Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randon

Reculte

What happens when labelling changes?

Future work

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Paulius Dilkas

School of Computing Science, University of Glasgow

16th January 2018

Algorithm selection

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Definition (Bischl et al. 2016)

Given a set \mathcal{I} of problem instances, a space of algorithms \mathcal{A} , and a performance measure $m \colon \mathcal{I} \times \mathcal{A} \to \mathbb{R}$, the algorithm selection problem is to find a mapping $s \colon \mathcal{I} \to \mathcal{A}$ that optimises $\mathbb{E}[m(i,s(i))]$.

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LLAMA (Kotthoff 2013)



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- McSplit, McSplit↓
 - (McCreesh, Prosser and Trimble 2017)
- clique encoding
 - (McCreesh, Ndiaye et al. 2016)
- k ↓
 - (Hoffmann, McCreesh and Reilly 2017)

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Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81400 pairs of graphs)

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Definition

A vertex-labelled graph is a 3-tuple $G=(V,E,\mu)$, where $\mu\colon V\to\{0,\dots,N-1\}$ is a vertex labelling function, for some $N\in\mathbb{N}$.

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$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left\lfloor \frac{p}{100\%} \times |V| \right\rfloor \right\}.$$

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- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average

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- 3 subproblems
 - no labels
 - vertex labels
 - vertex and edge labels

Features (34 in total)

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- 1–8 are from Kotthoff, McCreesh and Solnon 2016
 - number of vertices
 - number of edges
 - mean/max degree
 - density
 - mean/max distance between pairs of vertices
 - number of loops
 - \odot proportion of vertex pairs with distance ≥ 2 , 3, 4
 - connectedness

Features (34 in total)

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- ratios of features 1–5

Random forests (Breiman 2001)

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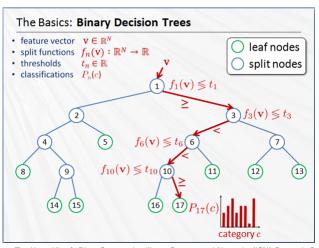
Feature

Random forests

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Future work



Source: Tae-Kyun Kim & Bjorn Stenger, Intelligent Systems and Networks (ISN) Research Group, Imperial College London

Random forests (Breiman 2001)

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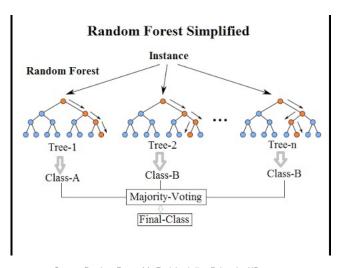
Random

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Source: Random Forests(r), Explained, Ilan Reinstein, KDnuggets

Results

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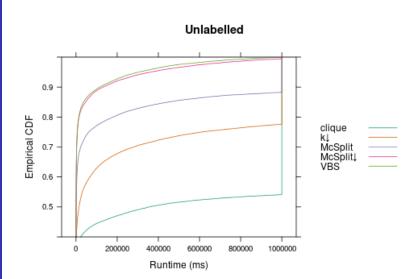
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What happens when labelling changes?



Results (27%)

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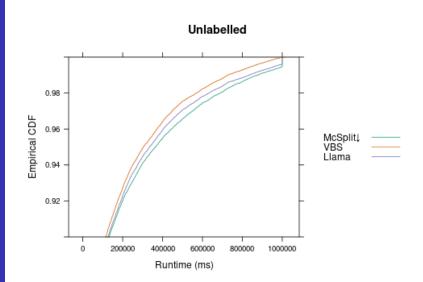
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Results

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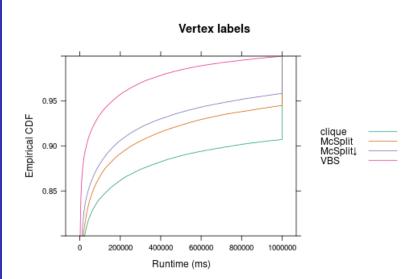
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Results (86%)

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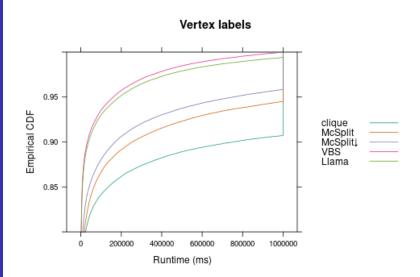
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Results

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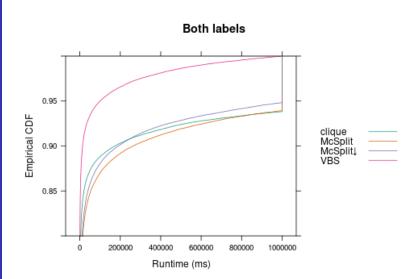
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Results (88%)

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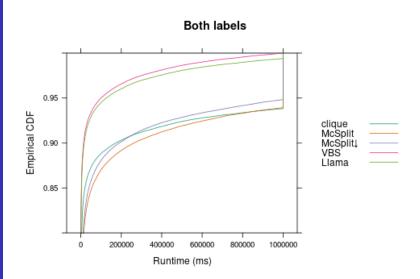
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Errors

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uture work

- Out-of-bag error
- For each algorithm
 - 1 − recall

Definition

For an algorithm A, recall (sensitivity) is

the number of instances that were correctly predicted as A the number of instances where A is the correct prediction

Errors (%)

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What happens when labelling changes?

Error	Labelling		
	no	vertex	both
out-of-bag	17	13	14
clique	30	8	7
McSplit	29	22	29
$McSplit \downarrow$	11	11	11
$k\downarrow$	80		

Convergence of errors for unlabelled graphs

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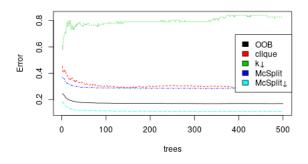
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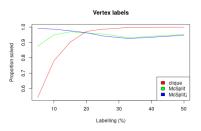
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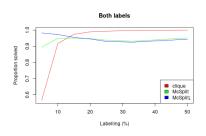
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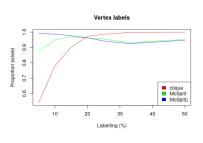
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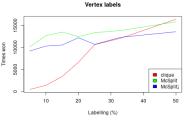
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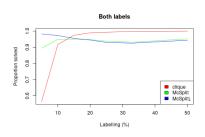
Randon forests

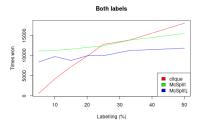
Results

What happens when labelling changes?









Future work

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What happens when labelling changes?

- Relationships between clique algorithm's performance and properties of the association graph
- How the association graph changes after making a decision
- Can $k \downarrow$ and clique work together?