

CSC418/2504 Computer Graphics

RobKaz

Some Slides/Images adapted from Marschner and Shirley
Some slides courtesy of Karan Singh, Videos courtesy of [AlanBeckerTutorials](#)

Announcements

- Assignment 6 due Friday, Assignment 7 due on March 29th
- Office hours will be in BA 5287 until further notice
 - (aka I've given up trying to get access to Dave's office)
- Undergraduate drop date: March 17th
- No lecture next week. We'll still have tutorial and office hours, and you can ask questions in preparation for Midterm 2.

Announcements

- A5 marks will be released in a day or so.
- Remark requests:
 - The TAs haven't seen remark requests made after the first round (they don't get MarkUs notifications)
 - A1, A2, A3, A4 remark requests are due by 11:59pm on Wednesday March 13th
 - Remark requests for A5, A6, and A7 will be due at 11:59pm on the day the remark request office hour takes place.

Any Questions ?

Today: Advanced Topics in Rendering

Lecture 9: Advanced Topics in Rendering

- Advanced ray tracing:
 - Instancing
 - Constructive Solid Geometry
 - Super-sampling/Anti-aliasing
 - Depth of field
 - Glossy reflections
 - Motion blur
- Advanced shading techniques
 - Cel shading/Toon shading

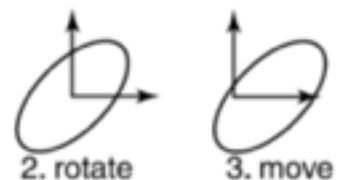
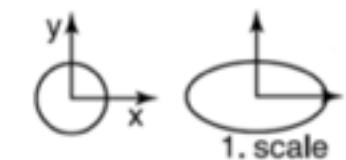
Lecture 9: Advanced Topics in Rendering

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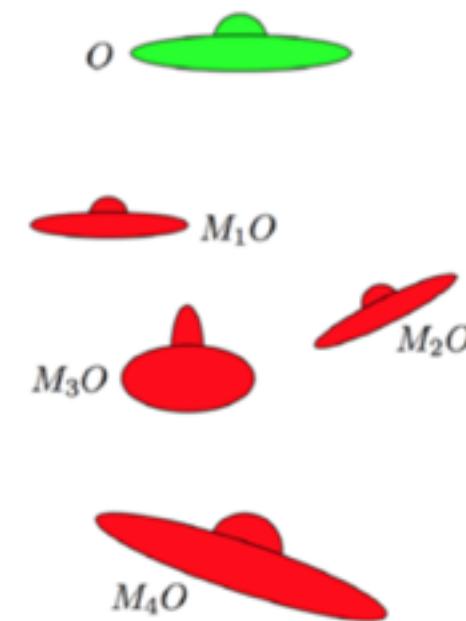
Copying and transforming objects

Instancing is an elegant technique to place various transformed copies of an object in a scene.

Expl.: circle → ellipse



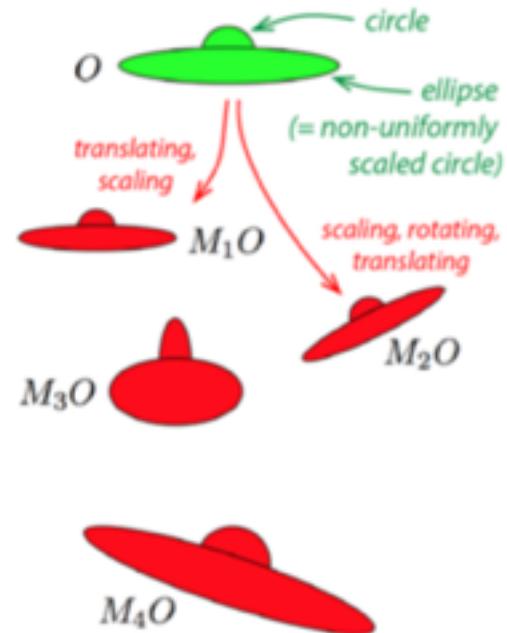
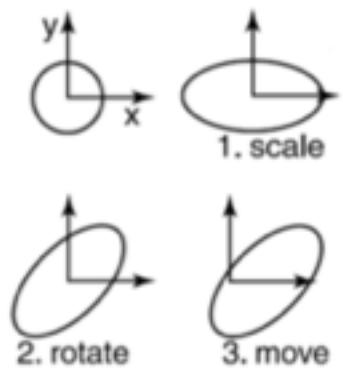
3. move



Copying and transforming objects

Instancing is an elegant technique to place various transformed copies of an object in a scene.

Expl.: circle → ellipse

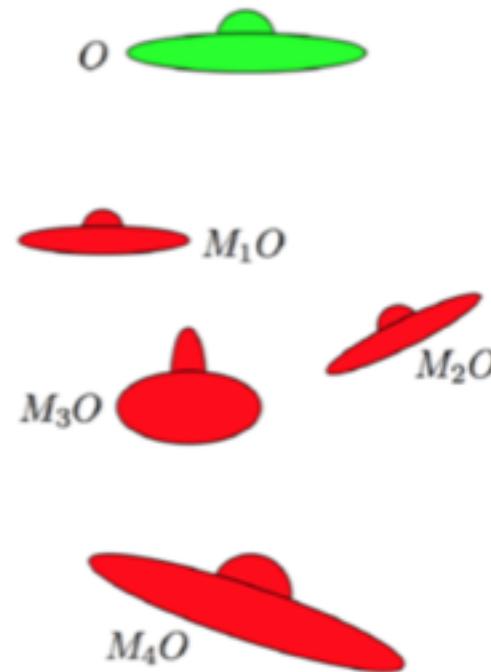


Copying and transforming objects

Instead of making actual copies, we simply store a **reference** to a base object, together with a **transformation matrix**.

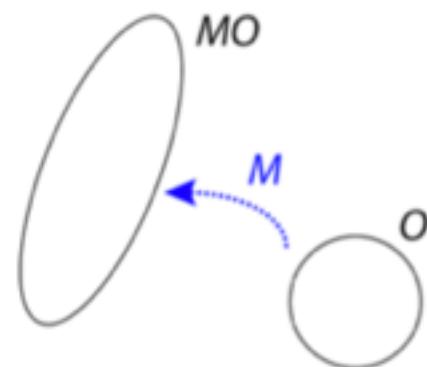
That can save us lots of storage.

Hmm, but how do we compute the **intersection** of a ray with a randomly rotated ellipse?



Ray-instance intersection

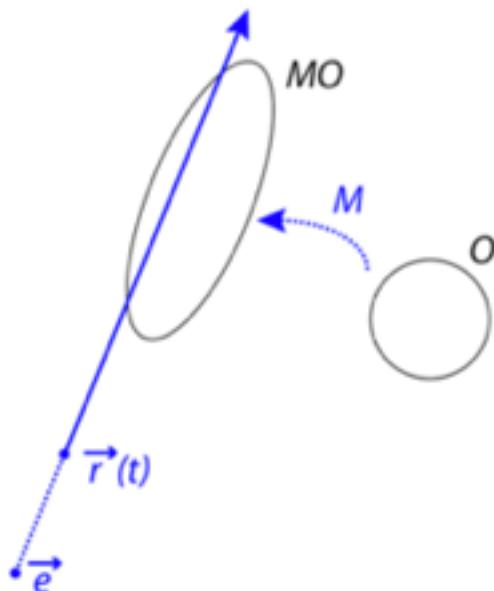
Assume an object O that is used to create an object MO via instancing.



Ray-instance intersection

Now, we want to create the intersection of MO with the ray $\vec{r}(t)$, which in turn is defined by the line

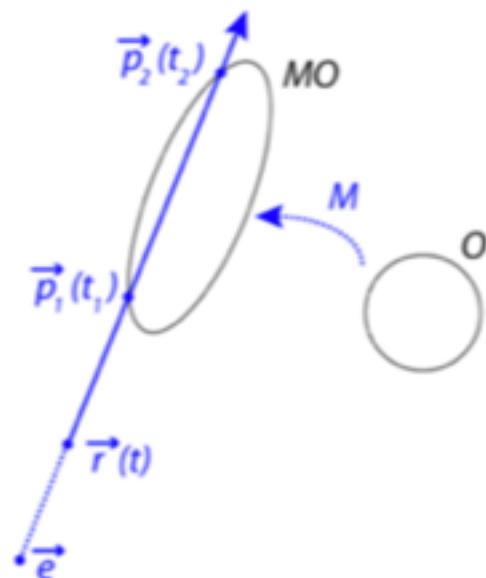
$$\vec{l}(t) = \vec{e} + t\vec{d}.$$



$$\vec{l}(t) = \vec{e} + t \vec{d}$$

Ray-instance intersection

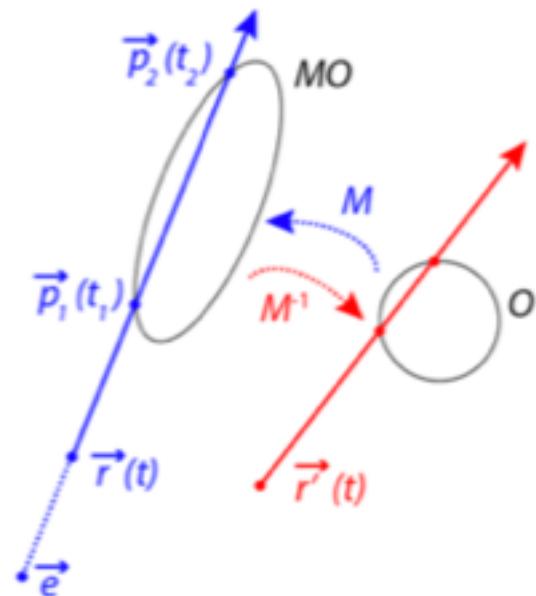
Fortunately, such
complicated intersection tests
(e.g. ray/ellipsoid) can often be
replaced by much simpler tests
(e.g. ray/sphere).



$$\vec{r}(t) = \vec{e} + t \vec{d}$$

Ray-instance intersection

To determine the intersections \vec{p}_i of a ray \vec{r} with the instance MO , we first compute the intersections \vec{p}'_i of the **inverse transformed ray** $M^{-1}\vec{r}$ and the **original object** O .



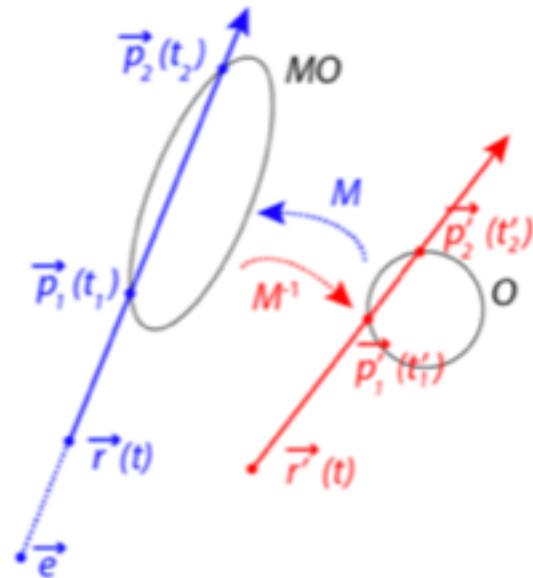
$$\vec{r}(t) = \vec{e} + t \vec{d}$$

Ray-instance intersection

The points \vec{p}_i are then simply

$$M\vec{p}'_i \text{ or } \vec{l}(t'_i)$$

because the linear transformation preserves relative distances along the line.

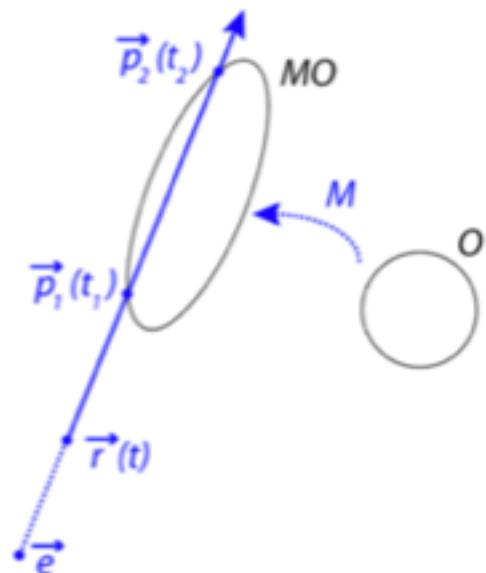


$$\vec{r}(t) = \vec{e} + t \vec{d}$$

Ray-instance intersection

Two pitfalls:

- The **direction vector** of the ray should *not* be normalized
- **Surface normals** transform differently!
→ use $(M^{-1})^T$ instead of M for normals



$$\vec{r}(t) = \vec{e} + t \vec{d}$$

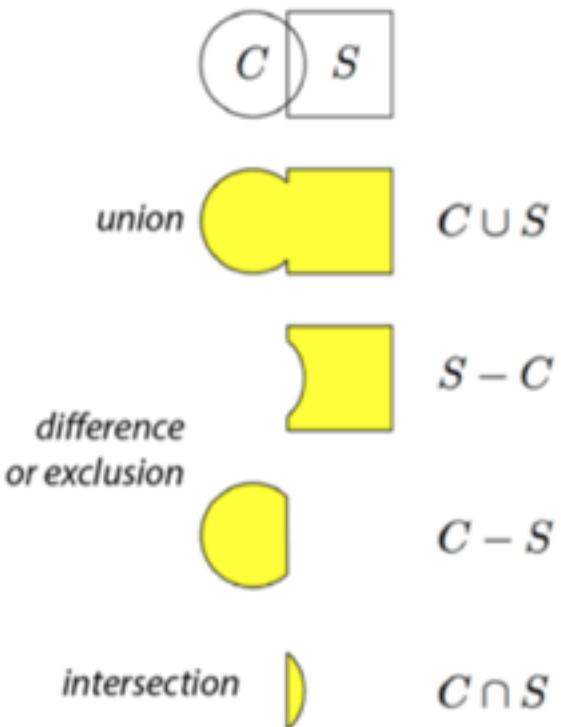
Lecture 9: Advanced Topics in Rendering

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Constructive solid geometry

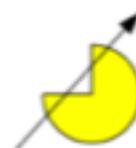
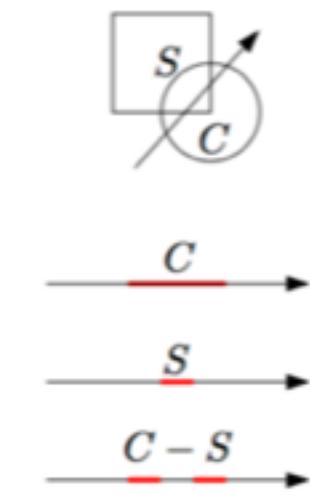
To model our scenes in ray tracing, we can basically use any object that allows us to calculate its intersection with a 3D line.

Using **Constructive Solid Geometry** (CSG), we can build complex objects from simple ones with **set operations**.



Intersection and CSG

Instead of actually constructing the objects, we can calculate **ray-object intersections** with the original objects and perform set operations on the resulting **intervals**.

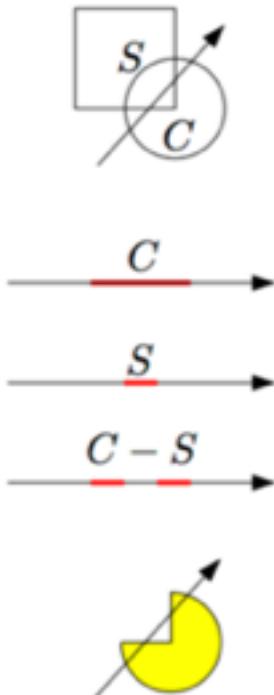


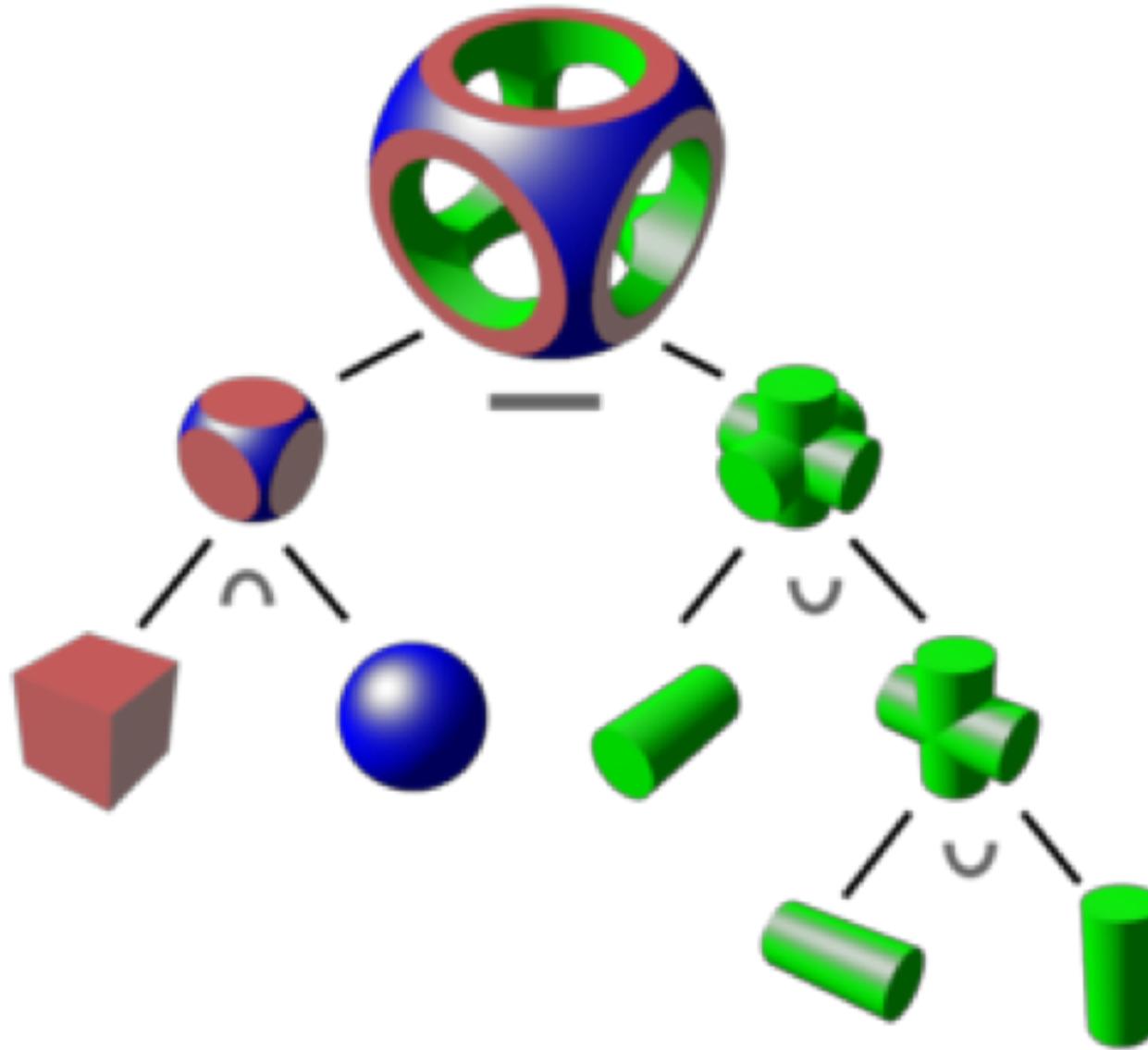
Intersection and CSG

For every base object, we maintain an **interval** (or set of intervals) representing the part of the ray **inside** the object.

The intervals for combined objects are computed with the **same set operations** that are applied to the base objects.

The borders of the resulting intervals are our intersection points.





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Distributed Ray Tracing

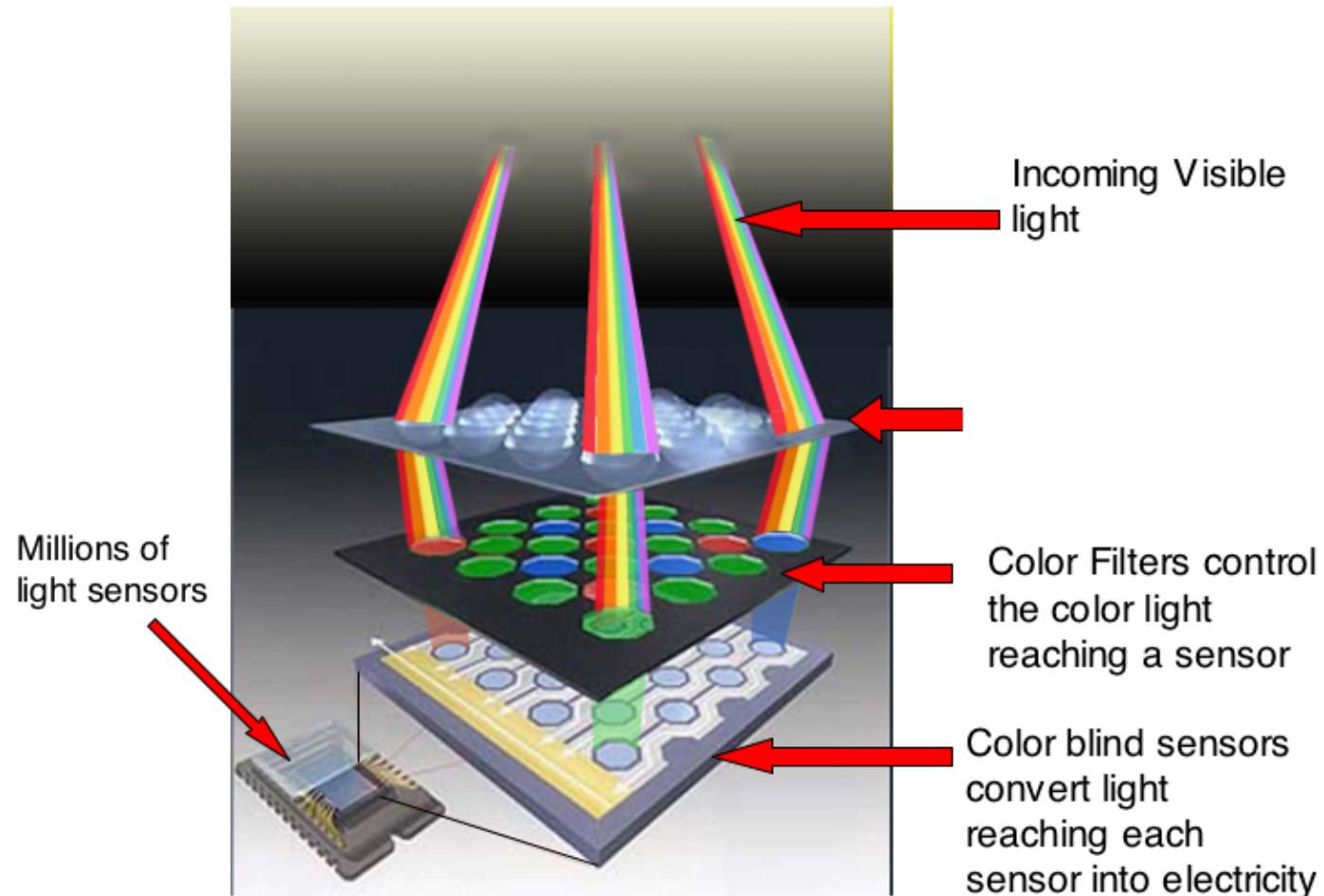
- Not ray tracing on a distributed system...
- Based on randomly distributed oversampling
- Reduces “aliasing artifacts” in renderings
- What is aliasing?
- Issue of having limited resolution on a screen.

Distributed Ray Tracing

- Real world has infinite resolution
- Each pixel is a small window through which we can see part of the scene.
- Single ray per pixel is an inaccurate representation

“Single ray per pixel is inaccurate”

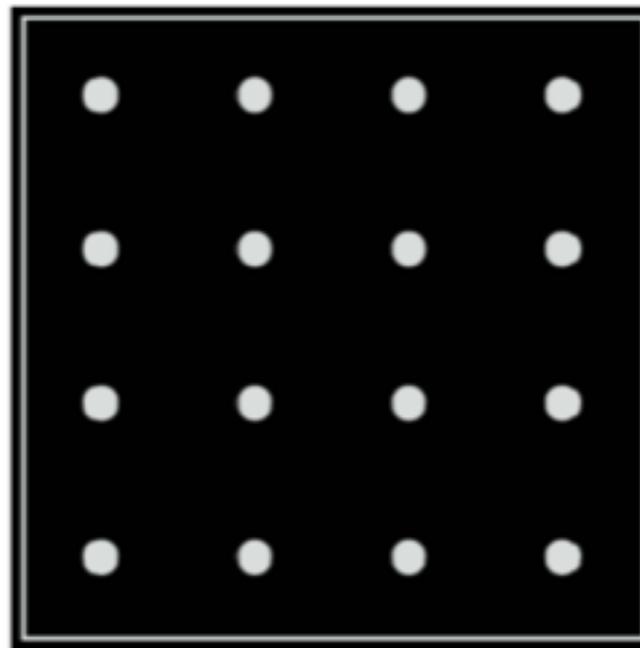
RGB Inside the Camera



Solution:

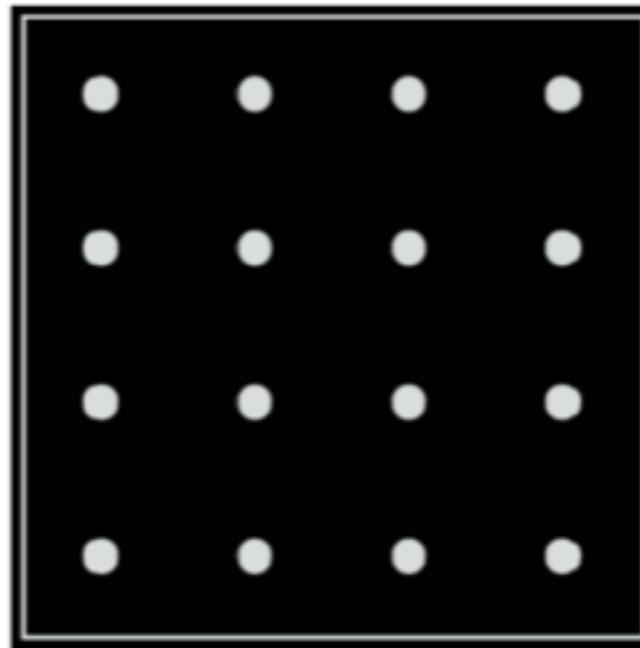
- Send multiple rays through a pixel
- This is called “Super sampling”
- How shall we choose samples (rays) in a given pixel?

Option 1: Regular sampling



Note, this black square is a single pixel

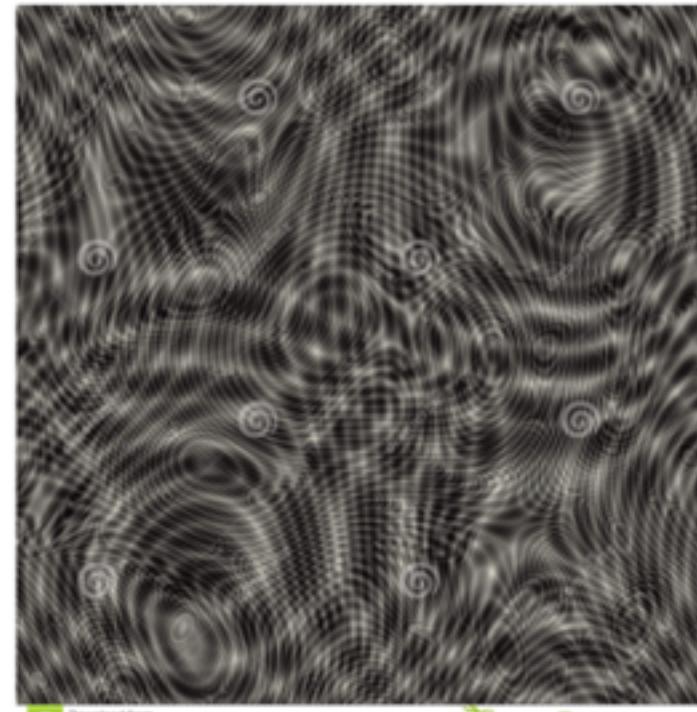
Option 1: Regular sampling



- Regularities can create moiré pattern (high frequency masquerading for low frequency)

Note, this black square is a single pixel

Aliasing example: Moiré pattern



Aliasing example: Moiré pattern

a·li·as·ing

/'älēəsīNG/ 

noun

1. PHYSICS • TELECOMMUNICATIONS

the misidentification of a signal frequency, introducing distortion or error.
"high-frequency sounds are prone to aliasing"

2. COMPUTING

in computer graphics, the jagged, or saw-toothed appearance of curved or diagonal lines on a low-resolution monitor.

Aliasing example: Moiré pattern

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Signal processing
definition



Aliasing example: Moiré pattern

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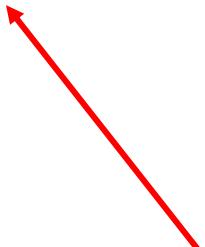
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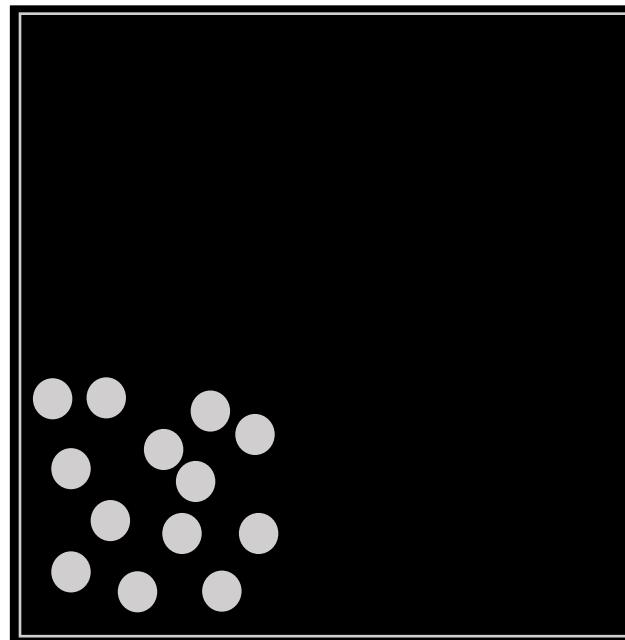
in computer graphics, the jagged, or saw-toothed appearance of curved or diagonal lines on a low-resolution monitor.

The computer graphics definition. An example of the signal processing def, think of each pixel as being a sample of the image



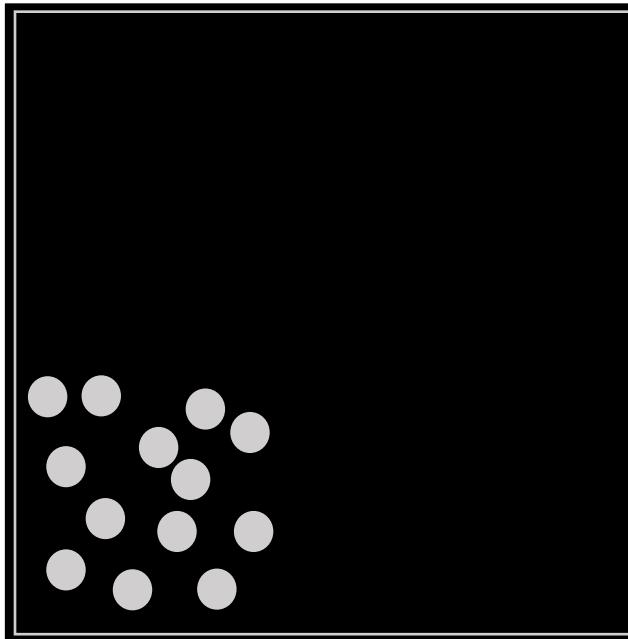
Board example

Option 2: Random sampling



Note, this black square is a single pixel

Option 2: Random sampling

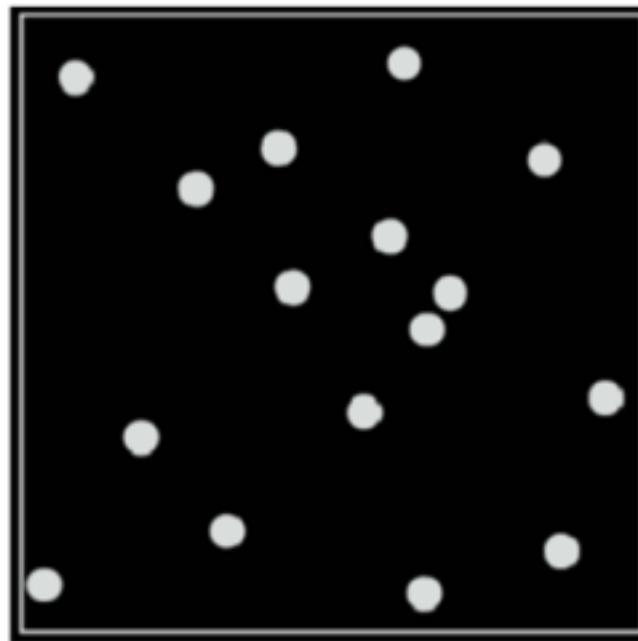


Could lead to a poor distribution (not even over the pixel)

Requires a lot of samples to make it equally distributed

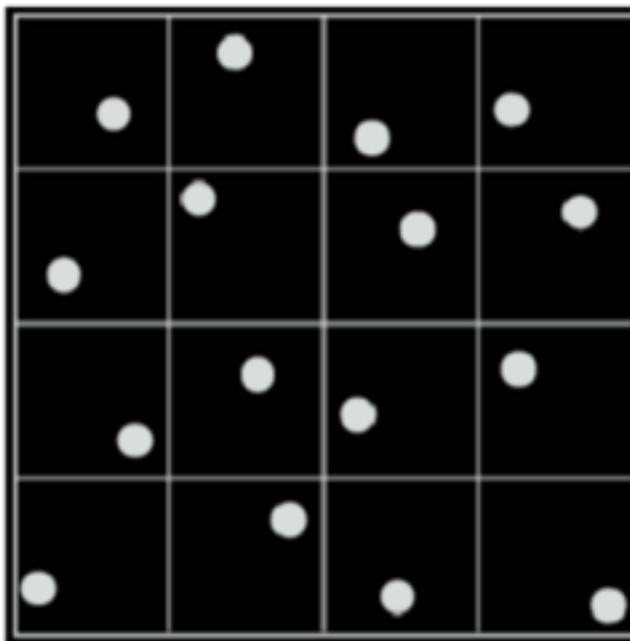
Note, this black square is a single pixel

Option 3: “Jitter” sampling



Note, this black square is a single pixel

Option 3: “Jitter” sampling

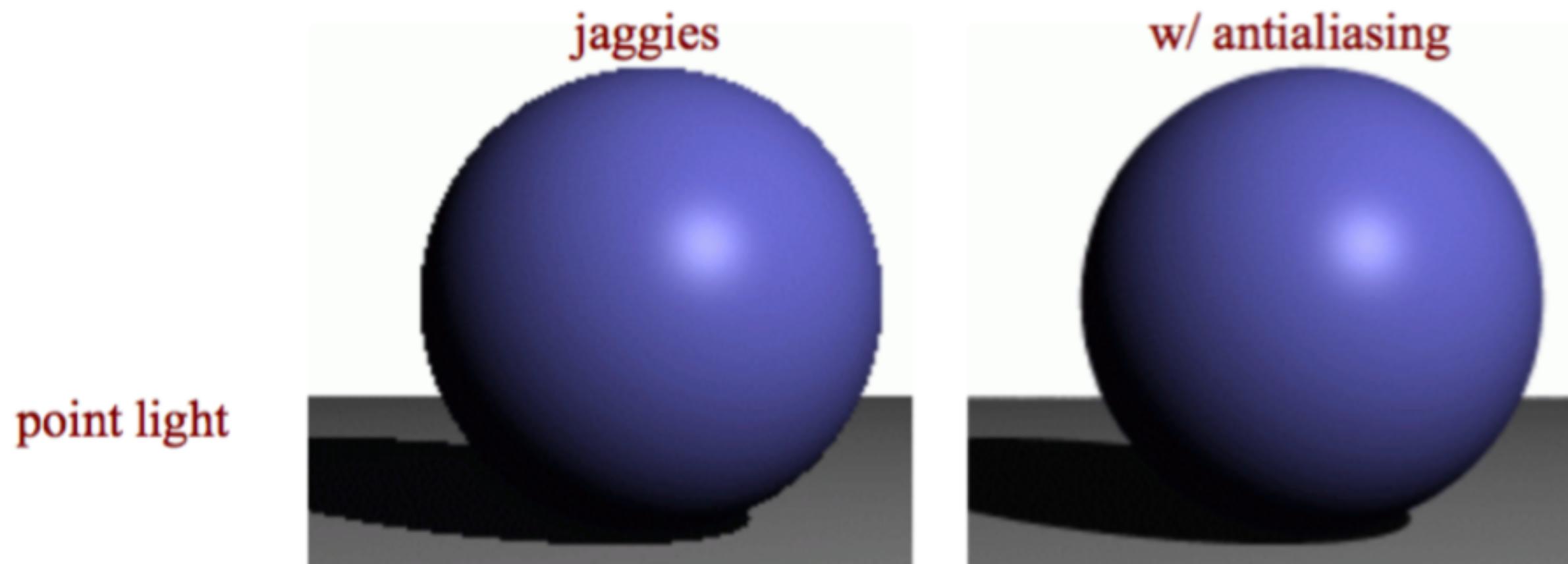


Randomly sample
within a regular grid
of “sub-pixels”

Ensures randomness
as well as being
evenly distributed
over the pixel

Note, this black square is a single pixel

Antialiasing - Supersampling



Lecture 9: Advanced Topics in Rendering

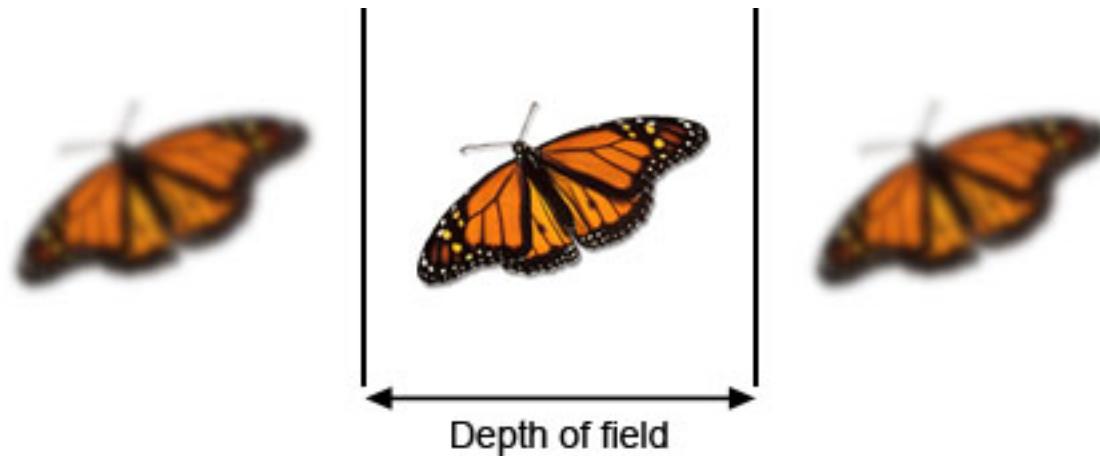
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Depth of field

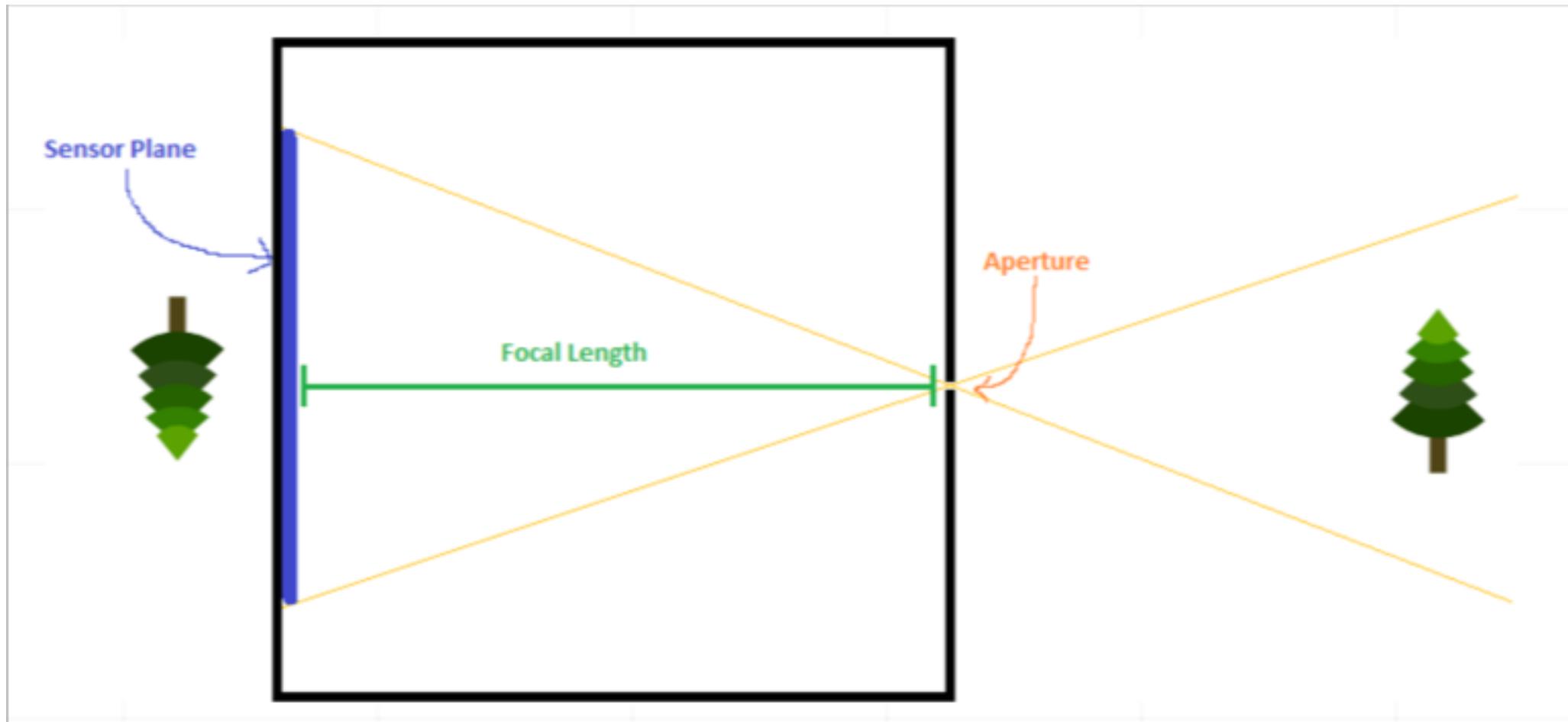


Source: Wikipedia

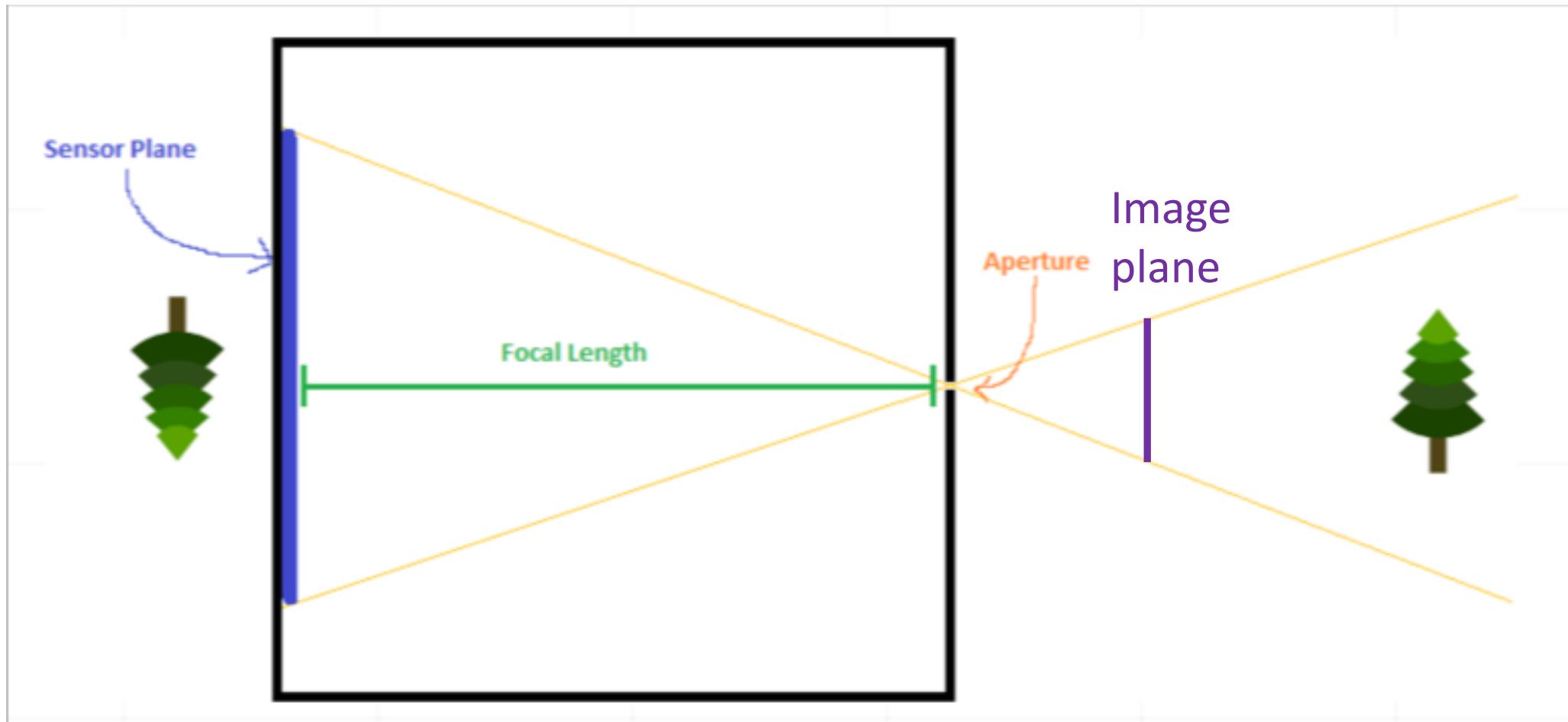
Depth of field



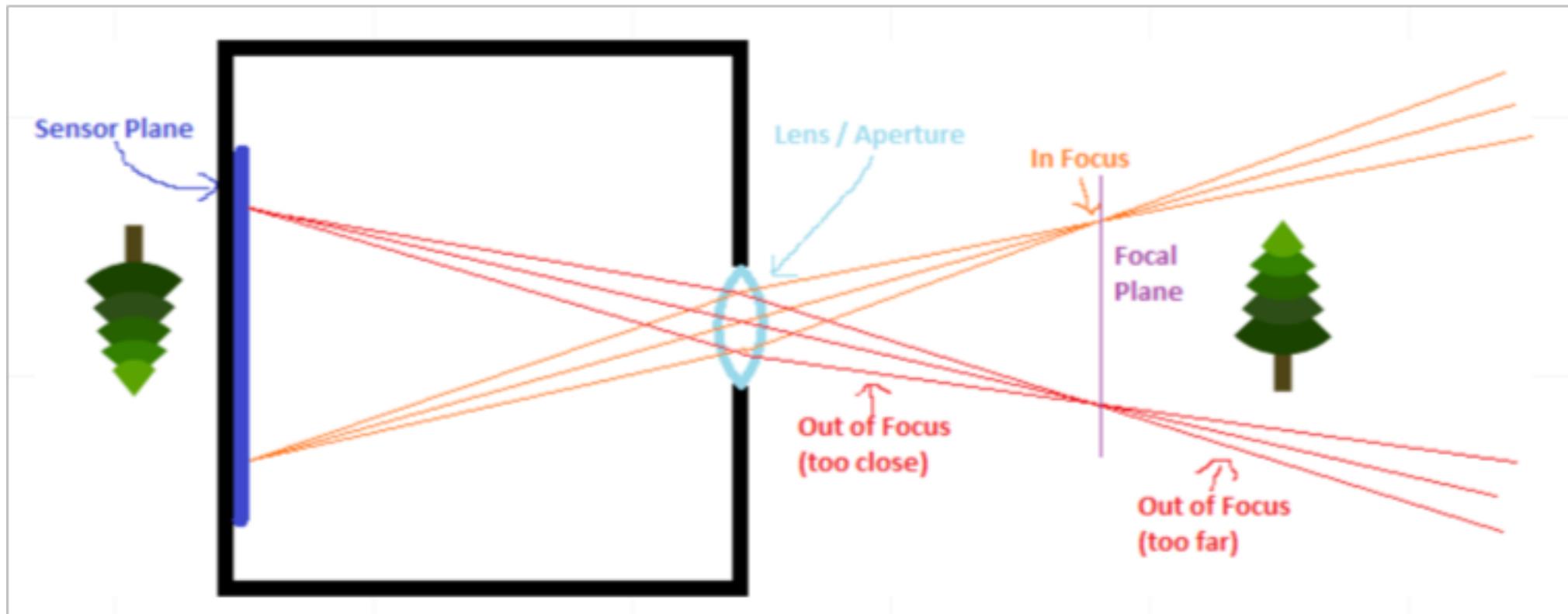
Depth of field



Depth of field

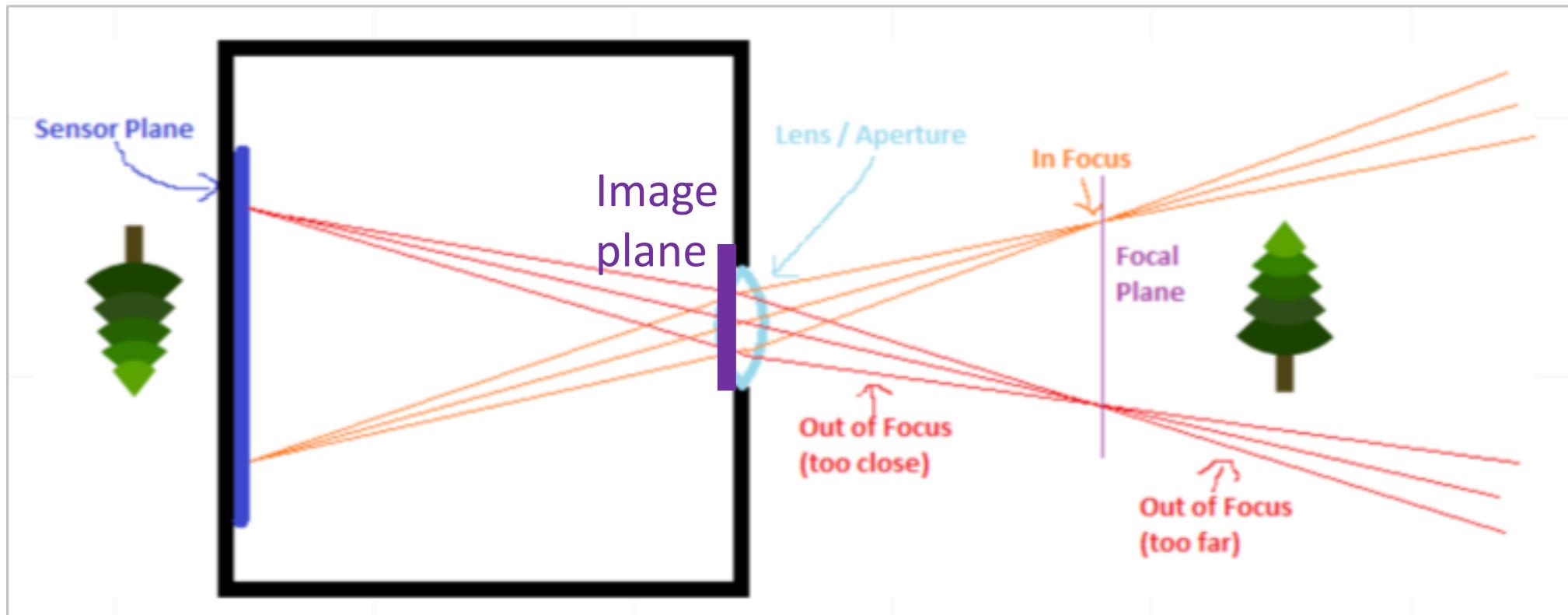


Depth of field



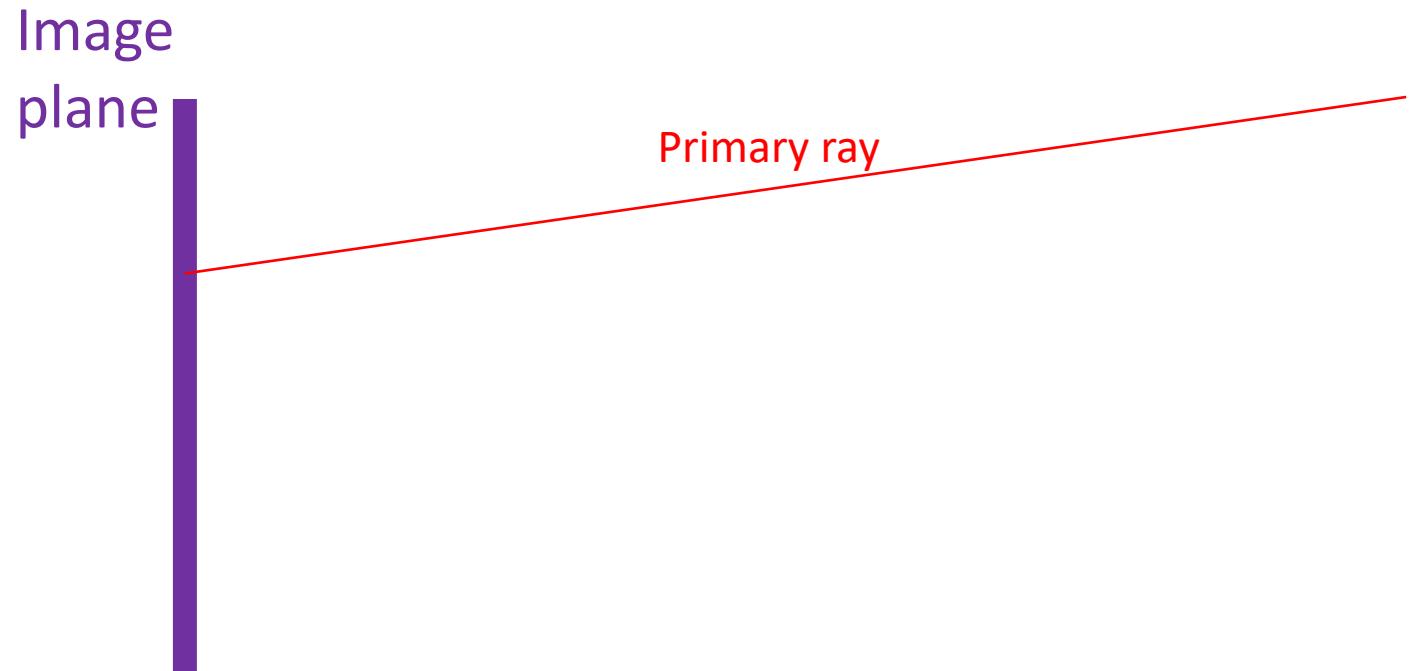
Depth of field

- Remember, our image plane was in front of the pinhole, let's put it on the lens



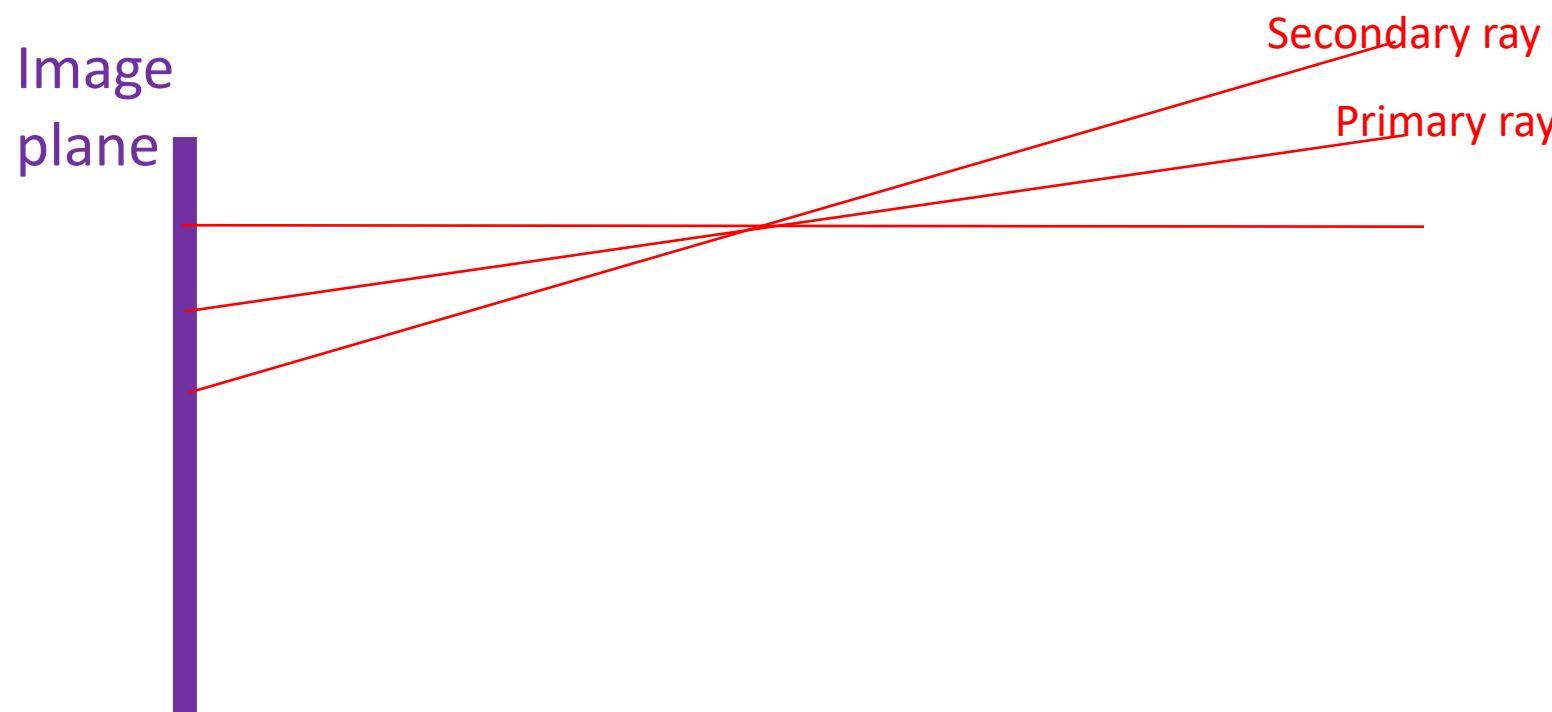
Simulating a lens

- The color for a **single pixel** is an average from a bunch of rays, all from a different origin



Simulating a lens

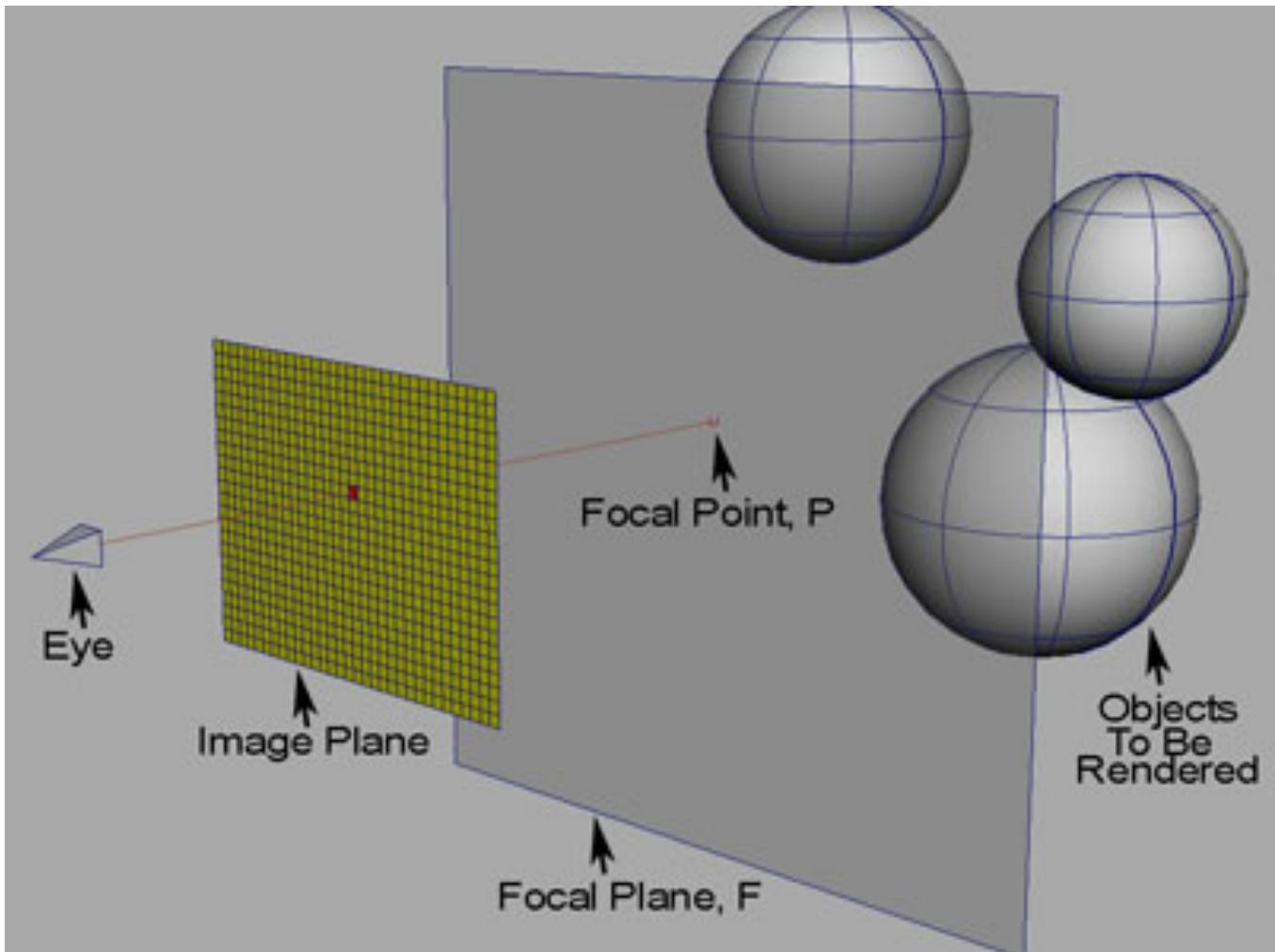
- The color for a **single pixel** is an average from a bunch of rays, all from a different origin



Note that although these other rays have origins at a different part of the image plane, they all color the same pixel

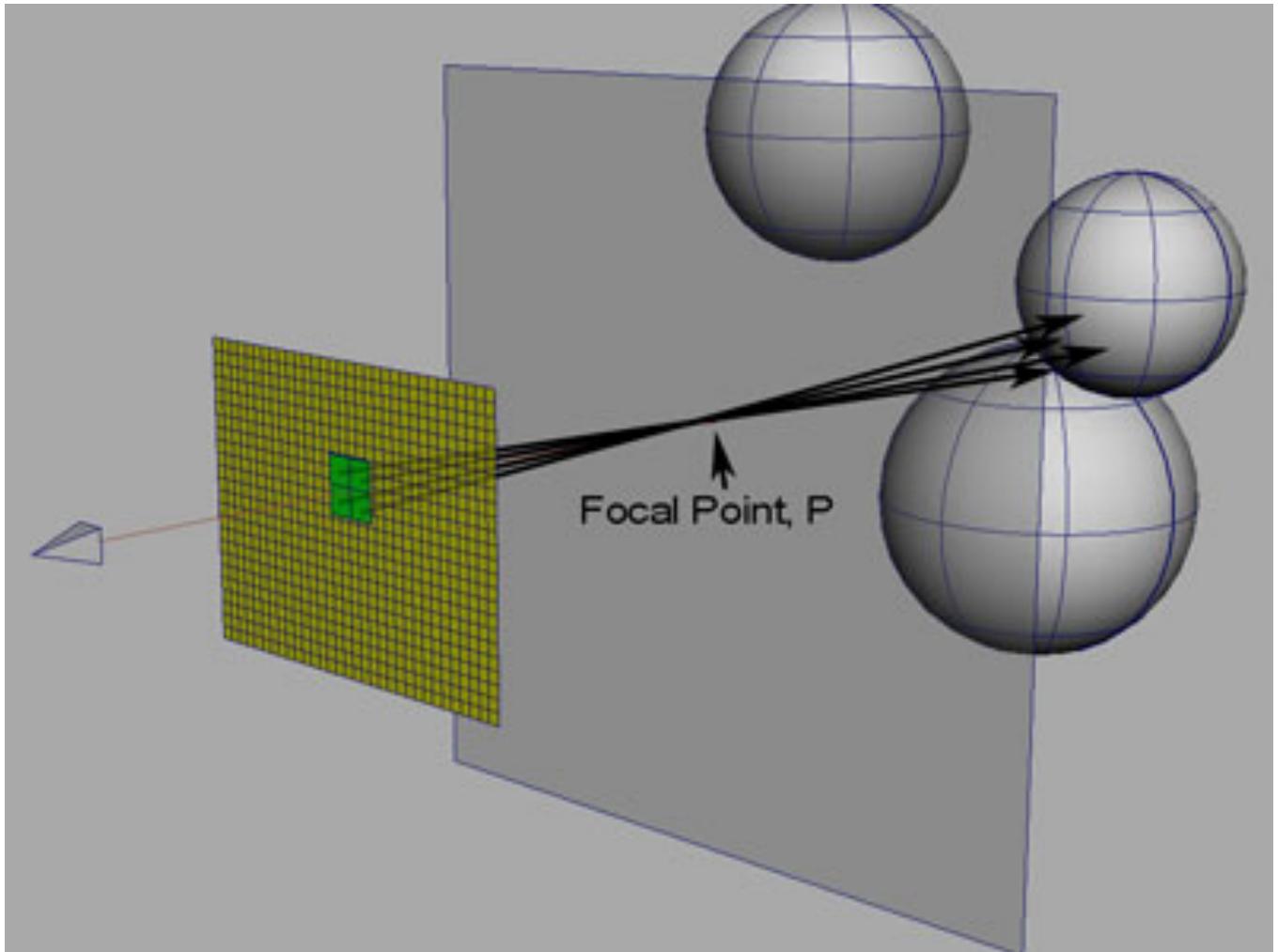
Depth of field

- For a single pixel:
- First, pick the focal distance from the image plane, and cast the primary ray that distance.
- This gives the focal point P of the primary ray



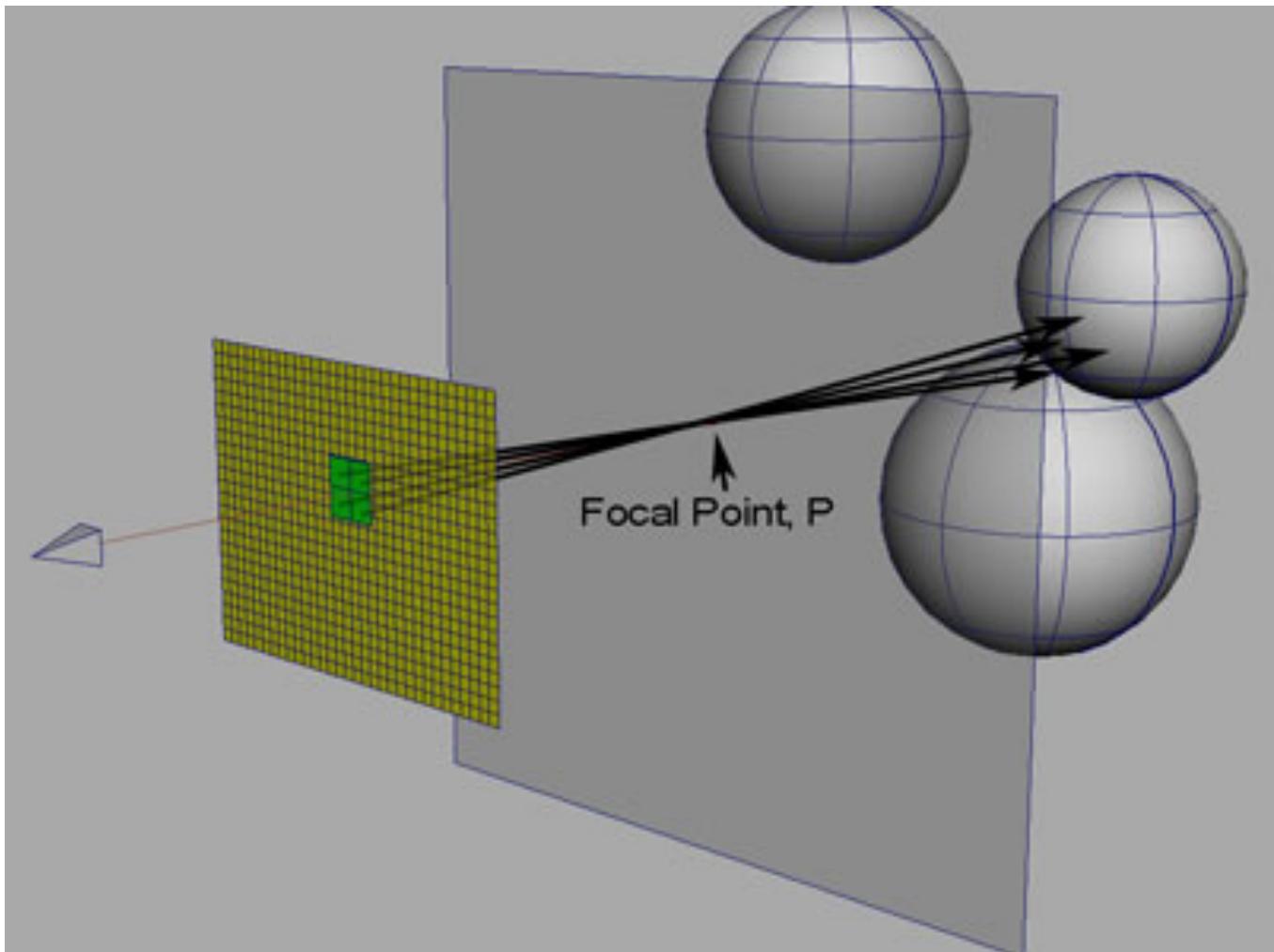
Depth of field

- For a single pixel:
- Next, to cast a secondary ray, change the origin to a nearby point, and change the direction so the secondary ray points to P
- (change the origin from O to O', and the new direction is P-O')



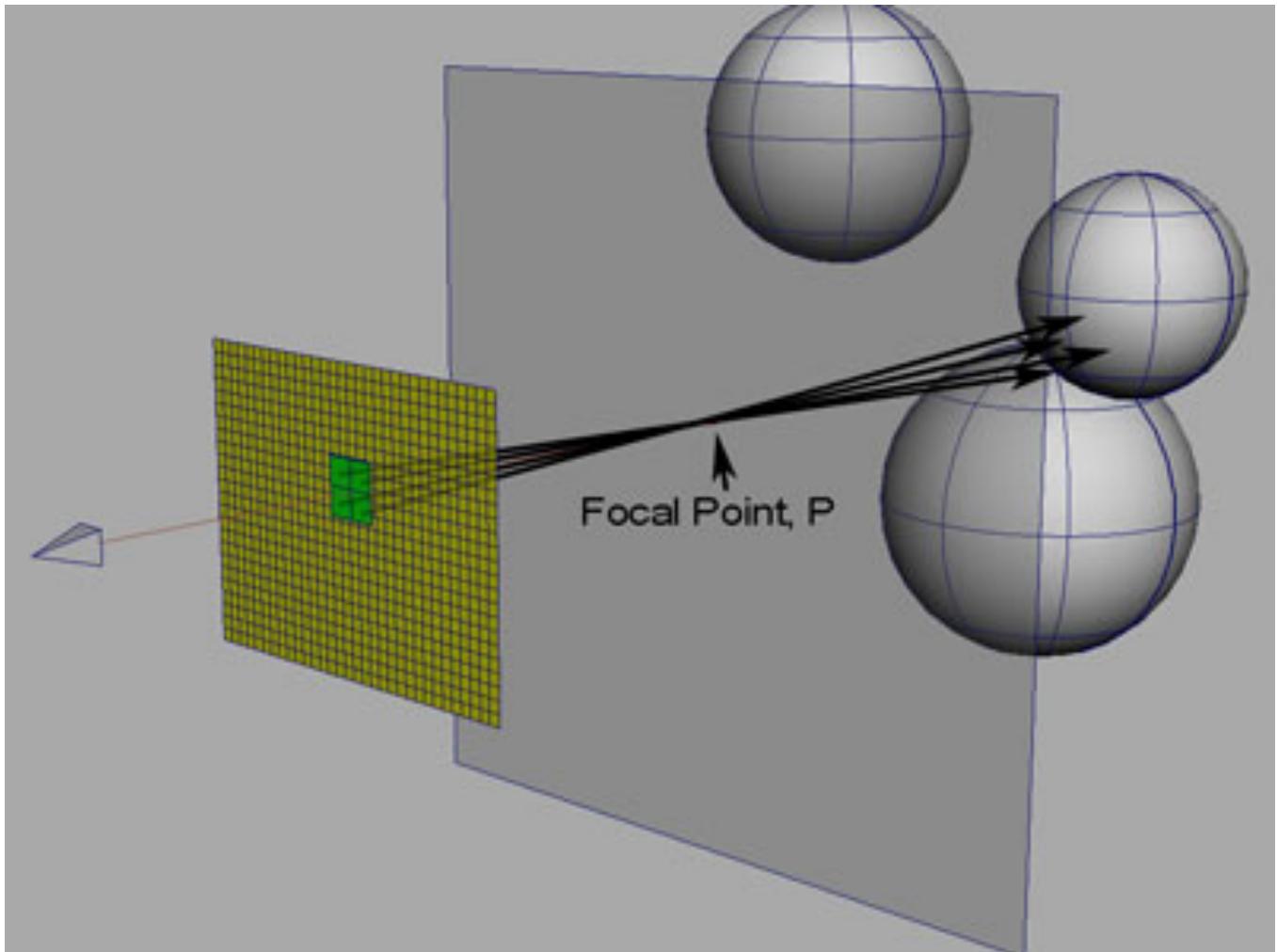
Depth of field

- For a single pixel:
- Do this a lot of times per pixel, averaging the color from casting each secondary ray
- (Note you'll still need to do anti-aliasing, or there will be jaggies for objects that are in-focus)



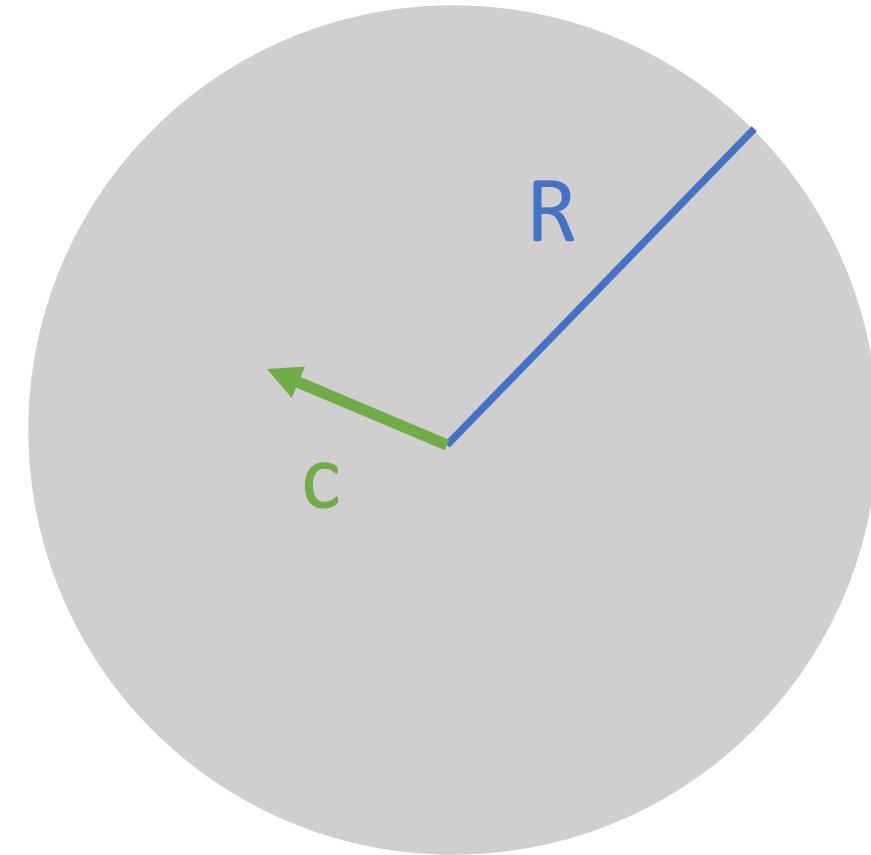
Depth of field – Aperture shape

- Picking an aperture shape:
 - In this picture, the origin is changed to be somewhere in this green square
 - Personally I prefer to change it by a vector on a disk



Depth of field – Aperture shape

- $O' = O + c$
- Where c is a random vector on the 2D disk of radius R centered at the origin
- The larger R is, the larger the aperture, the narrower the depth of field.
- (Look up how to randomly sample a disk uniformly)





Bokeh

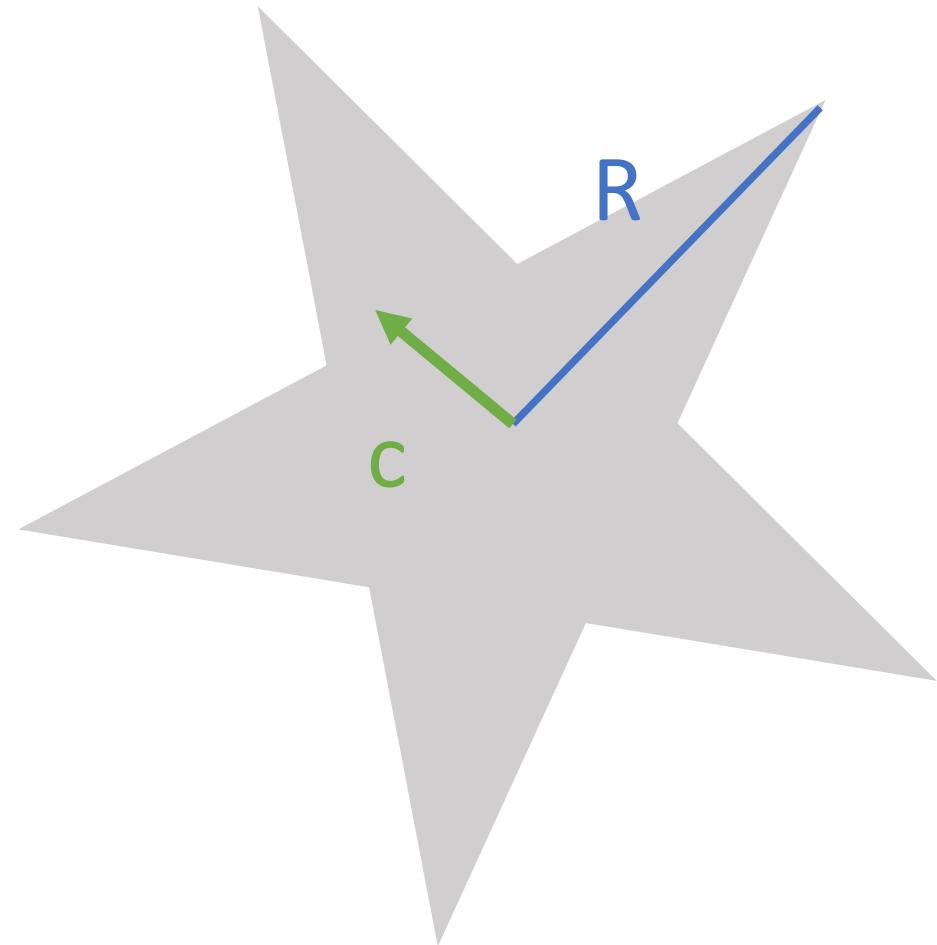


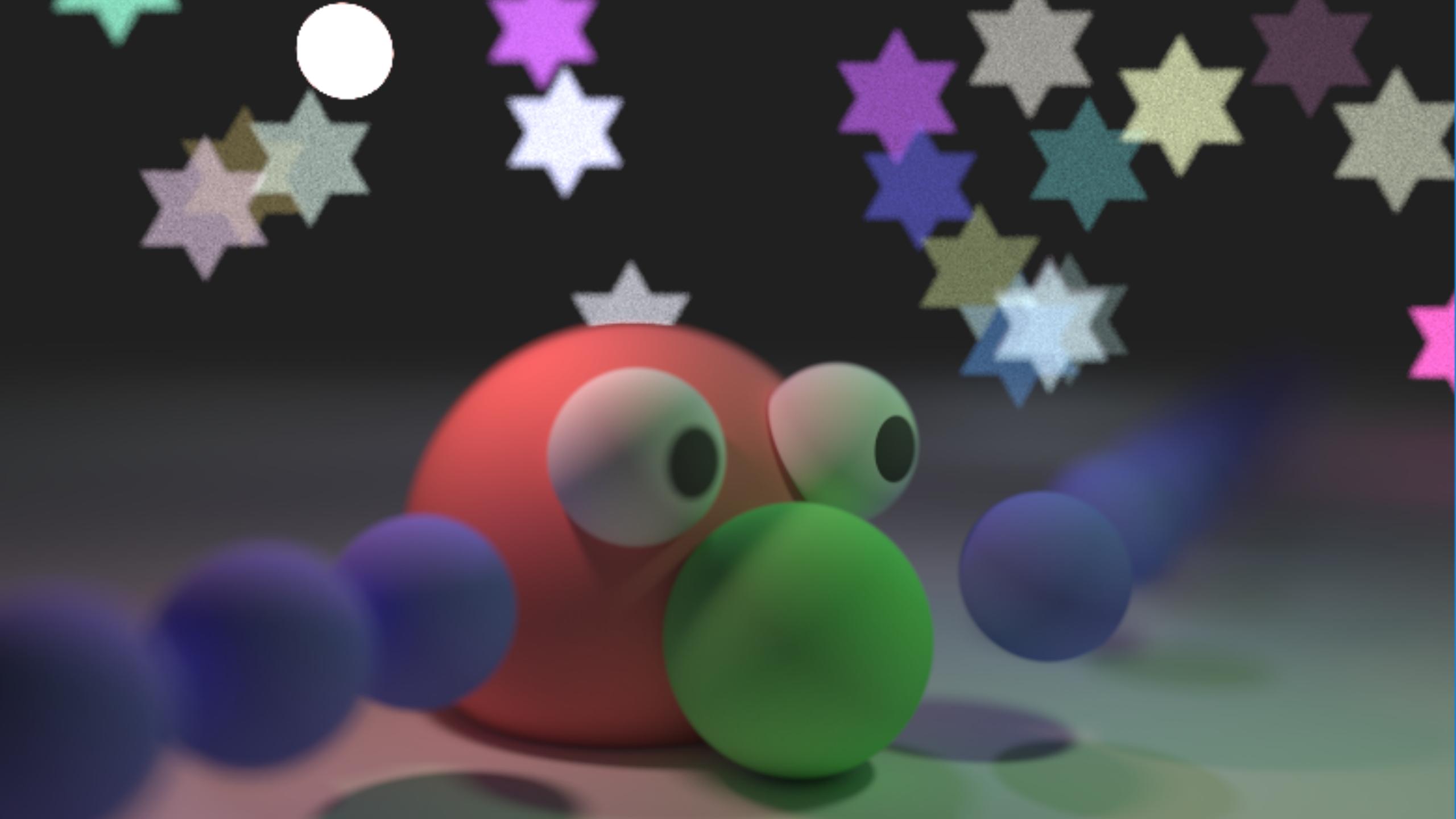
Aperture shape impacts the Bokeh



https://www.diyphotography.net/diy_create_your_own_bokeh/

Depth of field – Aperture shape

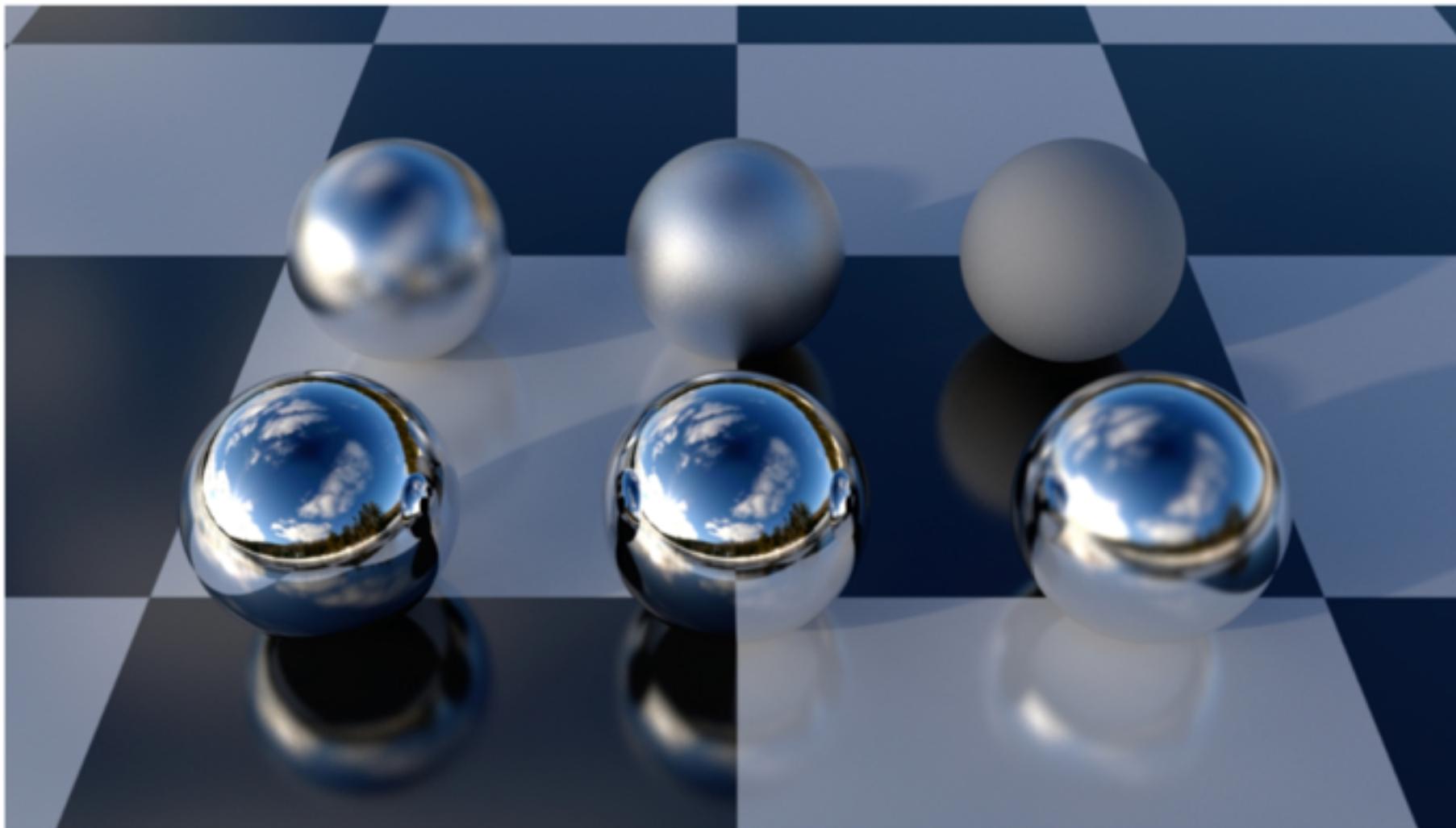




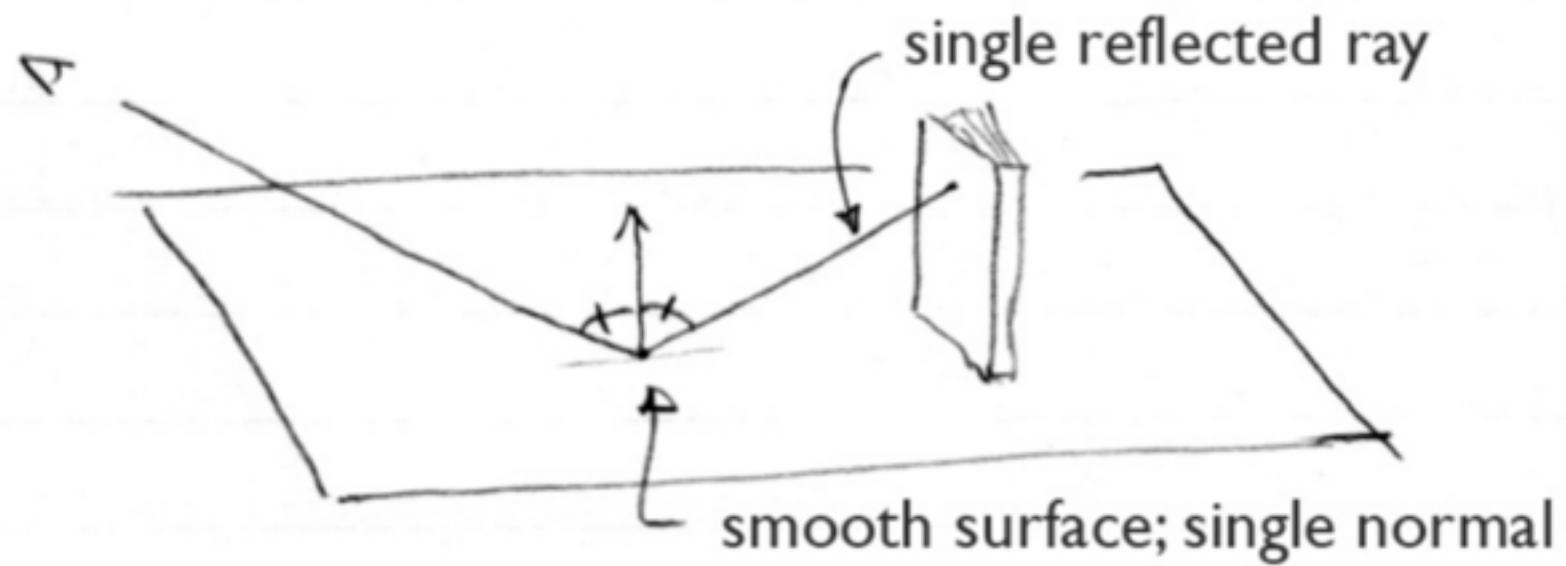
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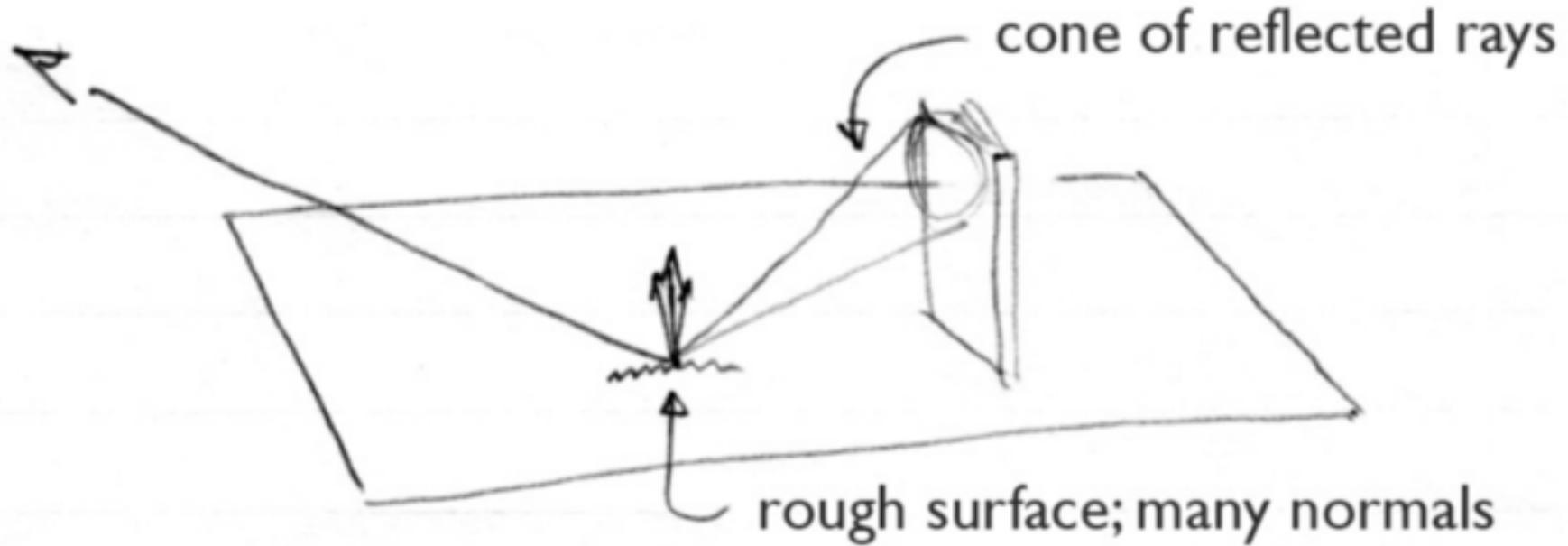
Glossy Reflections



Glossy Reflections

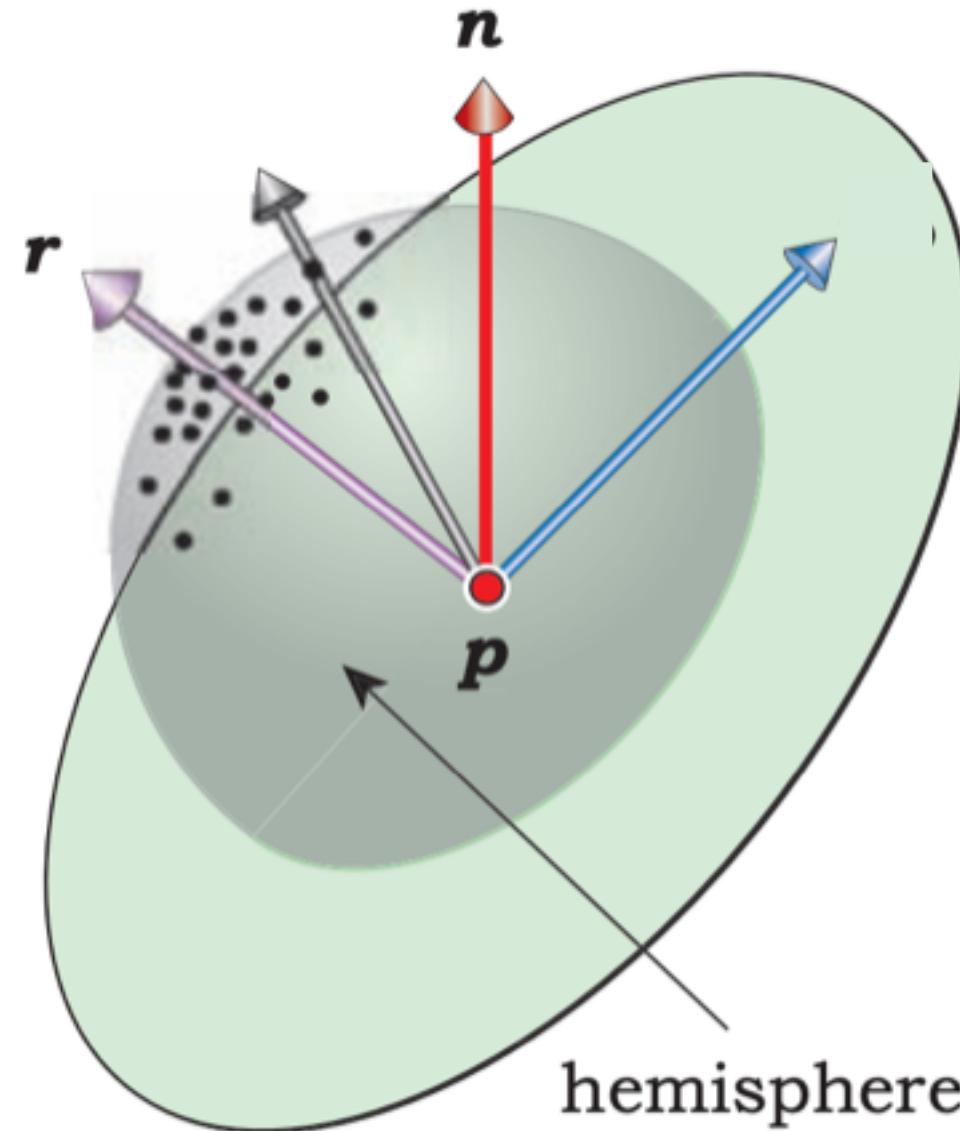


Glossy Reflections



Glossy Reflection

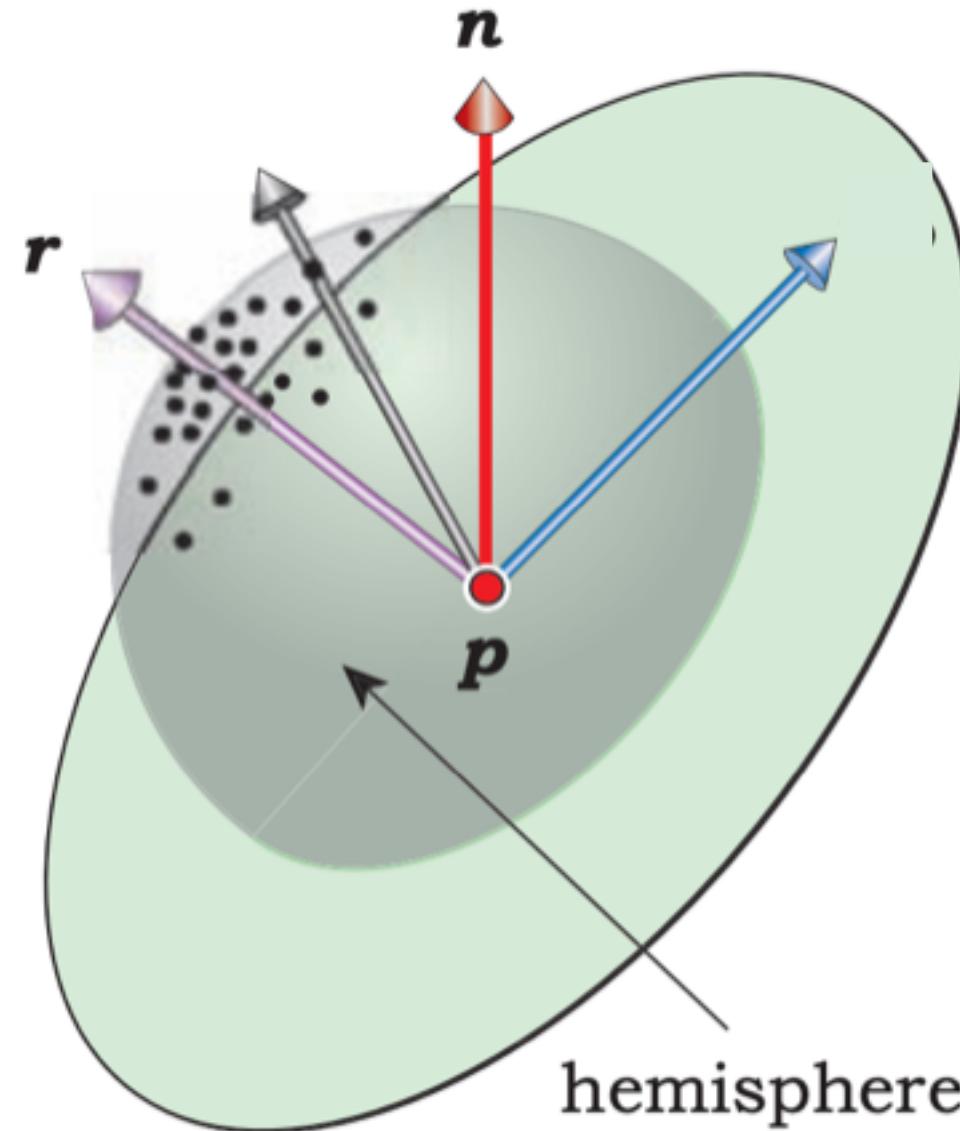
- We want to sample rays that are randomly clustered near the reflected ray



Source: “Ray Tracing from the ground up” By Kevin Suffern

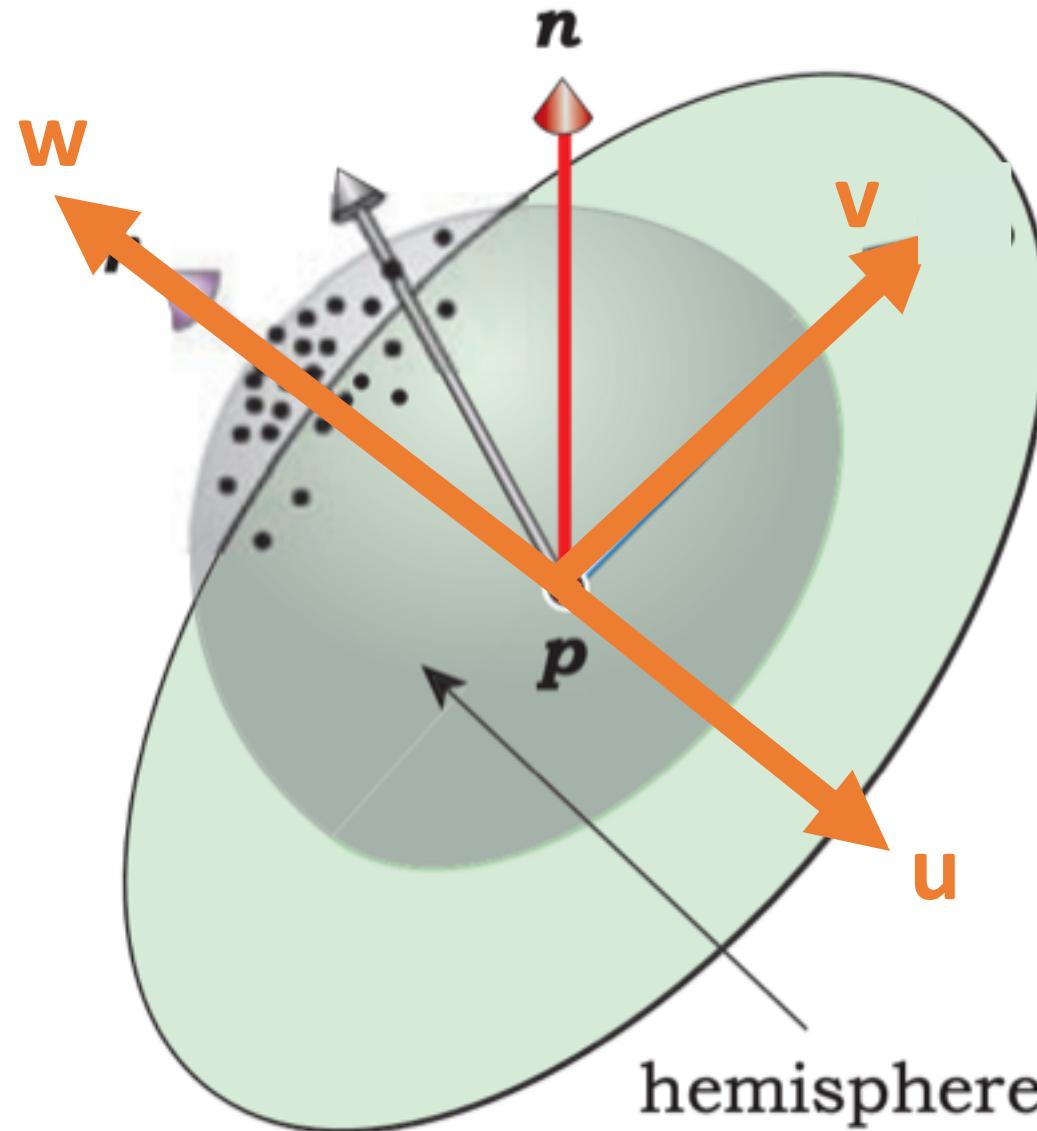
Glossy Reflection

- This green plane is perpendicular to the reflected ray r



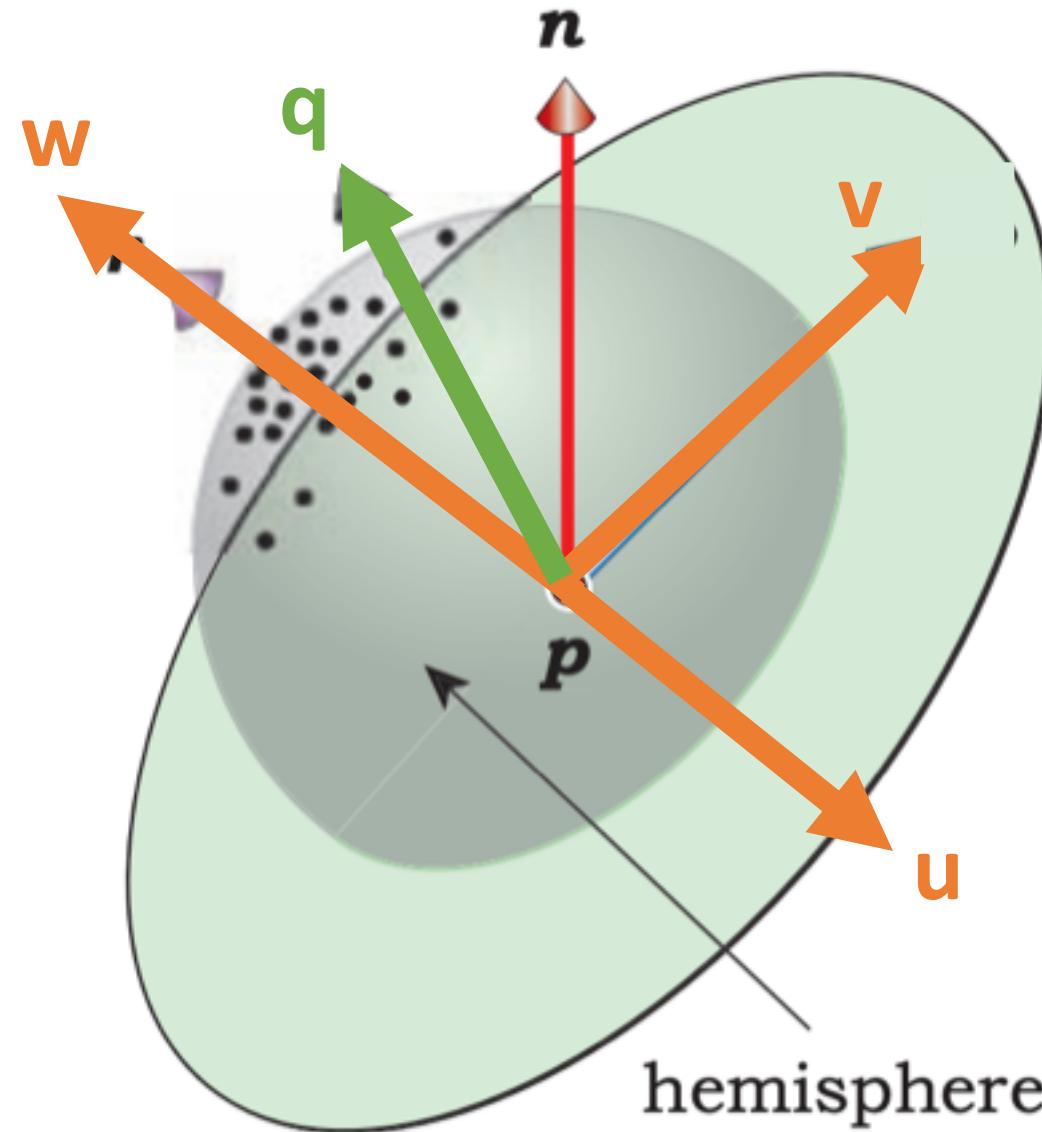
Glossy Reflection

- This green plane is perpendicular to the reflected ray r
- Make an orthonormal frame of reference (u, v, w) where $w = r$
 - Similar to making the camera basis, use n as the “up” vector



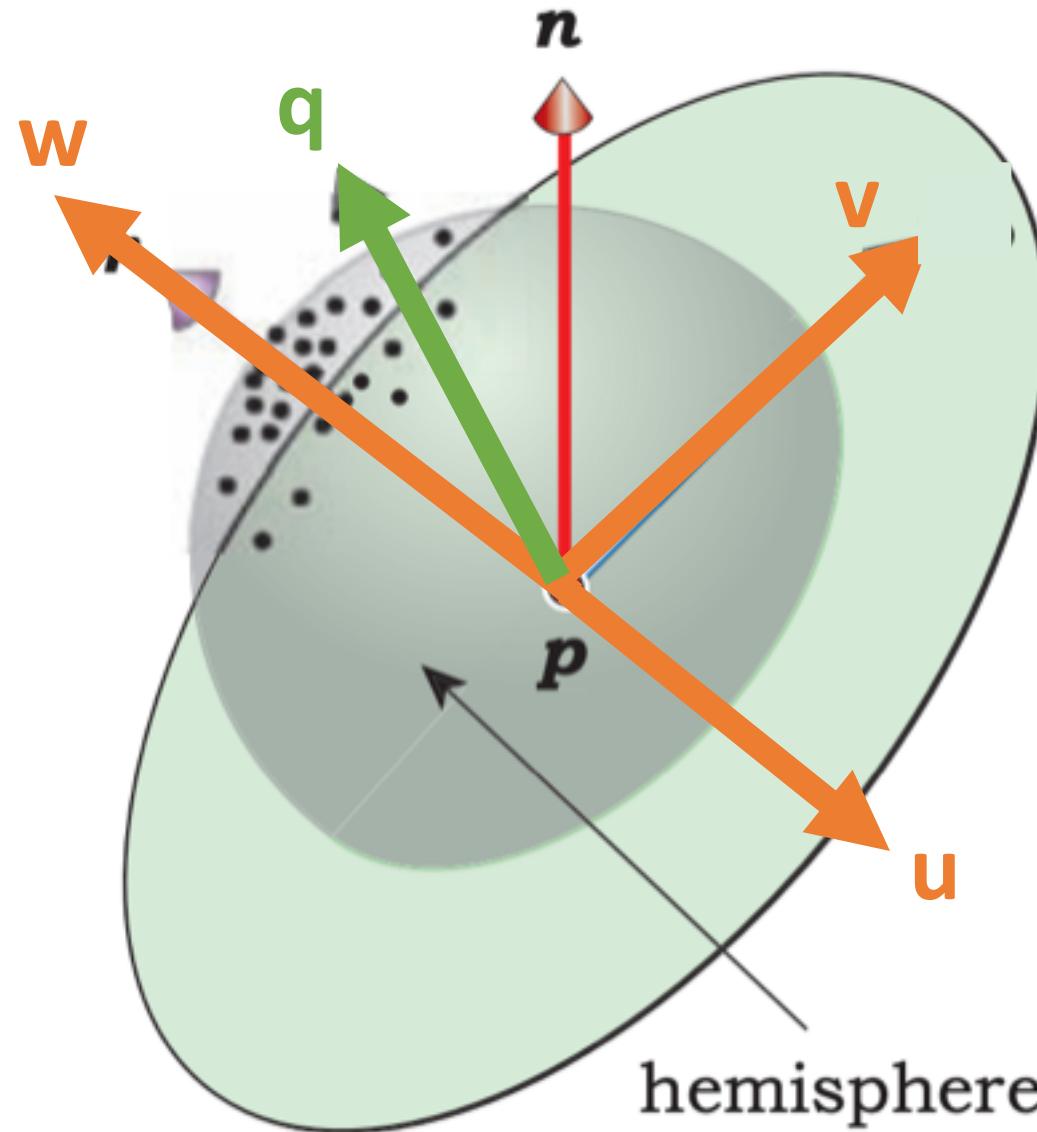
Glossy Reflection

- In (u,v,w) space it's easy to pick a vector near w . This will be our new ray to cast. Call it q



Glossy Reflection

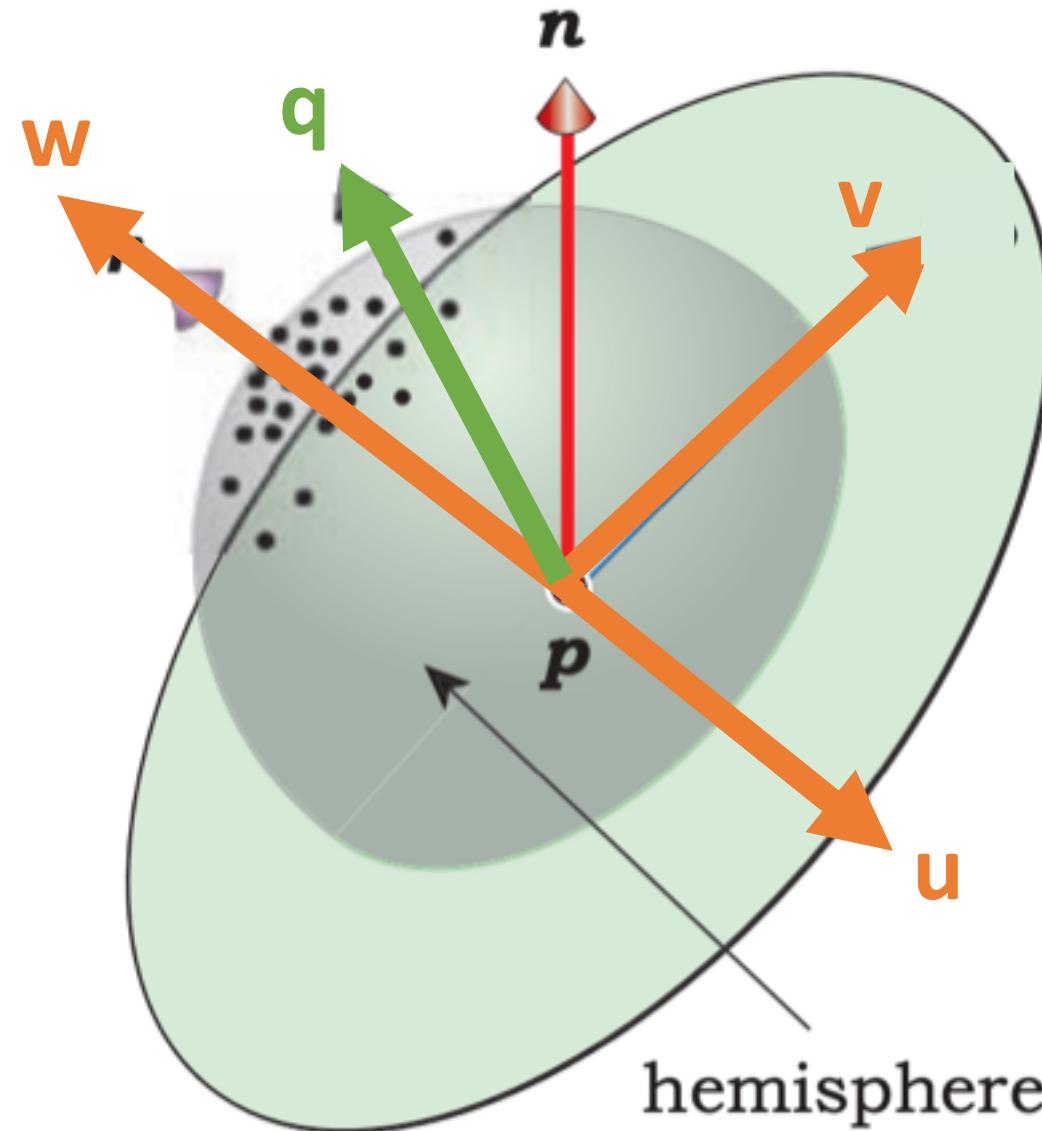
- In (u,v,w) space it's easy to pick a vector near w . This will be our new ray to cast. Call it q
- Use trigonometry and random distributions to pick q near w .



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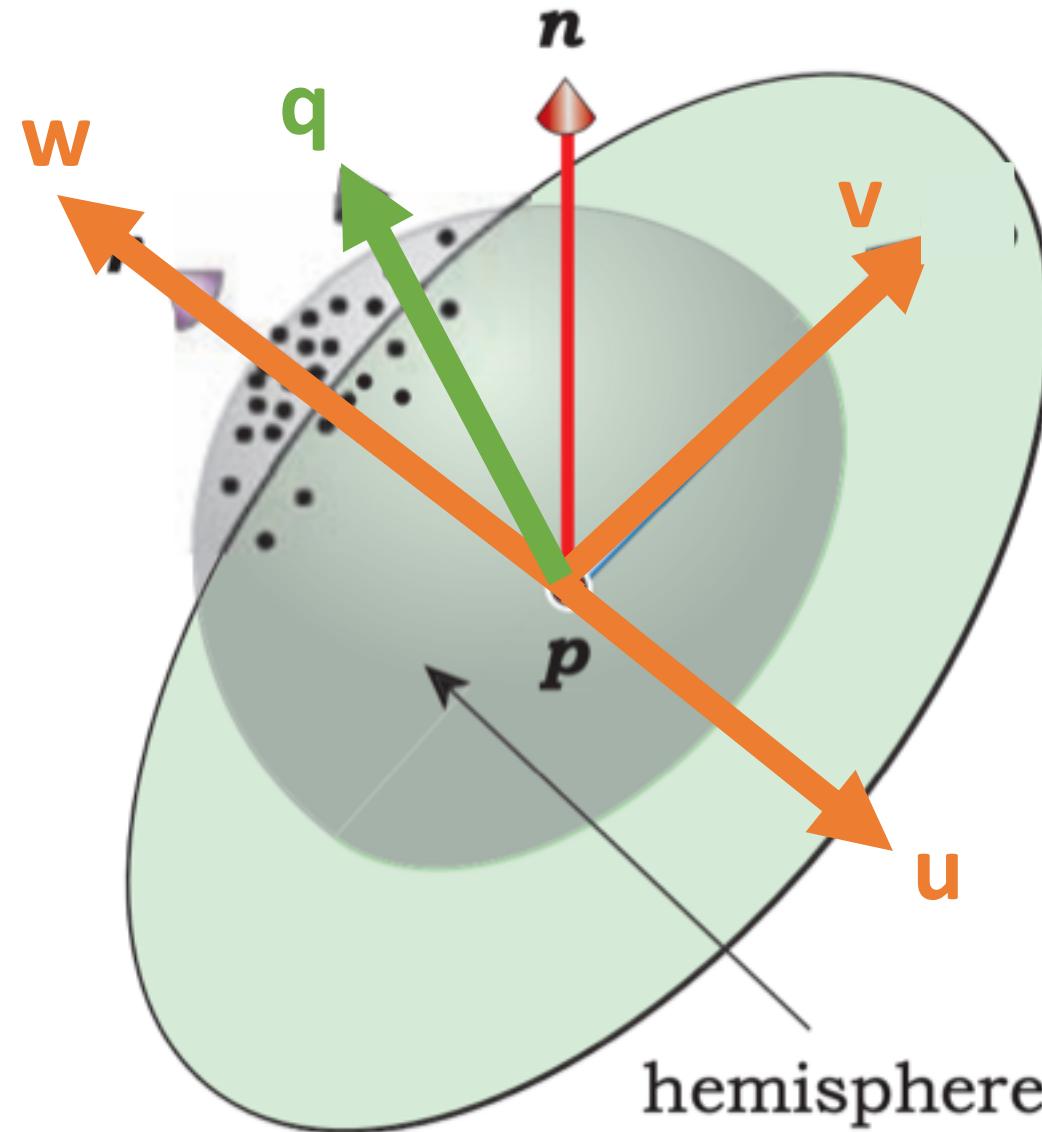
Glossy Reflection

- In (u,v,w) space it's easy to pick a vector near w . This will be our new ray to cast. Call it q
- Use trigonometry and random distributions to pick q near w .
- The larger the variance in the distribution, the more rough the surface



Glossy Reflection

- Transform q out of (u,v,w) space to cast the new ray



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Motion Blur

- Scene is still and sampled over time (temporal sampling)
- When image is taken and shutter is open for fixed amount of time, the final image is an average of the light rays over time period.
- When objects are in motion, they will appear blurred
- Introduce time variable throughout the system.
 - i.e. objects are hit by rays given their position at a particular time
 - Generate rays over shutter interval $T = T_0 + \xi(T_1 - T_0)$

Motion blur

- Parameterize each object's motion by time, $p(t)$
- Each ray, when cast, gets a time t_0 in a range (ie, $[0,1]$)
- The time t_0 each ray has, determines the scene the ray “sees”
 - ie, the positions of the objects the ray might hit are $p(t_0)$

Motion Blur

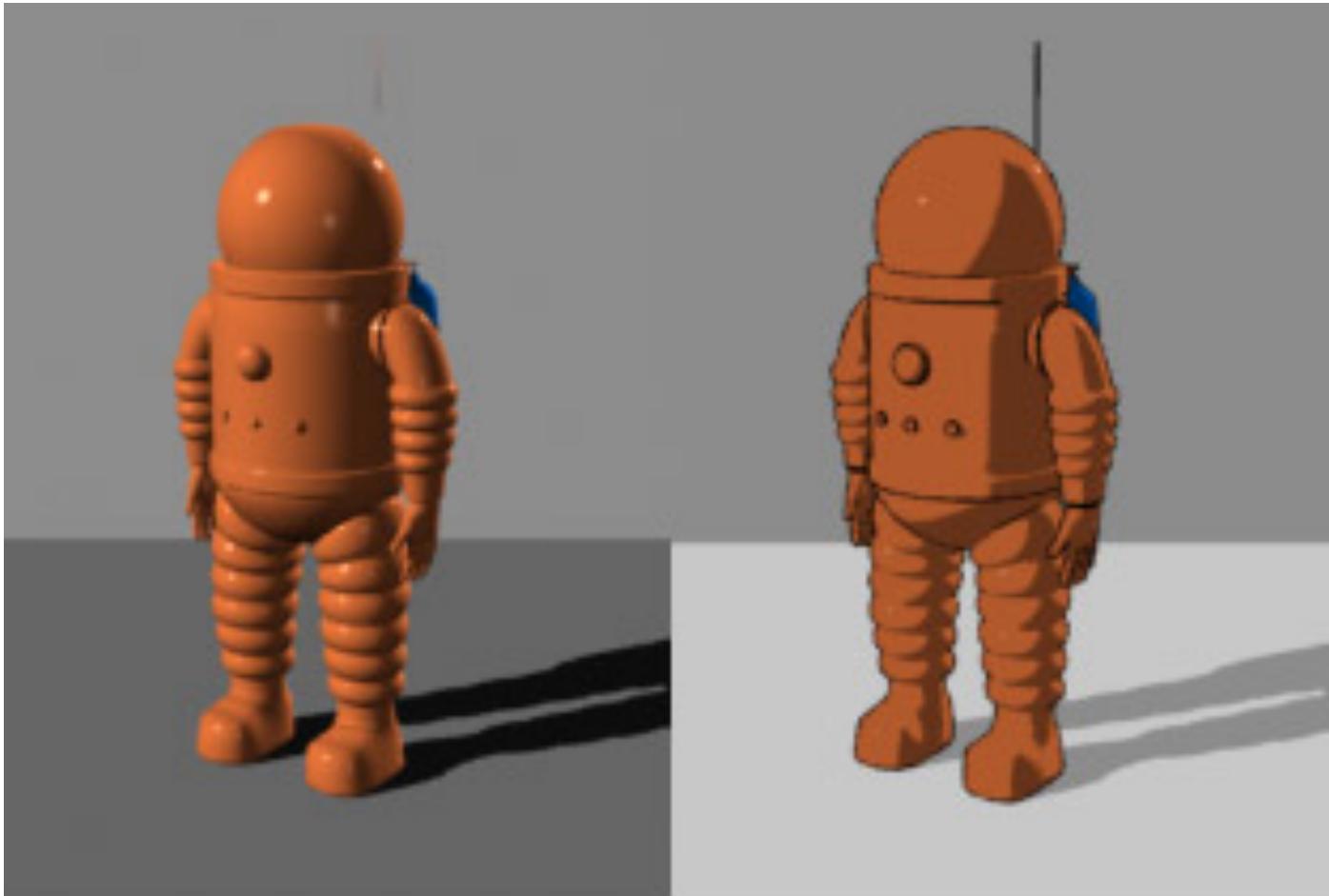


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Cel Shading

- Cel shading, or toon shading is an artistic rendering style meant to mimic a cartoon

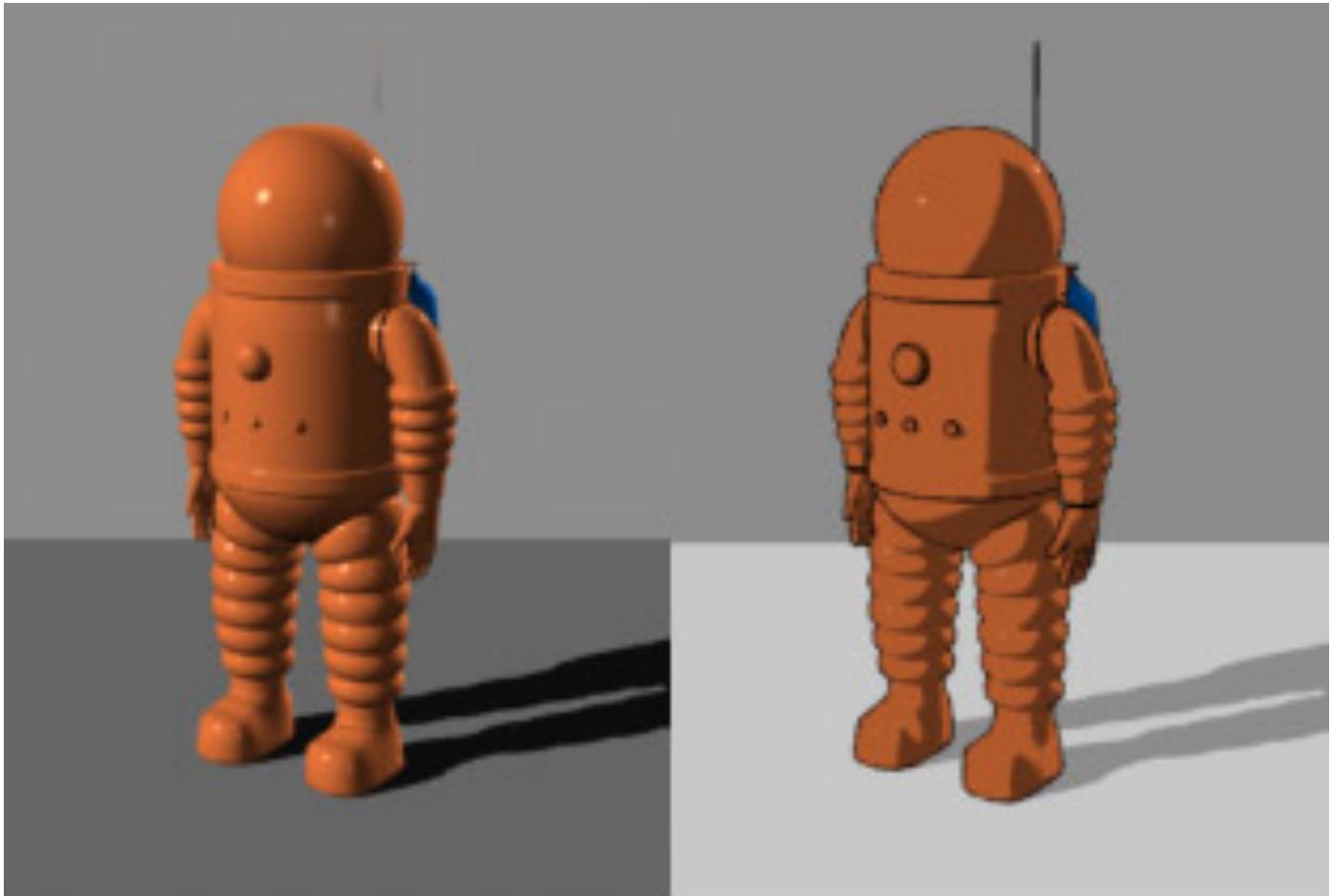


plastic shader

toon shader

Cel Shading

- Cel shading, or toon shading is an artistic rendering style meant to mimic a cartoon



plastic shader

toon shader

Cel Shading

- Render using multiple bands of color, rather than a continuous gradient



Normal
Shading



4 Band
Cel Shading



7 Band
Cel Shading

Cel Shading

- Key idea: threshold the dot products in the Blinn-Phong model. Use multiple thresholds for multiple bands

