

# CSC 317/2504: Computer Graphics

Course web site (includes all course information):

<https://github.com/dilevin/computer-graphics-csc317/>

**Lectures:** Monday 11:00-13:00 LEC101/LEC2001 BA1180

Slides and many lecture topic videos are available ahead of time.

Prof. Karan Singh

*karan@dgp.toronto.edu*

Office hours: open door or upon request by email.

**Tutorials:** Wednesday 11:00-12:00 LEC101/LEC2001 BA1180

**Questions:**

on Assignments: Github issues pages

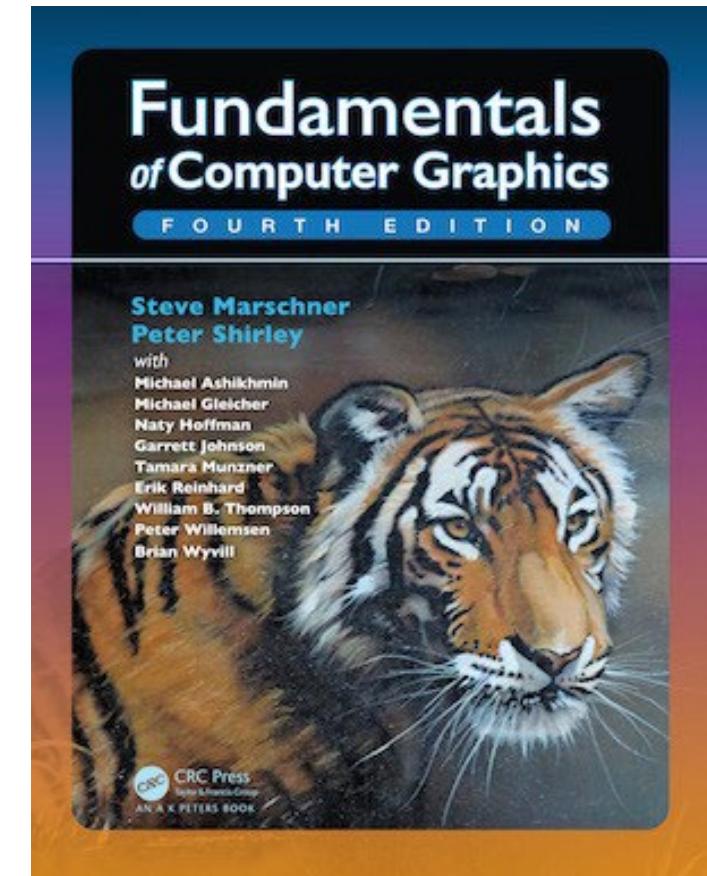
on Administrative stuff: Quercus <https://q.utoronto.ca/courses/354220>

**Textbooks:** Fundamentals of Computer Graphics

OpenGL Programming Guide & Reference

# You will need:

- A computer to install and program the assignments.
- An internet connection for online material and to join any occasional zoom meetings.
- Availability during class and tutorial times.
- The textbook for required readings



# Schedule (on the webpage)

Week	Topic / Event
1	<a href="#">Introduction</a> , <a href="#">tutorial</a> , <a href="#">Assignment 1 (Raster Images)</a> waitlisted ? zip assignment and email to TAs due 17/09
2	<a href="#">Lecture 2</a> , <a href="#">Assignment 2 Ray Casting</a> due 24/09
3	<a href="#">Lecture 3</a> , <a href="#">Assignment 3 Ray Tracing</a> due 01/10
4	<a href="#">Lecture 4</a> , <a href="#">Assignment 4 Bounding Volume Hierarchy</a> due 8/10
5	<a href="#">Lecture 5</a> , <a href="#">Assignment 5 Meshes</a> due 22/10
6	No Lecture, Thanksgiving
	First In-Tutorial Test October 16th
7	<a href="#">Lecture 6</a> , <a href="#">Assignment 6 Shader Pipeline</a> due 5/11
8	No Lecture, Reading Week !
9	<a href="#">Lecture 7</a> , <a href="#">Assignment 7 Kinematics</a> due 12/11
10	<a href="#">Lecture 8</a> , <a href="#">Assignment 8 Mass-Spring Systems</a> due 19/11
11	Lecture 9, Assignment on Generative AI due 26/11
12	Second In-Class Test December 3rd

# Marking Scheme (on the webpage)

%	Item
64	Assignments (best 8 of 9)
12	4 Quizzes (Online)
12	In Tutorial Test
12	In Class Test

**Academic Honesty Policy** is on the webpage and is mandatory reading!

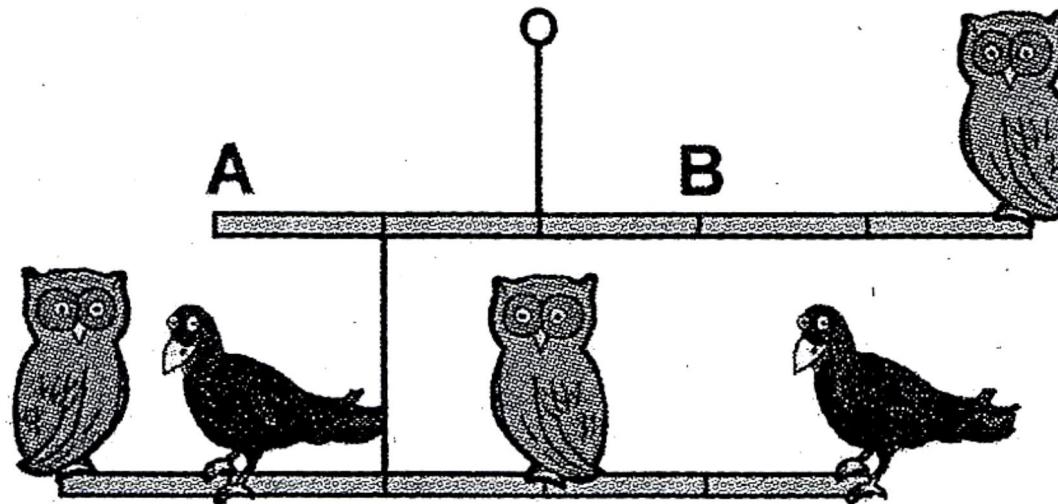
**Tutorials sessions** will be invaluable for the assignments.

# Prerequisites (pre-test)

Background in math, CS and programming is required for this course.

A quick self-monitored pre-test (15-20 mins should be enough to do it)

1. Show you the mathematical background expected and your readiness for this course.
2. Show you what you need to brush up on. Questions about these math operations will not be answered by either Professors or TAs, we expect you to know this stuff.



## Discrete Math

**Q1:** What is the intersection of the interval  $\mathcal{A} = [-1, 3]$  and  $\mathcal{B} = [0, 4]$ ?  $\mathcal{A} \cap \mathcal{B} =$

**Q2:** In a balanced binary tree with  $n$  leaf nodes, how many internal nodes are there?

**Q3:** In a balanced binary tree with  $n$  leaf nodes, how deep is the tree?  
(i.e., number of nodes on a shortest path from root to leaf)

**Q4:** What is  $5!$  (five factorial)?

**Q5:** How many different ways are there to choose  $k$  items from a set of  $n$  items?

## Linear Algebra

**Q6:** What size is the result of multiplying a  $2 \times 3$  matrix and a  $3 \times 4$  matrix?

**Q7:** What is the dot product between the vector  $\mathbf{a} = [1, 2, 3]$  and  $\mathbf{b} = [4, 5, 6]$ ?  $\mathbf{a} \cdot \mathbf{b} =$

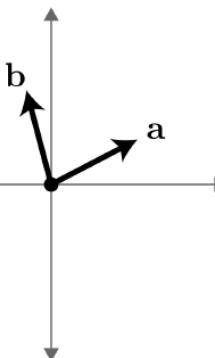
**Q8:** What is the cross product between the vector  $\mathbf{a} = [4, 0, 0]$  and  $\mathbf{b} = [0, 0, -2]$ ?  $\mathbf{a} \times \mathbf{b} =$

**Q9:** What is the matrix product of the matrix  $\mathbf{A} = \begin{pmatrix} 1 & 0 & 4 \\ 0 & 2 & 1 \\ 0 & -3 & 0 \end{pmatrix}$  and the vector  $\mathbf{b} = \begin{pmatrix} -4 \\ 5 \\ 6 \end{pmatrix}$ ?

$\mathbf{A} \mathbf{b} =$

**Q10:** Using matrices, express the solution to the following system of equations:

$3x_1 + 2x_2 - 1x_3 = 10, 2x_1 - 10x_3 = 0, -9x_1 + 9x_2 = -1.$  (Form the system, but do not solve).



**Q11:** Sketch the results of  $\mathbf{c} = \mathbf{a} + \mathbf{b}$  and  $\mathbf{d} = \mathbf{b} - \mathbf{c}$  on the plot:

## Mappings

**Q12:** Suppose we have a  $f : \mathcal{A} \rightarrow \mathcal{B}$ , what needs to be true to call  $f$  a *well-defined function*?

**Q13:** Is  $f(x) = x^2$  invertible? Why (not)?

**Q14:** If  $x$  and  $y$  are real numbers, what sets are the domain and range of  $f(x, y) = x^2 + y^2$ ? (use  $\mathbb{R}$ )

## Logarithms

**Q15:** Express  $\log(a^b)$  in terms of  $\log a$  and  $b$ .  $\log(a^b) =$

**Q16:** Express  $\log(ab)$  in terms of  $\log a$  and  $\log b$ .  $\log(ab) =$

## Trigonometry

**Q17:** Express  $\cos(a + b)$  in terms of  $\cos a$  and  $\cos b$ .  $\cos(a + b) =$

**Q18:** Given a triangle with side lengths  $a, b, c$  and opposite angles  $A, B, C$ , express  $\sin A$  in terms of  $a, b$ , and  $\sin B$ .  
 $\sin A =$

**Q19:** Given a right triangle with acute angles  $A$  and  $B$ , express the following in terms of opposite side length  $a$  and  $b$ :  
 $\sin A =$   $\cos A =$   $\tan A =$

## Quadratic equation

**Q20:** How many real-value solutions for  $x$  are possible to an equation of the form  $ax^2 + bx + c = 0$ ?

A) zero; B) one; C) two; D) three; E) zero, one or two; or F) zero, one, two or three.

**Q21:** Identify the solution(s), if any, to  $x^2 - 4x - 5 = 0$ .

## Linear interpolation

**Q22:** What is *the* linear function  $f : [0, 1] \rightarrow \mathbb{R}$ , so that  $f(0) = a$  and  $f(1) = b$ ?

**Q23:** What is *the* linear *vector-valued* function  $f : [0, 1] \rightarrow \mathbb{R}^3$ , so that  $f(0) = \mathbf{a}$  and  $f(1) = \mathbf{b}$ ?

## Derivatives

**Q24:** What is the derivative of the function  $f(t) = 3t^2$ ?  $\frac{df}{dt} =$

**Q25:** What is the second derivative of the function  $f(t) = 3t^2$ ?  $\frac{d^2f}{dt^2} =$

**Q26:** What is the partial derivative of the function  $f(x, y) = 3x^2 - 3y^2$  with respect to  $y$ ?  $\frac{\partial f}{\partial y} =$

**Q27:** Given a function  $f : \mathbb{R}^3 \rightarrow \mathbb{R}$ , how many dimensions does its gradient have?

**Q28:** Using partial derivative and vector notations express the gradient of a function  $f(x, y, z) : \mathbb{R}^3 \rightarrow \mathbb{R}$ .

$\nabla f =$

## C++ Programming

**Q29:** We want to call `func` on `x`, what should be written in place of the question mark in the following C++ code?

A) \*; B) &; or C) nothing.

```
bool func(double & x);  
...  
int main()  
{  
    double * x = new double();  
    func( ? x);  
}
```

## Geometry

**Q30:** What is the volume of a sphere with radius  $r$ ?

# **Today**

1. Introduction to Computer Graphics.
2. Preview of Assignments.
3. Raster Images.

# Introduction to Computer Graphics

# What is Computer Graphics?

Computers:

accept, process, transform and present information.

Computer Graphics:

accept, process, transform and present information  
**in a visual form.**

# Ok but... what is the course really about?

The science of turning the rules of geometry, motion and physics into (digital) pictures.

## What its not about?

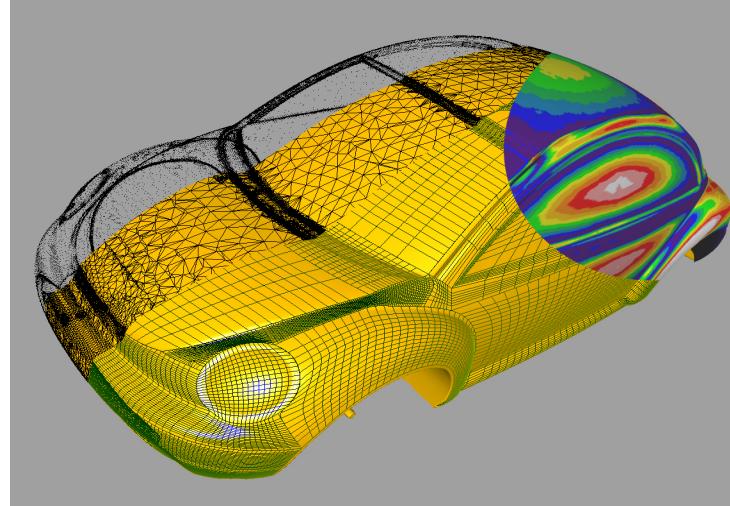
Photoshop, AutoCAD, Maya, Blender, Renderman, Graphics APIs.



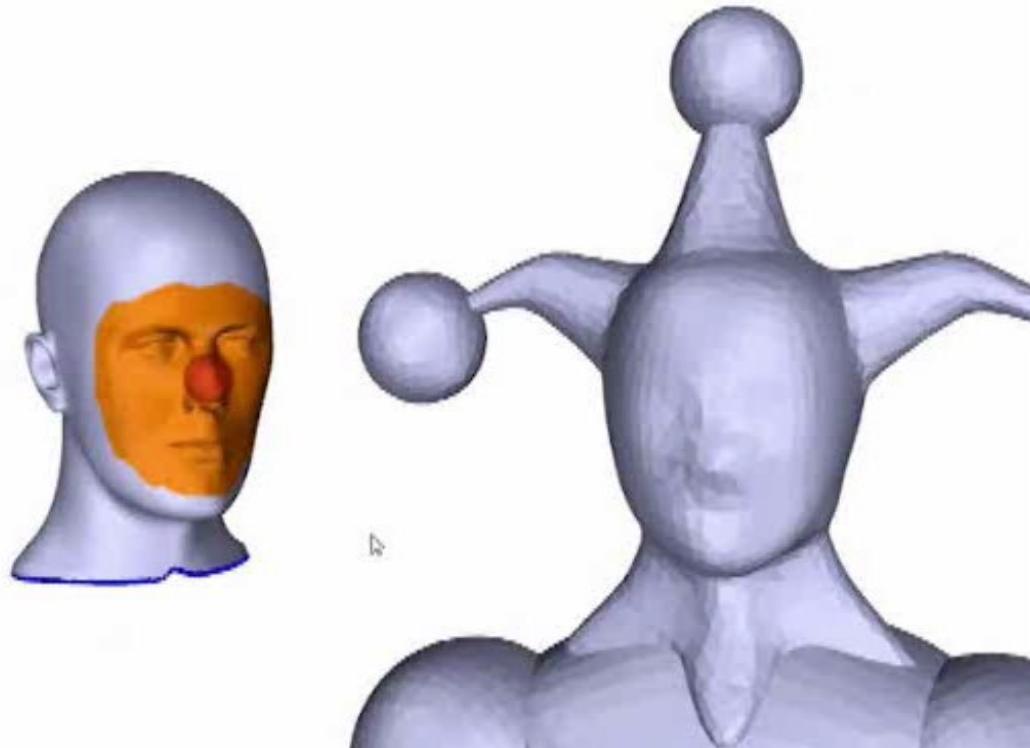
Evan Pan (CSC 317 alumnus)

# “Core” Areas of Computer Graphics

- Form (modeling)
  - How do we represent (2D or 3D) objects & scenes?
  - How do we build these representations?
- Function, Behavior (animation)
  - How do we represent the way objects move?
  - How do we define & control their motion?
- Appearance (rendering)
  - How do we represent the appearance of objects?
  - How do we simulate the image-forming process?



# Modeling



[MeshMixer. Schmidt, Singh, *SIGGRAPH 2010*]  
[www.meshmixer.com](http://www.meshmixer.com) (acquired by Autodesk Inc.)

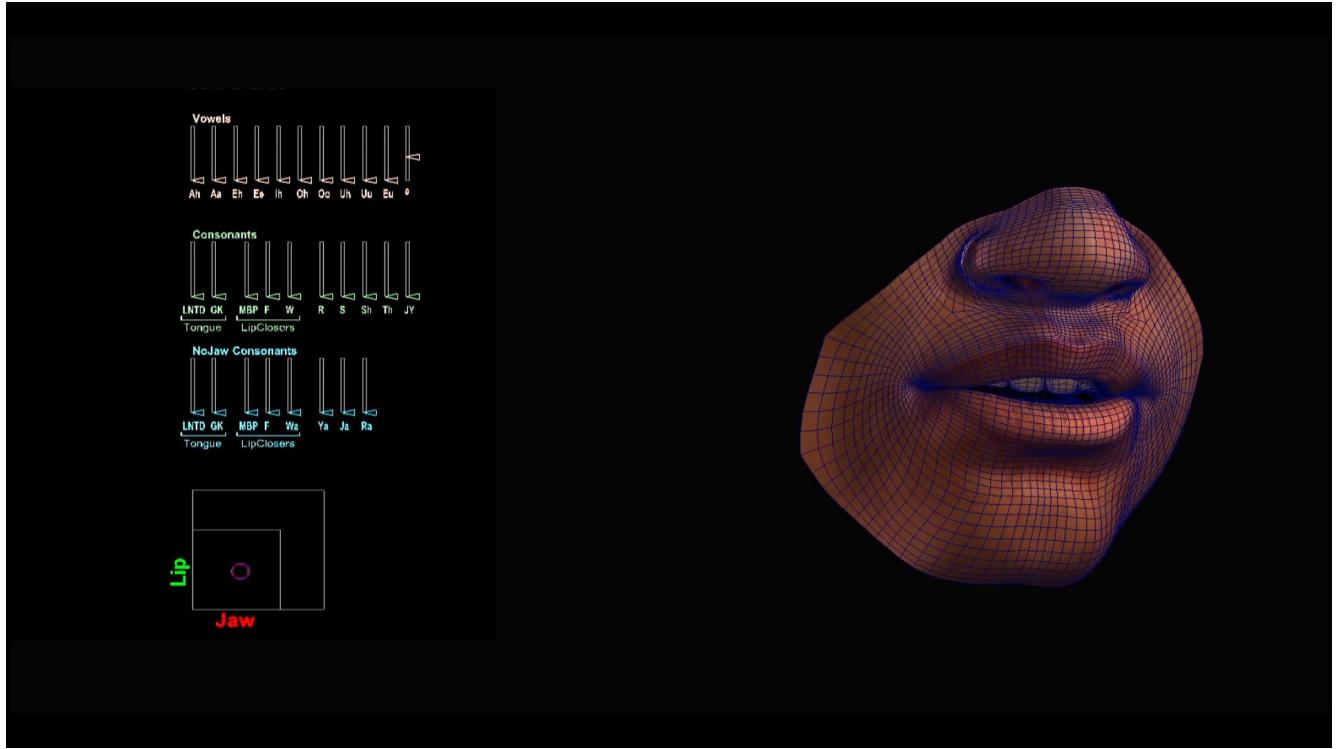


[Face-Extrusion Quadmeshes. Pandey, Baerentzen ,Singh, *SIGGRAPH 2022*]

# Animation

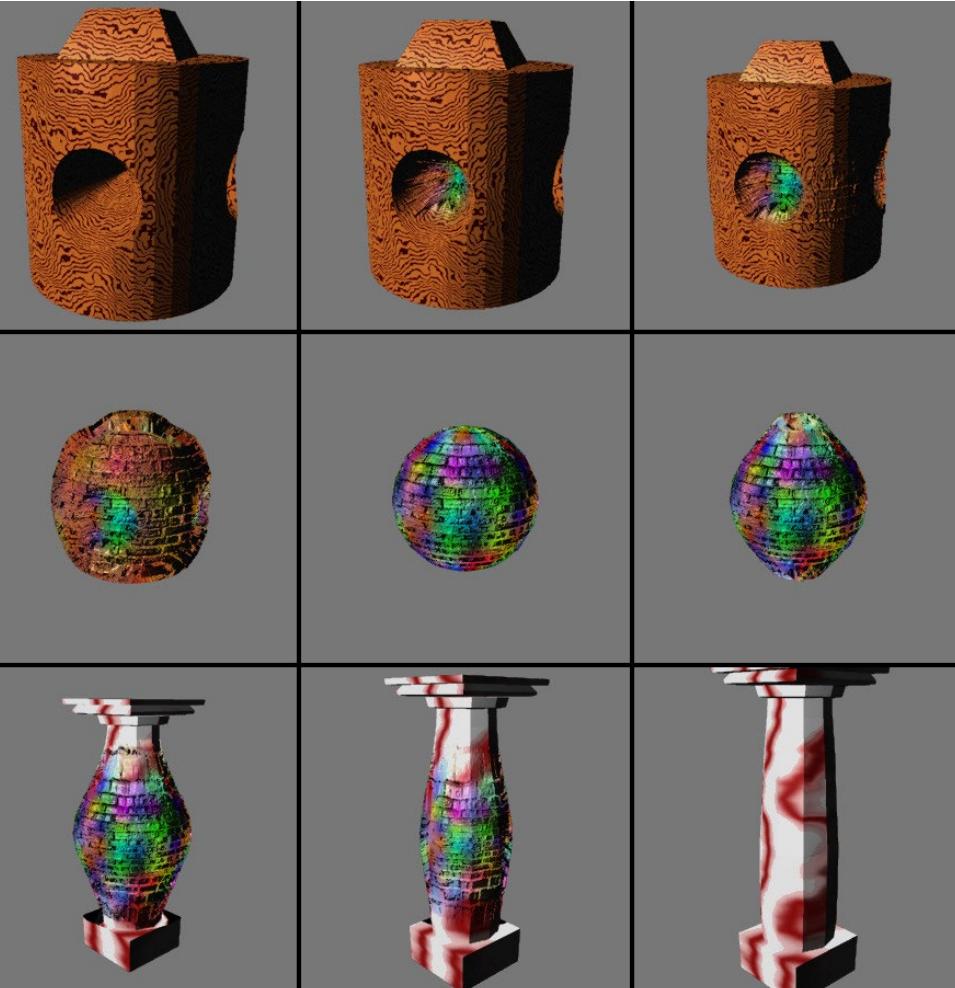


[Kinodynamic skinning using volume-preserving deformations, Angelidis, Singh, ACM SCA 2007]



[Visemenet: Zhou et al. SIGGRAPH 2018]

# Rendering



[Singh, around 1992]



[Weta Digital 2022]

# Other Areas of Computer Graphics

User Interaction

Virtual Reality

Visualization

Image Processing

3D Scanning and Fabrication

Computational Photography

# Movies

Drive new directions in CG  
Set quality standards for CG



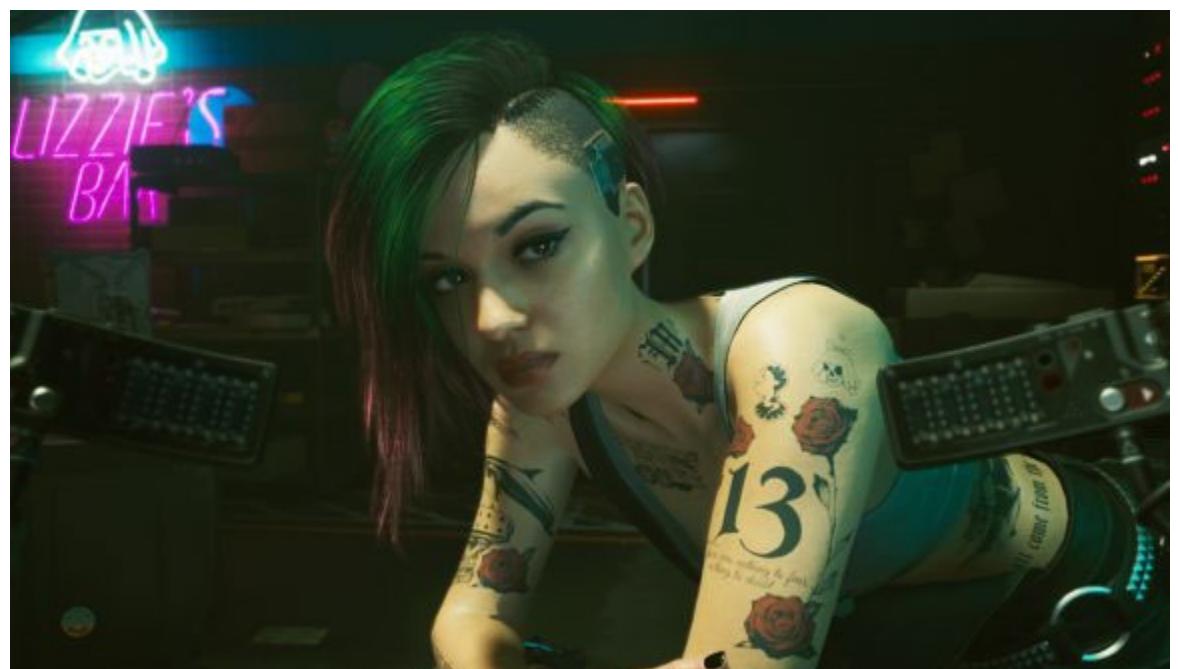
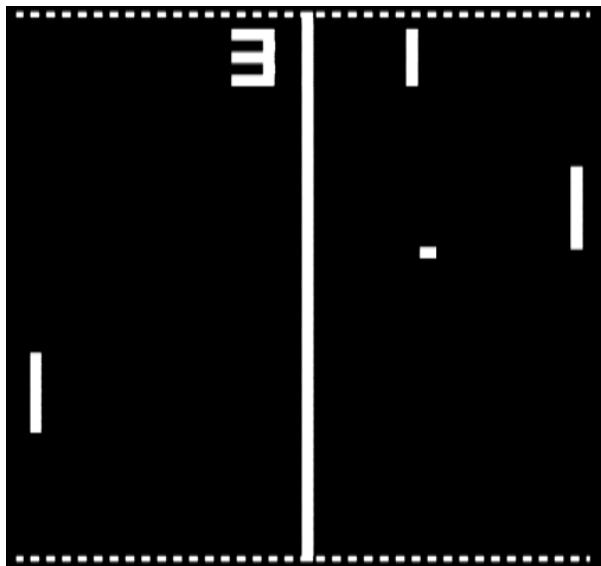




# Games

Drive interactivity and AI in CG

Push CG hardware to its limits





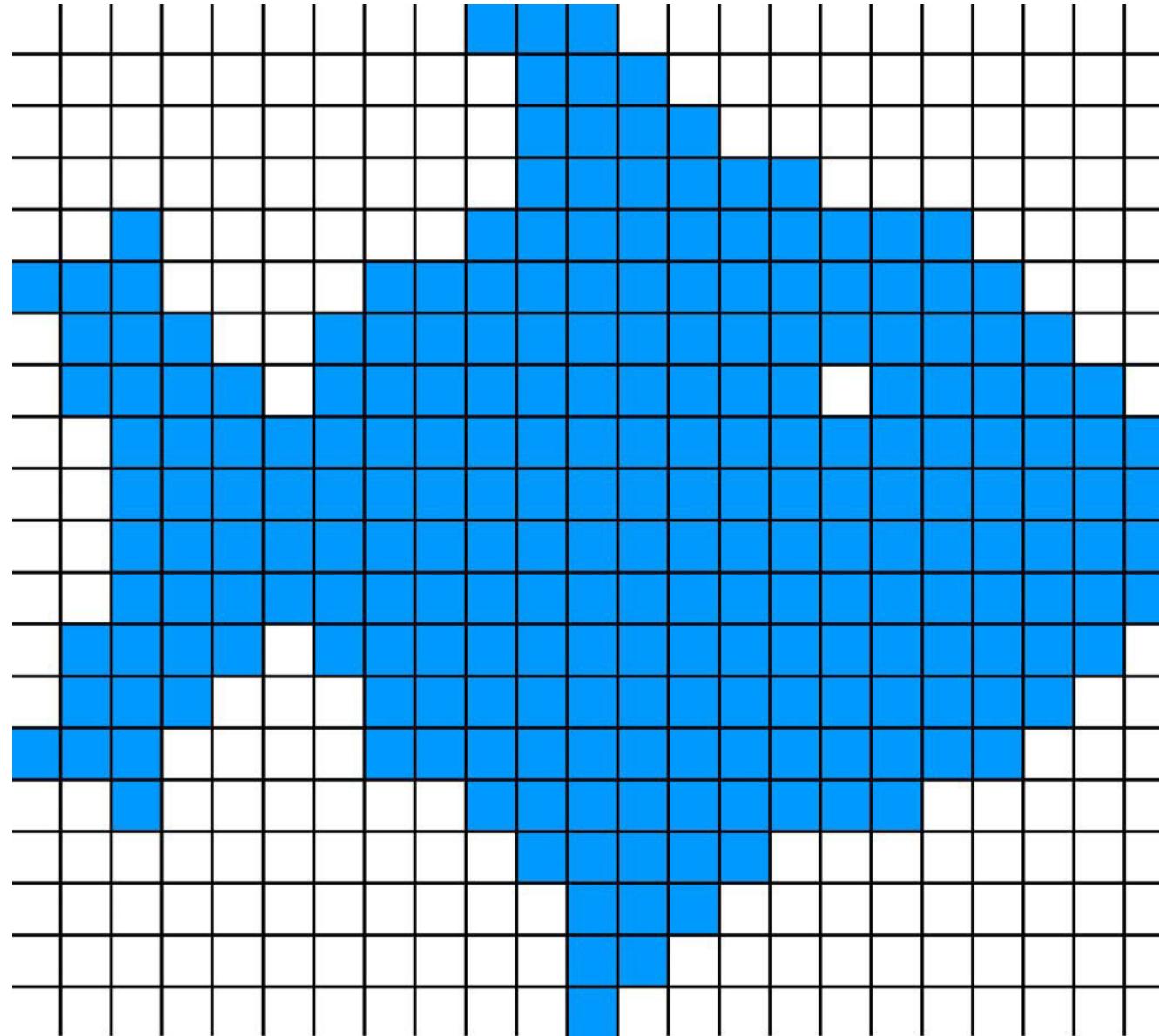
**Miasma Chronicles**  
The Bearded Ladies

Jali

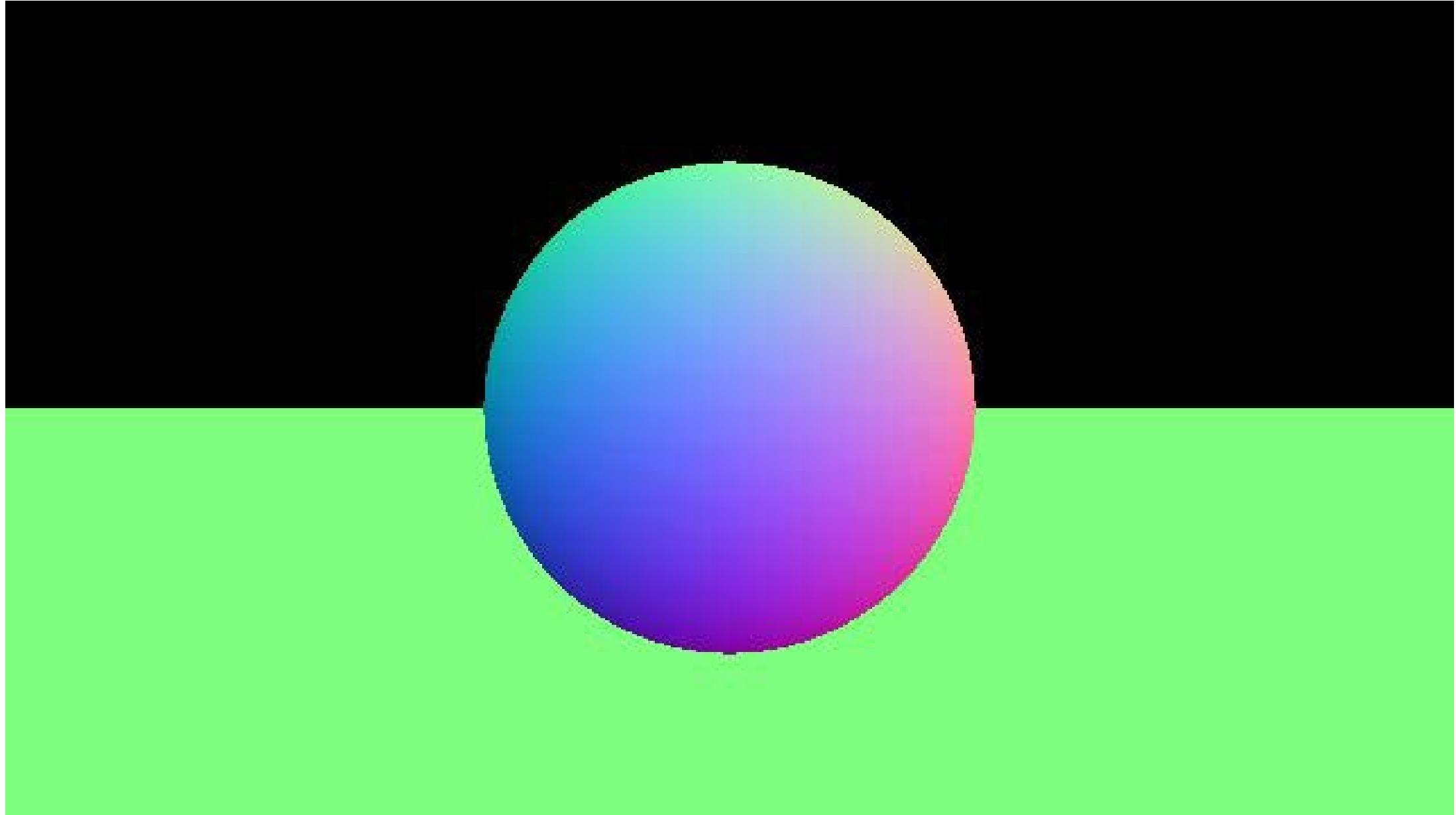
# Assignment Previews

1. Raster Images
2. Ray Casting
3. Ray Tracing
4. Boundary Volume Hierarchies
5. Meshes
6. Shaders
7. Kinematics
8. Mass-Springs
9. Generative AI

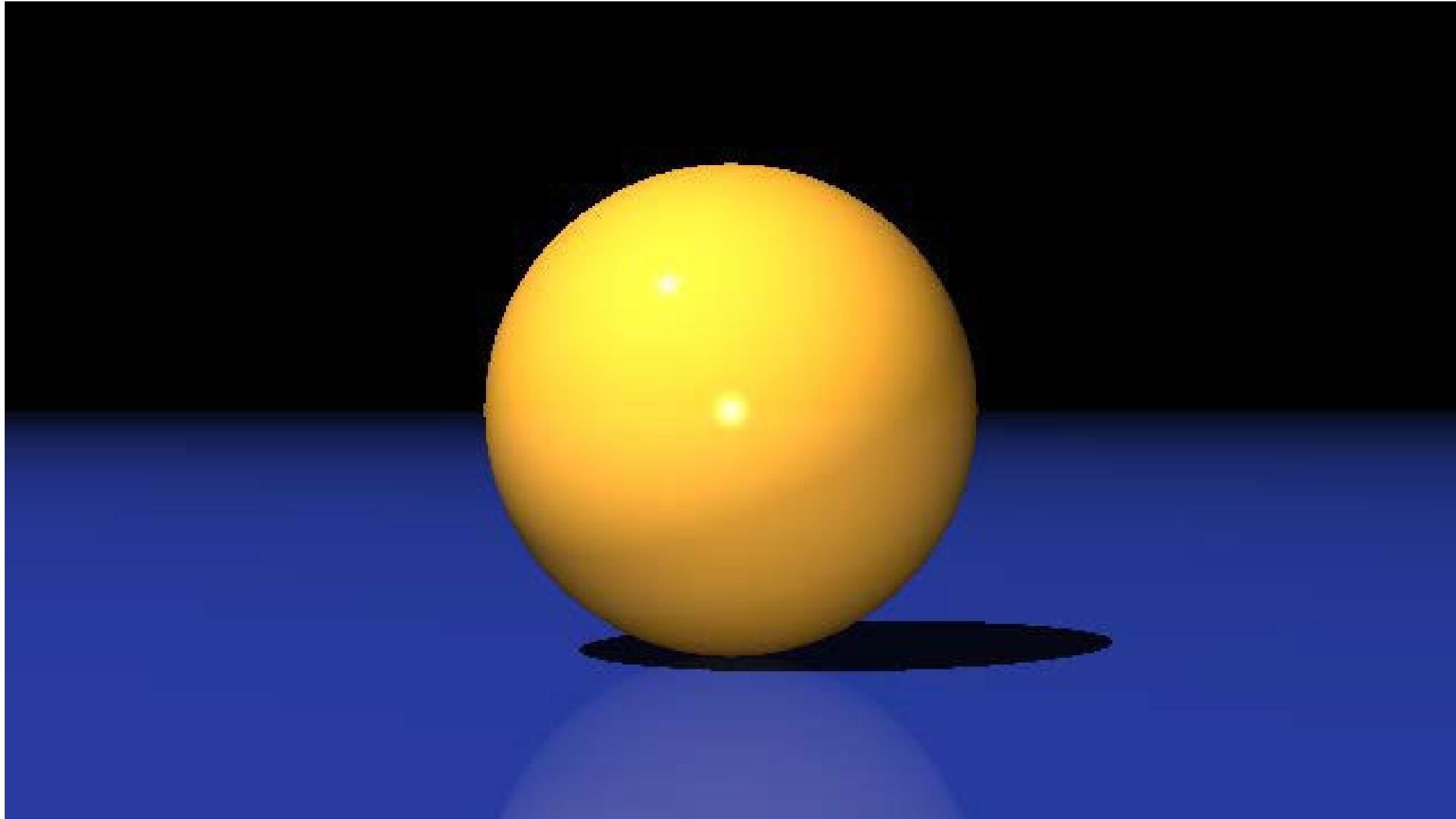
# Raster Images



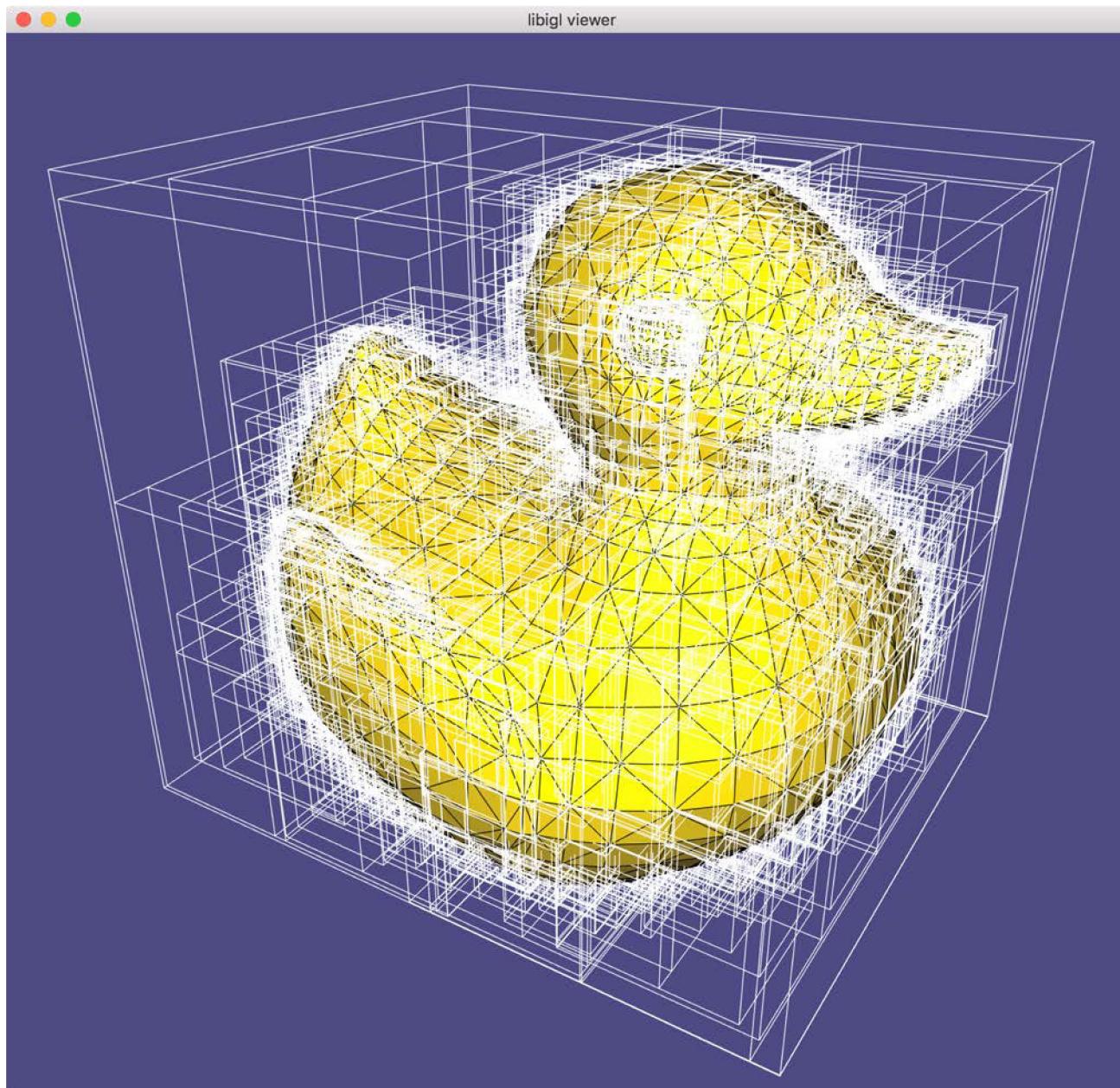
# Ray Casting



# Ray Tracing

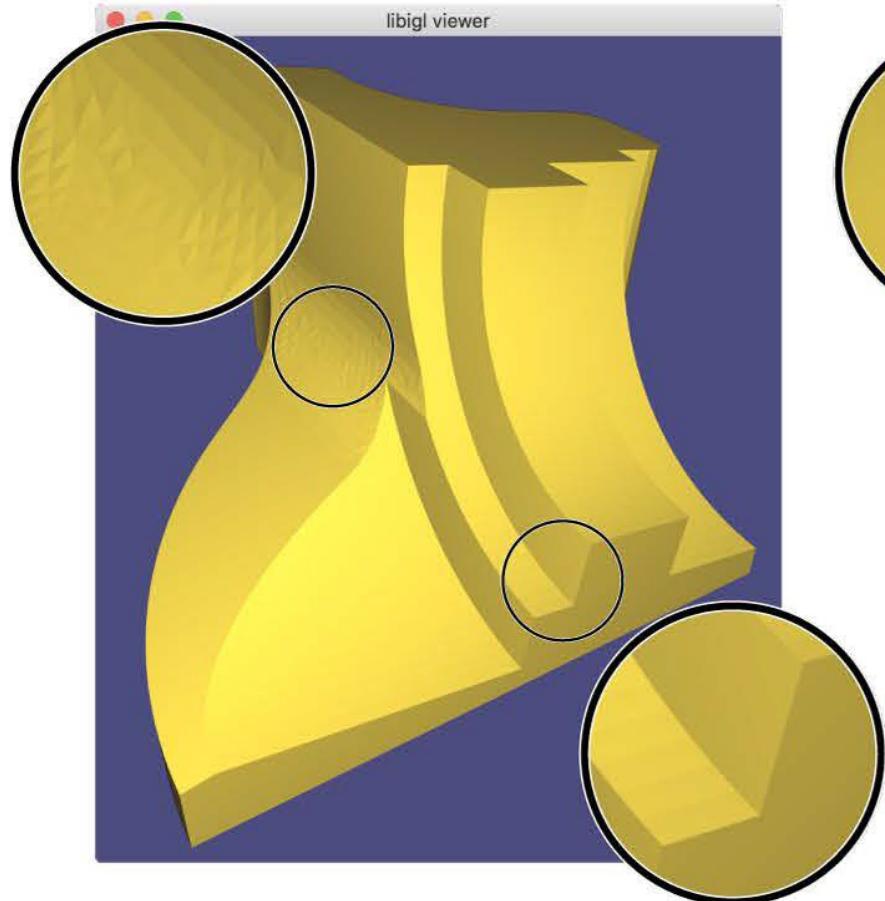


# Boundary Volume Hierarchies

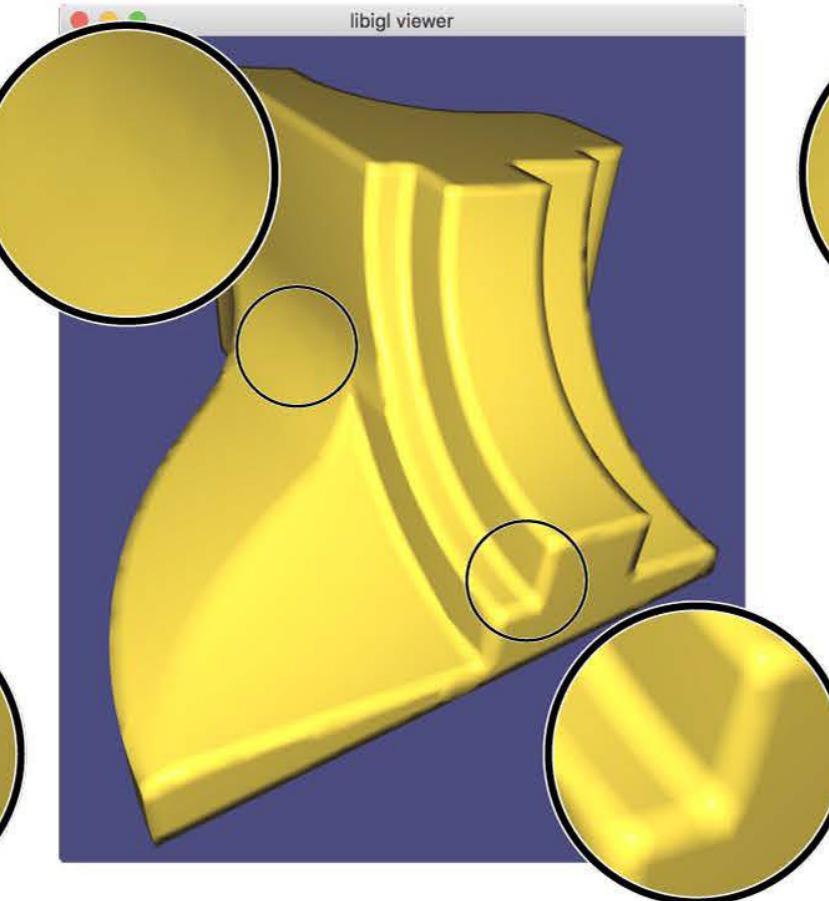


# Meshes

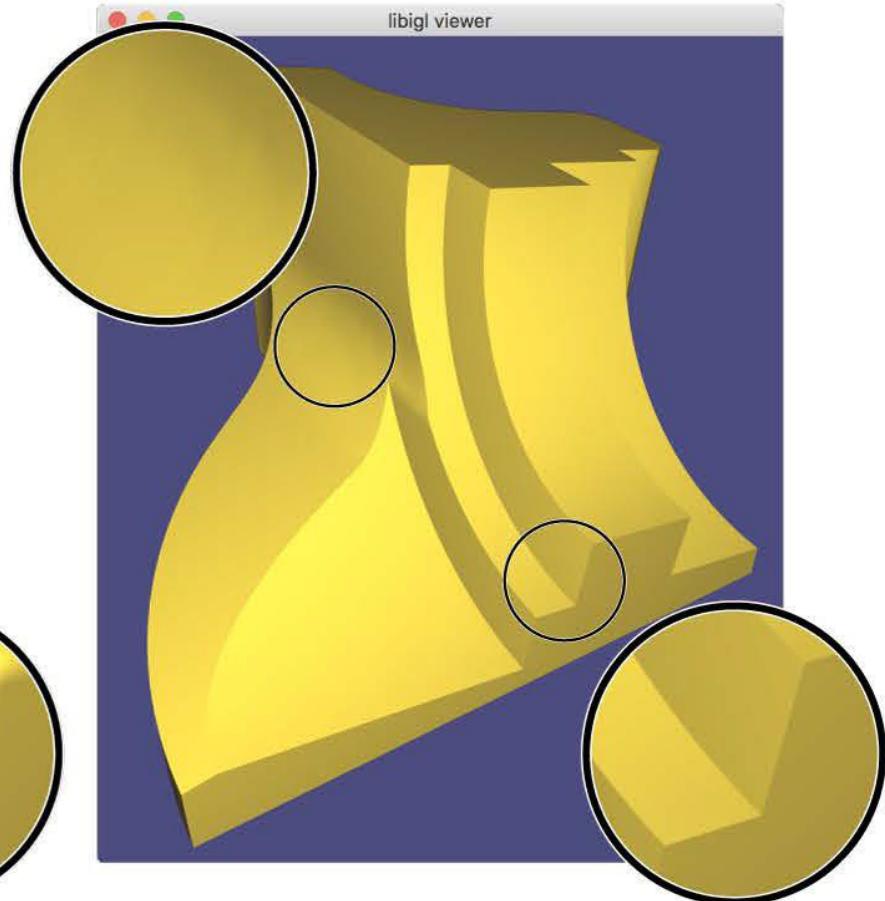
Per-face normals



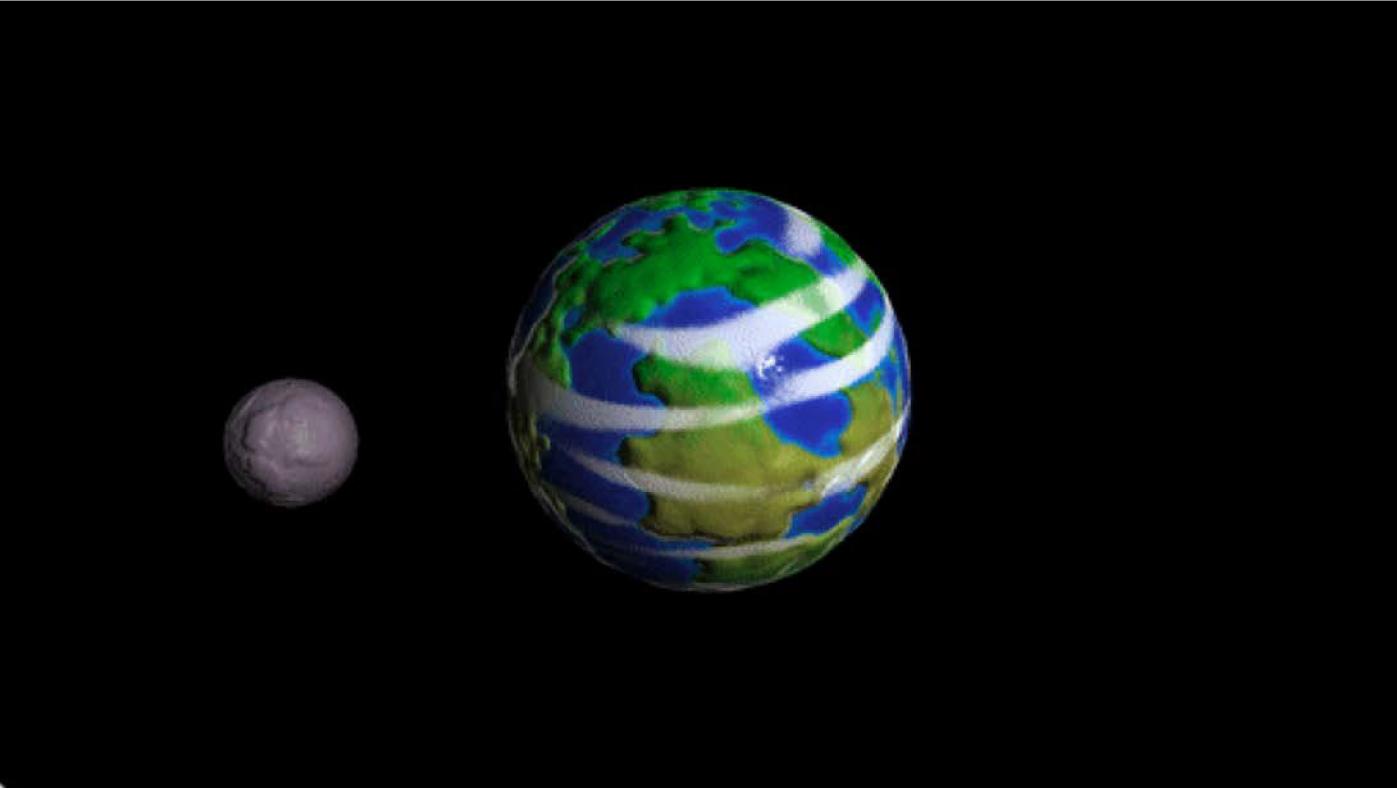
Per-vertex normals



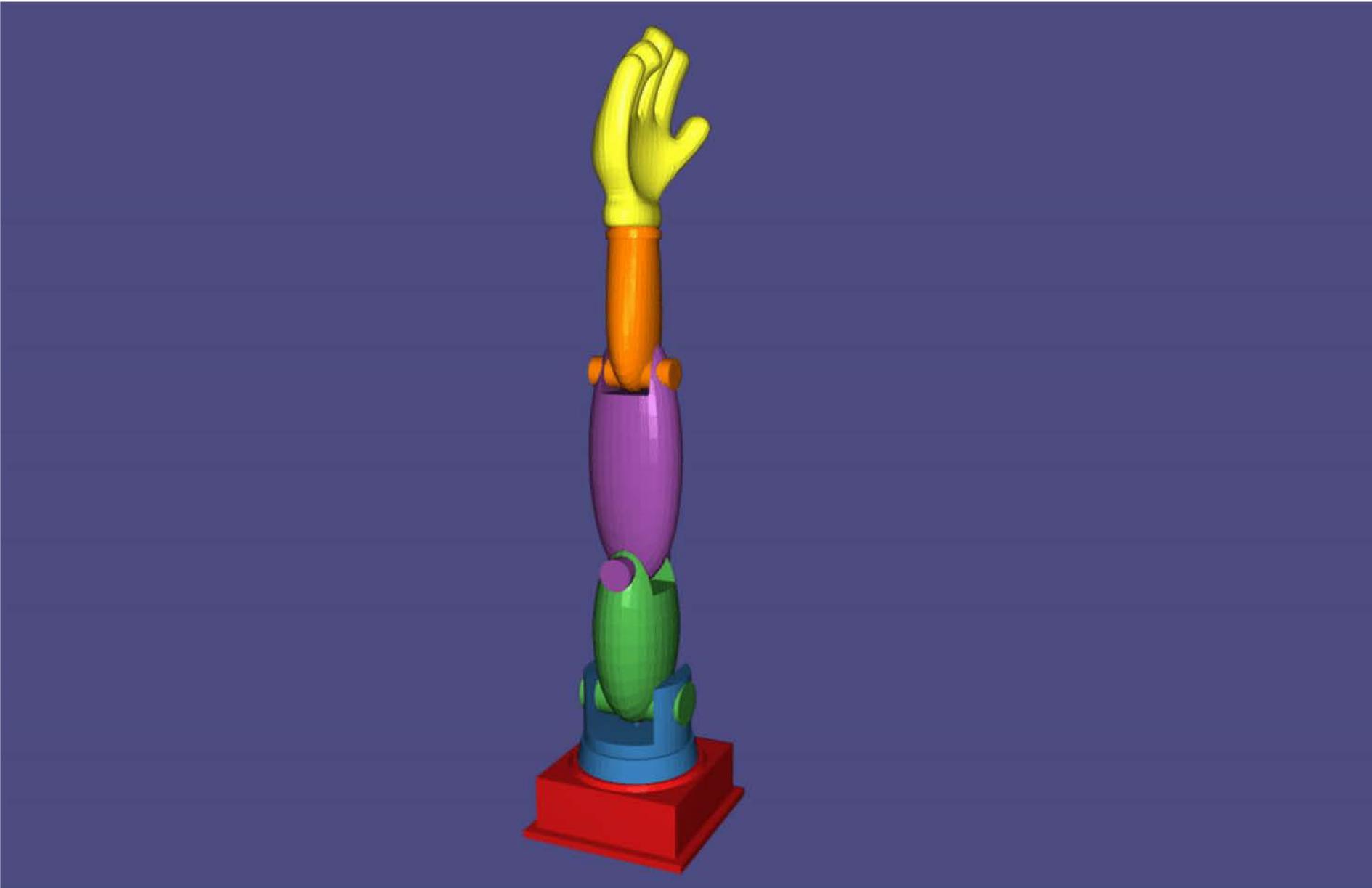
Per-corner normals



# Shaders



# Kinematics



# Mass-Springs



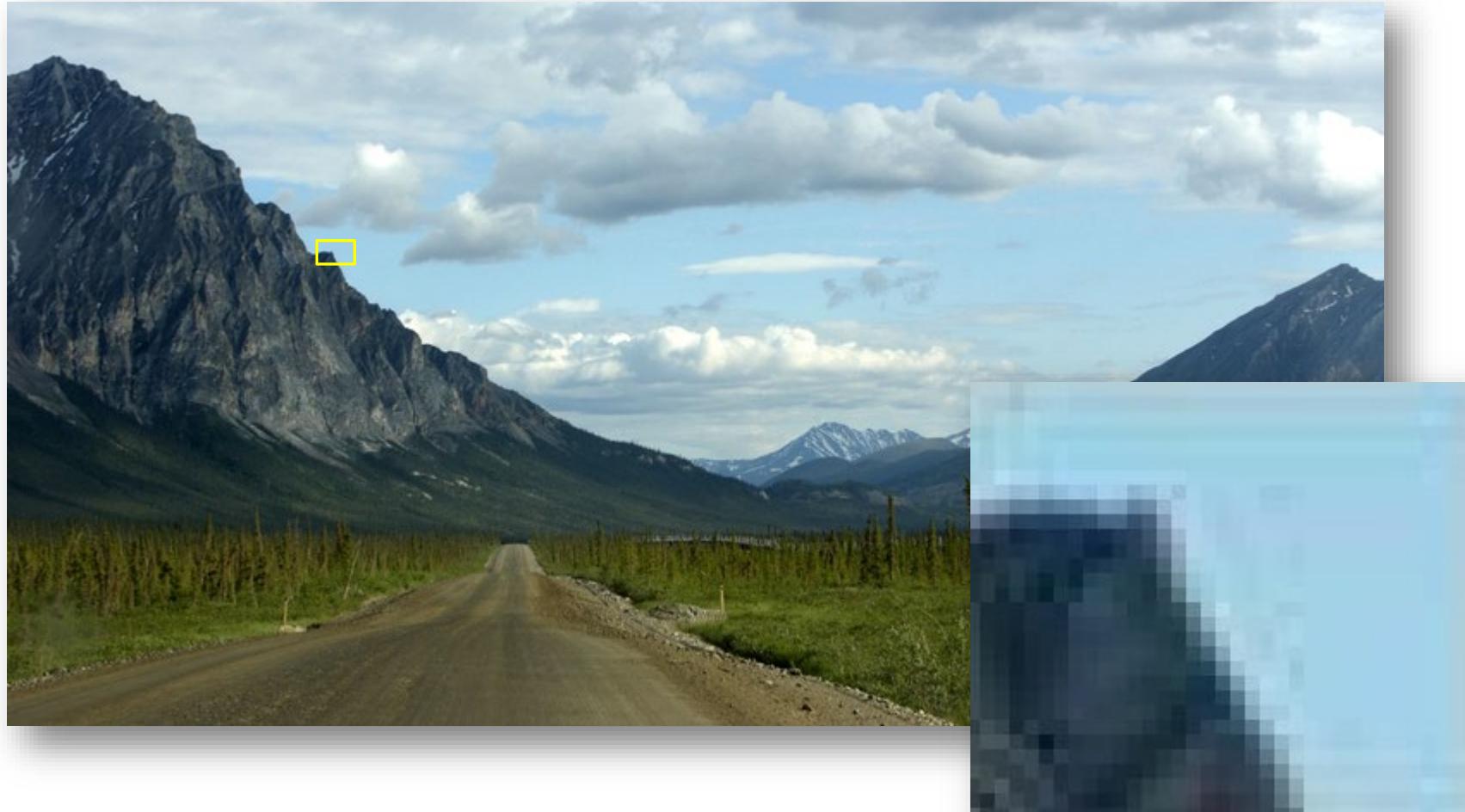
# Raster Images



# What is an Image?

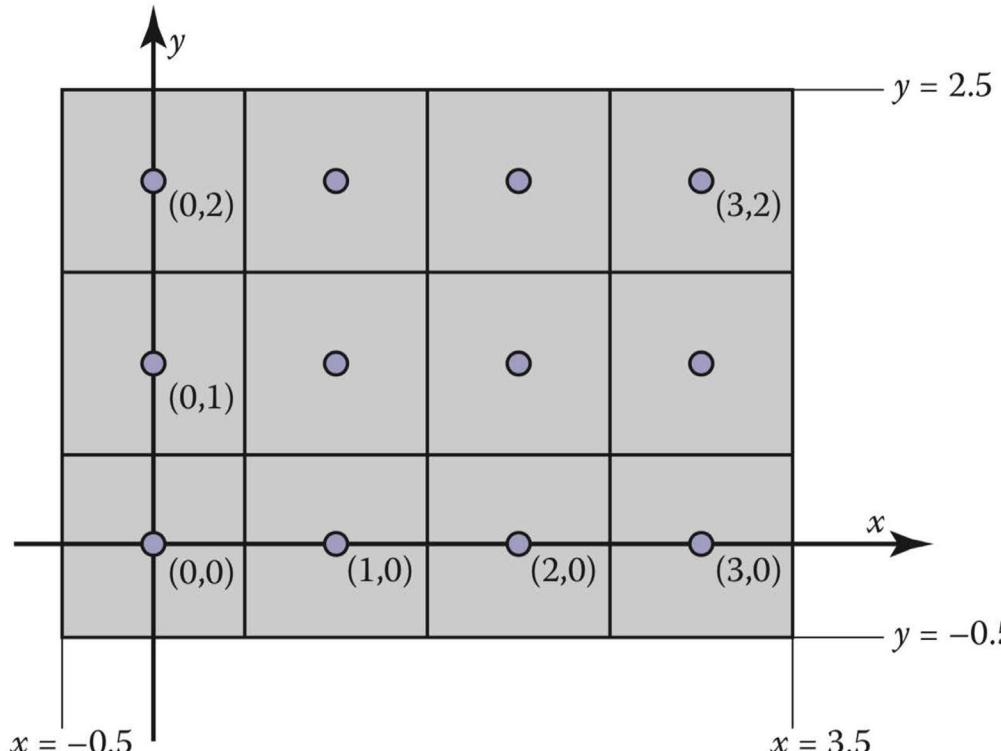
**Image** = distribution of light energy on 2D “film”

Digital images represented as rectangular arrays of **pixels**



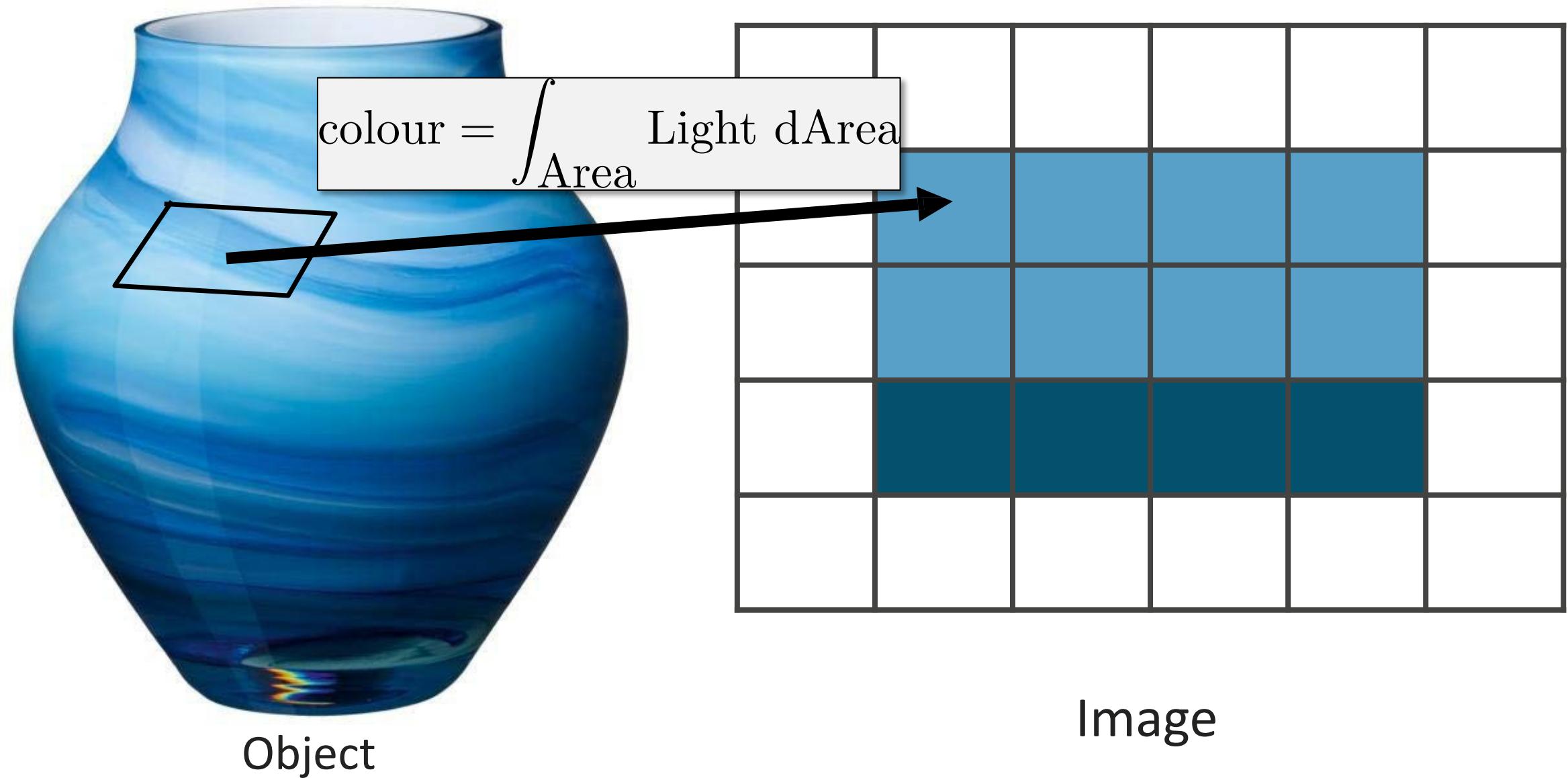
**Image = a function defined for an array of pixels**

$$I(x, y) : \mathbb{R}^2 \rightarrow \mathbb{R}^{+n}$$



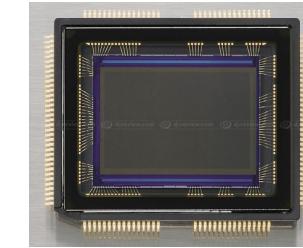
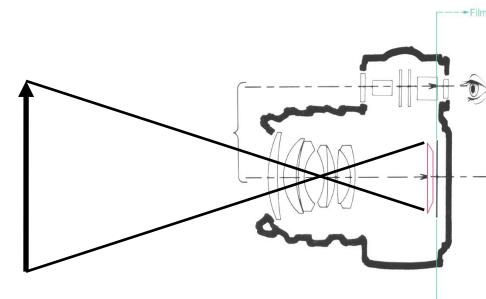
Pixel Co-ordinates

# A Pixel in 3D need not be 'square'



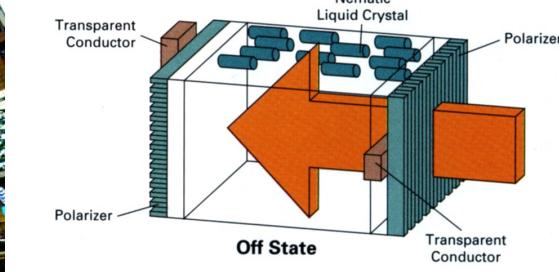
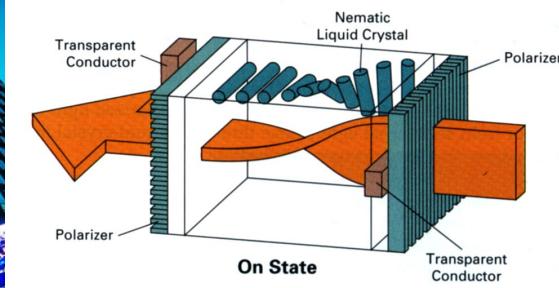
# Raster Devices and pixels

- Input (scanners, cameras)  
2D array sensor: digital camera

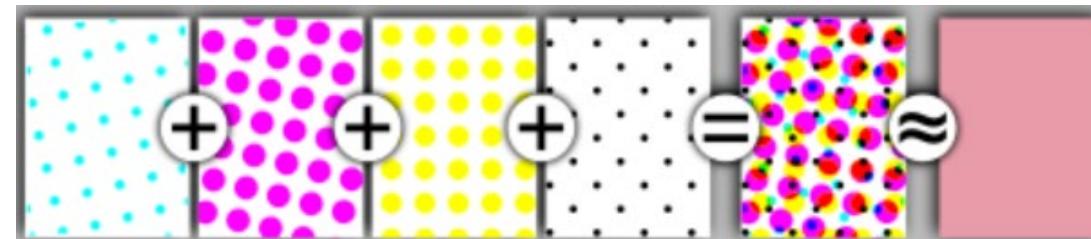


- Output (printers, displays)  
Emissive: light-emitting diode (LED)

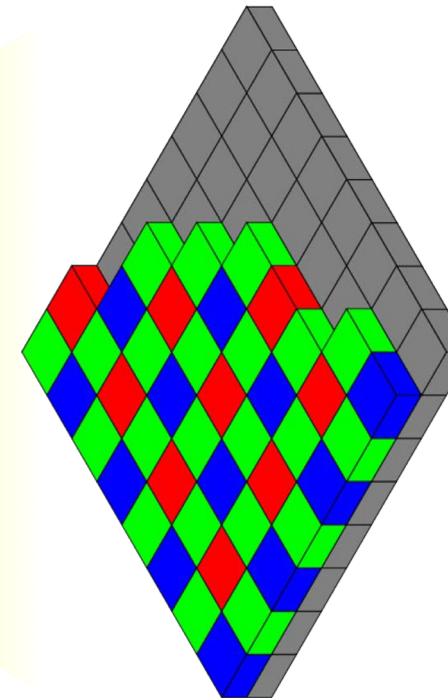
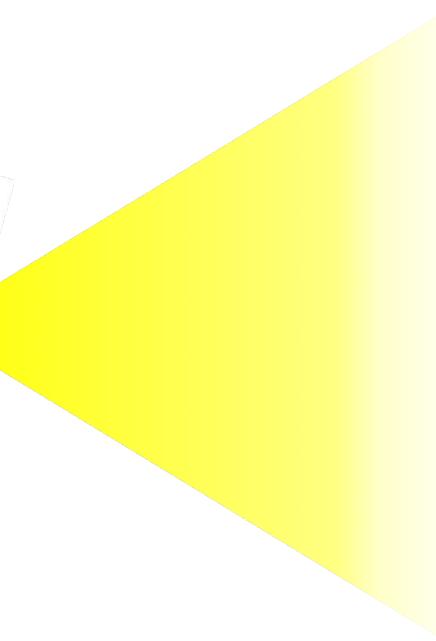
Transmissive: liquid crystal display (LCD)



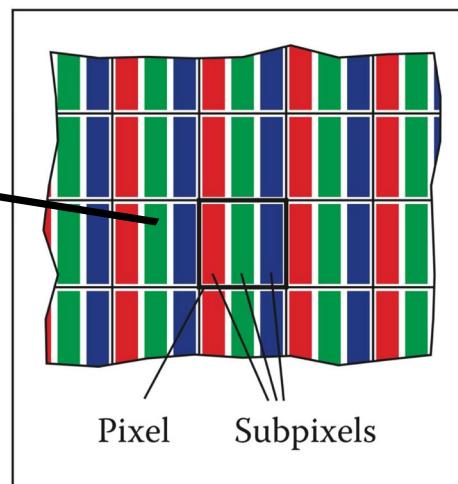
Ink-jet printer



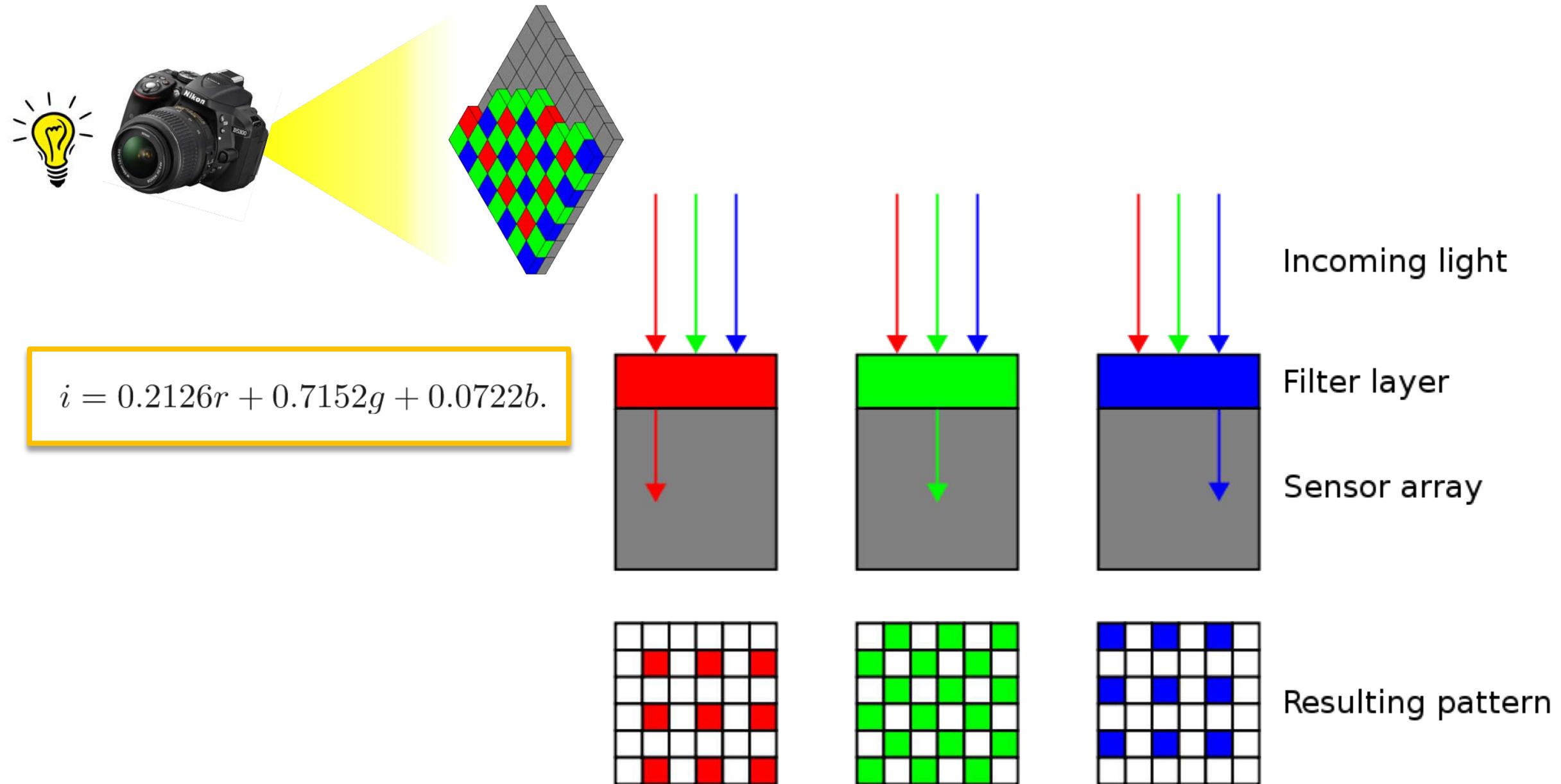
# Raster Input/Output



Bayer Filter



# Raster Input Devices

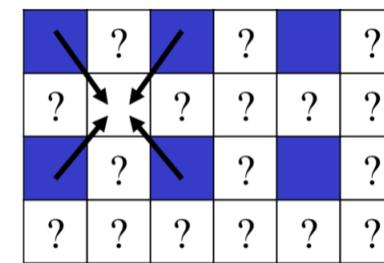
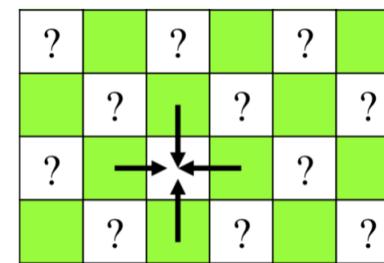
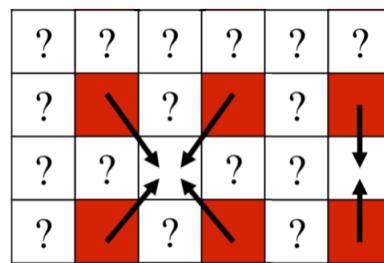
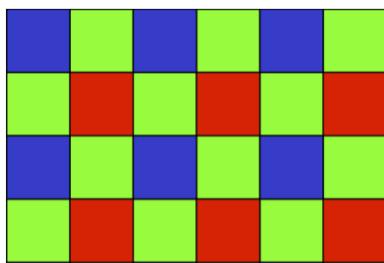


# Why more ‘green’ than ‘red’ or ‘blue’?

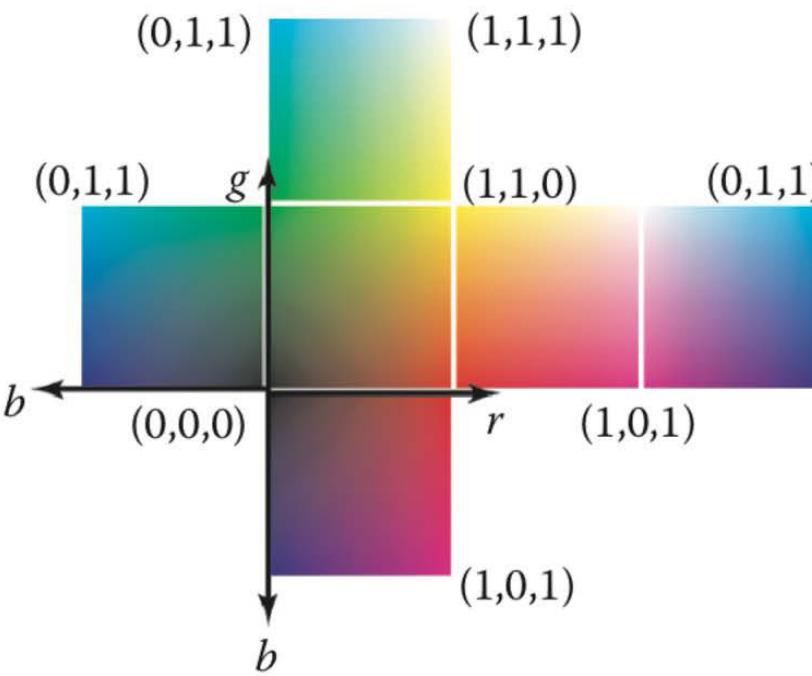
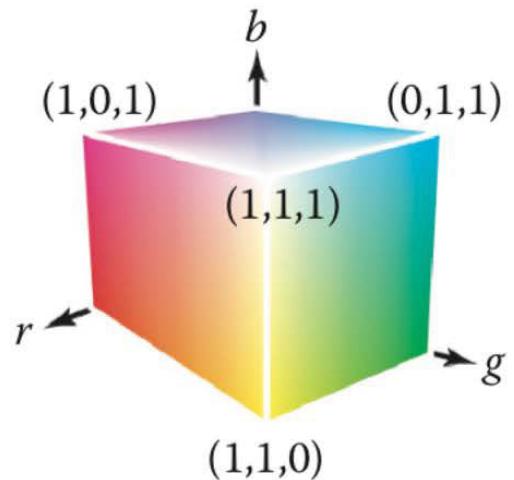


$$i = 0.2126r + 0.7152g + 0.0722b.$$

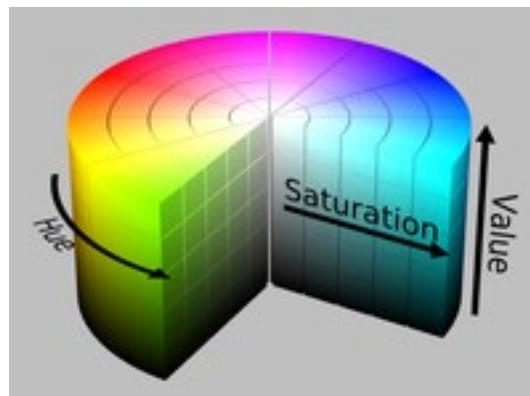
## Demosaicing an image



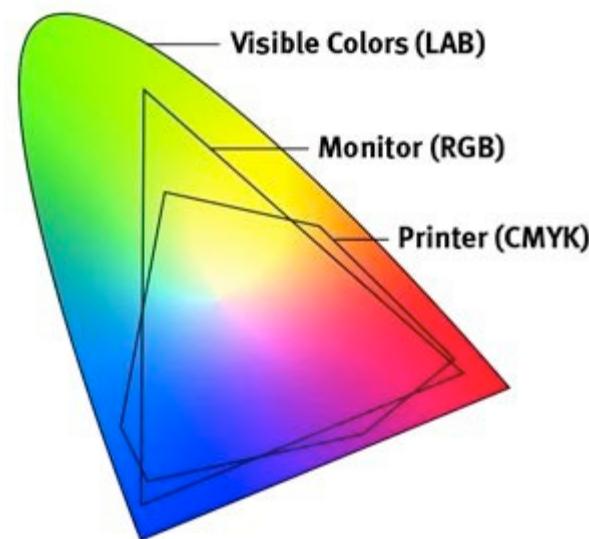
# RGB Images



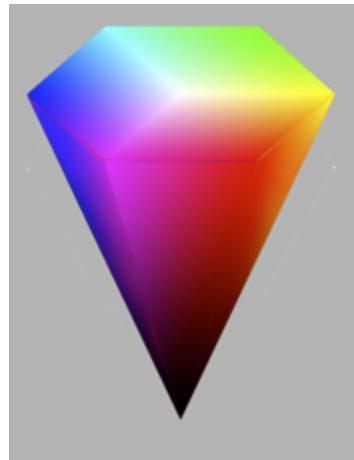
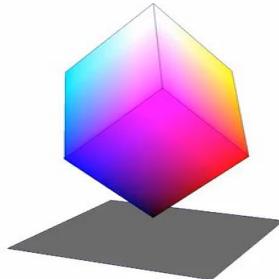
black = (0, 0, 0),  
red = (1, 0, 0),  
green = (0, 1, 0),  
blue = (0, 0, 1),  
yellow = (1, 1, 0),  
magenta = (1, 0, 1),



HSV



# HSV <=> RGB



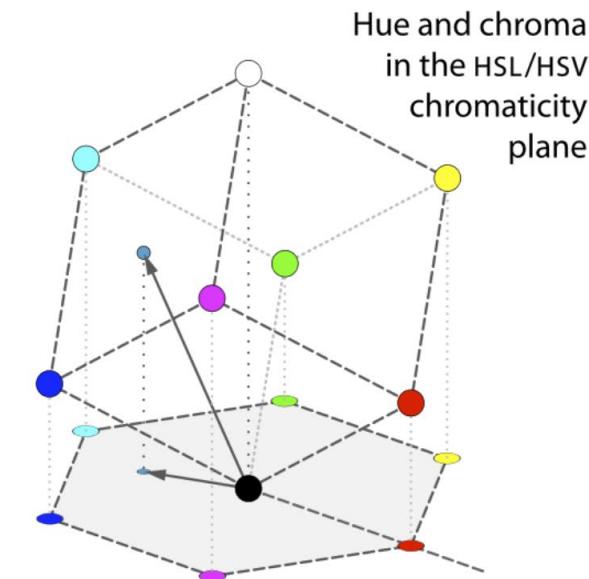
$M = \max(R, G, B)$   
 $m = \min(R, G, B)$   
**chroma**  $C = \text{range}(R, G, B) = M - m$

$$V = \max(R, G, B) = M$$

$$S_V = \begin{cases} 0, & \text{if } V = 0 \\ \frac{C}{V}, & \text{otherwise} \end{cases}$$

$$H' = \begin{cases} \text{undefined,} & \text{if } C = 0 \\ \frac{G-B}{C} \bmod 6, & \text{if } M = R \\ \frac{B-R}{C} + 2, & \text{if } M = G \\ \frac{R-G}{C} + 4, & \text{if } M = B \end{cases}$$

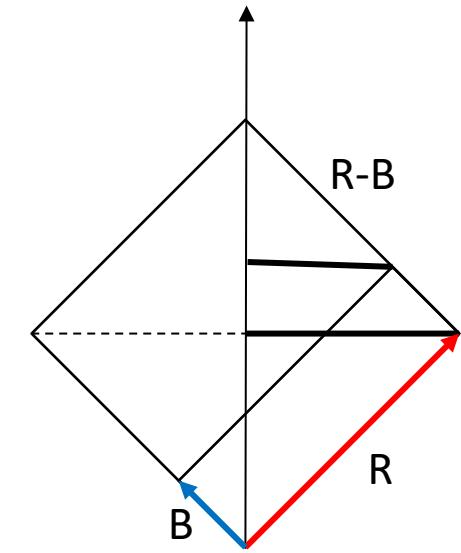
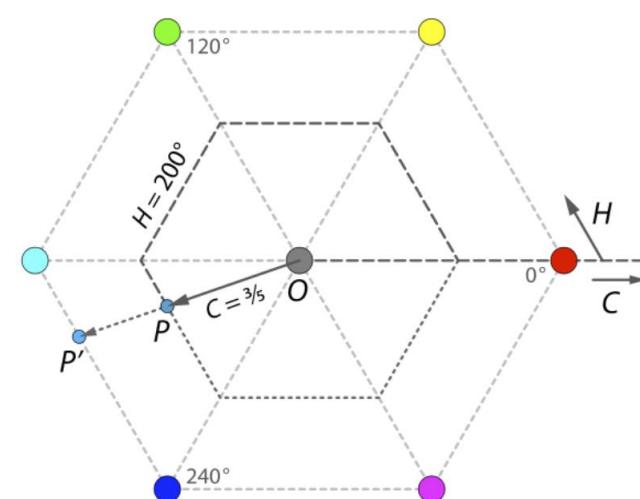
$$H = 60^\circ \times H'$$



$$\begin{array}{l} R = \frac{1}{5} \\ G = \frac{3}{5} \\ B = \frac{4}{5} \end{array}$$

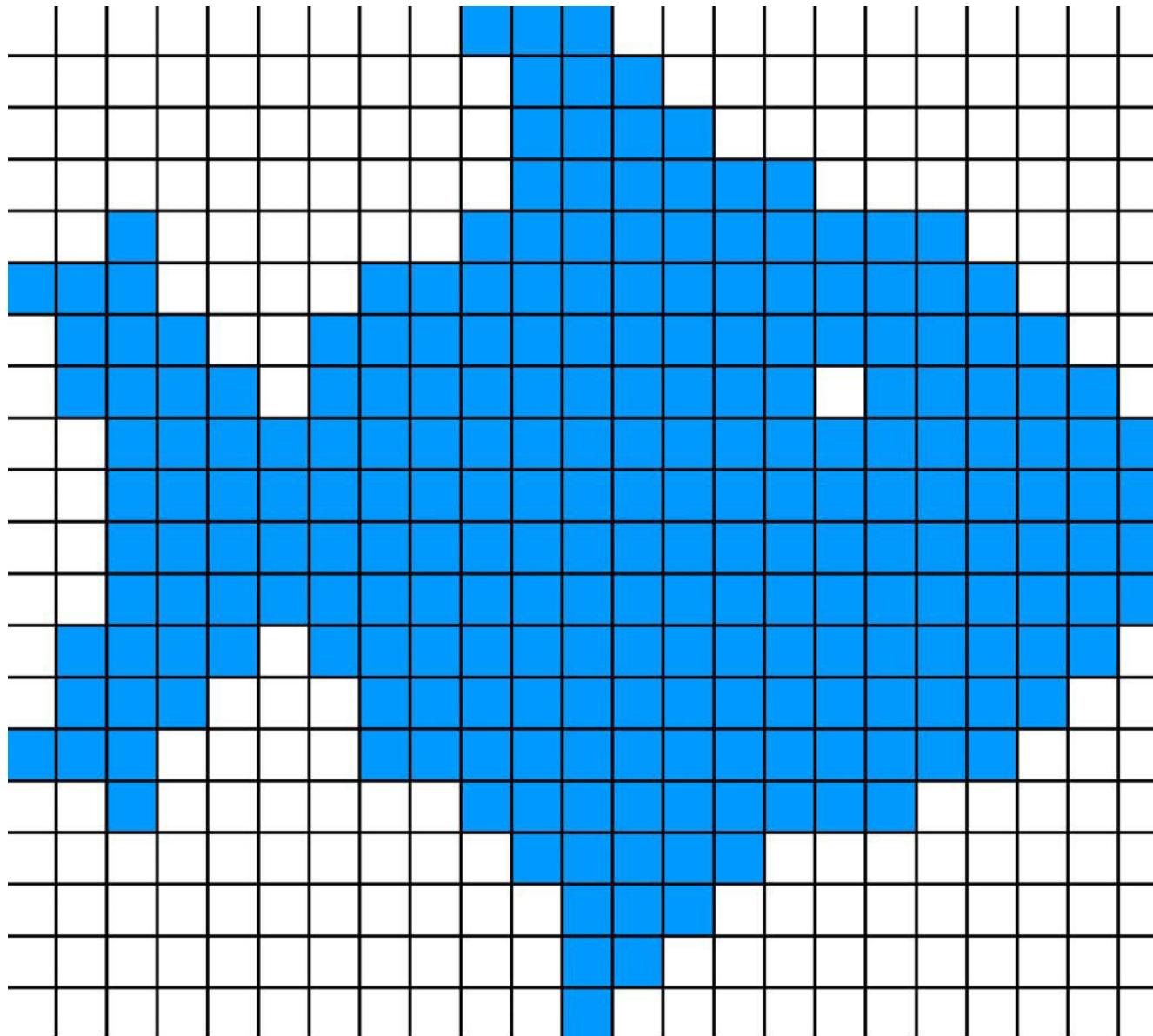
$$C = \frac{OP}{OP'} = B - R = \frac{4}{5} - \frac{1}{5} = \frac{3}{5} = .6$$

$$H = 60^\circ \times \left(4 + \frac{R-G}{C}\right) = 60^\circ \times \left(4 - \frac{2}{3}\right) = 200^\circ$$



$$\begin{array}{l} V=R \\ S=(R-B)/R \end{array}$$

# Raster Image



# Data Types for Raster Images

Storage for 1024x1024 image (1 megapixel) =  $2^{10} \times 2^{10}$  pixels

bitmap 1 bit per pixel (bpp) :  $2^7$ KB or 128KB (2<sup>3</sup> pixels per byte)

grayscale 8bpp: 1MB

grayscale 16bpp: 2MB

color RGB 24bpp: 3MB

color + alpha (transparency) 32bpp: 4MB

floating-point HDR color: 12MB (each of 3 color channels is a 32bit float i.e. 4B)

Q: Suppose you have a 767 X 772 rgb image stored in an array called `data`. How would you access the green value at the pixel on the 36th row and 89th column?

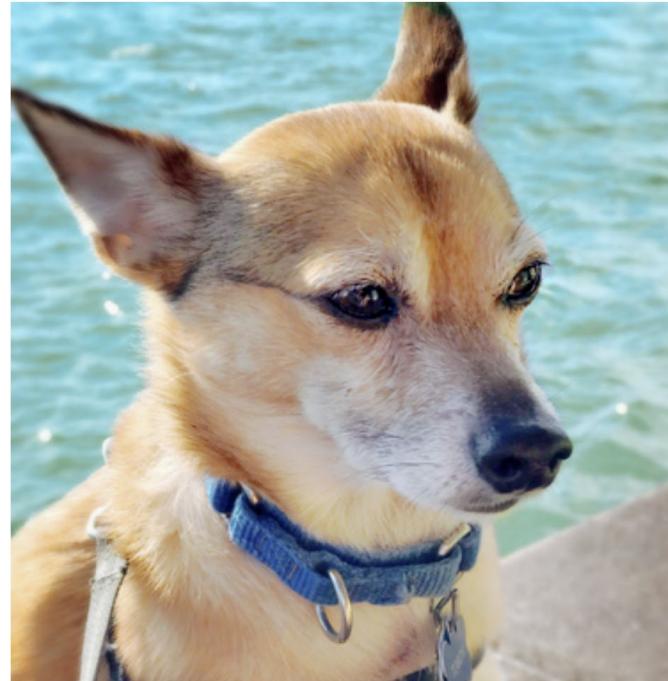
A: `data[1 + 3*(88+767*35)]` (Remember C++ starts counting with `0`).

# Assignment #1 tasks



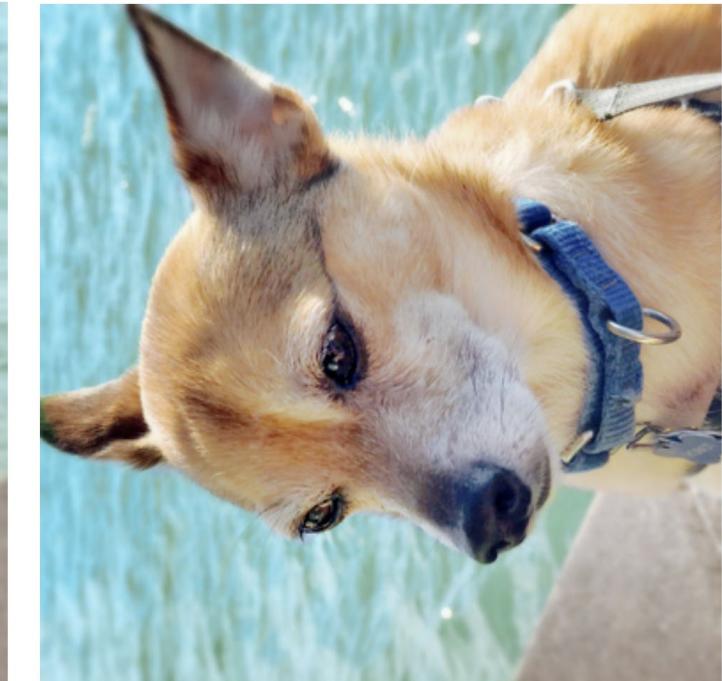
`src/reflect.cpp`

Horizontally reflect an image (like a mirror)



`src/rotate.cpp`

Rotate an image  $90^\circ$  counter-clockwise



# Assignment #1 tasks



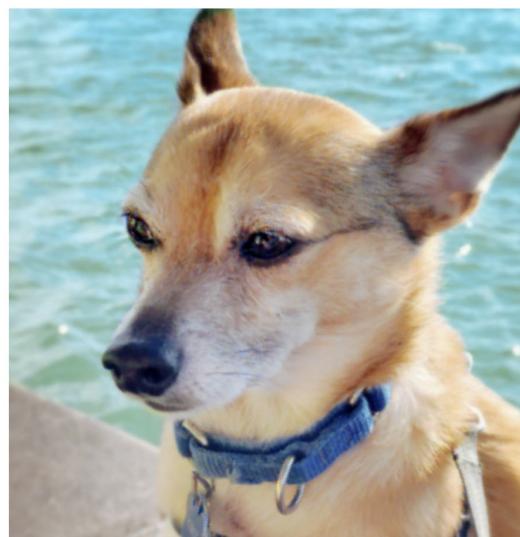
`src/rgb_to_gray.cpp`

Convert a 3-channel RGB image to a 1-channel grayscale image.



`src/demosaic.cpp`

Given a mosaiced image (interleaved GBRG colors in a single channel), created a 3-channel rgb image.



`src/simulate_bayer_mosaic.cpp`

Simulate an image acquired from the Bayer mosaic by taking a 3-channel rgb image and creating a single channel grayscale image composed of interleaved red/green/blue channels. The output image should be the same size as the input but only one channel.



# Assignment #1 tasks



`src/rgb_to_hsv.cpp`

Convert a color represented by red, green and blue intensities to its representation using hue, saturation and value.

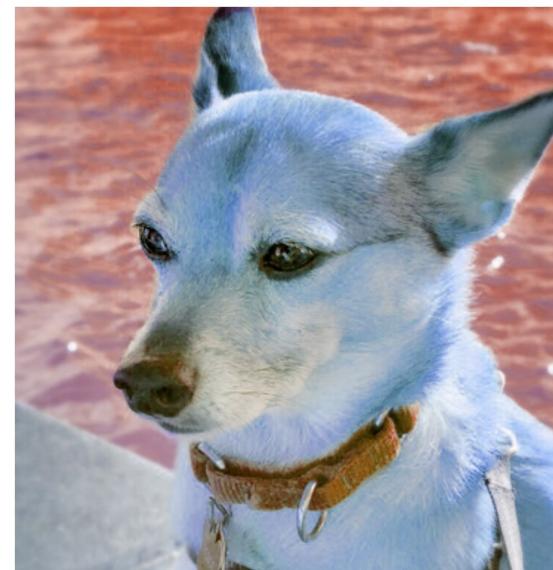
`src/hsv_to_rgb.cpp`

Convert a color represented by hue, saturation and value to its representation using red, green and blue intensities.

`src/hue_shift.cpp`

Shift the hue of a color rgb image.

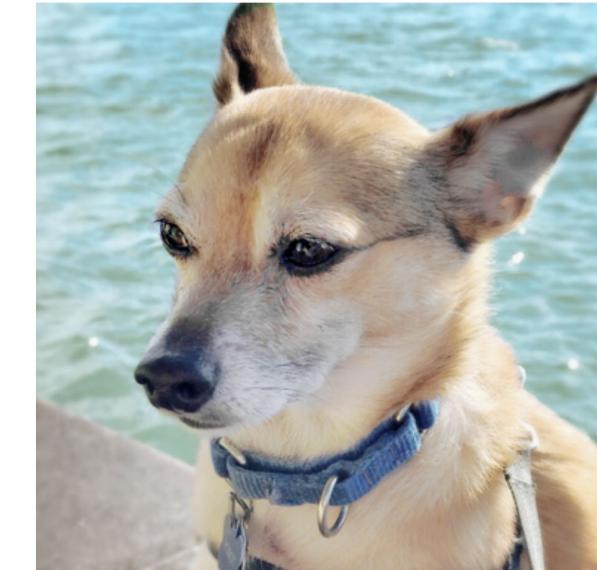
Hint: Use your `rgb_to_hsv` and `hsv_to_rgb` functions.



`src/desaturate.cpp`

Desaturate a given rgb color image by a given factor.

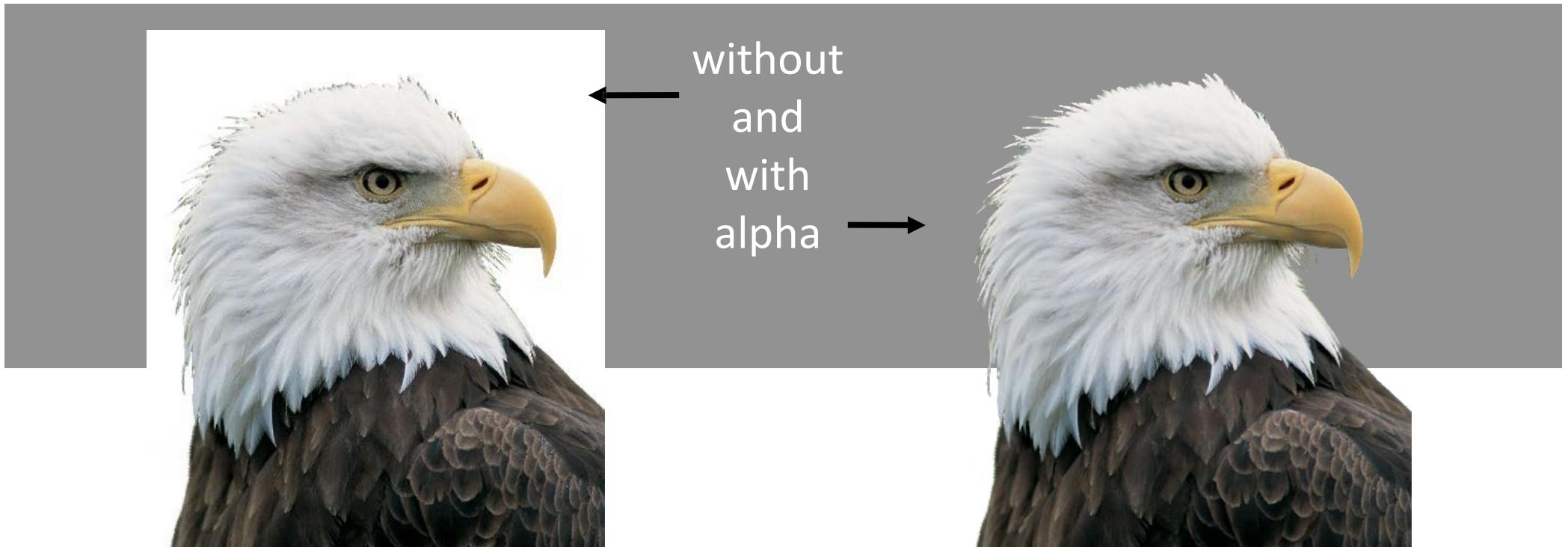
Hint: Use your `rgb_to_hsv` and `hsv_to_rgb` functions.



# Transparency

Append (Red, Green, Blue)

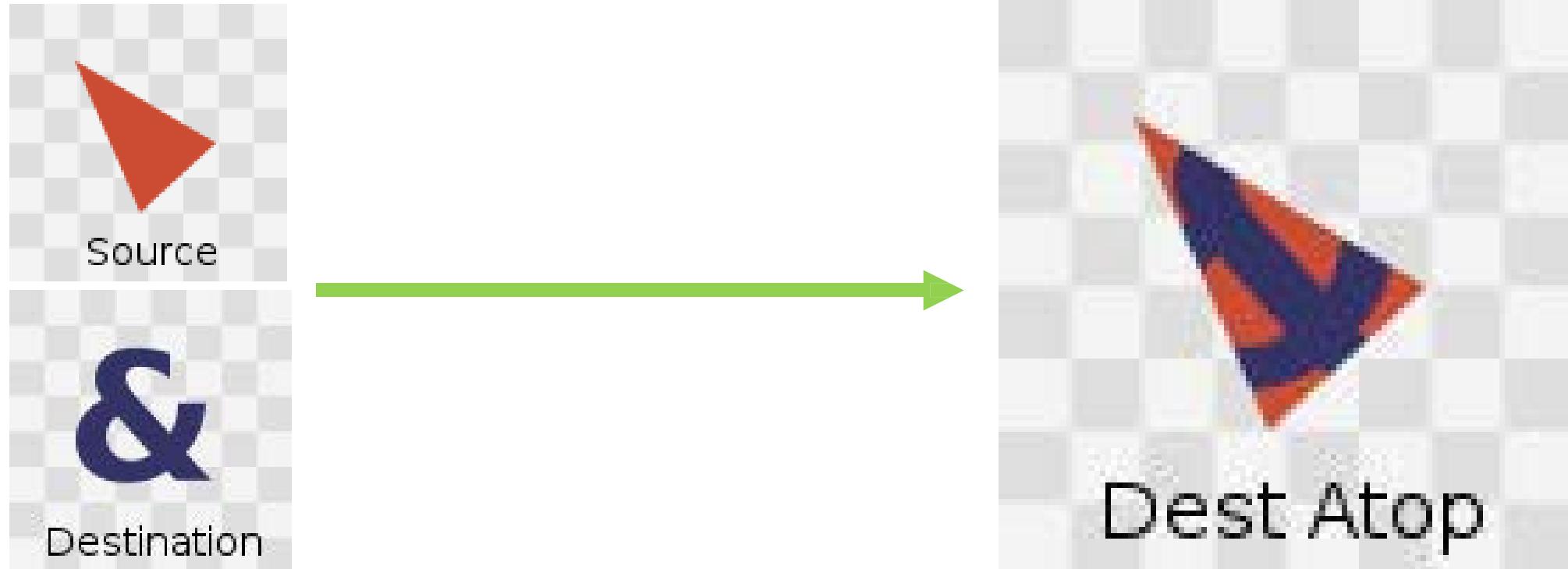
to be (Red, Green, Blue, Alpha)



$$\mathbf{c} = \alpha \mathbf{c}_f + (1 - \alpha) \mathbf{c}_b.$$

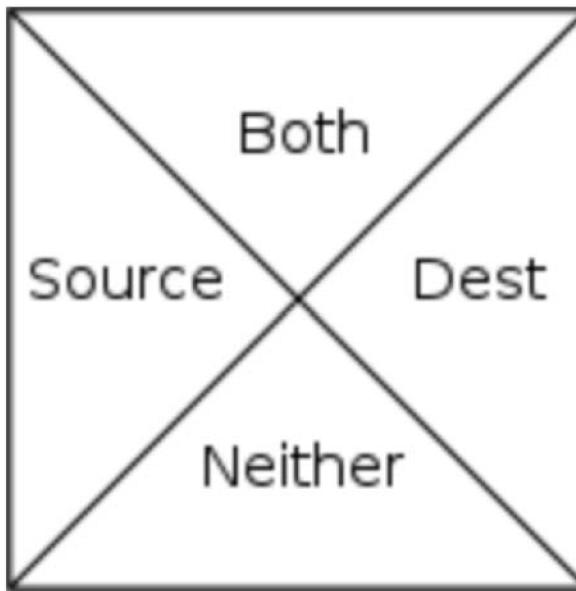
# Compositing

Compositing is about layering images on top of one another



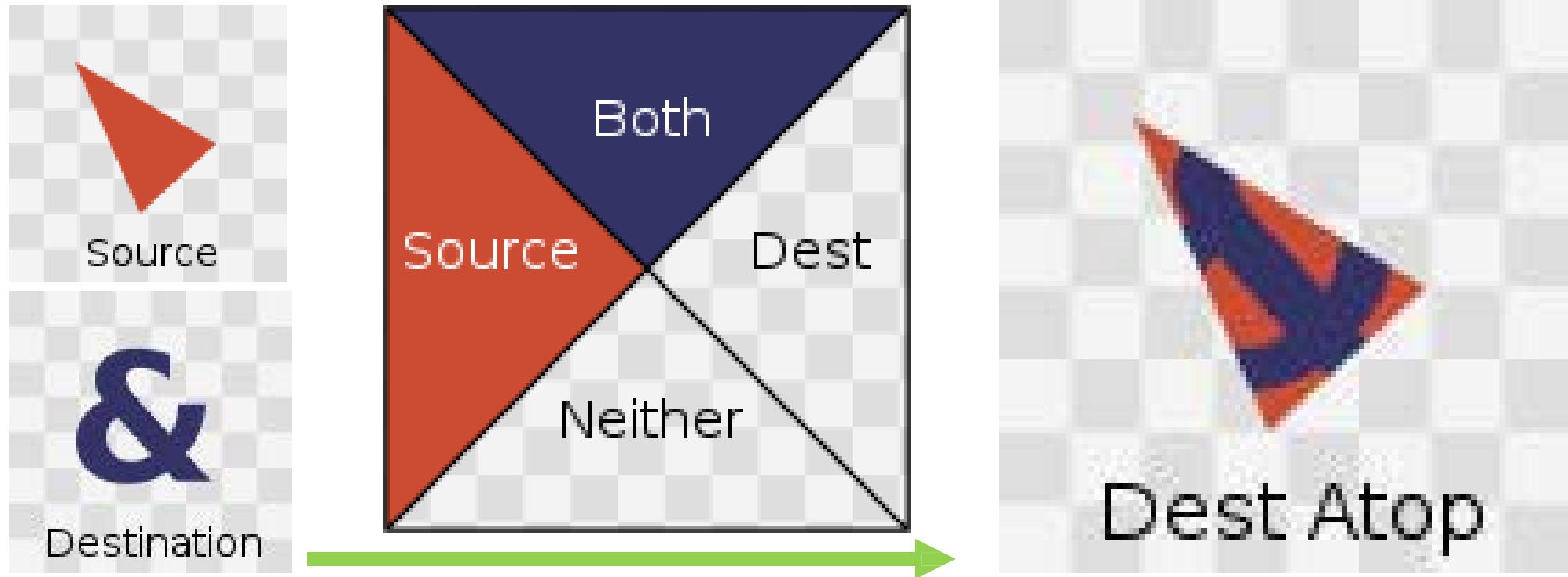
# Compositing

Compositing is about layering images on top of one another



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$$A_{\text{src}} \cdot [s] + A_{\text{dest}} \cdot [d] + A_{\text{both}} \cdot [b]$$

$$A_{\text{src}} = \alpha_s \cdot (1 - \alpha_d)$$

$$A_{\text{dst}} = \alpha_d \cdot (1 - \alpha_s)$$

$$A_{\text{both}} = \alpha_s \cdot \alpha_d$$

	[s]	[d]	[b]
Src	$s$	0	$s$
Atop	0	$d$	$s$
Over	$s$	$d$	$s$
In	0	0	$s$
Out	$s$	0	0
Dest	0	$d$	$d$
DestAtop	$s$	0	$d$
DestOver	$s$	$d$	$d$
DestIn	0	0	$d$
DestOut	0	$d$	0
Clear	0	0	0
Xor	$s$	$d$	0

$B(s, d)$  for color blending



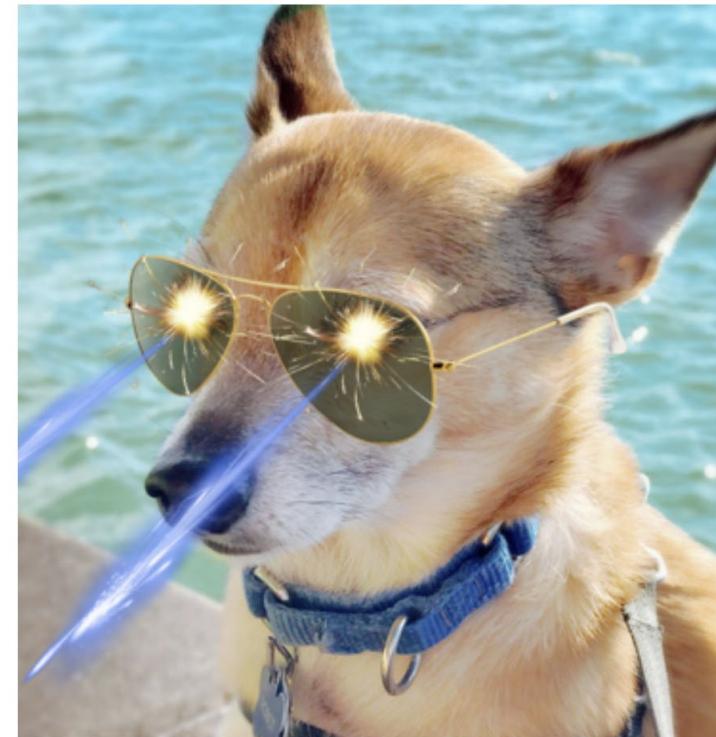
Dest Atop

# Assignment #1 tasks

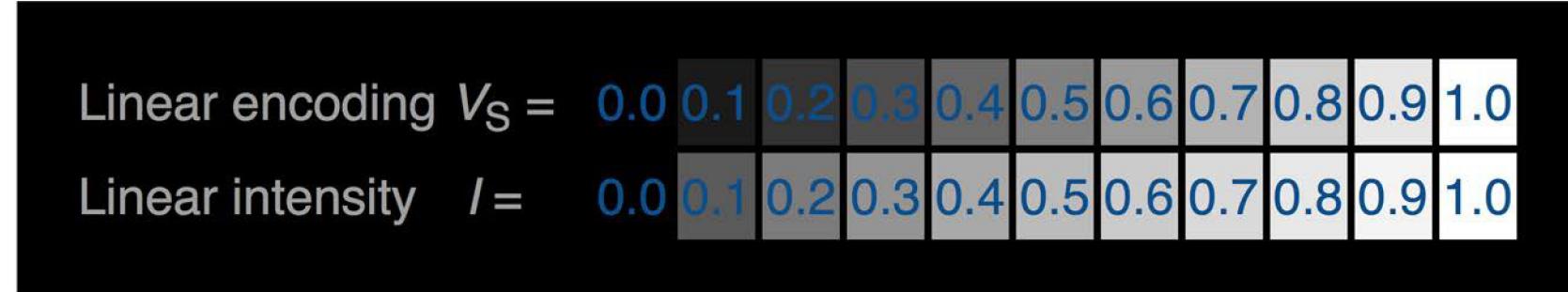


`src/over.cpp`

Compute  $C = A \text{ Over } B$ , where  $A$  and  $B$  are semi-transparent rgba images and "Over" is the Porter-Duff Over operator.



# Raster Image issues: Gamma Correction



Display intensity is nonlinear wrt input intensity

# Raster Image issues: Gamma Correction

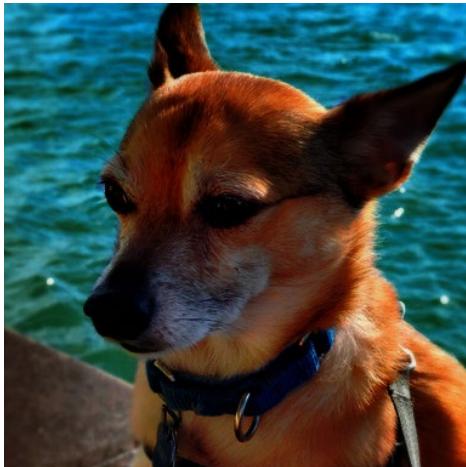
$$\text{displayed intensity} = (\text{maximum intensity}) a^{\gamma}$$

... of display      image amplitude [0,1]

<sup>gamma</sup>

Measuring Gamma for a display:

find image amplitude  $a$  for  $\frac{1}{2}$  display brightness =>  $\gamma = \frac{\ln 0.5}{\ln a}$



$\gamma=0.25$



$\gamma=0.5$



$\gamma=1.0$

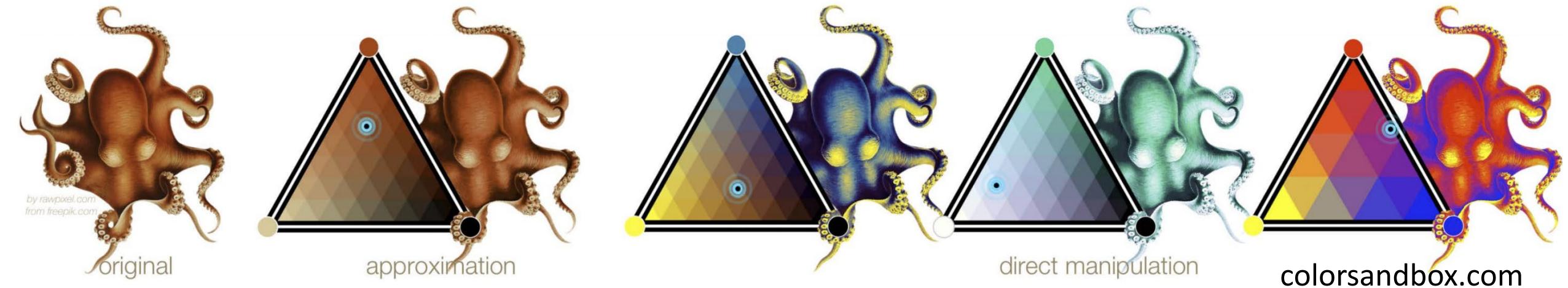
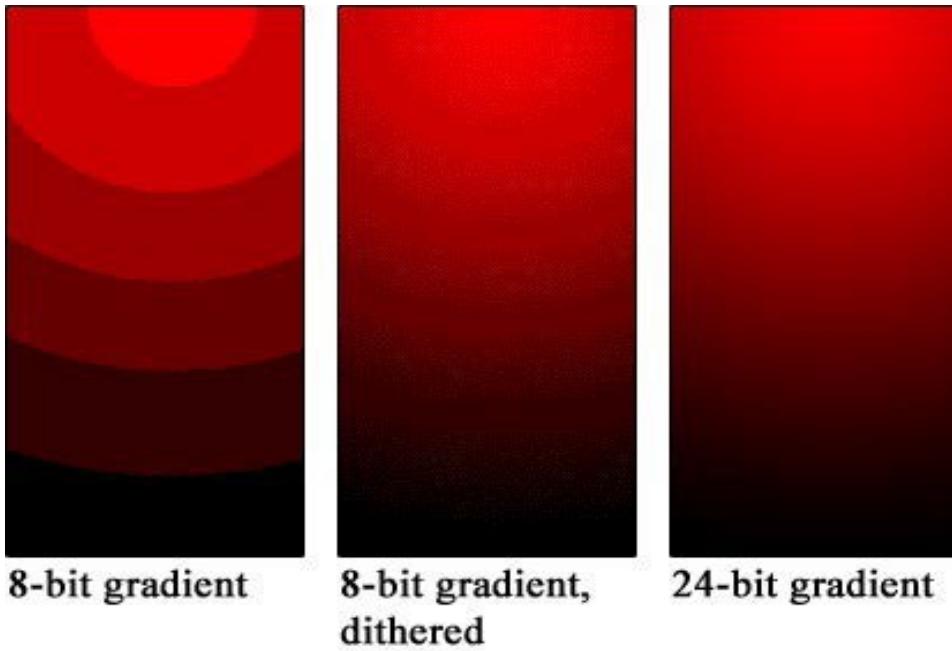


$\gamma=1.5$

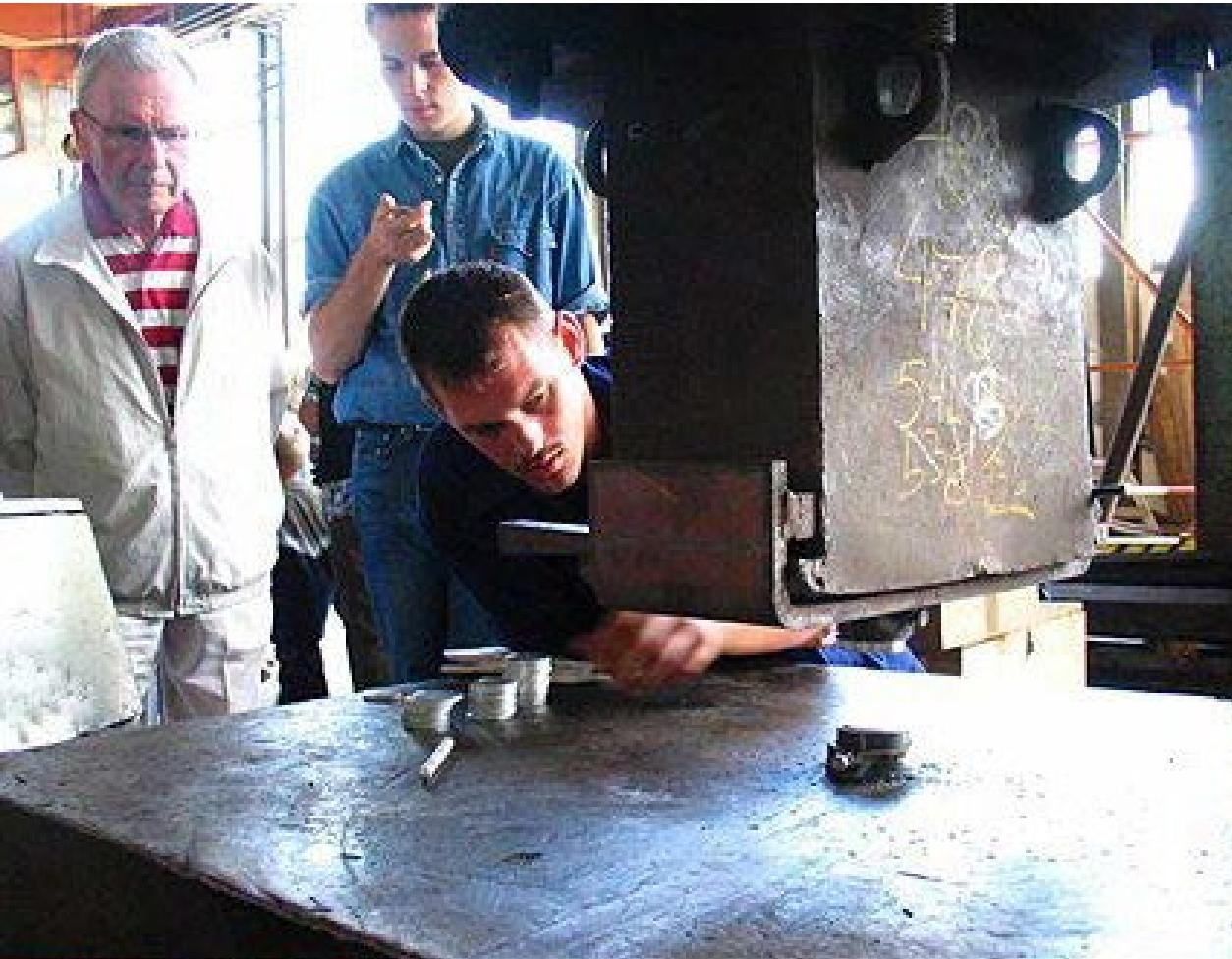


$\gamma=2.0$

# Raster Image issues: Banding



# Raster Image issues: Clipping



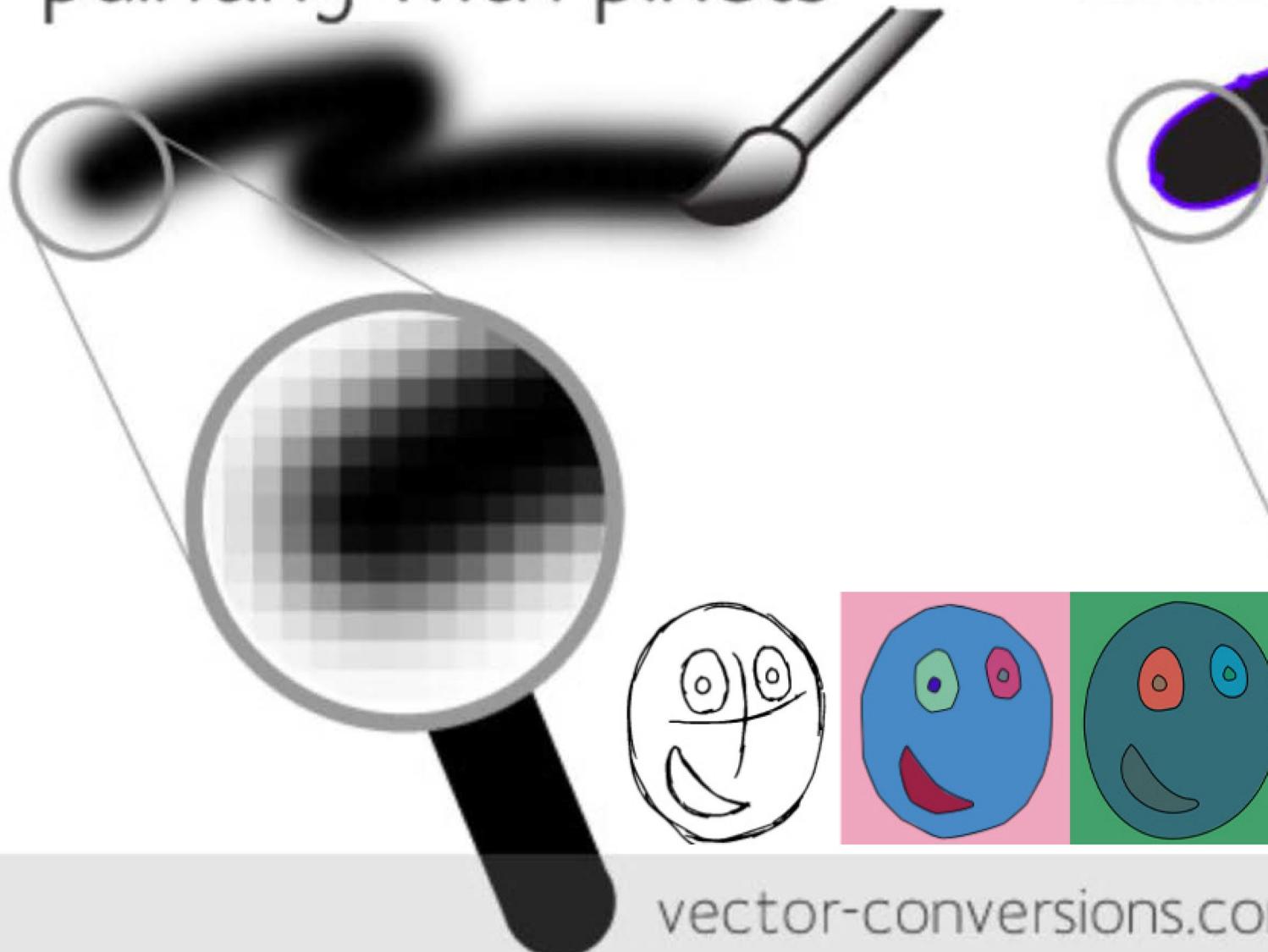
Original



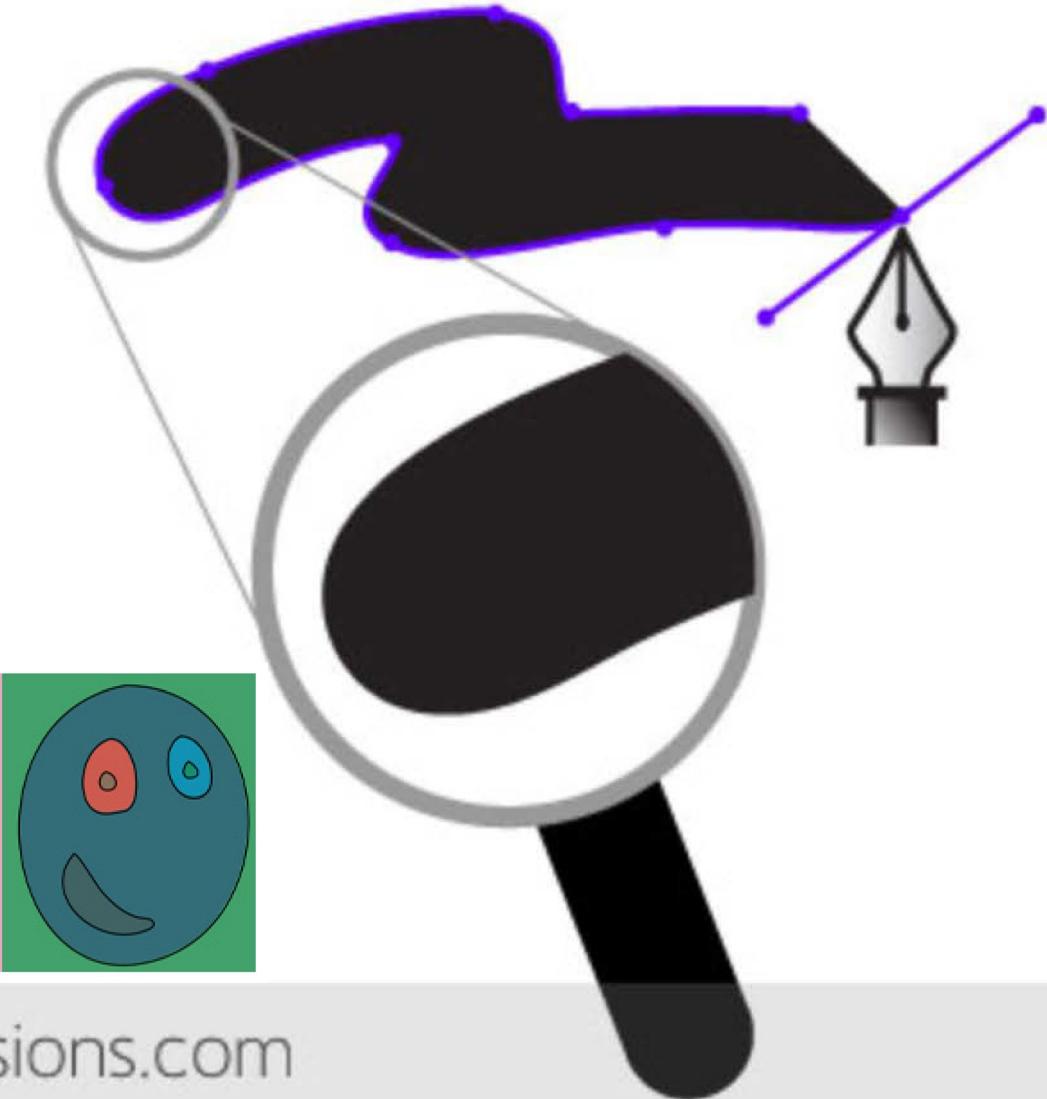
Clipped

## Aside: More Than Just Raster Images

painting with pixels



drawing with vectors



# **Assignment 1**

## **Available Right Now**

**Next Week: Ray Casting**