## LECTURE EXERCISES

## VINCENT TRAN

ABSTRACT. A collection of exercises mentioned by Rudenko in lecture that test your understanding but aren't significant enough to be a true "problem". All should be done at least once. They tend to be more computational. If you can't do it, you can probably open up an old algebra textbook and find it. Dummit and Foote is enormous so it probably contains it.

**Exercise 0.0.1.** Show that the identity and inverse of a group are unique. In addition, associativity holds for any number of elements, i.e.  $g_1g_2g_3\cdots g_n$  is well-defined no matter the bracket placement.

Exercise 0.0.2. Classify all the groups with three elements.

**Exercise 0.0.3.** Show that if  $f: G \to G$  is a function from a group G to itself is such that f(ab) = f(a)f(b), then f(e) = e and  $f(a^{-1}) = f(a)^{-1}$ .

**Exercise 0.0.4.** Show that  $\mathbb{S}_3$  is isomorphic to  $GL_2(\mathbf{F}_2)$ .

**Exercise 0.0.5.** Compute some operations in  $S_n$ .