

ENDSEM

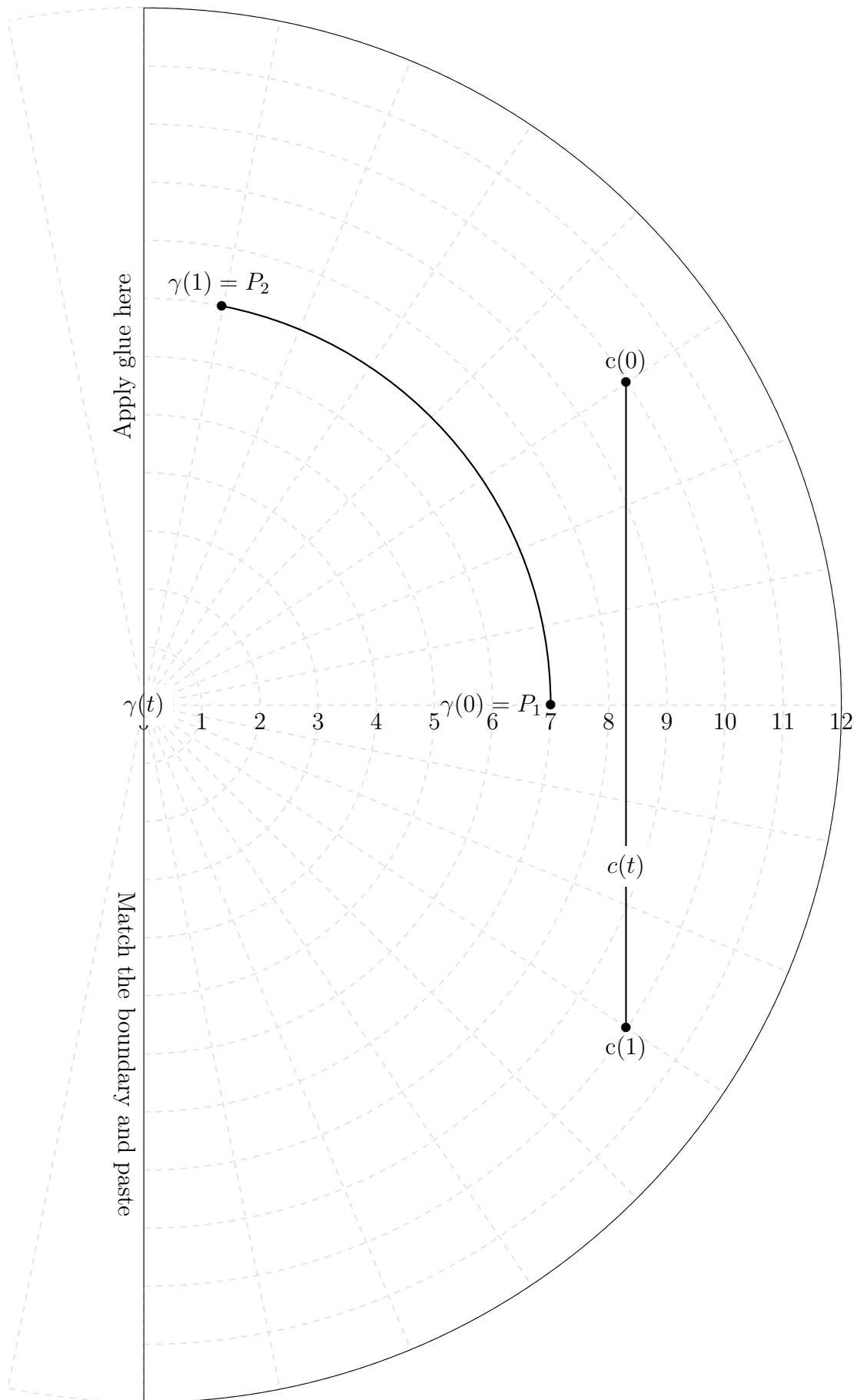
1. Have a careful look at paper model of a cone provided on the next page. Assume that the cone tip is origin in R^3 and the base rests on a plane parallel to $x - y$ plane. Give a C^3 parametrization¹ $S(u, v), (u, v) \in U \subset R^2$ of this cone, i.e. a function $S : U \rightarrow R^3$.
2. How do you describe curves γ and c on the surface of cone?²
3. With identified parametrization $S(u, v)$, calculate Riemannian metric g_{ij} , where $E = g_{11} = \langle S_u, S_u \rangle, G = g_{22} = \langle S_v, S_v \rangle, F = g_{12} = g_{21} = \langle S_u, S_v \rangle$ and S_u and S_v are partial derivatives $\frac{\partial S}{\partial u}$ and $\frac{\partial S}{\partial v}$ respectively.
4. What is the expression of length of a curve on cone?
5. Is γ a geodesic on S ? What is the length of γ ? Find out the geodesic and normal curvature at every point of $\gamma \subset S$.
6. Is c a geodesic on S ? What is the length of c ? Find out the geodesic and normal curvature at every point of c on cone.
7. Use Euler-Lagrange minimization to minimize length functional and find corresponding ODEs.
8. Use **bvp4c** and compute minimum length curve between P_1 and P_2 . What is the length of this curve? Is it same as γ ?

“The goal is to turn data into information, and information into insight.”

Carly Fiorina

¹Discount cone tip from the parametrization.

²For $\gamma : [0, 1] \rightarrow S$ and $c : [0, 1] \rightarrow S$, find $u^\gamma(t)$ and v^γ such that $\gamma(t) = S(u^\gamma(t), v^\gamma(t))$, similarly find $u^c(t)$ and $v^c(t)$ such that $c(t) = S(u^c(t), v^c(t))$.



Answers

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