

2. 1 $\forall x, \forall y. (Horse(x) \wedge Dog(y) \rightarrow Faster(x, y))$
- 2 $\exists y. [Greyhound(y) \wedge \forall z. (Rabbit(z) \rightarrow Faster(y, z))]$
- 3 $\forall y. (Greyhound(y) \rightarrow Dog(y))$ (background knowledge)
- 4 $\forall x, \forall y, \forall z. (Faster(x, y) \wedge Faster(y, z) \rightarrow Faster(x, z))$ (background knowledge)
- 5 $\neg \forall x, \forall y. (Horse(x) \wedge Rabbit(y) \rightarrow Faster(x, y))$ (negated conclusion)

Clausal Form:

- 1 $\forall x, \forall y. (Horse(x) \wedge Dog(y) \rightarrow Faster(x, y))$
 $\forall x, \forall y. (\neg (Horse(x) \wedge Dog(y)) \vee Faster(x, y))$
 $\forall x, \forall y. (\neg Horse(x) \vee \neg Dog(y) \vee Faster(x, y))$
 $\therefore \{ \neg Horse(x), \neg Dog(y), Faster(x, y) \}$
- 2 $\{ \neg Rabbit(z), Faster(Rocky, z) \}$
- 3 $\{ \neg Greyhound(y), Dog(y) \}$
- 4 $\forall x, \forall y, \forall z. (Faster(x, y) \wedge Faster(y, z) \rightarrow Faster(x, z))$
 $\forall x, \forall y, \forall z. (\neg (Faster(x, y) \wedge Faster(y, z)) \vee Faster(x, z))$
 $\forall x, \forall y, \forall z. (\neg Faster(x, y) \vee \neg Faster(y, z) \vee Faster(x, z))$
 $\therefore \{ \neg Faster(x, y), \neg Faster(y, z), Faster(x, z) \}$
5. $\{ Greyhound(Rocky) \}$

Negate the conclusion:

- $$\neg \forall x, \forall y. (Horse(x) \wedge Rabbit(y) \rightarrow Faster(x, y))$$
- $$\neg \forall x, \forall y. (\neg (Horse(x) \wedge Rabbit(y)) \vee Faster(x, y))$$
- $$\neg \forall x, \forall y. (\neg Horse(x) \vee \neg Rabbit(y) \vee Faster(x, y))$$
- $$\exists x \exists y. (Horse(x) \wedge Rabbit(y) \wedge \neg Faster(x, y))$$
- $$Horse(Foo) \wedge Rabbit(Bar) \wedge \neg Faster(Foo, Bar)$$
- $$\{ Horse(Foo) \}$$
- $$\{ Rabbit(Bar) \}$$
- $$\{ \neg Faster(Foo, Bar) \}$$

Resolution:

1	$\{\neg \text{Horse}(x), \neg \text{Dog}(y), \text{Faster}(x, y)\}$	premise
2	$\{\neg \text{Rabbit}(z), \text{Faster}(\text{Rocky}, z)\}$	premise
3	$\{\neg \text{Greyhound}(y), \text{Dog}(y)\}$	premise
4	$\{\neg \text{Faster}(x, y), \neg \text{Faster}(y, z), \text{Faster}(x, z)\}$	premise
5	$\{\text{Greyhound}(\text{Rocky})\}$	premise
6	$\{\text{Horse}(\text{Foo})\}$	premise
7	$\{\text{Rabbit}(\text{Bar})\}$	premise
8	$\{\neg \text{Faster}(\text{Foo}, \text{Bar})\}$	premise
9	$\{\neg \text{Dog}(y), \text{Faster}(\text{Foo}, y)\}$	1, 6
10	$\{\neg \text{Greyhound}(y), \text{Faster}(\text{Foo}, y)\}$	3, 9
11	$\{\text{Faster}(\text{Foo}, \text{Rocky})\}$	5, 10
12	$\{\neg \text{Faster}(\text{Rocky}, z), \text{Faster}(\text{Foo}, z)\}$	4, 11
13	$\{\text{Faster}(\text{Rocky}, z)\}$	2, 7
14	$\{\text{Faster}(\text{Foo}, \text{Bar})\}$	12, 13
15	$\{\}$	8, 14