DATA621 Home Work 3

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Home Work Assignment 3.

1.DATA EXPLORATION.(Exploratory Data Analysis EDA)

As first step in our EDA, let us load the train data and do a summary statistics on the loaded dataset.

```
# Let us load the train.csv data
train = read.csv('crime-training-data.csv')
test = read.csv('crime-evaluation-data.csv')
summary(train)
```

```
##
                           indus
                                               chas
                                                                  nox
          zn
##
    Min.
               0.00
                              : 0.460
                                                 :0.00000
                                                                     :0.3890
            :
                       Min.
                                         Min.
                                                             Min.
    1st Qu.:
               0.00
                       1st Qu.: 5.145
                                         1st Qu.:0.00000
                                                             1st Qu.:0.4480
               0.00
##
    Median :
                       Median : 9.690
                                         Median :0.00000
                                                             Median :0.5380
##
    Mean
            : 11.58
                              :11.105
                                                 :0.07082
                                                                     :0.5543
                       Mean
                                         Mean
                                                             Mean
##
    3rd Qu.: 16.25
                       3rd Qu.:18.100
                                         3rd Qu.:0.00000
                                                             3rd Qu.:0.6240
                              :27.740
##
    Max.
            :100.00
                      Max.
                                         Max.
                                                 :1.00000
                                                             Max.
                                                                     :0.8710
##
          rm
                           age
                                             dis
                                                                rad
##
    Min.
            :3.863
                     Min.
                             : 2.90
                                        Min.
                                                : 1.130
                                                          Min.
                                                                  : 1.00
##
    1st Qu.:5.887
                     1st Qu.: 43.88
                                        1st Qu.: 2.101
                                                           1st Qu.: 4.00
                     Median: 77.15
##
    Median :6.210
                                        Median : 3.191
                                                          Median: 5.00
            :6.291
                                                                  : 9.53
##
    Mean
                     Mean
                             : 68.37
                                        Mean
                                                : 3.796
                                                          Mean
##
    3rd Qu.:6.630
                     3rd Qu.: 94.10
                                        3rd Qu.: 5.215
                                                           3rd Qu.:24.00
##
    Max.
            :8.780
                     Max.
                             :100.00
                                        Max.
                                                :12.127
                                                          Max.
                                                                  :24.00
                         ptratio
##
                                          black
                                                             lstat
         tax
            :187.0
                             :12.6
                                             : 0.32
                                                                : 1.730
##
    Min.
                     Min.
                                      Min.
                                                        Min.
##
    1st Qu.:281.0
                      1st Qu.:16.9
                                      1st Qu.:375.61
                                                        1st Qu.: 7.043
##
    Median :334.5
                     Median:18.9
                                      Median :391.34
                                                        Median :11.350
##
    Mean
            :409.5
                     Mean
                             :18.4
                                      Mean
                                              :357.12
                                                        Mean
                                                                :12.631
##
    3rd Qu.:666.0
                     3rd Qu.:20.2
                                      3rd Qu.:396.24
                                                        3rd Qu.:16.930
##
                             :22.0
                                              :396.90
    Max.
            :711.0
                     Max.
                                      Max.
                                                        Max.
                                                                :37.970
##
         medv
                          target
##
    Min.
           : 5.00
                     Min.
                             :0.0000
##
    1st Qu.:17.02
                     1st Qu.:0.0000
##
    Median :21.20
                     Median :0.0000
##
    Mean
            :22.59
                     Mean
                             :0.4914
##
    3rd Qu.:25.00
                     3rd Qu.:1.0000
    Max.
            :50.00
                     Max.
                             :1.0000
```

We will make sure there is no inappropriate distribution of target(response) variables in our training data.

```
knitr::kable(table(train$target))
```

| Var1 | Freq |
|------|------|
| 0 | 237 |

| Var1 | Free |
|------|------|
| 1 | 229 |

Examination of Data Set.

- 1. There are 466 rows and 14 columns in the train data set. Out of 14 columns, 12 are continous variables and 2 are discrete variables. There are no NA values in the dataset.
- 2. On exploring the train data set, we see 13 predictor variables. All the variables are related to housing ranging from ethinicity, age group, income level to how big the houses are, number of square feet that is owned.
- 3. For the binary logistic regression, the variable target is the response variables, with value of 0 or 1. 1 indicates crime rate is above the median value.
- 4. On a general glance one might think of following variables be positively correlated with higher crime rate. Like lstat, indus, nox, ptratio etc. Similarly following variables as negatively correlated with higher crime rates. Like zn, rm, rad, medv.

Statistical Summary of Data Set:

```
summary = describe(train, quant = c(.25,.75))
knitr::kable(summary)
```

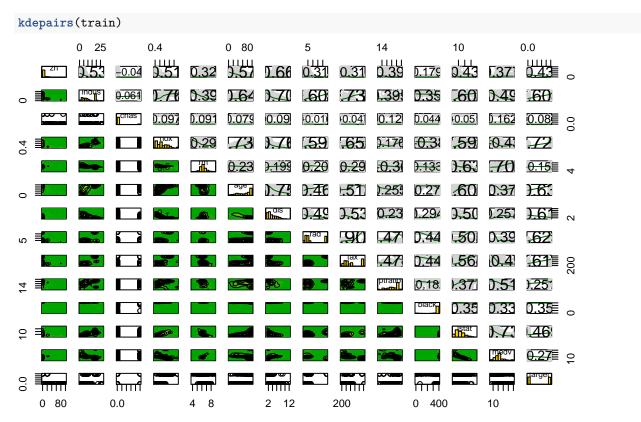
| | vars | n | mean | sd | median | trimmed | mad | min | max | rang |
|---------|------|-----|-------------|-------------|-----------|-------------|-------------|----------|----------|---------|
| zn | 1 | 466 | 11.5772532 | 23.3646511 | 0.00000 | 5.3542781 | 0.0000000 | 0.0000 | 100.0000 | 100.000 |
| indus | 2 | 466 | 11.1050215 | 6.8458549 | 9.69000 | 10.9082353 | 9.3403800 | 0.4600 | 27.7400 | 27.280 |
| chas | 3 | 466 | 0.0708155 | 0.2567920 | 0.00000 | 0.0000000 | 0.0000000 | 0.0000 | 1.0000 | 1.000 |
| nox | 4 | 466 | 0.5543105 | 0.1166667 | 0.53800 | 0.5442684 | 0.1334340 | 0.3890 | 0.8710 | 0.482 |
| rm | 5 | 466 | 6.2906738 | 0.7048513 | 6.21000 | 6.2570615 | 0.5166861 | 3.8630 | 8.7800 | 4.917 |
| age | 6 | 466 | 68.3675966 | 28.3213784 | 77.15000 | 70.9553476 | 30.0226500 | 2.9000 | 100.0000 | 97.100 |
| dis | 7 | 466 | 3.7956929 | 2.1069496 | 3.19095 | 3.5443647 | 1.9144814 | 1.1296 | 12.1265 | 10.996 |
| rad | 8 | 466 | 9.5300429 | 8.6859272 | 5.00000 | 8.6978610 | 1.4826000 | 1.0000 | 24.0000 | 23.000 |
| tax | 9 | 466 | 409.5021459 | 167.9000887 | 334.50000 | 401.5080214 | 104.5233000 | 187.0000 | 711.0000 | 524.000 |
| ptratio | 10 | 466 | 18.3984979 | 2.1968447 | 18.90000 | 18.5970588 | 1.9273800 | 12.6000 | 22.0000 | 9.400 |
| black | 11 | 466 | 357.1201502 | 91.3211298 | 391.34000 | 383.5064439 | 8.2432560 | 0.3200 | 396.9000 | 396.580 |
| lstat | 12 | 466 | 12.6314592 | 7.1018907 | 11.35000 | 11.8809626 | 7.0720020 | 1.7300 | 37.9700 | 36.240 |
| medv | 13 | 466 | 22.5892704 | 9.2396814 | 21.20000 | 21.6304813 | 6.0045300 | 5.0000 | 50.0000 | 45.000 |
| target | 14 | 466 | 0.4914163 | 0.5004636 | 0.00000 | 0.4893048 | 0.0000000 | 0.0000 | 1.0000 | 1.000 |

- 1. We cannot say what variable transformation to be performed based on Skewness and Kurtosis as they are not large enough.
- 2. The variable Zn is the only rightly skewed variables.

Visual Exploration of Data set:

Scatterplot

1. First we will see the scatterplot between the predictor variables and response variables.

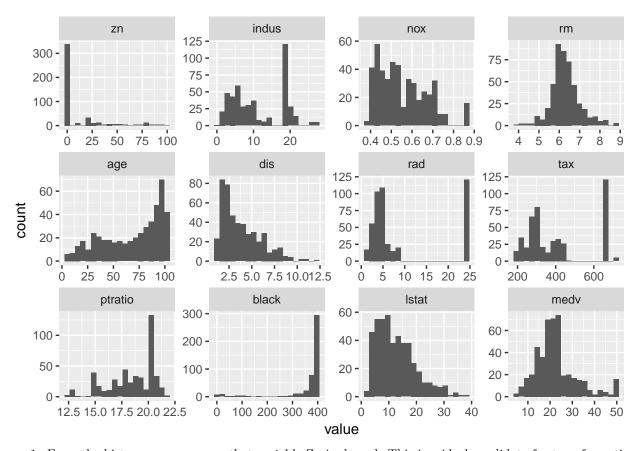


From the scatterplot, several of the predictor variables has non linear relationship with each other.

Histogram

```
ggtrain = reshape::melt(train, id.vars = "target") %>%
  dplyr::filter(variable != "chas") %>%
  mutate(target = as.factor(target))

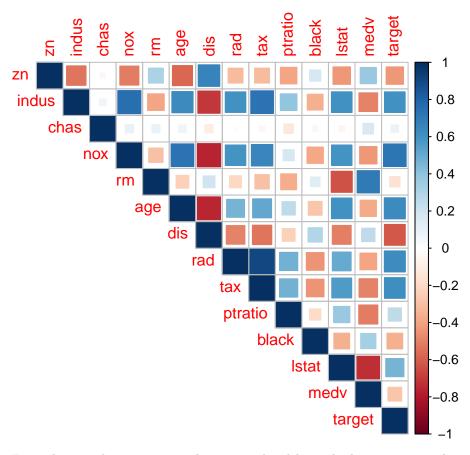
ggplot(data = ggtrain, aes(value)) +
  geom_histogram(bins = 20) +
  facet_wrap(~variable, scales = "free")
```



- 1. From the histogram we can see that variable Zn is skewed. This is a ideal candidate for transformation.
- 2. To some extent even the variables dis, age and lstat are skewed. So we can think of doing some transformation on these variables.

MultiCollinearity between predictor variables and also with response variables

```
cordata = cor(train)
corrplot(cordata, method = "square", type = "upper")
```



From the corrplot we can see that tax and rad has a high positive correlation. In our model we have to remove multicollinearity by checking the varaiance inflation factor.

With respect to response and predictor variables, the variable nox has highest correlation with response variable. We have to see how this affect our modelling.

2.DATA PREPARATION

From our visual exploration we have identified few variables to go through transformation based on the dataset.

1. We will apply log transform on the skewed variables Zn, age, and lstat. According to the book Sheather in book MARR in the chapter 8.

```
train_data_transform =
  train %>%
  mutate(
    log_age = log(age),
    log_lstat = log(lstat))
```

3. BUILDING MODELS

As approach we are going to build the following models.

Each of our logistic regression models will use bionomial regression with a logit link function

1. Using the data set asis with 13 predictor variables and 1 response variable. This model we will call it the Base Model with all original variables in data set.

Base Model

```
base_model = glm(target ~ . , family = "binomial", data = train)
summary(base_model)
##
## glm(formula = target ~ ., family = "binomial", data = train)
##
## Deviance Residuals:
      Min
                 1Q
                      Median
                                   30
                                           Max
## -2.2854 -0.1372 -0.0017
                               0.0020
                                        3.4721
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
## (Intercept) -36.839521
                            7.028726
                                     -5.241 1.59e-07 ***
                            0.034410 -1.794 0.072868 .
## zn
                -0.061720
## indus
                -0.072580
                            0.048546
                                     -1.495 0.134894
                1.032352
                            0.759627
                                       1.359 0.174139
## chas
## nox
                50.159513
                            8.049503
                                       6.231 4.62e-10 ***
## rm
                            0.741431 -0.934 0.350548
                -0.692145
                 0.034522
                            0.013883
                                       2.487 0.012895 *
## age
## dis
                 0.765795
                            0.234407
                                       3.267 0.001087 **
                 0.663015
                            0.165135
                                       4.015 5.94e-05 ***
## rad
                            0.003064 -2.152 0.031422 *
## tax
                -0.006593
                                       3.344 0.000825 ***
## ptratio
                 0.442217
                            0.132234
                -0.013094
                            0.006680
                                     -1.960 0.049974 *
## black
                 0.047571
                            0.054508
                                       0.873 0.382802
## 1stat
## medv
                 0.199734
                            0.071022
                                       2.812 0.004919 **
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
       Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 186.15 on 452 degrees of freedom
## AIC: 214.15
##
## Number of Fisher Scoring iterations: 9
knitr::kable(vif(base model))
```

| | X |
|-------------|----------|
| zn | 1.846737 |
| indus | 2.699928 |
| chas | 1.262505 |
| nox | 4.296876 |
| $_{\rm rm}$ | 6.070541 |
| age | 2.556302 |
| dis | 4.025192 |
| rad | 1.955112 |
| tax | 2.174569 |
| | |

```
ptratio 2.340600
black 1.091380
lstat 2.681384
medv 8.567935
```

```
hoslem.test(train$target, fitted(base_model))

##

## Hosmer and Lemeshow goodness of fit (GOF) test

##

## data: train$target, fitted(base_model)

## X-squared = 18.284, df = 8, p-value = 0.01919

rocBasePlot = roc(base_model$y, fitted(base_model))

AUC = as.numeric(pROC::roc(base_model$y, fitted(base_model))$auc)

AUC
```

Observations

[1] 0.9752732

From the above model, we see 5 out of the 13 variables has (stat-sig) p-values at a significance level greater than 0.05

The coefficient for nox has the highest, which has the highest positive correlation with response variables.

From the VIF function we can see that the following variables has VIF > 4. medv, dis, rm, nox. In our next model we can think of eliminating these as part of Multicollinearity test.

From the above Hoslem test we can see the value of p = 0.1919, which is significantly lesser than 0.05. Which says our model is pretty good.

From the AUC(Area under the curve) values above of 'r AUC' is relatively high at .974. This model is good at predicting the response variable.

Base Model and Transformed Variables

2. For our second model we are going to use 17 variables, which includes the log transformed variables.

```
base_transform_model = glm(target ~ . , family = "binomial", data = train_data_transform)
summary(base_transform_model)
```

```
##
## Call:
## glm(formula = target ~ ., family = "binomial", data = train_data_transform)
##
## Deviance Residuals:
##
       Min
                 10
                      Median
                                    30
                                            Max
                                         3.6868
           -0.1192 -0.0011
                                0.0011
##
  -2.1248
##
## Coefficients:
##
                 Estimate Std. Error z value Pr(>|z|)
                                      -3.121 0.001799 **
## (Intercept) -23.635217
                             7.571815
                -0.055881
                             0.035993
                                       -1.553 0.120526
## zn
                                       -1.930 0.053663
## indus
                -0.101194
                             0.052445
## chas
                 1.122399
                             0.801642
                                        1.400 0.161476
                                        6.300 2.98e-10 ***
                54.328789
                             8.623808
## nox
```

```
## rm
         -1.359041 0.810076 -1.678 0.093411 .
## age
         ## dis
         ## rad
## tax
         ## ptratio
         ## black
         -0.012212 0.006326 -1.931 0.053531 .
          ## 1stat
## medv
          ## log_age
          -3.089161 1.100215 -2.808 0.004988 **
## log_lstat
          -1.965229 1.628603 -1.207 0.227549
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
##
    Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 177.34 on 450 degrees of freedom
## AIC: 209.34
##
## Number of Fisher Scoring iterations: 9
knitr::kable(vif(base_transform_model))
```

| | X |
|-----------------------|-----------|
| zn | 1.868586 |
| indus | 2.825736 |
| chas | 1.276773 |
| nox | 4.563620 |
| rm | 6.971836 |
| age | 13.126723 |
| dis | 4.094431 |
| rad | 2.203775 |
| tax | 2.414672 |
| ptratio | 2.321585 |
| black | 1.098637 |
| lstat | 14.347795 |
| medv | 9.217597 |
| \log age | 9.991509 |
| \log_{lstat} | 18.646352 |

```
hoslem.test(train$target, fitted(base_transform_model))
##
## Hosmer and Lemeshow goodness of fit (GOF) test
##
## data: train$target, fitted(base_transform_model)
## X-squared = 25.751, df = 8, p-value = 0.001159
rocBaseTransformPlot = roc(base_transform_model$y, fitted(base_transform_model))
AUC = as.numeric(pROC::roc(base_transform_model$y, fitted(base_transform_model))$auc)
AUC
```

Observations

From the above model, we see 6 out of the 17 variables has (stat-sig) p-values at a significance level greater than 0.05

From the VIF function we can see 7 variables has VIF > 4. So this multicollinearity issue has confounded with the transformation model. So this issue will make this model not a good fit.

From the above Hoslem test we can see the value of p = 0.001159, which is significantly lesser than 0.05. Which says our model is pretty good.

From the AUC(Area under the curve) values above of 'r AUC' is relatively high at .977. This model is good at predicting the response variable.

Considering the confounding multicollinearity issue this model is creating, this will not be the ideal candidate.

Base Model Backward Elimination

3. For this model, we are going to use the Base Model and we are going to remove the variables which has higher p-value (>0.05).

The following variables have been removed from base model variables. zn, indus, chas, rm, lstat

```
train_new = subset(train, select = -c(zn, indus, chas, rm, lstat))
base_backward_model = glm(target ~ . , family = "binomial", data = train_new)
summary(base_backward_model)
##
## Call:
### glm(formula = target ~ . . family = "binomial" data = train_new)
```

```
## glm(formula = target ~ ., family = "binomial", data = train_new)
## Deviance Residuals:
##
        Min
                         Median
                                       3Q
                                                 Max
                      -0.01400
                                             3.06740
                                  0.00279
## -2.42422
            -0.19292
##
## Coefficients:
                 Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -32.301655
                            6.382694
                                      -5.061 4.17e-07 ***
## nox
                42.160350
                            6.674149
                                       6.317 2.67e-10 ***
                 0.031017
                            0.010681
                                       2.904 0.003684 **
## age
## dis
                 0.437803
                            0.172533
                                       2.538 0.011165 *
                 0.703446
                            0.140296
                                       5.014 5.33e-07 ***
## rad
## tax
                -0.008744
                            0.002611
                                      -3.348 0.000813 ***
## ptratio
                 0.395580
                            0.112482
                                       3.517 0.000437 ***
                -0.012490
                            0.006760
                                      -1.848 0.064662 .
## black
                            0.034116
                                       2.966 0.003020 **
## medv
                 0.101177
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
##
##
       Null deviance: 645.88
                              on 465
                                      degrees of freedom
## Residual deviance: 198.28
                              on 457
                                      degrees of freedom
## AIC: 216.28
##
```

Number of Fisher Scoring iterations: 9

knitr::kable(vif(base_backward_model))

| | Х |
|---------|----------|
| nox | 3.338245 |
| age | 1.726911 |
| dis | 2.800880 |
| rad | 1.646105 |
| tax | 1.706377 |
| ptratio | 1.703399 |
| black | 1.064837 |
| medv | 2.135365 |

hoslem.test(train\$target, fitted(base_backward_model))

```
##
## Hosmer and Lemeshow goodness of fit (GOF) test
##
## data: train$target, fitted(base_backward_model)
## X-squared = 2.3393, df = 8, p-value = 0.9688

rocBaseBackwardPlot = roc(base_backward_model$y, fitted(base_backward_model))
AUC = as.numeric(pROC::roc(base_backward_model$y, fitted(base_backward_model))$auc)
AUC
```

[1] 0.9712196

Observations

From the above model, we see all of our variables have p-values at a significance level lesser than 0.05

From the VIF function we can see 0 variables has VIF > 4.

From the above Hoslem test we can see the value of p = 0.9688, which is significantly greater than 0.05. Which says our model is not that good.

From the AUC(Area under the curve) values above of 'r AUC' is relatively high at .971.

Considering the higher p-value of Hoslem test is giving, there is issue with this model, this will not be the ideal candidate.

Step Model

4. For our final model, we will use the step function on the base model variables.

```
base_step_model = step(base_model)
```

```
## Start: AIC=214.15
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
##
       ptratio + black + lstat + medv
##
##
             Df Deviance
                            AIC
## - lstat
                  186.91 212.91
## - rm
                  187.03 213.03
## - chas
                  188.02 214.02
## <none>
                  186.15 214.15
                  188.52 214.52
## - indus
              1
## - zn
                  190.49 216.49
              1
## - tax
                  191.03 217.03
```

```
## - black 1 192.05 218.05
## - age 1 192.96 218.96
           1 195.29 221.29
## - medv
## - dis
            1 198.48 224.48
               198.76 224.76
## - ptratio 1
## - rad 1 223.66 249.66
## - nox
           1 257.46 283.46
##
## Step: AIC=212.91
## target ~ zn + indus + chas + nox + rm + age + dis + rad + tax +
     ptratio + black + medv
##
           Df Deviance AIC
##
           1 188.88 212.88
## - rm
                186.91 212.91
## <none>
## - indus
          1 189.14 213.14
         1 189.17 213.17
## - chas
## - zn
           1 190.90 214.90
## - tax
           1 191.41 215.41
## - black 1 192.77 216.77
## - medv 1 196.21 220.21
## - age
           1 197.65 221.65
## - dis
          1 199.62 223.62
## - ptratio 1 200.26 224.26
## - rad
        1 224.12 248.12
## - nox
            1 259.54 283.54
##
## Step: AIC=212.88
## target ~ zn + indus + chas + nox + age + dis + rad + tax + ptratio +
##
      black + medv
##
##
           Df Deviance
                         AIC
## <none>
               188.88 212.88
          1
## - indus
              190.94 212.94
            1 191.35 213.35
## - chas
## - zn
           1 193.34 215.34
## - tax
           1 193.67 215.67
## - black 1 194.32 216.32
## - age
            1
               197.65 219.65
## - dis
           1 200.09 222.09
## - ptratio 1
                200.29 222.29
## - medv
                201.97 223.97
            1
                225.37 247.37
## - rad
            1
## - nox
            1
                259.83 281.83
summary(base_step_model)
##
## Call:
## glm(formula = target ~ zn + indus + chas + nox + age + dis +
      rad + tax + ptratio + black + medv, family = "binomial",
##
      data = train)
## Deviance Residuals:
      Min
          1Q Median 3Q
                                       Max
```

```
## -2.4411 -0.1739 -0.0026 0.0030
                                      3.4506
##
## Coefficients:
               Estimate Std. Error z value Pr(>|z|)
##
## (Intercept) -36.364060 6.862463 -5.299 1.16e-07 ***
              -0.059091 0.032498 -1.818 0.069016 .
## zn
## indus
              -0.067194 0.048295 -1.391 0.164128
                          0.777917
                                    1.566 0.117418
## chas
               1.217987
## nox
              48.468529
                         7.790233 6.222 4.92e-10 ***
                         0.011164 2.863 0.004197 **
## age
              0.031961
## dis
               0.703484
                         0.220707
                                     3.187 0.001436 **
                                     3.963 7.41e-05 ***
               0.620491
                          0.156587
## rad
                         0.003012 -2.122 0.033812 *
## tax
               -0.006392
## ptratio
                         0.118437 3.258 0.001120 **
               0.385927
## black
               -0.012935
                          0.006940 -1.864 0.062342 .
## medv
                0.119666
                          0.035873
                                    3.336 0.000851 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## (Dispersion parameter for binomial family taken to be 1)
##
      Null deviance: 645.88 on 465 degrees of freedom
## Residual deviance: 188.88 on 454 degrees of freedom
## AIC: 212.88
##
## Number of Fisher Scoring iterations: 9
knitr::kable(vif(base step model))
```

| | х |
|--------------------------|----------|
| zn | 1.753036 |
| indus | 2.659125 |
| chas | 1.204903 |
| nox | 4.080484 |
| age | 1.708242 |
| dis | 3.614058 |
| rad | 1.806566 |
| tax | 2.090838 |
| ptratio | 1.902591 |
| black | 1.082317 |
| $\overline{\text{medv}}$ | 2.248962 |

```
hoslem.test(train$target, fitted(base_step_model))
```

```
##
## Hosmer and Lemeshow goodness of fit (GOF) test
##
## data: train$target, fitted(base_step_model)
## X-squared = 14.842, df = 8, p-value = 0.06228

rocBaseStepPlot = roc(base_step_model$y, fitted(base_step_model))
AUC = as.numeric(pROC::roc(base_step_model$y, fitted(base_step_model))$auc)
AUC
```

[1] 0.9746467

Observations

From the above model, we see one variable has been dropped out of 12. we see 2 out of the 12 variables has (stat-sig) p-values at a significance level greater than 0.05

From the VIF function we can see that the following variables has VIF > 4. nox.

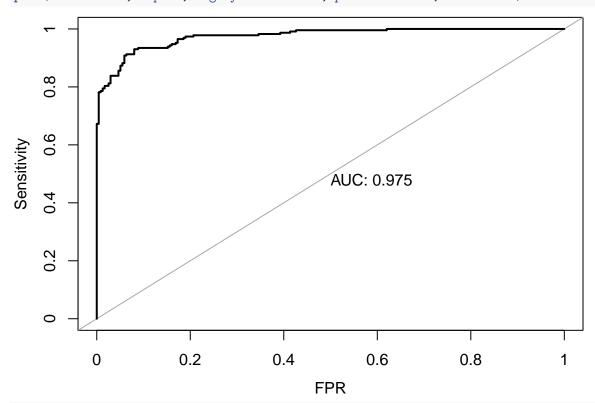
From the above Hoslem test we can see the value of p = 0.06228, which is little more than 0.05. Which says our model is pretty good.

From the AUC(Area under the curve) values above of 'r AUC' is relatively high at .974. This model is good at predicting the response variable.

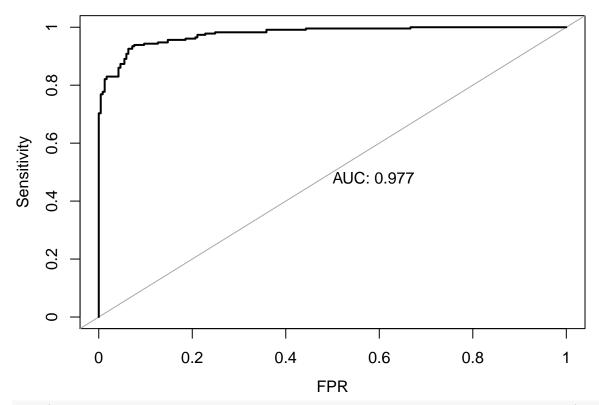
4. MODEL SELECTION:

From our 4 Model, we will first see the ROC and AUC curve.

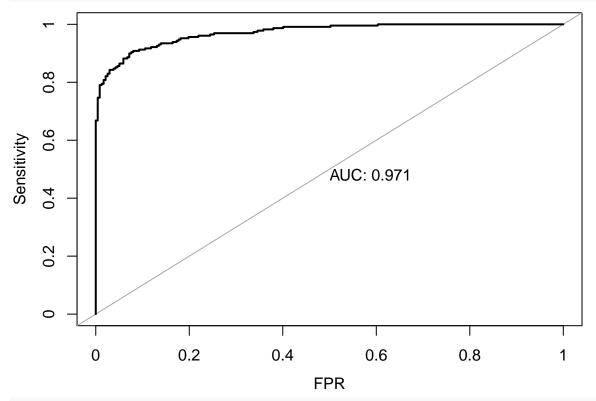
plot(rocBasePlot, asp=NA, legacy.axes = TRUE, print.auc=TRUE, xlab="FPR")



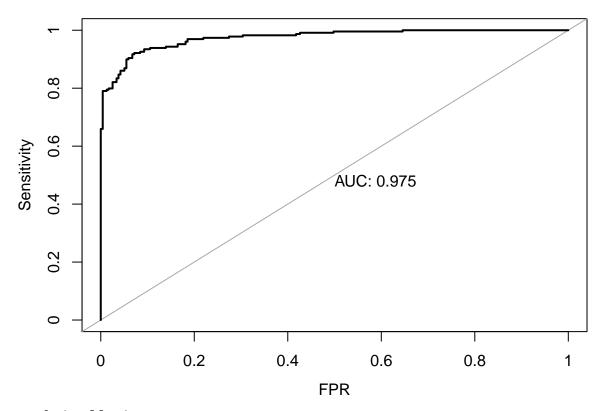
plot(rocBaseTransformPlot, asp=NA, legacy.axes = TRUE, print.auc=TRUE, xlab="FPR")



plot(rocBaseBackwardPlot, asp=NA, legacy.axes = TRUE, print.auc=TRUE, xlab="FPR")



plot(rocBaseStepPlot, asp=NA, legacy.axes = TRUE, print.auc=TRUE, xlab="FPR")



confusion Matrix.

```
# Confusion Matrix of Base Model
baseConfusion = as.factor(as.integer(fitted(base_model) > .5))
baseCM = confusionMatrix(baseConfusion, as.factor(base_model$y), positive = "1")
caretResults = data.frame(Accurarcy = baseCM$overall[['Accuracy']],
                           ClassErrorRate = 1 - baseCM$overall[['Accuracy']],
                           Precision = baseCM$byClass[['Precision']],
                           Senstivity = baseCM$byClass[['Sensitivity']],
                           Specificity = baseCM$byClass[['Specificity']],
                           F1 = baseCM$byClass[['F1']])
# Confusion Matrix of Base Transformation Model
baseTransformConfusion = as.factor(as.integer(fitted(base_transform_model ) > .5))
baseTransformCM = confusionMatrix(baseTransformConfusion, as.factor(base_transform_model$y), positive =
caretTransformResults = data.frame(Accurarcy = baseTransformCM$overall[['Accuracy']],
                           ClassErrorRate = 1 - baseTransformCM$overall[['Accuracy']],
                           Precision = baseTransformCM$byClass[['Precision']],
                           Senstivity = baseTransformCM$byClass[['Sensitivity']],
                           Specificity = baseTransformCM$byClass[['Specificity']],
                           F1 = baseTransformCM$byClass[['F1']])
# Confusion Matrix of Base Backward Elimination Model
baseBackwardConfusion = as.factor(as.integer(fitted(base_backward_model ) > .5))
baseBackwardCM = confusionMatrix(baseBackwardConfusion, as.factor(base_backward_model$y), positive
caretBackwardResults = data.frame(Accurarcy = baseBackwardCM$overall[['Accuracy']],
                           ClassErrorRate = 1 - baseBackwardCM$overall[['Accuracy']],
                           Precision = baseBackwardCM$byClass[['Precision']],
                           Senstivity = baseBackwardCM$byClass[['Sensitivity']],
                           Specificity = baseBackwardCM$byClass[['Specificity']],
                           F1 = baseBackwardCM$byClass[['F1']])
```

| Accurarcy | ${\bf ClassErrorRate}$ | Precision | Senstivity | Specificity | F1 |
|-----------|------------------------|-----------|------------|-------------|-----------|
| 0.9248927 | 0.0751073 | 0.9330357 | 0.9126638 | 0.9367089 | 0.9227373 |
| 0.9270386 | 0.0729614 | 0.9333333 | 0.9170306 | 0.9367089 | 0.9251101 |
| 0.9120172 | 0.0879828 | 0.9196429 | 0.8995633 | 0.9240506 | 0.9094923 |
| 0.9248927 | 0.0751073 | 0.9292035 | 0.9170306 | 0.9324895 | 0.9230769 |

After analyzing all our four models, we will be using the Base_Step_Model for our prediction.

Because of the Observations we discussed.

Evalution

Finally, when we apply the Step model to the evalution data, it predicts there are 21 obs below the median crime rate and 19 above the median crime rate.

```
eval_results = predict(base_step_model, newdata = test)
table(as.integer(eval_results > .5))

##
## 0 1
## 21 19
```