Algorithm Selection for Maximum Common Subgraph

aulius Dilka

Algorithm selection

Algorithms

Labelling

Feature

Randon

Results

What happens when labelling changes?

Future work

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

FATA seminar

16th January 2018

Algorithm selection

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Definition (Bischl et al. 2016)

Given a set \mathcal{I} of problem instances, a space of algorithms \mathcal{A} , and a performance measure $m \colon \mathcal{I} \times \mathcal{A} \to \mathbb{R}$, the algorithm selection problem is to find a mapping $s \colon \mathcal{I} \to \mathcal{A}$ that optimises $\mathbb{E}[m(i,s(i))]$.

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LLAMA (Kotthoff 2013)



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- McSplit, McSplit↓
 - (McCreesh, Prosser and Trimble 2017)
- clique encoding
 - (McCreesh, Ndiaye et al. 2016)
- k ↓
 - (Hoffmann, McCreesh and Reilly 2017)

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Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81,400 pairs of graphs)

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Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81,400 pairs of graphs)

Definition

A vertex-labelled graph is a 3-tuple $G=(V,E,\mu)$, where $\mu\colon V\to\{0,\dots,N-1\}$ is a vertex labelling function, for some $N\in\{1,\dots,|V|\}.$

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$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left\lfloor \frac{p}{100\%} \times |V| \right\rfloor \right\}.$$

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Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left| \frac{p}{100\%} \times |V| \right| \right\}.$$

- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average

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- In my data: 5%, 10%, 15%, 20%, 25%, 33%, 50%

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- 3 subproblems
 - no labels
 - vertex labels
 - vertex and edge labels

Features (34 in total)

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The first 9 are from Kotthoff, McCreesh and Solnon 2016

- number of vertices
- number of edges
- mean/max degree
- density
- mean/max distance between pairs of vertices
- standard deviation of degrees
- number of loops
- **1** proportion of vertex pairs with distance ≥ 2 , 3, 4
- onnectedness
- labelling percentage
- ratios of features 1–5

Random forests

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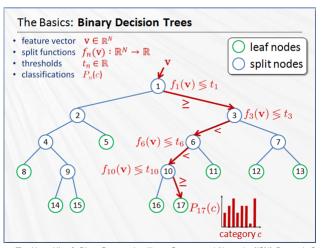
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Source: Tae-Kyun Kim & Bjorn Stenger, Intelligent Systems and Networks (ISN) Research Group, Imperial College London

Results

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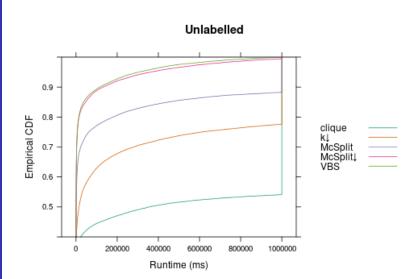
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Results (27%)

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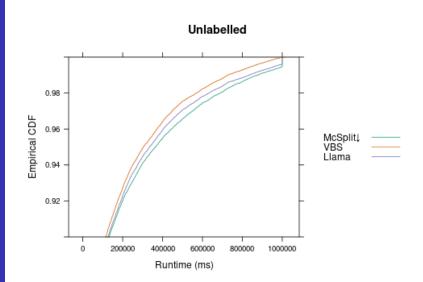
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forests

Results

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Results

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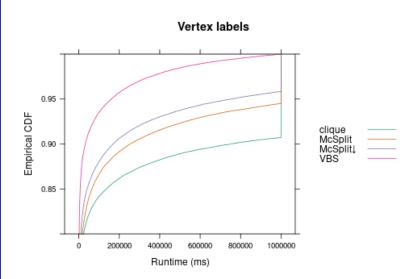
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Results (86%)

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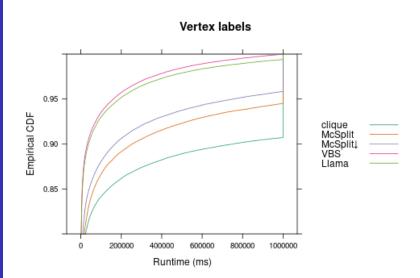
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Results

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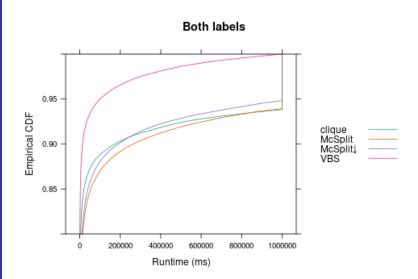
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Results (88%)

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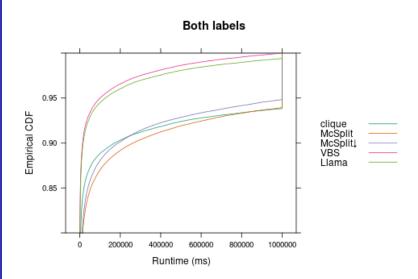
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Errors

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- Out-of-bag
- ullet (for each algorithm) 1- recall

Definition

For an algorithm A, recall is

the number of instances that were correctly predicted as A the number of instances where A is the correct prediction

Errors (%)

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Error	Labelling		
	no	vertex	both
out-of-bag	17	13	14
clique	30	8	7
McSplit	29	22	29
$McSplit \downarrow$	11	11	11
$k\downarrow$	80		

Convergence of errors for unlabelled graphs

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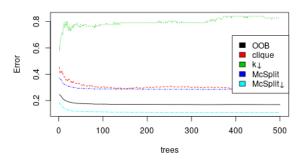
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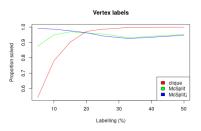
Algorithms

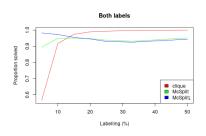
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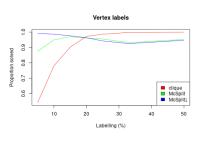
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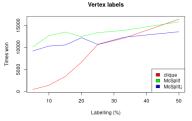
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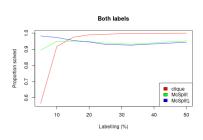
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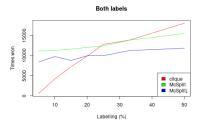
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Future work

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What happens when labelling changes?

- Relationships between clique algorithm's runtime and properties of the association graph
- How the association graph changes after making a decision
- Can $k \downarrow$ and clique work together?