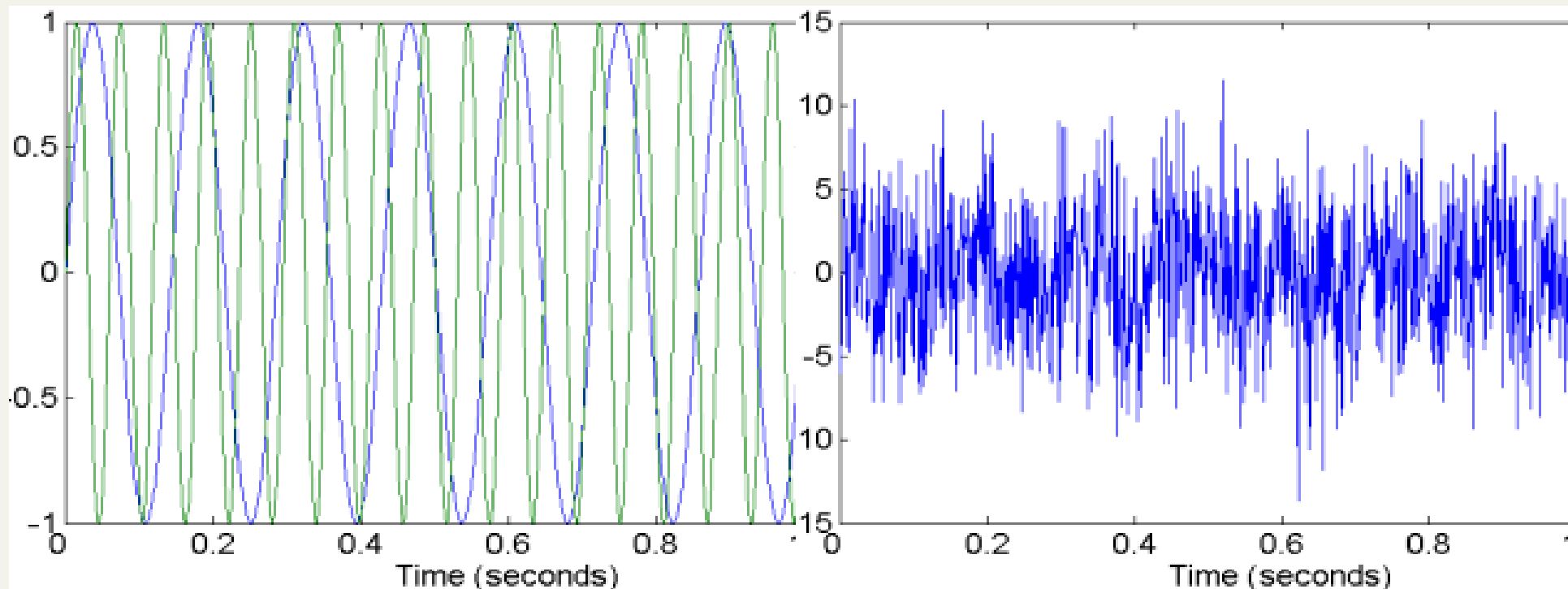
# Data Quality: Missing Values

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- Reasons for missing values
  - Information is not collected  
(e.g., people decline to give their age and weight)
  - Attributes may not be applicable to all cases  
(e.g., annual income is not applicable to children)
- Handling missing values
  - Eliminate Data Objects
  - Estimate Missing Values
  - Ignore the Missing Value During Analysis
  - Replace with all possible values (weighted by their probabilities)

# Data Quality: Noise

- Noise refers to modification of original values
  - Examples: distortion of a person's voice when talking on

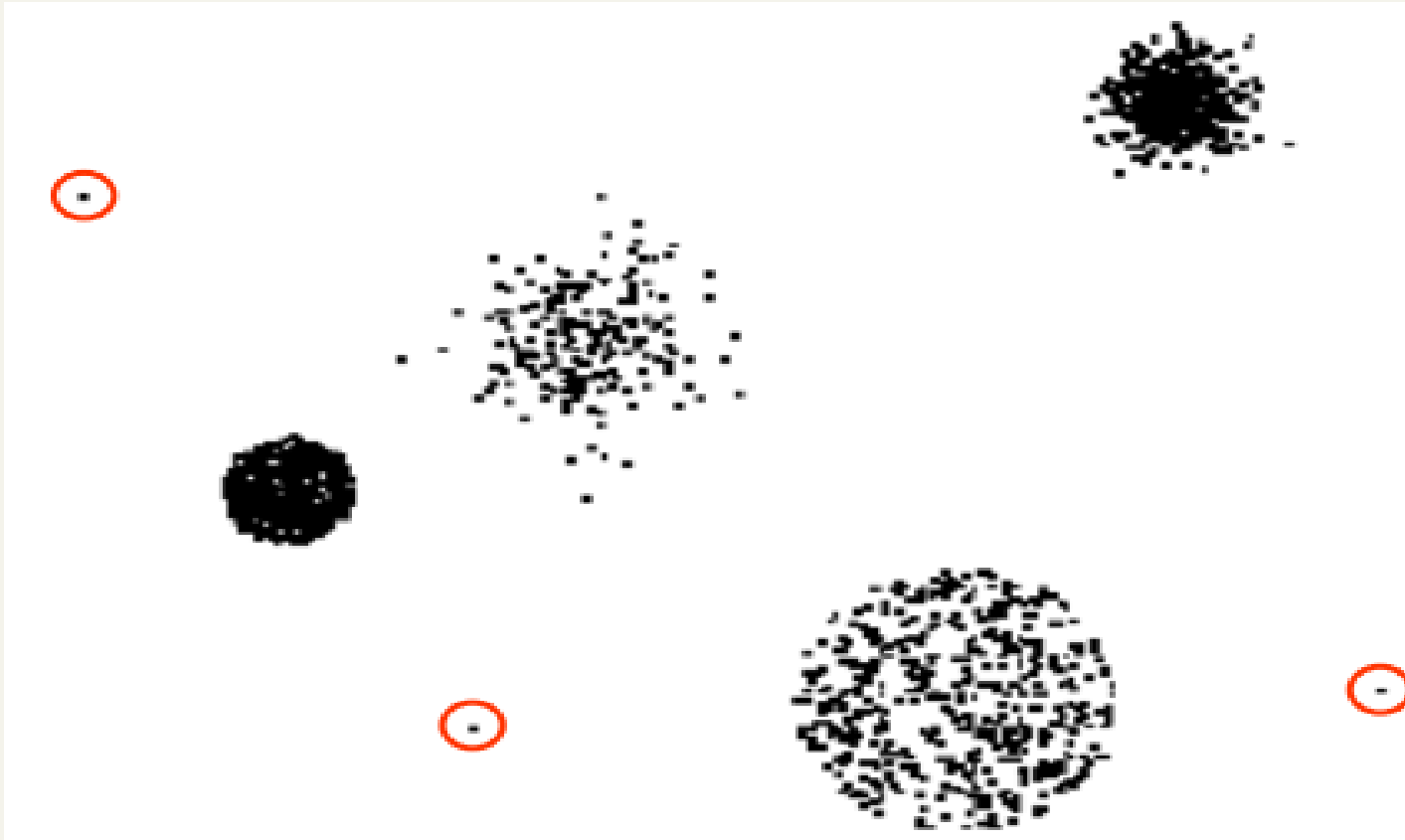




# Data Quality: Outliers

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- Outliers are data objects with characteristics that are considerably different than most of the other data objects in the data set



# Data Quality: Duplicate Data

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- Data set may include data objects that are duplicates, or almost duplicates of one another
  - Major issue when merging data from heterogenous sources
- Examples:
  - Same person with multiple email addresses
- Data cleaning
  - Process of dealing with duplicate data issues

# Data Preprocessing

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- Imputation
- Outlier management
- One hot encoding
- Feature selection
- Filter and Wrapper approach

# Imputation (filling in) of missing data

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- Imputation is performed using a number of different algorithms, which can be subdivided into single and multiple imputation methods.
- Single imputation methods
  - a missing value is imputed by a single value
- Multiple-imputation methods
  - several likelihood- ordered choices for imputing the missing value are computed and one “best” value is selected.

- **Single imputation**
  - Mean imputation
  - Hot deck imputation
- **Multiple imputation**

# Single imputation

Contd...

## Mean imputation

- Mean imputation, also called unconditional mean imputation, is a widely used imputation method
- Mean imputation assumes that the mean of a variable is the best estimate for any case that has missing information on this variable
- For **continuous variable**, each missing value is imputed with the mean of known values for the same variable
- For **categorical variable**, the missing values of are the mode of the observed values of same variable

| Case | Var1 | Var2 | Var3 |
|------|------|------|------|
| 1    | 9    | 8    | 8    |
| 2    | 7.44 | 7    | 6    |
| 3    | 8    | 5    | 6    |
| 4    | 7    | 4    | 5    |
| 5    | 9    | 5    | 7    |
| 6    | 8    | 8    | 9    |
| 7    | 6    | 7    | 6    |
| 8    | 5    | 9    | 7    |
| 9    | 7    | 8    | ?    |
| 10   | 8    | 8    | 7    |

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## ■ *Advantages*

- fast,
- simple,
- ease to implement, and
- no cases are excluded

## ■ *Limitations*

- underestimation of the population variance
- thus a small standard error
- possibility of Type I error.

# Single imputation

Contd...

## Hot deck imputation

- Hot-deck imputation is a procedure where the imputed values come from other cases in the same data set
- for each object that contains missing values, the most similar object is found, and the missing values are imputed from that object

| Case | Var1 | Sex | Var2 | Var3 |
|------|------|-----|------|------|
| 1    | 9    | F   | 8    | 8    |
| 2    | 8.25 | F   | 7    | 6    |
| 3    | 8    | F   | 5    | 6    |
| 4    | 7    | F   | 4    | 5    |
| 5    | 9    | F   | 5    | 7    |
| 6    | 8    | M   | 8    | 9    |
| 7    | 6    | M   | 7    | 6    |
| 8    | 5    | M   | 9    | 7    |
| 9    | 7    | M   | 8    | ?    |
| 10   | 8    | M   | 8    | 7    |



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- *Advantages*

- preserves the population distribution
- it is better than mean imputation

- *Limitations*

- distort correlations and covariances

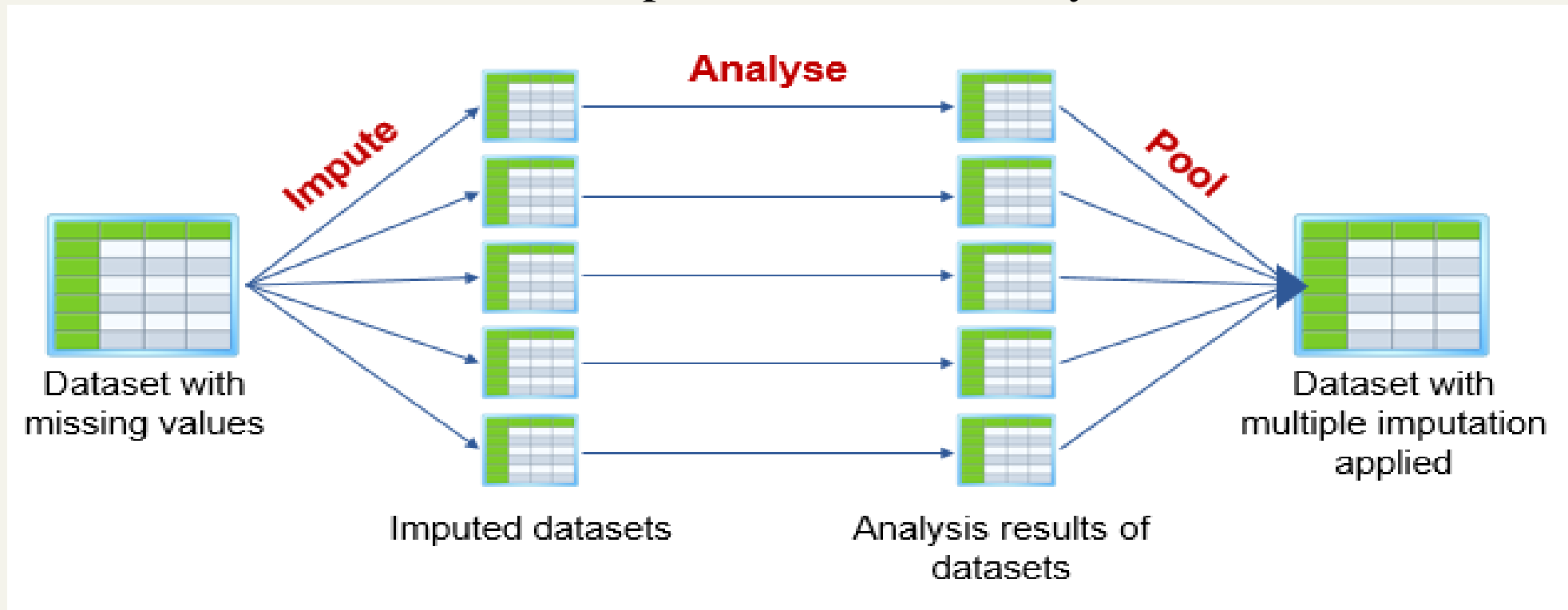
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## **Other type of Single imputation**

- Regression imputation
- Cold-deck imputation
- Expectation Maximisation (EM)
- Sequential imputation
- Last observation carried forward
- Worst case and Best case imputation

# Multiple imputation

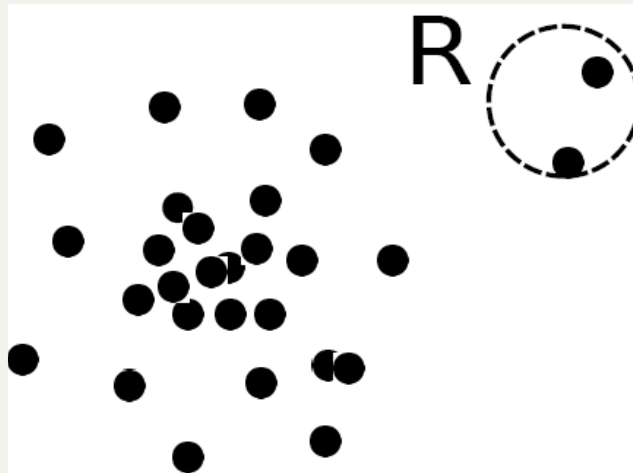
- The idea of Multiple Imputation is to replace each missing value with multiple acceptable values that represent a distribution of possibilities.
- This results in a number of complete datasets (usually 3-10):



# Outlier management

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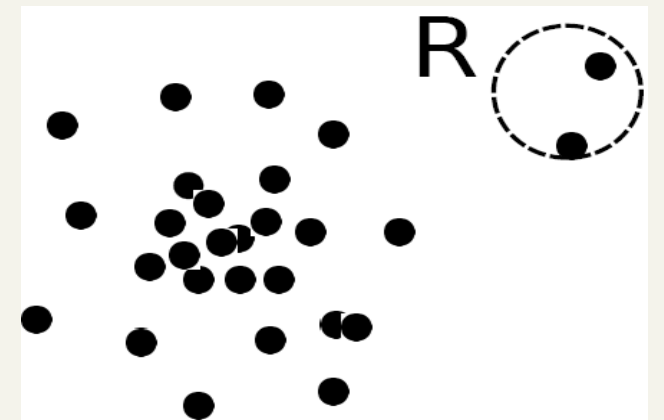
- **Outlier:** A data object that **deviates significantly** from the normal objects as if it were **generated by a different mechanism**
  - Ex.: Unusual credit card purchase
- Outliers are different from the noise data
  - Noise is random error or variance in a measured variable
  - Noise should be removed before outlier detection



# Types of Outliers

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- Three kinds:
  - *Global*,
  - *Contextual*
  - *Collective*
- **Global outlier** (or point anomaly)
  - Object is  $O_g$  if it significantly deviates from the rest of the data set
  - Ex. Intrusion detection in computer networks
  - Issue: Find an appropriate measurement of deviation



# Types of Outliers

Contd...

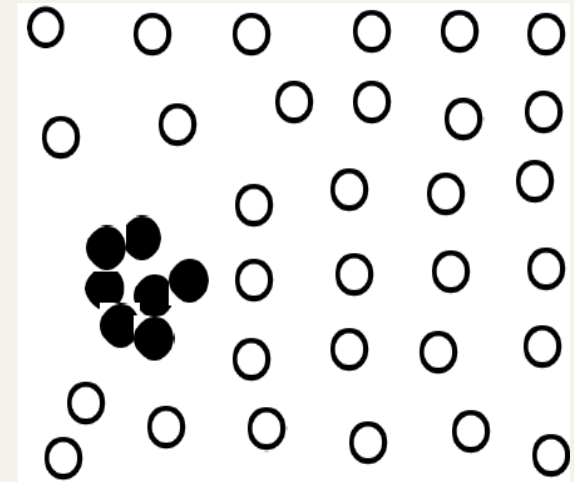
- **Contextual outlier** (or *conditional outlier*)
  - Object is  $O_c$  if it deviates significantly based on a selected context
  - Ex. 40° C in Mathura: outlier? (depending on summer or winter?)
  - Attributes of data objects should be divided into two groups to detect  $O_c$ 
    - Contextual attributes: defines the context, e.g., time & location
    - Behavioral attributes: characteristics of the object, used in outlier evaluation, e.g., temperature, pressure, humidity
  - Issue: How to define or formulate meaningful context?

# Types of Outliers

Contd...

## ■ Collective Outliers

- A subset of data objects *collectively* deviate significantly from the whole data set, even if the individual data objects may not be outliers
- Applications: E.g., *intrusion detection*:
  - When a number of computers keep sending denial-of-service packages to each other
- Detection of collective outliers
  - Consider not only behavior of individual objects, but also that of groups of objects
  - Need to have the background knowledge on the relationship among data objects, such as a distance or similarity measure on objects.



# Outlier Detection

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- Two ways to categorize outlier detection methods:
  - Based on whether user-labeled examples of outliers can be obtained:
    - Supervised,
    - Unsupervised, and
    - Semi-supervised methods
  - Based on assumptions about normal data and outliers:
    - Statistical,
    - proximity-based, and
    - clustering-based methods



# Supervised Methods

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- Modeling outlier detection as a classification problem
- Methods for Learning a classifier for outlier detection effectively:
  - Model normal objects & report those not matching the model as outliers, or
  - Model outliers and treat those not matching the model as normal
- Challenges
  - Imbalanced classes, i.e., outliers are rare

# Unsupervised Methods

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- Assume the normal objects are somewhat ``clustered'' into multiple groups, each having some distinct features
- An outlier is expected to be far away from any groups of normal objects
- Weakness: Cannot detect collective outlier effectively
  - Normal objects may not share any strong patterns, but the collective outliers may share high similarity in a small area

# Semi-Supervised Methods

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- In many applications, the number of labeled data is often small: Labels could be on outliers only, normal objects only, or both
- If some labeled normal objects are available
  - Use the labeled examples and the proximate unlabeled objects to train a model for normal objects
  - Those not fitting the model of normal objects are detected as outliers

# Statistical Methods

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- Statistical methods (also known as model-based methods) assume that the normal data follow some statistical model
  - The data not following the model are outliers.
- Methods are divided into two categories: *parametric* vs. *non-parametric*
- **Parametric method**
  - Assumes that the normal data is generated by a parametric distribution with parameter  $\theta$
  - The probability density function of the parametric distribution  $f(x, \theta)$  gives the probability that object  $x$  is generated by the distribution
- **Non-parametric method**
  - Not assume an a-priori statistical model and determine the model from the input data
  - Not completely parameter free but consider the number and nature of the parameters are flexible and not fixed in advance
  - Examples: histogram

# Parametric Methods I: Univariate Outliers Based on Normal Distribution

- Often assume that data are generated from a normal distribution, learn the parameters from the input data, and identify the points with low probability as outliers
- Ex: Avg. temp.: {24.0, 28.9, 28.9, 29.0, 29.1, 29.1, 29.2, 29.2, 29.3, 29.4}
  - Use the maximum likelihood method to estimate  $\mu$  and  $\sigma$

$$\hat{\mu} = \bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\hat{\sigma}^2 = \frac{1}{n} \sum_{i=1}^n (x_i - \bar{x})^2$$

- For the above data with  $n = 10$ , we have  $\hat{\mu} = 28.61$   $\hat{\sigma} = \sqrt{2.29} = 1.51$

$\mu \pm 3\sigma$  region contains 99.7% data

- Consider the value 24
- $28.61 - 3*1.51 = 24.08$
- So, 24 is an outlier

# Statistical Methods – Box Plot

- Values less than  $Q1 - 1.5 \times IQR$  and greater than  $Q3 + 1.5 \times IQR$  are outliers
- Consider the following dataset:
- 10.2, 14.1, 14.4, 14.4, 14.5, 14.5, 14.6, 14.7, 14.7, 14.7, 14.9, 15.1, 15.9, 16.4

Here,

$$Q2(\text{median}) = 14.6$$

$$Q1 = 14.4$$

$$Q3 = 14.9$$

$$IQR = Q3 - Q1 = 14.9 - 14.4 = 0.5$$

Outliers will be any points:

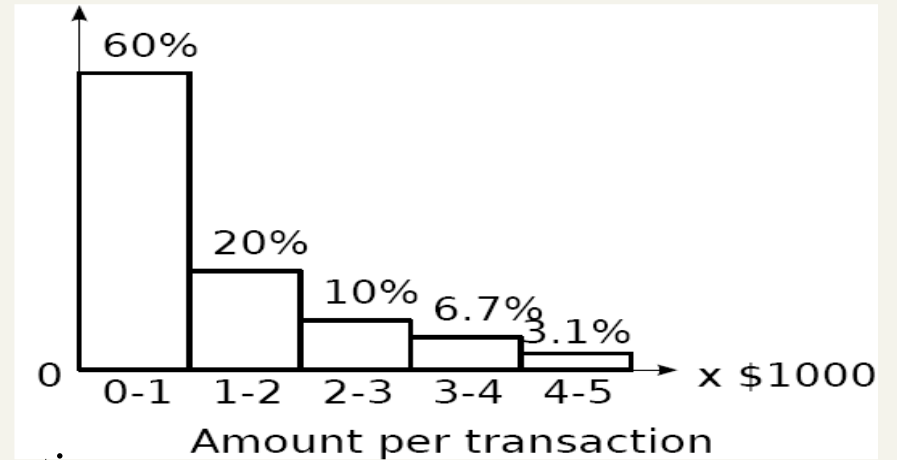
$$\text{below } Q1 - 1.5 \times IQR = 14.4 - 0.75 = 13.65 \text{ or}$$

$$\text{above } Q3 + 1.5 \times IQR = 14.9 + 0.75 = 15.65$$

So, the outliers are at 10.2, 15.9, and 16.4.

# Non-Parametric Methods: Detection Using Histogram

- The model of normal data is learned from the input data without any *a priori* structure.
- Often makes fewer assumptions about the data, and thus can be applicable in more scenarios
- Outlier detection using histogram:
  - Figure shows the histogram of purchase amounts in transactions
  - A transaction in the amount of \$7,500 is an outlier, since only 0.2% transactions have an amount higher than \$5,000
- Problem: Hard to choose an appropriate bin size for histogram
  - Too small bin size → normal objects in empty/rare bins, false positive
  - Too big bin size → outliers in some frequent bins, false negative



# Statistical Methods – Other Methods

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- Grubbs test
- Mahalanobis distance
- Chi Square test



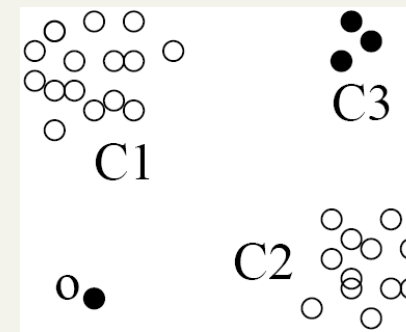
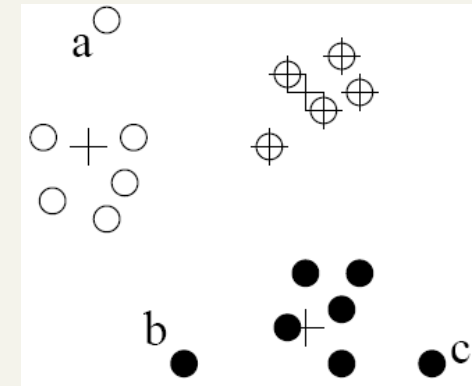
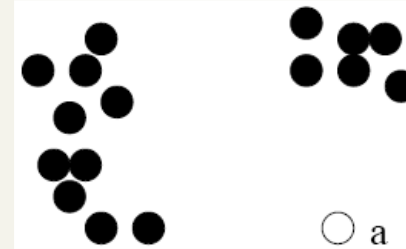
# Proximity-Based Methods

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- An object is an outlier if the nearest neighbors of the object are far away, i.e., the **proximity** of the object **significantly deviates** from the proximity of most of the other objects in the same data set
- Two types of proximity-based outlier detection methods
  - **Distance-based outlier detection:** An object  $o$  is an outlier if its neighborhood does not have enough other points
  - **Density-based outlier detection:** An object  $o$  is an outlier if its density is relatively much lower than that of its neighbors

# Clustering-Based Outlier Detection

- An object is an outlier if
  - it does not belong to any cluster,
  - there is a large distance between the object and its closest cluster , or
  - it belongs to a small or sparse cluster



# Clustering-Based Method: Strength and Weakness

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## ■ Strength

- Detect outliers without requiring any labeled data
- Work for many types of data
- Clusters can be regarded as summaries of the data
- Once the cluster are obtained, need only compare any object against the clusters to determine whether it is an outlier (fast)

## ■ Weakness

- Effectiveness depends highly on the clustering method used—they may not be optimized for outlier detection
- High computational cost: Need to first find clusters
- A method to reduce the cost: Fixed-width clustering
  - A point is assigned to a cluster if the center of the cluster is within a pre-defined distance threshold from the point
  - If a point cannot be assigned to any existing cluster, a new cluster is created and the distance threshold may be learned from the training data under certain conditions