Programming with ispc

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Agenda

SIMD on CPU

Auto-vectorisation

Programming in ISPC

ISPC Performance

SIMD on CPU

Auto-vectorisation

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ISPC Performance

What is SIMD?

- Single Instruction Multiple Data.
- Fixed-size vector registers that contain multiple values.
- *Vector instructions* that operate on vector registers.
 - ▶ A form of explicit ILP where instruction is the same.
 - If vector register contains four floats, then single SIMD instruction can replace four scalar instructions.
- On x86, an extension to the scalar instruction set.

Scalar Operation

$$A_1 \times B_1 = C_1$$
 $A_2 \times B_2 = C_2$
 $A_3 \times B_3 = C_3$
 $A_4 \times B_4 = C_4$

SIMD Operation

$$\begin{array}{c|c}
A_1 \\
A_2 \\
A_3 \\
A_4
\end{array} \times \begin{array}{c|c}
B_1 \\
B_2 \\
B_3 \\
B_4
\end{array} = \begin{array}{c|c}
C_1 \\
C_2 \\
C_3 \\
C_4
\end{array}$$

1

x86 example

The registers xmm0-xmm15 are 128 bits each, and operated on with instructions like ADDSS, SUBSS, MULSS.

- Instead of add eax ebx use e.g. addss xmm0 xmm1.
- Follows all the normal assembly rules.

¹https://medium.com/wasmer/webassembly-and-simd-13badb9bf1a8

When is SIMD useful?

- In our ontology, SIMD is regular and flat data parallelism on vectors of static size.
- When program is not bottlenecked by IO or memory traffic.
 - ► Although bulk memory reads can sometimes be vectorised.

SIMD is cheap

- It's already part of the CPU and uses the same memory.
- Using an SIMD instruction has zero latency.
- Compare to GPUs, which have huge overhead.

SIMD is not multithreading

- Both techniques can be used simultaneously.
- ▶ Will only focus on SIMD for this lecture.
- Speedup limited to SIMD vector size (in practice 4 or 8).
 - Often much less.

Applying vectorisation

 In principle, we can use SIMD instructions whenever independent operations with same operator occur

```
float x = a + b;
float y = b + c;
float z = d + e;
float v = e + f;
```

- Compilers do try to do this...
- ... but vectorisation mostly shines when doing bulk data-parallel operations

```
for (int i = 0; i < n; i++) {
   xs[i] *= 2;
}</pre>
```

Simple vectorisation

```
for (int i = 0; i < n; i++) {
    xs[i] *= 2;
}</pre>
```

Parallel?

Simple vectorisation

```
for (int i = 0; i < n; i++) {
    xs[i] *= 2;
}
Parallel?</pre>
```

Conceptually vectorise by *strip-mining* the loop into chunks corresponding to the vector size (e.g. 4):

```
for (int j = 0; j < n; j += 4) {
  for (int i = j; i < 4; i++) {
    xs[i] *= 2;
  }
}</pre>
```

- Inner loop can be replaced with vector instructions.
- Separate loop for any remaining < 4 iterations.

```
for (int j = 0; j < n; j += 4)
  for (int i = j; i < 4; i++)
   xs[i] *= 2;
# eax: j
# ebx: i*4
# ecx: n
# rdi: xs
loop:
 movdqu xmm0, xmmword ptr [rdi + ebx]
 paddd xmm0, xmm0
 movdqu xmmword ptr [rdi + ebx], xmm0
  add
         eax, 4
  add
         ebx, 16
  cmp
      eax, ecx
  jl
         .loop
```

Vectorising functions with straight-line code is easy

Suppose to want to vectorise this single function to operate on a vector of values at a time:

```
int f(int x, int y) {
  return (x + y) / 2;
}
```

Scalar version handles one x/y pair at a time.

Vector version handles four x/y pairs at a time.

```
add edi, esi
shr exi, 31
```

paddd xmm1, xmm0
psrad xmm1, 1

What about control flow?

Vectorising scalar function with control flow²

```
int f(int a, int b) {
  if (a < 0)
     a = 0;
                                                             with mask m0 m1 m2 m3
  else
                                 m0 | m1 | m2 | m3
                                                   m0 m1 m2 m3
     a += b;
                                                             with mask m0 m1 m2 m3
                                             +=
  return a:
                                 return
```

- Masking, just like in NumPy.
- Control flow turned into data flow.
- Doing this by hand gets very tiresome and is error-prone.
- Vector capabilities differ a lot between architectures.

²Example from ispc paper.

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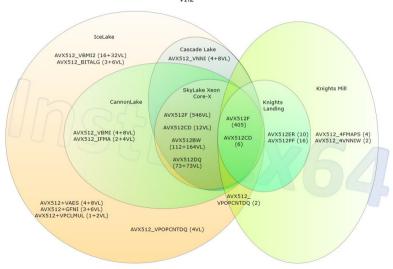
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- **AVX**: 256-bit registers (YMM0–YMM15). 86 instructions, only floating-point.
- 2013 AVX2: 137 new instructions, now also with integers.
- **AVX-512**: 512-bit registers (ZMM0-ZMM31), and a *zoo* of layers, not expected to be in all processors.

The 17+1 levels of AVX512 in Intel processors 2018-03-02 according to the 32th Intel ISA-ER v1.2



SIMD on CPL

Auto-vectorisation

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Auto-vectorisation

Write ordinary C code and hope that a sufficiently smart compiler can figure out what you mean and make use of whatever instruction set is supported on your computer.

Good: you don't have to learn anything new!

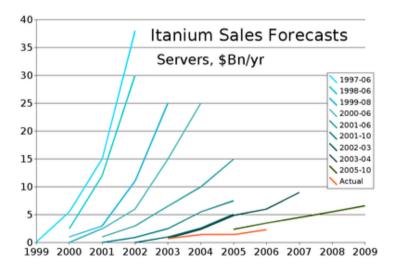
Auto-vectorisation

Write ordinary C code and hope that a sufficiently smart compiler can figure out what you mean and make use of whatever instruction set is supported on your computer.

Good: you don't have to learn anything new!

Bad: does it work?

What happened last time we depended on Sufficiently Smart Compilers?



Auto-vectorisation, example A

Auto-vectorisation, example A

```
.L4:

movdqu (%rax), %xmm0

addq $16, %rax

pslld $1, %xmm0

movups %xmm0, -16(%rax)

cmpq %rdx, %rax

jne .L4
```

Auto-vectorisation, example A

```
void A(int n, int *xs) {
  for (int i = 0;
       i < n:
       i++) {
    xs[i] *= 2;
$ acc -03 A.c -S
 Vectorised!
```

```
.L4:
  movdqu (%rax), %xmm0
  addq $16, %rax
  pslld $1, %xmm0
  movups %xmm0, -16(%rax)
  cmpq %rdx, %rax
  jne .L4
```

Auto-vectorisation, example B

```
int B(int n, int *xs) {
  int res = 0;
  for (int i = 0;
       i < n;
       i++) {
    res += xs[i];
  return res;
```

Auto-vectorisation, example B

```
int B(int n, int *xs) {
  int res = 0:
  for (int i = 0;
       i < n:
       i++) {
    res += xs[i];
  return res;
```

```
.L4:
movdqu (%rax), %xmm2
        $16, %rax
addq
paddd
       %xmm2, %xmm0
        %rdx, %rax
cmpa
       . L4
ine
movdga %xmm0, %xmm1
movl
        %edi. %edx
psrlda $8, %xmm1
andl
        $-4. %edx
paddd
        %xmm1, %xmm0
movdaa
       %xmm0, %xmm1
psrldq $4, %xmm1
paddd
        %xmm1. %xmm0
movd
        %xmm0. %eax
```

Auto-vectorisation, example B

```
.L4:
                                  movdqu (%rax), %xmm2
                                          $16, %rax
                                  addq
int B(int n, int *xs) {
                                  paddd
                                         %xmm2, %xmm0
  int res = 0:
                                          %rdx, %rax
                                  cmpa
 for (int i = 0;
                                          . L4
                                  ine
       i < n:
                                  movdga %xmm0, %xmm1
       i++) {
                                  movl
                                          %edi. %edx
    res += xs[i];
                                  psrlda $8, %xmm1
                                  andl
                                          $-4. %edx
  return res:
                                  paddd
                                          %xmm1, %xmm0
                                  movdaa
                                         %xmm0, %xmm1
Tricky, but vectorised!
                                  psrldq $4, %xmm1
                                  paddd
                                          %xmm1. %xmm0
                                  movd
                                          %xmm0. %eax
```

Auto-vectorisation, example C

```
void C(int n,
       int *ys,
       int *xs) {
  int acc = 0;
  for (int i = 0;
       i < n;
       i++) {
    acc += xs[i];
    ys[i] = acc;
```

Auto-vectorisation, example C

```
void C(int n,
       int *vs.
                            .L4:
       int *xs) {
                                   %rdi, %rax
                             mova
  int acc = 0:
                            .L3:
  for (int i = 0;
                             addl (%rdx,%rax,4), %ecx
       i < n:
                                   1(%rax), %rdi
                             leaq
       i++) {
                             movl %ecx, (%rsi, %rax, 4)
    acc += xs[i];
                             cmpq %rax, %r8
    vs[i] = acc:
                                   . L4
                             ine
```

Auto-vectorisation, example C

```
void C(int n,
       int *vs.
                             .L4:
       int *xs) {
                                   %rdi, %rax
                             mova
  int acc = 0:
                             .L3:
  for (int i = 0;
                             addl (%rdx,%rax,4), %ecx
       i < n:
                                    1(%rax), %rdi
                             leaq
       i++) {
                             movl %ecx, (%rsi, %rax, 4)
    acc += xs[i];
                             cmpq %rax, %r8
    vs[i] = acc:
                                    . L4
                             ine
 Not vectorised.
```

Vectorising powi()

```
float powi(float a, int b) {
    float r = 1;
    while (b--) r *= a;
    return r;
}
```

Vectorising powi()

```
float powi(float a, int b) {
    float r = 1;
    while (b--) r *= a;
    return r;
}
```

Two ways of vectorising

1. Make a single call powi(a,b) faster by trying to do multiple iterations of the while loop in parallel (probably infeasible).

Vectorising powi()

```
float powi(float a, int b) {
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    return r;
}
```

Two ways of vectorising

- 1. Make a single call powi(a,b) faster by trying to do multiple iterations of the while loop in parallel (probably infeasible).
- 2. Make multiple *instances* of powi(a,b) faster:

```
for (int i = 0; i < n; i++) {
  cs[i] = powi(as[i], bs[i]);
}</pre>
```

- (1) much harder, (2) often what we want.
- How would a compiler know?

Vectorising powi() with option (2)

```
float powi(float a, int b) {
    float r = 1;
    while (b--) r *= a; // AVX2 assembly for this loop below
    return r;
}
```

Vectorising powi() with option (2)

```
float powi(float a, int b) {
   float r = 1:
   while (b--) r *= a; // AVX2 assembly for this loop below
   return r:
LBB0_3:
 vpaddd
         %ymm5, %ymm1, %ymm8 # Decrement b.
 vblendvps %ymm7, %ymm8, %ymm1, %ymm1 # Only active lanes.
          %vmm0, %ymm3, %ymm7
 vmulps
                              # r * a
 vblendvps %mm6, %mm7, %mm3, %mm3 # Only active lanes.
 vpcmpegd %ymm4, %ymm1, %ymm8
                             # Compare b with zero.
         %vmm6, %vmm7
                                   # Compute which lanes
 vmovaps
 vpandn %mm6, %mm8, %mm6 # still active.
 vpand
          %ymm2, %ymm6, %ymm8
                              # AND with current
 vmovmskps %ymm8, %eax
                                   # Any lanes active?
 testl
       %eax, %eax
          LBB0_3
                                   # Redo if so.
 ine
```

A C compiler probably cannot do this.

Motivation for ispc

- Around 2010, Matt Pharr from Intel's graphics group had too much time and too much trouble with extant auto-vectorisers
- Motivating problem: graphics
 - Often embarassingly parallel

```
for (int j = 0; j < height; j++) {
   for (int i = 0; i < width; i++) {
      // compute pixel i, j
   }
}</pre>
```

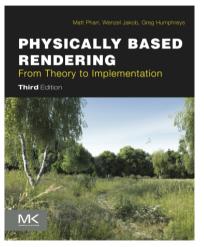
- Often lots of control flow in the loop body.
- ► If we could have one vector lane compute one pixel, then we could compute 4/8/16 pixels simultaneously.
- Even today, auto-vectorisers choke on anything non-trivial (ask Cosmin about stencils)

Quotes from Matt Pharr

- 1. They'd inform the graphics folks that they'd improved their auto-vectorizer in response to our requests and that it did everything we had asked for.
- 2. We'd try it and find that though it was better, boy was it easy to write code that wasn't actually compiled to vector code—it'd fail unpredictably.
- 3. We'd give them failing cases, a few months would would pass and they'd inform us that the latest version solved the problem.

They tried to patch things up at first but eventually they threw up their hands and came up with #pragma simd, which would disable the "is it safe to vectorize this" checks in the auto-vectorizer and vectorize the following loop no matter what. (Once a #pragma is proposed to solve a hard problem, you know things aren't in a good place.)

As an aside, Matt Pharr is likely the only programming language designer to win an Academy Award



Winner of a 2014 Scientific and Technical Academy Award

Auto-vectorisation is not a programming model

- A compiler can easily tell you what fails to vectorise.
- Not so clear why.
- You need to become an expert in the compiler and tickle your code in just the right way.
- This is a horrible way to program.

And then they release a new compiler with subtly different behaviour...

With a proper programming model, then the programmer learns the model (which is hopefully fairly clean), one or more compilers implement it, the generated code is predictable (no performance cliffs), and everyone's happy.

Single Program Multiple Data (SPMD)

- Essentially the model also used by CUDA.
- Multiple instances of program is running.
- Group of running instances is called a gang.

```
void inc(int xs[], int ys[], int result[]) {
  result[programIndex] =
    (xs[programIndex] + ys[programIndex]) / 2;
}
```

- In principle, one instance per array element.
- On GPU, many instances are useful to allow latency hiding.
- On CPU, rarely more than twice the SIMD width.

SIMD on CPL

Auto-vectorisation

Programming in ISPC

ISPC Performance

Intel SPMD Program Compiler

ispc is a compiler for a variant of the C programming language, with extensions for "single program, multiple data" (SPMD) programming.

ispc is

- a variant of C-much scalar C is also valid ispc.
- a low-level parallel language.
- not quaranteed to be deterministic.
- a compiler with only few *compiler optimisations*.

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ispc is a compiler for a variant of the C programming language, with extensions for "single program, multiple data" (SPMD) programming.

ispc is

- a variant of C-much scalar C is also valid ispc.
- a low-level parallel language.
- not quaranteed to be deterministic.
- a compiler with only few compiler optimisations.

What makes it relevant for our course is that it is a good example of using the right programming model.

Disclaimer

I am not an ispc expert.

I am merely an enthusiast, and I think its design is a masterpiece of simplicity, worthy of study.

Most of what I know is from

- 1. ispc: A SPMD Compiler for High-Performance CPU Programming (paper)
- 2. The story of ispc (series of blog posts by Matt Pharr)³
- 3. The User's Guide⁴

³https://pharr.org/matt/blog/2018/04/18/ispc-origins.html

⁴https://ispc.github.io/ispc.html

ispc SPMD gang abstraction using SIMD instructions

SPMD implementation in ispc

- Call to ispc function spawns gang of program instances.
- All instances done when function returns.
- Gang size is SIMD width or a small multiple.
- Lockstep execution one "line" at a time.
- Each instance gets a copy of each non-uniform variable.

```
export void f(uniform int n, uniform float as[]) {
  for (int i = programIndex;
    i < n;
    i += programCount) {
    float a = as[i];
    // All instances finish previous line
    // before continuing
    as[i] = a * 2;
  }
}</pre>
```

Abstraction versus implementation

Model is SPMD

- Running a gang spawns programCount logical execution flows.
- ► Each has distinct value of programIndex.
- ► (PMPH students: sound familiar?).
- ► We program against this **abstraction**.

Implementation is SIMD

- Variables mapped to slots in SIMD registers.
- SIMD instructions carry out work of gang.
- Control flow implemented by masking or arithmetic.

Abstraction is intentionally leaky

- uniform values and cross-instance communication (later) let us mess up.
- ispc concerned with real-world performance, not purity.
- An expert programmer can often predict the SIMD instructions generated by compiler.

In principle, ispc could also generate GPU code! Good idea?

Previous example in ispc

```
float powi(float a, int b) {
    float r = 1:
    while (b--) r *= a:
    return r:
export void f(uniform int n.
              uniform float as[],
              uniform int bs[].
              uniform float cs[]) {
  for (int i = programIndex;
       i < n:
       i += programCount) {
    cs[i] = powi(as[i], bs[i]);
```

Previous example in ispc (better)

```
float powi(float a, int b) {
    float r = 1:
    while (b--) r *= a;
    return r:
export void f(uniform int n.
              uniform float as[],
              uniform int bs[].
              uniform float cs[]) {
  foreach (i = 0 ... n) {
    cs[i] = powi(as[i], bs[i]);
```

To inspect generated assembly

\$ ispc powi.isc --target=avx2 --emit-asm -o powi.s

3

To inspect generated assembly

```
$ ispc powi.isc --target=avx2 --emit-asm -o powi.s
```

To generate object file and header file

```
$ ispc powi.isc --target=avx2 -o powi.o -h powi.h
```

Then from some C program we can say

```
#include "powi.h"
```

f(1024, as, bs, cs);

```
float *as = malloc(1024*sizeof(float));
int *bs = malloc(1024*sizeof(int));
float *cs = malloc(1024*sizeof(float));
... initialize as. bs. cs...
```

Mandelbrot in C

```
static inline int mandel(float c re, float c im, int count) {
  float z re = c re, z im = c im;
  int i:
  for (i = 0; i < count; ++i) {
    if (z re * z re + z im * z im > 4.)
      break:
    float new re = z re*z re - z im*z im;
    float new im = 2.f * z re * z im;
    z re = c re + new re;
    z \text{ im} = c \text{ im} + \text{new im}:
  return i:
Also valid ispc!
```

Mandelbrot in C

```
void mandelbrot c(float x0, float y0,
                   float \times 1, float \vee 1,
                   int width, int height,
                   int maxIterations.
                   int output[]) {
  float dx = (x1 - x0) / width, <math>dy = (y1 - y0) / height;
  for (int j = 0; j < height; i++) {
    for (int i = 0; i < width; i++) {
      float x = x0 + i * dx, y = y0 + i * dy:
      int index = i * width + i:
      output[index] = mandel(x, y, maxIterations);
```

Mandelbrot in ispc

```
export void mandelbrot ispc
    (uniform float \times 0, uniform float \vee 0,
     uniform float \times 1, uniform float \vee 1,
     uniform int width, uniform int height,
     uniform int maxIterations.
     uniform int output[]) {
  float dx = (x1 - x0) / width, <math>dy = (y1 - y0) / height;
  for (uniform int j = 0; j < height; j++) {</pre>
    foreach (i = 0 ... width) {
      float x = x0 + i * dx, y = y0 + j * dy;
      int index = i * width + i:
      output[index] = mandel(x, y, maxIterations);
```

Benefits of uniform

- A uniform variable has same value in all program instances:
 - + Can be stored in non-vector register.
 - + Takes less space in memory if spilled.
 - + CPU can co-issue with vector instructions.
 - + Dereferencing uniform pointer is load, not vector gather.
 - + uniform branching avoids masking.
- Unadorned types are variant by default:
 - ► Each program instance has its own copy.
 - uniform converts automatically to variant.

uniform and control flow

```
float a = ...;
uniform int b = 0;
if (a == 0) {
    ++b;
    // b is 1
else {
    b = 10:
    // b is 10
```

- Whether b is 1 or 10 depends on whether any of the values of a in the executing gang were 0.
- Be careful!

SIMD on CPL

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Summation in ispc

- reduce_add() takes varying value and returns uniform sum of that value across all of the active program instances.
- Is this correct?
- Is this optimal?

Summation in ispc — better

Writing reduce_add() ourselves

```
uniform int own reduce add(int x) {
  uniform int sums[programCount];
  sums[programIndex] = x;
  if (programIndex == 0) {
    for (uniform int i = 1; i < programCount; i++) {</pre>
      sums[0] += sums[i];
  return sums[0]:
Builtin one is probably smarter.
```

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.
uniform int32 extract(int32 x, uniform int i);
```

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.
uniform int32 extract(int32 x, uniform int i);

// Returns 'x' provided by program
// instance 'offset' steps away.
int32 rotate(int32 value, uniform int offset)
```

Other functions for cross-instance communication

```
// Returns 'x' provided by program instance 'i'.
uniform int32 extract(int32 x, uniform int i);

// Returns 'x' provided by program
// instance 'offset' steps away.
int32 rotate(int32 value, uniform int offset)

// Exclusive scan of provided 'v's.
int32 exclusive_scan_add(int32 v)
```

1D stencil

```
static inline void relax c(float *output,
                             float* input.
                             int n) {
  for (int i = 0; i < n; i++) {
    float l, c, r;
    l=input[i == 0 ? n-1 : i-1];
    c=input[i];
    r=input\Gamma(i+1) \% n;
    output[i] = (l + c + r)/3;
Runtime for n=1000000: 140 \mu s
```

Try it with ispc

```
export void relax ispc naive(uniform float output[],
                              uniform float input[].
                              uniform int n) {
  foreach (i = 0 ... n) {
    float l, c, r;
    l=input[i == 0 ? n-1 : i-1];
    c=input[i];
    r=input\Gamma(i+1) \% n;
    output[i] = (l + c + r)/3;
```

Try it with ispc

```
export void relax ispc naive(uniform float output[],
                               uniform float input[].
                               uniform int n) {
  foreach (i = 0 ... n) {
    float l, c, r;
    l=input[i == 0 ? n-1 : i-1];
    c=input[i];
    r=input\Gamma(i+1) % n;
    output \Gammai\gamma = (l + c + r)/3;
```

Runtime for n=1000000: $403\mu s$ – what happened?

ispc compiler output

```
relax.ispc:6:13: Performance Warning: Modulus
        operator with varying types is very inefficient.
    r=input[(i+1) % n];
relax.ispc:4:7: Performance Warning: Gather required
        to load value.
    l=input[i == 0 ? n-1 : i-1];
relax.ispc:6:7: Performance Warning: Gather required
        to load value.
    r=input[(i+1) % n];
```

Forces **scalarisation**—but at least the compiler will tell us!

Better way of writing it

```
export void relax_ispc(uniform float output[].
                       uniform float input[],
                       uniform int n) {
  if (programIndex == 0) {
    output[0] = (input[n-1] + input[0] + input[1])/3;
    output[n-1] = (input[n-2]+input[n-1]+input[0])/3:
  foreach (i = 1 ... n-2) {
    float l.c.r:
    c=input[i];
    l=input[i-1]:
    r=input[i+1];
    output[i] = (l + c + r)/3;
```

Runtime for n=1000000: $32\mu s$ – much better!

Better way of writing it

```
export void relax_ispc(uniform float output[].
                        uniform float input[],
                        uniform int n) {
  if (programIndex == 0) {
    output[0] = (input[n-1] + input[0] + input[1])/3;
    output[n-1] = (input[n-2]+input[n-1]+input[0])/3:
  foreach (i = 1 ... n-2) {
    float l.c.r:
    c=input[i];
    l=input[i-1]:
    r=input[i+1];
    output[i] = (l + c + r)/3;
```

Runtime for n=1000000: $32\mu s$ – **much better!** If we do the same thing to the C implementation... $38\mu s$.

Memory accesses

```
Uniform vs[i]; // 'uniform' i
       movss xmm0, dword ptr [rdi + 4*rax]
       shufps xmm0, xmm0, 0
Regular vs[programIndex]:
       movups (%rdi), %xmm0
Irregular vs[is[programIndex]]:
       movss xmm0, dword ptr [rdi + rsi]
       insertps xmm0. dword ptr [rdi + rcx]. 16
       insertps xmm0. dword ptr [rdi + r8]. 32
       insertps xmm0, dword ptr [rdi + rax], 48
```

ispc can always fall back to scalar code.

The GPU perspective

- GPUs have the notion of coalesced memory.
- In the same clock cycle, neighbouring threads should access neighbouring memory locations.
- Allows a single memory bus transaction to service multiple threads.

ispc is similar, but not identical.

- + GPU coalesced memory is *dynamic*—as long as the indexes are OK at runtime, all is well.
- With ispc, the indexing must be *statically* regular.
- This is because (most) CPUs do not actually have real gather instructions.
- GPUs are throughput-oriented, CPUs often more about latency.

Implementing filtering in ispc

How do we filter in parallel?

```
int filter(float *output, float *input, int n) {
  int i = 0:
 for (int i = 0; i < n; i++) {
    float v = input[i];
    if (v >= 0) {
      output[j++] = v;
  return i:
  ■ n=100000: 461µs
 Looks sequential, but we know better
```

Filtering in Futhark

```
let filter (as: [7f32]: [7f32] =
  let keep = map (a \rightarrow if a >= 0 then 1 else 0) as
  let offsets1 = scan (+) 0 keep
 let num to keep = reduce (+) 0 keep
 in scatter (replicate num to keep 0)
             (map2 (\i k ->
                        i.f k == 1
                        then i-1
                        else -1)
                    offsets1 keep)
             as
```

- scan then scatter
- Is that a good fit for ispc?

Filtering in Futhark

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                    offsets1 keep)
             as
```

- scan then scatter
- Is that a good fit for ispc?
- No, because we do not need to *maximise* parallelism
- n=100000: $51.30\mu s$ on gpu04-diku-apl

Sliding-window SIMD

Idea: slide a programCount-sized window sequentially over the input.

```
uniform int m = 0:
foreach (i = 0 ... n) {
  float j = input[i];
  int keep = j \ge 0;
  int offset = exclusive scan add(keep);
  output[m + offset] = i:
  m += reduce add(keep);
return m;
Correct?
```

Slidina-window SIMD

Idea: slide a programCount-sized window sequentially over the input.

```
uniform int m = 0:
foreach (i = 0 ... n) {
  float j = input[i];
  int keep = j \ge 0;
  int offset = exclusive scan add(keep);
  output[m + offset] = i:
  m += reduce add(keep);
return m;
Correct?
```

No, might write garbage.

```
uniform int m = 0:
foreach (i = 0 ... n) {
  float j = input[i];
  int keep = j >= 0;
  int offset = exclusive scan add(keep);
  if (keep) {
    output\m + offset\ = j;
  m += reduce add(keep);
return m:
  ■ n=100000: 407µs
 What is the likely culprit?
```

```
uniform int m = 0:
foreach (i = 0 ... n) {
  float j = input[i];
  int keep = j >= 0;
  int offset = exclusive scan add(keep);
  if (keep) {
    output[m + offset] = j;
  m += reduce add(keep);
return m:
  ■ n=100000: 407µs
  What is the likely culprit?
  That predicated memory write!

    Optimisation: turn control flow into data.
```

```
uniform int m = 0:
foreach (i = 0 ... n) {
  float j = input[i];
  int keep = i >= 0:
  int offset = exclusive scan add(keep);
  if (!keep) {
    offset = programCount-1:
  output[m + offset] = j;
  m += reduce add(keep);
return m;
  ■ n=100000: 137µs
  Why is this valid?
```

Summary

- Almost all CPUs support some kind of SIMD instructions.
- Utilising them can result in nontrivial speedup.
- Manual vectorisation sucks.
- Auto-vectorisation sucks.
- The SPMD programming model seems promising.

For the weekly assignment

- Several tasks about implementing things in ispc.
- See how fast you can make them go compared to C.
- $100 \times \text{speedup belongs to Futhark; don't expect that much.}$