Possible values of Y, in {1,2,3,4,6,9}.

$$P(Y_{1} = Y_{1}) = \begin{cases} P(x_{1}=1, X_{2}=1) = \frac{1}{36} & Y_{1}=1 \\ P(x_{1}=1, X_{2}=2) + P(x_{1}=2, X_{2}=1) = \frac{2}{36} + \frac{2}{36} = \frac{6}{36} & Y_{1}=2 \\ P(x_{1}=1, X_{2}=3) + P(x_{1}=3, X_{2}=1) = \frac{3}{34} + \frac{3}{36} = \frac{6}{36} & Y_{1}=3 \\ P(x_{1}=2, X_{2}=2) = \frac{4}{36} & Y_{1}=4 \\ P(x_{1}=2, X_{2}=3) + P(x_{1}=3, X_{2}=2) = \frac{6}{34} + \frac{6}{36} = \frac{12}{36} & Y_{1}=6 \\ P(x_{1}=3, X_{2}=3) = \frac{9}{36} & Y_{1}=9 \end{cases}$$

$$P(2=3) = P(x_1+x_2=3) = \begin{cases} P(x_1=1, x_2=1) = \frac{1}{36} & 3=2 \\ P(x_1=1, x_2=2) + P(x_1=2, x_2=1) = \frac{14}{36} & 3=3 \\ P(x_1=1, x_2=3) + P(x_1=2, x_2=1) = \frac{14}{36} & 3=4 \end{cases}$$

$$P(x_1=1, x_2=3) + P(x_1=3, x_2=2) + P(x_1=3, x_2=1) = \frac{10}{36} \quad 3=4$$

$$P(x_1=2, x_2=3) + P(x_1=3, x_2=2) = \frac{12}{36} \quad 3=5$$

$$P(x_1=3, x_2=3) = \frac{9}{36} \quad 3=6$$

$$\frac{3}{3} P(x=x|x+y=t) = \frac{P(x=x, x+y=t)}{P(x+y=t)} = \frac{P(x=x, y=t-x)}{P(x+y=t)}$$

$$= \frac{P(x=x) P(y=t-x)}{P(x+y=t)} = \frac{\binom{n_1}{x} p^x (1-p)^{n-x} \binom{n_2}{t} p^{t-x} (1-p)}{\binom{n_1+n_2}{t} p^t} = \frac{\binom{n_1}{x} p^x (1-p)^{n-x} \binom{n_2}{t} p^t}{\binom{n_1+n_2}{t} p^t} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_1+n_2}{t} p^t} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_1+n_2}{t-x}} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_1}{t-x}} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_1}{x} \binom{n_2}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_2}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_1}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_2}{t-x}}{\binom{n_2}{t-x}} = \frac{\binom{n_2}{t-x}}{\binom{n_2}{t$$

$$P(x=x \mid x+y=t) = \frac{P(x=x, y=t-x)}{P(x=x, y=t-x)} \begin{bmatrix} x \sim P(\lambda_1) \\ y \sim P(\lambda_2) \\ y \sim P(\lambda_2) \end{bmatrix}$$

$$= \frac{P(x=x) P(y=t-x)}{P(x+y=t)} = \frac{e^{\lambda_1} \lambda_1}{e^{(\lambda_1+\lambda_2)}} \begin{bmatrix} e^{\lambda_2} \lambda_2^{b-x} \\ e^{(\lambda_1+\lambda_2)} \end{bmatrix} = \frac{e^{\lambda_1} \lambda_1}{e^{(\lambda_1+\lambda_2)}} \begin{bmatrix} e^{\lambda_2} \lambda_2^{b-x} \\ e^{(\lambda_1+\lambda_2)} \end{bmatrix}$$

i.e.  $X \mid X + Y = \sum_{i=1}^{n} \beta_{i} m \left( t_{i} + \frac{\lambda_{i}}{\lambda_{i} + \lambda_{i}} \right)$ 

(3)  $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$   $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$   $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$   $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$   $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$   $f_{\chi}(x) = \begin{cases} 3(1-x)^{2} & 0 < x < 1 \end{cases}$ 

Y = Him (X1, X2, X3, X4); Z = Hax (X1, X2, X3, X4)

X1, X2, X3, Xy 1.i.d. from 1x(x)

d-f- & Y: Fy (y) = P(Y = y) = 1 - P(Y > y)

 $(e < j \times)$   $\frac{\gamma}{\pi} - 1 =$  $((e \ge \times)$   $\gamma - 1) =$ 

 $= 1 - \left(1 - \left\{1 - \left(1 - 9\right)^{3}\right\}\right)^{4}$ 

= 1- (1-4)12 06461

(1x 2 -1) = 12 (1-2)11 - 10 < 2 < 1

d.f. & 2: FZ(3) = P(2 < 3) = TIP(x; < 3) = [P(x < 3)]4 = (1-(1-3)3)4 coes 2 2 1

 $f_{2}(3) = \int 12(1-3)^{2}(1-(1-3)^{3})^{3}$  occh

13 pt do Ox reso per la Cara of Max.

6 Similar to 5

tings, market the constant

1 X: arrival time of XLY 1.i.d Exp(x). - p.d. ffm= x = xx regd prob = P(X < Y, Y-X & E) +P(Y < X), X-Y & E)  $= P(Y-t \leq X \leq Y) + P(X-t \leq Y \leq X)$ = P(X & Y & X+E) + P(Y & X & Y+E)  $[J+p-d-f f X,y \rightarrow \lambda^{n} e^{-\lambda(x+y)}] \sim 200,900$  $\Rightarrow = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{1}{\lambda^2} e^{-\lambda(x+y)} dy dx + \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{1}{\lambda^2} e^{-\lambda(x+y)} dx dy$ = 22 Jexs e- 2y dy dx  $=2\lambda^{2}\frac{1}{4}\left(1-e^{-\lambda t}\right)\int_{-\infty}^{\infty}e^{-2\lambda x}dx=\left(1-e^{-\lambda t}\right)$ 

(8) X 1, X2 ~ U(0,1) ANTE (20 5) 1 (1) 57 15 5 1-1- $Y_{1} = X_{1} + X_{2} =$   $Y_{2} = X_{2} - X_{1}$   $Y_{1} = X_{1} + X_{2}$   $Y_{2} = X_{2} - X_{1}$   $|J| = \frac{1}{2}$   $|J| = \frac{1}{2}$   $|J| = \frac{1}{2}$ ; OLX, 21), OLX2 C1

=> fy1, y2 (\$1, y2) = 1/2; ocy, +y2<2, ocy, -y2<2 Range unconditionally 0<4,<2 & -1<42<1  $x_2 = \frac{y_1 + y_2}{2} | Alm O (x_1 L1 ) = 0 < \frac{y_1 - y_2}{2} < 1$  $y_{1}-2 < y_{1} < 2+y_{2}$  - (1).

Also 
$$0 < x_2 < 1$$
;  $0 < \frac{y_1 + y_2}{2} < 1$   
 $0 < y_1 + y_2 < 2$   
 $-y_2 < y_1 < 2 - y_2$   
 $b - y_1 < y_2 < 2 - y_1$   $-(2)$ 

Combining (1) 
$$\Delta$$
 (2)  
 $\max(y_2, -y_1) < y_1 < \min(2+y_2, 2-y_2)$   
 $\Delta = \max(y_1, 2-y_1) < y_2 < \min(y_1, 2-y_1)$  (3)

Many of 
$$Y_2$$

$$f_{Y_2(y_2)} = \frac{1}{2} \int dy_1 = (1+y_2) \qquad \text{if } -1 < y_2 < 0$$

$$(using (4)) \longrightarrow = \frac{1}{2} \int dy_1 = (1-y_2) \text{ if } 0 < y_2 < 1$$

$$y_2$$

(i.e. 
$$\neq \infty$$
 (anchy dist (0,1)  
In gen.  $\times \infty$  (anchy  $(M, 0) \rightarrow f_{\times}(x) = \frac{0}{\pi} \frac{1}{1 + (x-u)^{2}}$ , -4< x <  $\delta$ ).

$$f_{X,y}(x,y) = \frac{1}{\lceil \alpha_1 \rceil \lceil \alpha_2 \rceil \rceil} x^{\chi_1-1} y^{\chi_2-1} = \frac{x+y}{\vartheta}; x>0, y>0$$

$$= 0 \quad \text{old}.$$

$$U = X+y \quad \text{old} \quad X=UV \quad \text{old} \quad \text{$$

$$A = \frac{x + \lambda}{\lambda + \lambda}$$

$$A = \frac{\lambda}{\lambda + \lambda}$$

$$A = \frac{\lambda}{\lambda}$$

$$A = \frac{\lambda}{\lambda + \lambda}$$

$$A = \frac{\lambda}{\lambda$$

Range 4>0,0<4<1 tu, v(u, v) = 1 (uv) (u(1-v)) e . u 4>0,02421

 $f_{U,V}(u,v) = \begin{cases} \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} \\ \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} & \frac{1}{|\alpha_1+\alpha_2|} \end{cases} \times \frac{1}{|\alpha_1+\alpha_2|} \times \frac{1}{|\alpha_1$ U>0,0<V< 1N1 - 1/ U = L O + U X O/A.  $f_{\nu}(u) = \frac{1}{[\alpha_{1} + \alpha_{2} + \alpha_{1} + \alpha_{2}]} e^{-4/6} \qquad u > 0$  $f_{V}(Q) = \frac{1}{B(d_{1}, d_{2})} Q^{\alpha_{1}-1}(1-Q)^{\alpha_{2}-1} Q^{\alpha_{2}-1}$ V~ Beta.  $f_{X,Y} = \frac{c^2}{(1+x^4)(1+y^4)} - 4 < x < 4$  $U_1 = \frac{x}{y}$ ,  $U_2 = y$   $\begin{cases} x = U_1U_2 \\ y = U_2 \end{cases}$   $J = \begin{vmatrix} u_2 & u_1 \\ 0 & 1 \end{vmatrix} = u_2$ Range - d < u, < d, -d < u2 < d  $f_{0_{1},0_{2}}(u_{1},u_{2}) = \frac{e^{2} |u_{2}|}{(1+u_{1}^{4}u_{2}^{4})(1+u_{2}^{4})} - 4 < u_{1} < t_{1} - 4 < u_{2} < t_{1}$  $f_{U_1}(u_1) = \int_{-1}^{1} f_{U_1, U_2}(u_1, u_2) du_2 = 2 C \int_{0}^{1} \frac{u_2}{(1+u_1^{\prime\prime} u_2^{\prime\prime})(1+u_2^{\prime\prime})} du_2$  $= \frac{C \Pi}{2} \cdot \frac{1}{1 + u_1 r} \quad (on integrable).$ ∫fy(4,) du,=1 => c= 2/12

=) fu, (4,) = # -d < h, < t.

(auchy dist.

(12) 
$$f_{X,Y}(x,y) = \frac{1}{2\pi} e^{-\frac{1}{2}(x^2 + y^2)} - 4 < x < a, -a < y < a$$

$$X = R \omega_0 \Re$$

$$Y = R \sin \Re$$

$$J = \left| \begin{array}{ccc} \omega_0 \theta & -r \sin \theta \\ \sin \theta & r \cos \theta \end{array} \right| = r$$

Range Y>0, 0 < 0 < 27

$$f_{R, \mathbf{m}}(r, \theta) = \frac{1}{2\pi} e^{-r^2/2} r$$
,  $r > 0$ ,  $0 < \theta < 2\pi$ 

$$f_{R}(\tau) = re^{-\tau/2}$$

$$f_{\widehat{H}}(0) = \frac{1}{2\pi}$$

$$0 < 0 < 2\pi$$

$$f(0) = \frac{1}{2\pi}$$

$$0 < 0 < 2\pi$$

$$f(0) \sim U(0, 2\pi)$$

( Dad -) Pilled JE

3) R LAD are indep.

Define 
$$y = \frac{R^2}{2}$$
  $y > 0$ 

$$R = \sqrt{2}\sqrt{y} \qquad \frac{dr}{dy} = \frac{1}{\sqrt{2}y}$$

$$f_{\gamma}(y) = \frac{1}{\sqrt{2y}} \sqrt{2y} e^{-y}$$

$$= 0$$

$$= 0$$

$$= \sqrt{2y}$$

```
U = x^2 + y^2 = R^2 - f^2 f r.v. R
       V = \frac{x}{y} = \omega t \oplus - f \partial_t r. v. \oplus
  Since R & B are indep, U & V are also indep
          i.e. x2+y2 & xy are indep
         U, ~ U(0,1)
 (13)
         - fund ~ Exp(1) - straight for round
           U2 ~ U(0,1)
           2 TU 2 ~ U(0, 200) - stronglit form)
 => - In U, ~ Exp(1) & 2TT U2~ U[0,2T) and are indep
   By problem # (12)
it dust of (-InU, 2TU2) in some on it dust of (RM)
      i.e. (-InU1, 2TU2) = (R, P)
      i.e. \left(-2\ln \upsilon_1, 2\pi \upsilon_2\right) \stackrel{d}{=} \left(R^2, \mathcal{C}\right)
      i. e (J-2InU, Go(2RU2),

V-2InU, Sim(2RU2))
      i.e. (x1, x2) = (R600, RSin1)
            => { X, and X2 are i.i.d N(0,1) x. v-8.
ALL Sol
  Direct method U,, U2 1.1.d U(0,1).
               f_{U_1,U_2}(u_1,u_2) = 1; o < u_1 < 1, o < u_2 < 1
            X1 = V-2 In U1 Cos (27 U2)
            X2= V-2 ln U2 Sin (2T U2)
    Range of X1; - x < x1 < x, sty - x < x2 < x
```

$$X_{1}^{n} + X_{2}^{n} = -2 \ln U_{1}$$

$$\frac{X_{2}}{X_{1}} = \tan \left(2\pi U_{2}\right)$$

$$U_{1} = \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right)$$

$$U_{2} = \frac{1}{2\pi} \tan^{-1}\left(\frac{X_{2}}{X_{1}}\right)$$

$$J = \left(\exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right)\left(-x_{1}\right) + \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right)\left(-x_{2}\right)$$

$$-\frac{X_{2}}{2\pi}\left(x_{1}^{n} + x_{2}^{n}\right) + \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right)\left(-\frac{1}{2\pi}\right)$$

$$|\mathcal{I}| = \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right) + \frac{1}{2\pi} \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right) + \frac{1}{2\pi} \exp\left(-\frac{1}{2}(x_{1}^{n} + x_{2}^{n})\right)$$

$$= \left(\frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{1}}\right) \left(\frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{2}}\right)$$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{1}}$$

$$= \left(\frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{2}}\right) \left(\frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{2}}\right)$$

$$= \frac{1}{\sqrt{2\pi}} e^{-\frac{1}{2}x_{1}}$$

 $f_{\gamma_{1},\gamma_{2},\gamma_{3}}(y_{1},y_{2},y_{3}) = y_{2}y_{3}^{2} e^{-33}; \quad 0 < y_{1}< 1; \quad 0 < y_{2}< 1; \quad y_{3}>0$   $f_{\gamma_{1},\gamma_{2},\gamma_{3}}(y_{1}) = \int_{0}^{y_{2}} y_{2} dy_{2} \int_{0}^{y_{2}} y_{3}^{2} e^{-33} dy_{3} = i \quad 0 < y_{1}< 1$   $1.e. \quad y_{1} \sim U(0,1)$ 

 $f_{\gamma_2(y_2)} = y_2 \int_0^1 dy_1 \int_0^{x_2} y_3^2 e^{-y_3} dy_3$ 

 $f_{y_2} = y_2 \times 1 \times 2$   $0 < y_2 < 1$  $1.2. \quad y_2 \sim Beta(2,1)$   $\int_{x}^{x} x \cdot Beta(m,n) = \frac{I_m \cdot I_m}{I_m \cdot I_m} \times \frac{m-1}{I_m \cdot I_m}$ 

 $f_{y_3}(y_3) = \left( \int_{0}^{1} dy_1 \int_{0}^{1} y_2 dy_2 \right) y_3^2 e^{-y_3}$   $= \frac{1}{2} e^{-y_3} 0 y_3^2 \qquad 0 < y_3 < 4$ 

Y . Y .

(a) 
$$f_{X_{1}, X_{2}}(x_{1}, x_{2}) = \frac{1}{11} \frac{1}{2^{N/2} \left[\frac{n_{1}^{2}}{2}\right]} e^{-x_{1}/2} x_{1}^{\frac{n_{1}^{2}}{2}-1}, x_{1} > 0$$

$$= c \frac{11}{11} e^{-x_{1}/2} x_{1}^{\frac{n_{1}^{2}}{2}-1}, x_{1} > 0$$

$$Y_{1} = \frac{x_{1}}{x_{2}} ; Y_{2} = x_{1} + x_{2} \left[ \begin{array}{c} x_{1} = \frac{y_{1}y_{2}}{y_{1}+1} \\ x_{2} = \frac{y_{2}}{y_{1}+1} \end{array} \right]$$

$$= \frac{1}{11} = \frac{1}{11} \frac$$

$$\frac{Z_{1}}{X_{2}/n_{2}} \sim F_{n_{1},n_{2}} > F drol^{-} in th (n_{1},n_{2}) d.f$$

$$\frac{Z_{2}}{X_{2}/n_{3}} = \frac{X_{3}/n_{3}}{n_{3}} = n_{1}F$$

$$2 = \frac{x_3/n_3}{x_1+x_2/n_1+n_2} \sim F_{n_3, n_1+n_2}$$

(16) 
$$X \sim N(0,1)$$
  $Y \sim \chi^{2}_{N} - imdef$   
 $f_{X,Y} = \frac{1}{\sqrt{2}\pi} e^{-\chi^{2}/2} \frac{1}{2^{n/2} \lceil n \rceil_{2}} e^{-\chi/2} y^{n/2-1}$ 

$$T = \frac{x}{\sqrt{y/n}}$$
 define duming  $U = y$   $\begin{pmatrix} x \\ y \end{pmatrix} \rightarrow \begin{pmatrix} T \\ U = y \end{pmatrix}$ 

$$X = T \sqrt{\frac{1}{n}}$$

$$Y = 0$$

$$X = T \sqrt{\frac{1}{n}}$$

$$Y = 0$$

$$= \int_{T,U} \left( t,u \right) = \frac{1}{\sqrt{2\pi} \, 2^{n/2} \, \left[ \sqrt{n} \, \exp \left( -\frac{1}{2} \, \frac{t^2 \, u}{n} \right) \exp \left( -\frac{u}{2} \right) \right] u^{n/2} = \frac{1}{2}$$

$$f_{T}(t) = \int_{0}^{t} f(t, u) du = \int_{0}^{t} \frac{1}{T_{N}U} \int_{0}^{t} \frac{u^{N-1/2}}{u^{N-1/2}} \exp\left(-\frac{u}{2}\left(1 + \frac{t^{N}}{n}\right)\right) du$$

$$= \sqrt{2\pi} \frac{2^{N/2} \left[n_{2} \sqrt{n}\right]}{\sqrt{2\pi}} \int_{0}^{t} \frac{u^{N-1/2}}{\sqrt{n}} \exp\left(-\frac{u}{2}\left(1 + \frac{t^{N}}{n}\right)\right) du$$

(17) 
$$H_{Y}(t) = E(e^{tY}) = E(e^{t\sum_{i} X_{i}^{T}})$$

$$= \prod_{i=1}^{n} E(e^{tX_{i}^{T}})$$

$$= \prod_{i=1}^{n} H_{X_{i}^{T}}(t)$$

$$X_{i}^{T} \sim X_{i}^{T} \rightarrow = \prod_{i=1}^{n} (1-2t)^{-n/2} = (1-2t)^{-n/2}$$

$$\Rightarrow Y \sim X_{i}^{T}$$

Jt p.d.f. & y & Xn+1

$$f_{y, X_{n+1}}(y, x) = \left(\frac{1}{2^{n/2}} \left(\frac{1}{\sqrt{2^{n/2}}} e^{-\frac{x}{2}/2}\right) \times \left(\frac{1}{\sqrt{2^{n/2}}} e^{-\frac{x^{n/2}}{2}}\right)$$

$$T = \frac{x_{n+1}}{\sqrt{y_n}}$$

$$V = V$$

$$V = V$$

$$J = \begin{vmatrix} \sqrt{u} \\ \sqrt{n} \end{vmatrix} = \sqrt{\frac{u}{n}}.$$

it p.d.f. of Thu

$$f_{T,U}(b,u) = \left(\frac{1}{2} \frac{h^2}{n} \sqrt{n}\right)^{-1} \exp\left(-\frac{1}{2} \frac{b^2 u}{n}\right) \exp\left(-\frac{u}{2}\right) \frac{u^{n/2-1}}{u^{n/2}}$$

$$f_{T}(b) = \left(2^{nh} \left[ \frac{n}{2} \sqrt{2x} \sqrt{x} \right]^{-1} \right)^{\frac{1}{N}} u^{\frac{n-1}{2}} \exp\left(-\frac{u_{2}}{2}\left(1 + \frac{b^{2}}{x}\right)\right) du$$

$$= \left(2^{nh} \left[ \frac{n}{2} \sqrt{2x} \sqrt{x} \right]^{-1} \right)^{-1} \frac{\frac{n+1}{2}}{\left(\frac{1}{2}\left(1 + \frac{b^{2}}{x}\right)\right)^{\frac{n+1}{2}}}, -4 \times b \times dx$$

$$= \frac{\frac{n+1}{2}}{\sqrt{\pi} \left[ \frac{n}{2} \sqrt{x} \right]} \left(1 + \frac{b^{2}}{x}\right)^{-\frac{n+1}{2}}, -4 \times b \times dx$$

$$P(2 = 3) = P(X + V = 3) = P\left(\frac{3}{x = 0}(X = x \cap Y = 3 - x)\right)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3} P(x = x \cap Y = 3 - x)$$

$$= \sum_{x = 0}^{3$$

$$P(x=x, 2=3) = P(x=x, Y=3-x)$$

 $= \begin{cases} p^{2}q^{3} ; & x=0,1,\ldots 2; & 3=0,1,\ldots 2 \end{cases}$ 

$$P(|X=x||2=3) = \frac{P(x=x,2=3)}{P(z=x,2=3)}$$

$$= \frac{1}{3+1} = \frac{1}{3+$$

$$Z = m_{1}(x, y)$$

$$P(2 = 3) = P(x_{s} = 3, y = 3)$$

$$+P(x = 3, y > 3)$$

$$+P(x > 3, y = 3)$$

$$= (2 + 3)^{3} + \sum_{y=3+1}^{y} P(x = 3, y = y)$$

$$+ \sum_{y=3+1}^{y} P(x = x, y = 3)$$

$$= (2 + 3)^{3} + \sum_{y=3+1}^{y} 2 + \sum_{x=3+1}^{y} 2 + \sum_{$$