

Peer-Assisted Content Distribution Aided by Video Popularity Evolution Model

Mohamad Dikshie Fauzie* Achmad Husni Thamrin* Jun Murai† *Graduate School of Media and Governance †Faculty of Environment and Information Studies
Keio University, 252-0882 Kanagawa, Japan
dikshie@sfc.wide.ad.jp husni@ai3.net jun@wide.ad.jp

Abstract—Generally content distribution network (CDN) have adopted two different architectures: client-server model that's is the most common architecture model and peer-assisted CDN. In client-server model, clients download content dedicated and geographically managed servers while in peer-assisted model, clients download part of content from each other client besides from CDN servers. In this paper, we develop a peer-assisted CDN model based on previous work. Our model is quite different from previous work. We add Youtube VoD views popularity model aspect to our peer-assisted CDN model. From simulation-based experiments driven by real-world Youtube datasets, we find that peers in our model can contribute to deliver contents higher than previous work on the other hand number of access to cache in peer also higher than previous work. We do significance test for both metrics (peer contributions and number of access to cache) and find that p -values are less than 1% thus the results are significant.

Index Terms—Internet Video on Demand (VoD), P2P, CDN, and Caching.

I. INTRODUCTION

Streaming content, especially video, represents a significant fraction of the traffic volume on the Internet, and it has become a standard practice to deliver this type of content using Content Delivery Networks (CDNs) such as Akamai and Limelight for better scaling and quality of experience for the end users. For example, YouTube uses Google cache and MTV uses Akamai in their operations.

With the spread of broadband Internet access at a reasonable flat monthly rate, users are connected to the Internet 24 hours a day and they can download and share multimedia content. P2P (peer to peer) applications are also widely deployed. In China, P2P is very popular; we see many P2P applications from China such as PPLive, PPStream, UUSe, Xunlei, etc. [1]. Some news broadcasters also rely on P2P technology to deliver popular live events. For example, CNN uses the Octoshape [2] solution that enables their broadcast to scale and offer good video quality as the number of users increases.

From the Internet provider point of view, the presence of so many always-on users suggests that it is possible to delegate a portion of computing, storage and networking tasks to the users, thus creating P2P networks where users can share files and multimedia content. Starting from file sharing protocols, P2P architectures have evolved toward video on demand and support for live events.

Alternatively, video contents can be efficiently distributed on services offered by managed network architectures and

CDN companies. The major issues of CDN are high deployment cost and good but not unlimited scalability in the long term. Given the complementary features of P2P and CDN, in recent years some hybrid solutions have been proposed and applied to the operational of CDN [3]–[5] to take the best of both approaches. In Peer assisted CDN, users can download content from CDN nodes from or other users or peers. A user may cache the content after download to serve requests from other users. Due to the complexity of the behavior of peers, the process should be done in the home gateway user where the ISP can control it.

In this work, we will revisit Guo et al., [6] work's PROP as basis to evaluate of the peer-assisted CDN and propose an improvement the model for the PROP. We also examine the characteristics of Internet VoD by investigating real-world datasets obtained from Youtube. In P2P assisted CDN for video on demand (VoD), most of researcher assume that catalog of video popularity rank is already established following zipf distribution. This become basis for P2P assisted CDN model in PROP [6]. Our work is quite different whereas we will use VoD view popularity to aid the PROP model. We use Youtube VoD view model for this purpose. A twofold of our contributions as follows: (1) We use the idea of VoD view popularity model to aid the PROP model. To our knowledge, the combination of PROP model and VoD view popularity model is the first. (2) From simulation-based experiments, we find that peer contributions become higher than the PROP model.

Our paper presentation as follows: (1) we describe related work in sect.II; (2) we explain detail of Youtube popularity evolution model in sect.III; (3) we explain the caching strategy for CDN and peer in sect.IV; (4) we explain our simulation design, simulator, and its evaluation in sect.V. Finally, we present our conclusions in section VI.

II. RELATED WORK

Content Distribution Networks with peer assist have been successfully deployed on the Internet, such as Akamai [7], [3] and LiveSky [8]. The authors of [7] examine the risks and benefits of peer-assisted content distribution in Akamai and measure the effectiveness of its peer-assisted approach. The authors of [3] conclude from two real world traces that hybrid CDN-P2P can significantly reduce the cost of content distribution and can scale to cope with the exponential growth

of Internet video content. Yin et al. [8] described commercial operation of a peer-assisted CDN in China. LiveSky solved several challenges in the system design, such as dynamic resource scaling of P2P, low startup latency, ease of P2P integration with the existing CDN infrastructure, and network friendliness and upload fairness in the P2P operation. Xu et al. [9] used game-theory to show the right cooperative profit distribution of P2P can help the ISP to maximize the utility. Their model can easily be implemented in the context of current Internet economic settlements. Misra et al. [10] also mentioned the importance of P2P architecture to support content delivery networks. The authors use cooperative game theory to formulate simple compensation rules for users who run P2P to support content delivery networks.

The idea of telco- or ISP-managed CDN has been proposed in recent years. The complexity of the CDN business encourage telcos and ISPs to manage their own CDN, rather than allow others to run CDNs on their networks. It has been shown that it is cost effective [11] [12]. Kamiyama et al. [13] proposed optimally ISP operated CDN. Kamiyama et al. mentioned that, in order to deliver large and rich Internet content to users, ISPs need to put their CDNs in data centers. The locations are limited while the storage is large, making this solution effective, using optimum placement algorithm based on real ISP network topologies. The authors found that inserting a CDN into an ISP's ladder-type network is effective in reducing the hop count, thus reduce total link cost. Based on the author definition: Ladder-type network is a network with a maximum degree under 10. Cisco has initiated an effort to connect telco- or ISP-managed CDNs to each other, to form a CDN federation [11] using open standards [14]. They argue that the current CDN architecture is not close enough to the users and ISPs can fill this position.

The idea of utilizing the user's computation power to support ISP operation is not new. The Figaro project [15] proposed the residential gateway as an integrator of different networks and services, becoming an Internet-wide distributed content management for a proposed future Internet architecture [15]. Cha et al., [16] performed trace analysis and found that an IPTV architecture powered by P2P can handle a much larger number of channels, with lower demand for infrastructure compared to IP multicast. Jiang et al. [17] proposed scalable and adaptive content replication and request routing for CDN servers located in users' home gateways. Maki et al., [18] propose traffic engineering for peer-assisted CDN to control the behavior of clients, and present a solution for optimizing the selection of content files. Mathieu et al., [19] are using data gathered from France telecom network to calculate reduction of network load if customers are employed as peer-assisted content delivery.

Guo et al., [6] work's PROP is closest with our work. PROP uses local system (local counter) to calculate the segment popularity in peer-assisted proxy system. PROP uses popularity for proxy cache replacement strategy. In peer side, the author use utility function for cache replacement strategy. A utility function assigns numerical value to outcomes, in such a way that outcomes with higher utility are always preferred over outcomes with lower utilities. The utility function

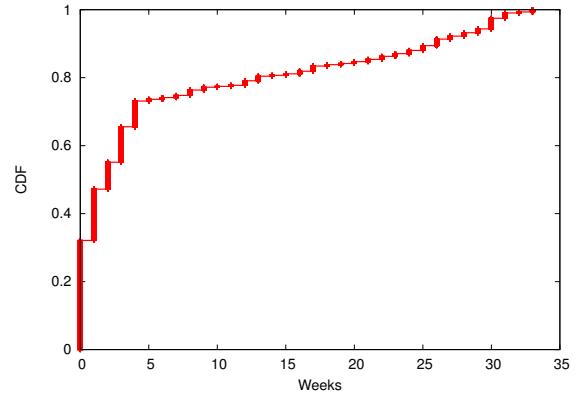


Fig. 1: Time to peak empirical distribution.

is also function from popularity. While the authors successfully show that the results are very good, the peer-assisted system behavior over time is not explain because the author focus on properties such as proxy cache size variations and peer cache size variations. The explanation of the optimal number of replicas is not also clear because unavailable information when the snapshot is taken. In our work, we complement Guo et al., [6] work with VoD viewing popularity evolution model and describe the behavior of the peer-assisted CDN over the time.

III. CHARACTERIZING INTERNET VOD POPULARITY

Before analyzing the system description and video caching, we first examine the popularity characteristics of Internet VoD services. We use YouTube as example of VoD service. The studies of content popularity evolution are mostly considered in short time periods. Borghol et al., [20] measure the evolution of content popularity in long periods (36 weeks, from 3 August 2008 until 29 March 2009) in which view count statistics of YouTube.

In datasets, we have one-week spacing between consecutive snapshots. We can get how many times the video was viewed during the one-week period since last week or since snapshot $(i - 1)$. Borghol et al., [20] define time-to-peak for a video as its age (time since upload) at which its weekly viewing rate is the highest during measurement (from the first week until end of measurement).

The time-to-peak distributions is shown in fig.1. Figure 1 shows Borghol et al., [20] work that around three-quarters of a large fraction videos peak within the first six weeks since their upload and beyond six weeks we have uniform distribution thus the time-to-peak is exponentially distributed mixture with uniform distribution. Because we know the peak time (at-peak phase) of every video, we can also know before-peak phase and after-phase of every videos.

To estimate the the rate parameter of exponential part of time-to-peak distribution, we use Maximum Likelihood Estimation (MLE) [21]. Using MLE method, we can get exponential parameter $\lambda = 0.59$. For weekly views distribution, Borghol et al., [20] found that beta distribution is a good model to explain video views popularity evolution thus we follow

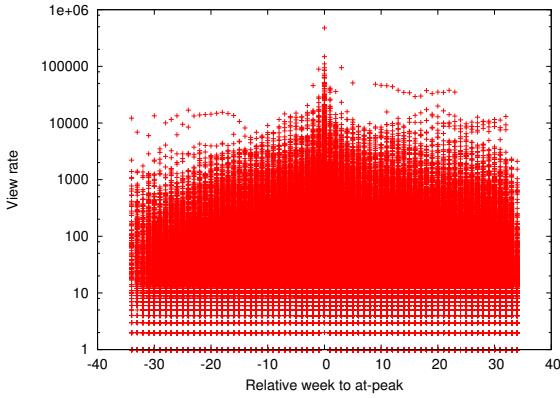


Fig. 2: View rate distribution versus week relative to at-peak phase week for every videos, where y-axis in logscale. Every points lie in negative x-axis mean view rate of every videos in before-peak phase. Every points lie in x-axis= 0 mean view rate of every videos at-peak phase. Every points lie in positive x-axis mean view rate of every videos in after-peak phase.

A	view rate	1	1	1	10	1	1	1
	relative week to peak	-3	-2	-1	0	1	2	3
↓								
B	view rate	1	1	1	10	1	1	1
	relative week to peak	-3	-2	-1	0	1	2	3
	number of week	0	1	2	3	4	5	6

Fig. 3: Transformation of view rate distribution. We add number week and make it as x-axis, View rate as y-axis, and relative week to peak as z-axis.

Borghol et al., [20] for weekly views distribution model.

To reveal data distribution of view rate for every video, we plot view rate versus week where we shift week of view rate at-peak phase to zero. Therefore we can get view rate distribution relative to at-peak week as shown in fig. 2

IV. SYSTEM DESCRIPTION

In our work, we use Youtube VoD view model to aid our work that based from PROP. The Youtube VoD view model will be used in peer-caching strategy side to exploits the video popularity.

A. Peer caching strategy

As we mentioned before, we use Youtube VoD view model in peer caching strategy side. Our utility function is different from PROP. Our utility function need the estimation of video position whether the requested video is in before-peak phase, at-peak phase, or after-peak phase. How we estimate the video

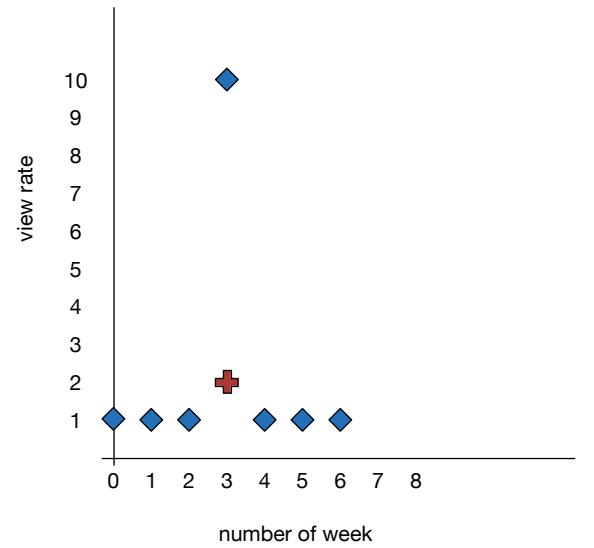


Fig. 4: Final view rate distribution after transformation where x-axis is number of week, y-axis is view rate.

position is shown in fig. 3 and fig. 4. In fig. 3 part A, we have view rate (y-axis) and relative week to peak (x-axis) which is view rate distribution versus week relative to at-peak phase as also shown completely in fig. 2. We transform these numbers by adding number of week and make number of week as x-axis, view rate as y-axis, and relative week to peak as z-axis fig. 3 part B. This transformation is shown in fig. 4 as diamond points. We want to estimate what is the position of that video. Is the video in at-peak phase, before-phase, or after phase. We can estimate the that video position by averaging relative week to peak numbers (the points at z-axis) of the nearest point from datasets. If the average value less than 0 we estimate the video position at before-peak phase, if the average value equal to 0 we estimate the video position at at-peak phase, and if the average value more than 0 we estimate the video position at after-peak phase.

For example: there is a peer that request a video where the position of video in third week with the last week view rate $vr = 2$ (we can get as this data from CDN) shown in fig. 4 as red cross. In this case, the nearest points are the point at third week (2, 1, -1) and the point at fifth week (4, 1, 1). By averaging the points at z-axis of the nearest points $(-1 + 1)/2 = 0$, we can get estimate that video is in at-peak phase.

Since we can estimate before-peak week, at-peak week, and after-peak week of video, we modified the original utility function from PROP by adding a weight as follows:

$$u = \frac{(f(p) - f(p_{min}))(f(p_{max}) - f(p))}{r^{\alpha+\beta}} + weight \quad (1)$$

where $weight$ is proportion of view count that we get from Youtube datasets. In before-peak week, we get $weight = 0.149538787758$, in at-peak week, we get $weight = 0.470040393021$, and in after-peak week, we get $weight = 0.380420819221$. p represents popularity of the video, p_{min} represents estimation of minimum popularity in P2P system,

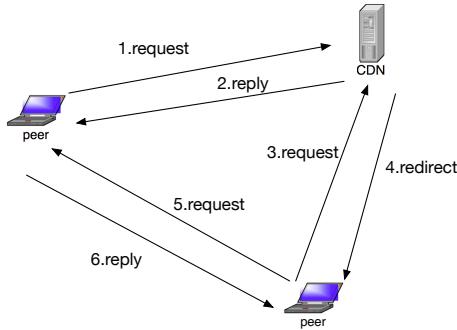


Fig. 5: Peer interaction in simulator.

p_{max} represents estimation of maximum popularity in P2P system, r represents the number of replicas of the video in the system, and $f(p)$ is monotonic non-decreasing function. α and β are the adjustment factor. The CDN can calculate p_{min} and p_{max} then propagate to the P2P system. To able to track the simulation, we use default value from PROP for $\alpha = \beta = 1$ and $f(p) = \log(p)$. We choose the video with the smallest u value as the candidate to be replaced when a peer's cache capacity is full.

V. EVALUATION

In order to evaluate the proposed peer-caching strategy using before-peak, at-peak, and after-peak information from Youtube VoD view model, we have to compare our model to PROP model. We evaluate three metrics which are peer contribution to delivery contents during simulation, access frequency of cache during simulation, and number of replicas. Peer contribution metric related to byte-hit-ratio. Byte-hit-ratio is defined as the total bytes contents served by peers normalized by the total bytes of video all peers and CDN consume. It means more peer contributions, more byte-hit-ratio because peer can get content from another peers. Access frequency of cache reflects the storage utilization. More access means more peer storage utilization. Number of replicas is also related to peer storage utilization. How ever, too many replicas will waste the storage resources. To evaluate these metrics, we developed a peer-assisted CDN simulator.

A. Simulation Design

An event driven simulator is developed using Python for this purpose. In our simulator, time is divided into rounds. During a round, a peer request a video.

In fig.5, we describe the process of a peer that requests a video in simulator which derived from PROP. A peer and a CDN are implemented in object oriented model. When a peer requests a video, it always goes to a CDN server (step 1). The CDN provides the videos to the peer (step 2). If there is another peer request same video, that request will go to CDN (step 3). A CDN will check its record to see if there are some peers cache that requested video. If there are some peers cache that requested video, a CDN will reply with redirect message that asking a peer to download requested video from other

peer (step 4). If there are no peers have requested video, a CDN will serve the video. A peer then can request the video to other peer and get the video (step 5 and step 6). From above description, we can see that deploying peer-assisted CDN can save some traffic since the clients which form P2P network can sharing the contents or videos.

1) *Catalog Generator:* The goal for catalog generator is to create a catalog video that consist video-id, time when a video is uploaded, a video size, and view count terminus. We made catalog that consists of 10000 videos thus we have video-id from 0 until 9999. We assume that a video is uploaded to server following poisson process with mean rate $\lambda = 1$ thus we can get the time when a video is uploaded. The view count terminus for every video is assigned randomly from Youtube datasets and video size for every video is assigned randomly between 1MB and 200MB.

In last step, we assign file size of video randomly between 1MB and 200MB. Finally, we have a catalog that consists of: video-id, time when a video is uploaded, view count terminus, and video size.

2) *Peer Request Generator:* In catalog generator, we assume peer request a video to CDN following poisson process with a mean rate $\lambda = 1$ [22] finally we generate video request for 360 days of simulation.

We assume that a peer choose a video based on a preference from view count and view rate. First, we calculate the number of videos at-peak time as follows: sample N value from the time-to-peak distribution and determine the number of videos n_j^{at} that peak at week j . Total number of video $N = n_j^{before} + n_j^{at} + n_j^{after}$.

Next, we determine view count terminus which are the number of final view count of video. In view count terminus, we assume that a video will not get big additional view after at-peak phase. We assign view count terminus randomly from datasets. After determining view count terminus, we assign beta distribution parameter for every video. Since we can estimate the time of at-peak phase for each video, we know the mode of beta distribution value and we can calculate α and β value using the mode of distribution formula: $m = \frac{\alpha-1}{\alpha+\beta-2}$. We assign α value randomly between 1 and 2 thus we can calculate β value. With the knowledge of beta distribution of every video and its view count terminus, we can know the view count and view rate of every video as function from time. The knowledge of view count and view rate, will be used top generate a video choice that used by a peer. For video choice, we estimate that a peer will choose video proportionally considering view count and view rate of the video. We can get view count and view rate from probability distribution function (PDF) and cumulative distribution function (CDF) of beta distribution above multiply by video's view count terminus. Finaly, we have requests catalog that consists of: peer-id, request time, and video-id to be choosen.

3) *Simulation Parameters and Scenarios:* The simulation parameters are follows:

- Length: 360 days.
- Video size: random between 1MB and 200MB.
- Peer capacity: [500MB].
- CDN capacity: 10000MB.

- Number of peers: 100000.
- Number of videos: 10000.

We compare our results to original PROP [6] implementation. There are three scenarios in our simulations. First, peers choose a video that has a popularity following from Youtube data sets that we already explained in V-A1. Second, peers choose a video that has a popularity following from Youtube data sets and we shift the requests time four weeks. Third, peers choose a video that has a popularity following zipf distribution with rate= 0.9 [23].

B. Result and Discussion

Figure 6a, 6b, and 6c show the absolute peer contribution to deliver videos compared between model and prop. Figure 6a and fig.6b show same pattern. The peers give more contribution in the tail while in the third scenario the peer give more contribution in body. A peers can give more contribution because a video has longer duration than other videos in a peer's cache thus other peer's requests are served by the peer. A video has longer duration than other videos in peer's cache because that a video has bigger utility function than other videos for example a video that will enter the cache.

Denote u_{dl} is utility function for a video inside the cache and u_{ms} is utility function for a video that will enter the cache. In order a video in cache has longer duration, the utility function for u_{dl} must be bigger than the utility function for u_{ms} .

$$u_{dl} > u_{ms}$$

$$\frac{(f(p_{dl}) - f(p_{min}))(f(p_{max}) - f(p_{dl}))}{r^{\alpha+\beta}}_{dl} + weight_{dl} > \frac{(f(p_{ms}) - f(p_{min}))(f(p_{max}) - f(p_{ms}))}{r^{\alpha+\beta}}_{ms} + weight_{ms}$$

We assume that number of replicas are same, thus:

$$(f(p_{dl}) - f(p_{min}))(f(p_{max}) - f(p_{dl})) - (f(p_{ms}) - f(p_{min}))$$

VI. CONCLUSION AND FUTURE WORK

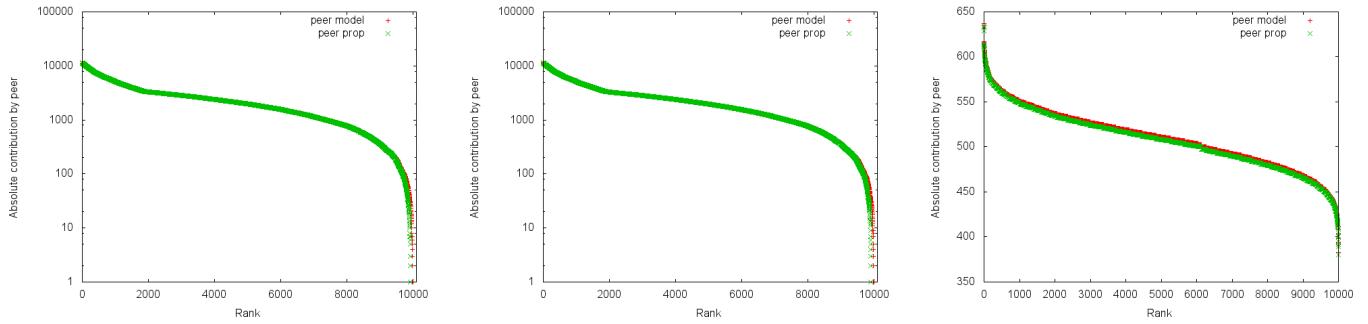
This paper presents a scheme for a ISP managed peer-assisted CDN model that Some areas of improvement that we have identified for future are: We are also very interested to include energy trade off this peer-assisted CDN architecture in order to know how much energy saving by ISP and how much increase of energy at users home gateway side in this architecture.

ACKNOWLEDGMENT

The authors would like to thank Internet research laboratory member at Keio University and anonymous reviewers.

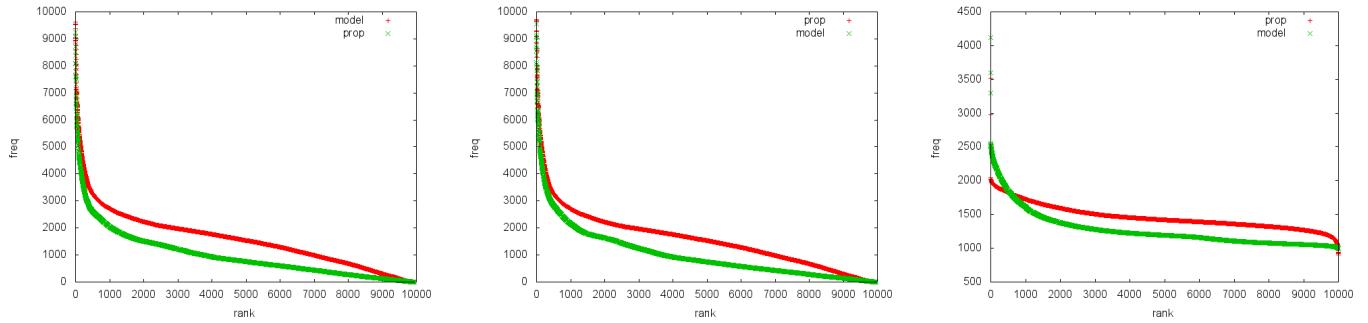
REFERENCES

- [1] L. Vu, I. Gupta, K. Nahrstedt, and J. Liang, "Understanding overlay characteristics of a large-scale peer-to-peer iptv system," *ACM Trans. Multimedia Comput. Commun. Appl.*, vol. 6, no. 4, pp. 31:1–31:24, Nov. 2010. [Online]. Available: <http://doi.acm.org/10.1145/1865106.1865115>
- [2] Octoshape, "Octoshape," <http://www.octoshape.com/cnn-com-using-octoshapes-p2p-for-live-feed/>.
- [3] C. Huang, A. Wang, J. Li, and K. W. Ross, "Understanding hybrid cdn-p2p: why limelight needs its own red swoosh," in *Proceedings of the 18th International Workshop on Network and Operating Systems Support for Digital Audio and Video*, ser. NOSSDAV '08. New York, NY, USA: ACM, 2008, pp. 75–80. [Online]. Available: <http://doi.acm.org/10.1145/1496046.1496064>
- [4] H. Jiang, J. Li, Z. Li, and J. Liu, "Efficient hierarchical content distribution using p2p technology," in *Networks, 2008. ICON 2008. 16th IEEE International Conference on*, dec. 2008, pp. 1 –6.
- [5] H. Yin, X. Liu, T. Zhan, V. Sekar, F. Qiu, C. Lin, H. Zhang, and B. Li, "Design and deployment of a hybrid cdn-p2p system for live video streaming: experiences with livesky," in *Proceedings of the 17th ACM international conference on Multimedia*, ser. MM '09. New York, NY, USA: ACM, 2009, pp. 25–34. [Online]. Available: <http://doi.acm.org/10.1145/1631272.1631279>
- [6] L. Guo, S. Chen, and X. Zhang, "Design and evaluation of a scalable and reliable p2p assisted proxy for on-demand streaming media delivery," *Knowledge and Data Engineering, IEEE Transactions on*, vol. 18, no. 5, pp. 669–682, May 2006.
- [7] M. Zhao, P. Aditya, A. Chen, Y. Lin, A. Haeberlen, P. Druschel, B. Maggs, B. Wishon, and M. Ponec, "Peer-assisted content distribution in akamai netsession," in *Proceedings of the 2013 Conference on Internet Measurement Conference*, ser. IMC '13. New York, NY, USA: ACM, 2013, pp. 31–42. [Online]. Available: <http://doi.acm.org/10.1145/2504730.2504752>
- [8] H. Yin, X. Liu, T. Zhan, V. Sekar, F. Qiu, C. Lin, H. Zhang, and B. Li, "Livesky: Enhancing cdn with p2p," *ACM Trans. Multimedia Comput. Commun. Appl.*, vol. 6, no. 3, pp. 16:1–16:19, Aug. 2010. [Online]. Available: <http://doi.acm.org/10.1145/1823746.1823750>
- [9] K. Xu, Y. Zhong, and H. He, "Can p2p technology benefit eyeball ISPs? a cooperative profit distribution answer," *CoRR*, vol. abs/1212.4915, 2012.
- [10] V. Misra, S. Ioannidis, A. Chaintreau, and L. Massoulié, "Incentivizing peer-assisted services: a fluid shapley value approach," *SIGMETRICS Perform. Eval. Rev.*, vol. 38, no. 1, pp. 215–226, Jun. 2010. [Online]. Available: <http://doi.acm.org/10.1145/1811099.1811064>
- [11] Cisco, "Cdn federation," 10 2012, available on http://www.cisco.com/web/about/ac79/docs/sp/CDN-Federation_Phase-2-Pilot.pdf.
- [12] W. B. Norton, *The Internet Peering Playbook: Connecting to the Core of the Internet*, 2nd ed. DrPeering Press, December 2012.
- [13] N. KAMIYAMA, T. MORI, R. KAWAHARA, and H. HASEGAWA, "Optimally designing isp-operated cdn," *IEICE Transactions on Communications*, vol. E96.B, no. 3, pp. 790–801, March 2013.
- [14] IETF, "Cdn interconnect ietf working group," 2013, available on <https://datatracker.ietf.org/wg/cdn/>. [Online]. Available: <https://datatracker.ietf.org/wg/cdn/>
- [15] Figaro-project, <http://www.ict-figar.eu/>, 2012.
- [16] M. Cha, P. Rodriguez, S. Moon, and J. Crowcroft, "On next-generation telco-managed p2p tv architectures," in *Proceedings of the 7th international conference on Peer-to-peer systems*, ser. IPTPS'08. Berkeley, CA, USA: USENIX Association, 2008, pp. 5–5. [Online]. Available: <http://dl.acm.org/citation.cfm?id=1855641.1855646>
- [17] W. Jiang, S. Ioannidis, L. Massoulié, and F. Picconi, "Orchestrating massively distributed cdns," in *Proceedings of the 8th international conference on Emerging networking experiments and technologies*, ser. CoNEXT '12. New York, NY, USA: ACM, 2012, pp. 133–144. [Online]. Available: <http://doi.acm.org/10.1145/2413176.2413193>
- [18] N. MAKI, T. NISHIO, R. SHINKUMA, T. MORI, N. KAMIYAMA, R. KAWAHARA, and T. TAKAHASHI, "Traffic engineering of peer-assisted content delivery network with content-oriented incentive mechanism," *IEICE Transactions on Information and Systems*, vol. E95.D, no. 12, pp. 2860–2869, December 2012.
- [19] B. Mathieu and Y. Levene, "Impact of ftth deployment on live streaming delivery systems," in *Computers and Communications (ISCC), 2012 IEEE Symposium on*, july 2012, pp. 000 259 –000 264.
- [20] Y. Borghol, S. Mitra, S. Ardon, N. Carlsson, D. Eager, and A. Mahanti, "Characterizing and modelling popularity of user-generated videos," *Perform. Eval.*, vol. 68, no. 11, pp. 1037–1055, Nov. 2011. [Online]. Available: <http://dx.doi.org/10.1016/j.peva.2011.07.008>



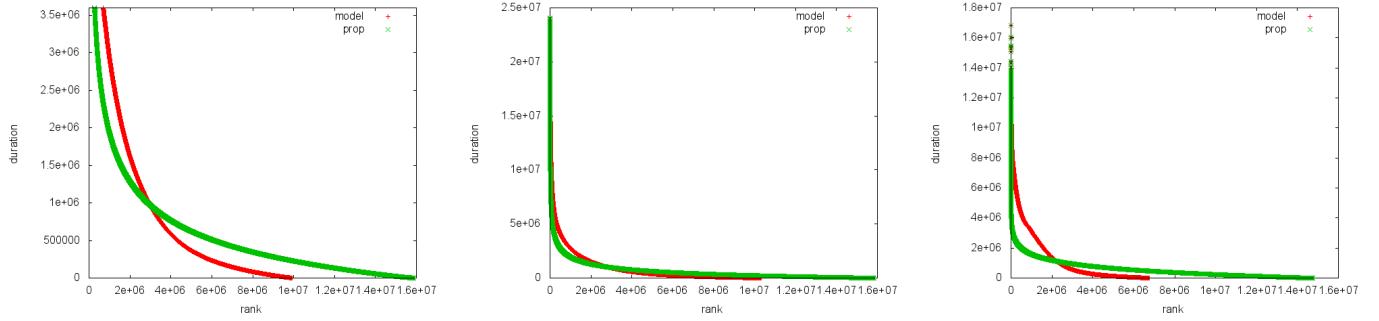
(a) Absolute of contribution of peer for the first scenario.
(b) Absolute of contribution of peer for the second scenario.
(c) Absolute contribution of peers for the third scenario.

Fig. 6: Peer contributions compared between model and prop.



(a) Frequency a video in peers for the first scenario.
(b) Frequency a video in peers for the second scenario.
(c) Frequency a video in peers for the third scenario.

Fig. 7: Frequency a video in peers compared between model and prop.



(a) Cache duration in peers for the first scenario.
(b) Cache duration in peers for the second scenario.
(c) Cache duration in peers for the third scenario.

Fig. 8: Duration compared between model and prop.

- [21] A. Clauset, C. R. Shalizi, and M. E. Newman, "Power-law distributions in empirical data," *SIAM review*, vol. 51, no. 4, pp. 661–703, 2009.
- [22] M. Zink, K. Suh, Y. Gu, and J. Kurose, "Characteristics of youtube network traffic at a campus network - measurements, models, and implications," *Comput. Netw.*, vol. 53, no. 4, pp. 501–514, Mar. 2009. [Online]. Available: <http://dx.doi.org/10.1016/j.comnet.2008.09.022>
- [23] F. Guillemin, T. Houdoin, and S. Moteau, "Volatility of youtube content in orange networks and consequences," in *Communications (ICC), 2013 IEEE International Conference on*, June 2013, pp. 2381–2385.

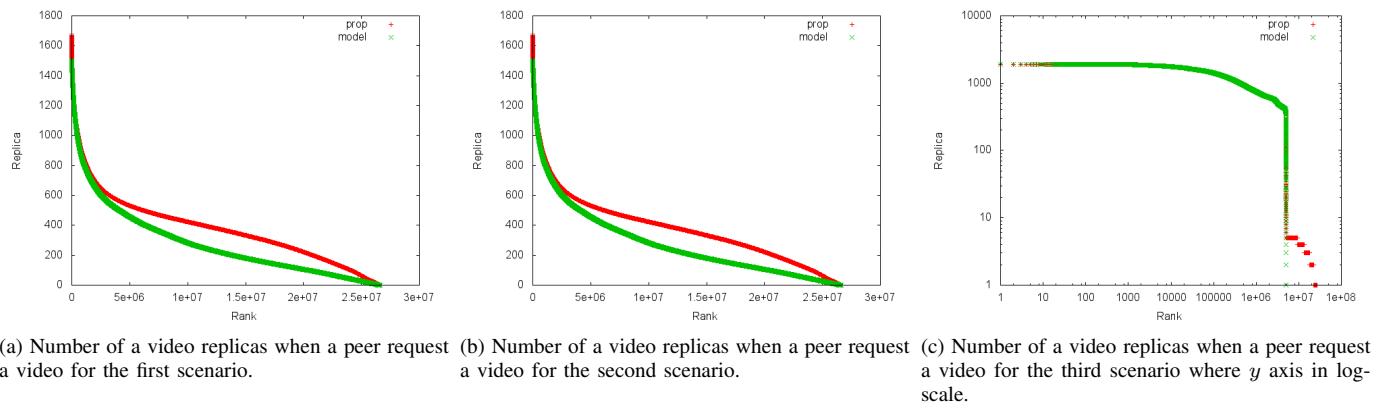


Fig. 9: Replicas compared between model and prop.