Algorithm Selection for Maximum Common Subgraph

aulius Dilka

Algorithm selection

Algorithms

Labelling

Feature

Randon

Results

What happens when labelling changes?

Future work

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

FATA seminar

16th January 2018

Algorithm selection

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

.

Feature

Randon forests

Results

What happens when labelling changes?

Future work

Definition (Bischl et al. 2016)

Given a set \mathcal{I} of problem instances, a space of algorithms \mathcal{A} , and a performance measure $m \colon \mathcal{I} \times \mathcal{A} \to \mathbb{R}$, the algorithm selection problem is to find a mapping $s \colon \mathcal{I} \to \mathcal{A}$ that optimises $\mathbb{E}[m(i,s(i))]$.

Algorithm selection

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

eature

Randor

Reculto

What happens when labelling changes?

Future work

Definition (Bischl et al. 2016)

Given a set \mathcal{I} of problem instances, a space of algorithms \mathcal{A} , and a performance measure $m \colon \mathcal{I} \times \mathcal{A} \to \mathbb{R}$, the algorithm selection problem is to find a mapping $s \colon \mathcal{I} \to \mathcal{A}$ that optimises $\mathbb{E}[m(i,s(i))]$.

LLAMA (Kotthoff 2013)



Algorithms

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

Labelling

Feature

Randon forests

Results

What happens when labelling changes?

- McSplit, McSplit↓
 - (McCreesh, Prosser and Trimble 2017)
- clique encoding
 - (McCreesh, Ndiaye et al. 2016)
- k ↓
 - (Hoffmann, McCreesh and Reilly 2017)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

-...

Randon

Results

What happen when labelling changes?

Future work

Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81,400 pairs of graphs)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randor

Results

What happen when labelling changes?

Future work

Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81,400 pairs of graphs)

Definition

A vertex-labelled graph is a 3-tuple $G=(V,E,\mu)$, where $\mu\colon V\to\{0,\dots,N-1\}$ is a vertex labelling function, for some $N\in\{1,\dots,|V|\}.$

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithm

Labelling

Featur

Randon forests

Result

What happens when labelling changes?

uture work

Data from Foggia, Sansone and Vento 2001; Santo et al. 2003 (81,400 pairs of graphs)

Definition

A vertex-labelled graph is a 3-tuple $G=(V,E,\mu)$, where $\mu\colon V\to\{0,\dots,N-1\}$ is a vertex labelling function, for some $N\in\{1,\dots,|V|\}.$

Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left\lfloor \frac{p}{100\%} \times |V| \right\rfloor \right\}.$$

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randor forests

Results

What happen when labelling changes?

Future work

Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left| \frac{p}{100\%} \times |V| \right| \right\}.$$

- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randon forests

Results

What happens when labelling changes?

Future work

Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left| \frac{p}{100\%} \times |V| \right| \right\}.$$

- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average
- Typical values explored: 33%, 50%, 75%
 - Often just 33%

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randon forests

Results

What happens when labelling changes?

Future work

Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left| \frac{p}{100\%} \times |V| \right| \right\}.$$

- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average
- Typical values explored: 33%, 50%, 75%
 - Often just 33%
- In my data: 5%, 10%, 15%, 20%, 25%, 33%, 50%

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithm selection

Algorithms

Labelling

Feature

Randon forests

Results

What happens when labelling changes?

Future work

Definition

$$N = \max \left\{ 2^n : n \in \mathbb{N}, \, 2^n < \left| \frac{p}{100\%} \times |V| \right| \right\}.$$

- 5% labelling 20 vertices per label on average
- 50% labelling 2 vertices per label on average
- Typical values explored: 33%, 50%, 75%
 - Often just 33%
- In my data: 5%, 10%, 15%, 20%, 25%, 33%, 50%
- 3 subproblems
 - no labels
 - vertex labels
 - vertex and edge labels

Features (34 in total)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilkas

Algorithn selection

Algorithms

Labelling

Features

Randon forests

Result

What happens when labelling changes?

Future work

The first 9 are from Kotthoff, McCreesh and Solnon 2016

- number of vertices
- number of edges
- mean/max degree
- density
- mean/max distance between pairs of vertices
- standard deviation of degrees
- number of loops
- **1** proportion of vertex pairs with distance ≥ 2 , 3, 4
- onnectedness
- labelling percentage
- ratios of features 1–5

Random forests

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

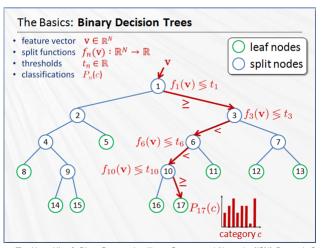
Eastura

Random forests

Results

What happens when labelling changes?

⁼uture work



Source: Tae-Kyun Kim & Bjorn Stenger, Intelligent Systems and Networks (ISN) Research Group, Imperial College London

Results

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka:

Algorithm selection

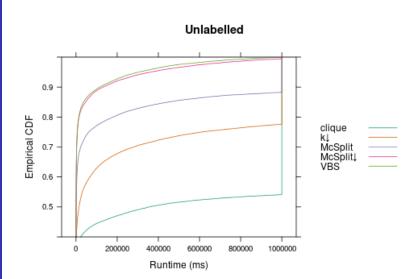
Algorithms

Ecoture

Randor forests

Results

What happens when labelling changes?



Results (27%)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

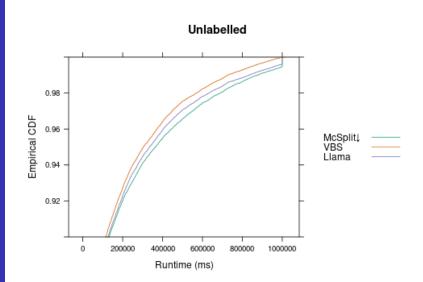
E .

D. . . J. .

forests

Results

What happens when labelling changes?



Results

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

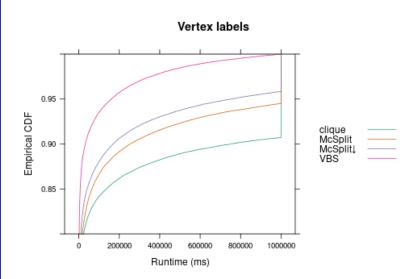
- .

Randor

forests

Results

What happens when labelling changes?



Results (86%)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

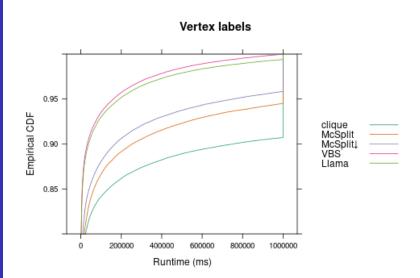
E .

Dandas

forests

Results

What happens when labelling changes?



Results

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

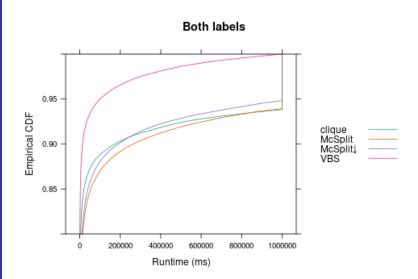
Algorithms

- .

Randor forests

Results

What happens when labelling changes?



Results (88%)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

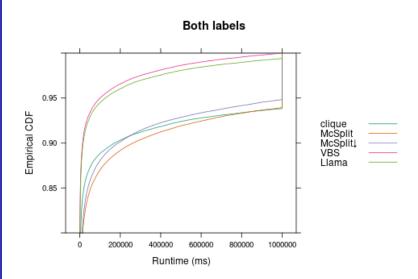
- .

.

Randor forests

Results

What happens when labelling changes?



Errors

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

Labelling

Feature

Randon

Results

What happens when labelling changes?

uture work

- Out-of-bag
- ullet (for each algorithm) 1- recall

Definition

For an algorithm A, recall is

the number of instances that were correctly predicted as A the number of instances where A is the correct prediction

Errors (%)

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

Feature

Randor

Results

What happens when labelling changes?

Error	Labelling		
	no	vertex	both
out-of-bag	17	13	14
clique	30	8	7
McSplit	29	22	29
$McSplit \downarrow$	11	11	11
$k\downarrow$	80		

Convergence of errors for unlabelled graphs

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka:

Algorithm selection

Algorithms

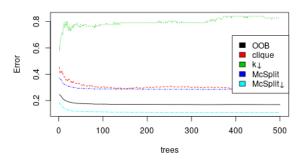
Footure

D . . . I . ..

forests

Results

What happens when labelling changes?



What happens when labelling changes?

Algorithm Selection for Maximum Common Subgraph

aulius Dilka

Algorithm selection

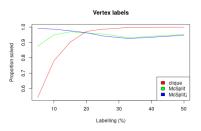
Algorithms

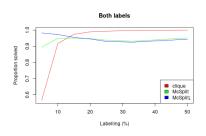
- .

Randor forests

Reculto

What happens when labelling changes?





What happens when labelling changes?

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

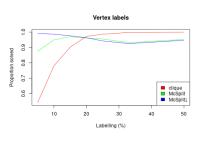
Labelling

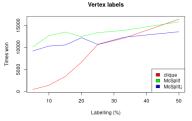
Feature

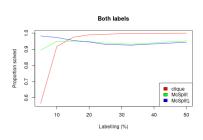
Randon forests

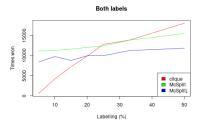
Results

What happens when labelling changes?









Future work

Algorithm Selection for Maximum Common Subgraph

Paulius Dilka

Algorithm selection

Algorithms

Labelling

Feature

Random forests

Results

What happens when labelling changes?

- Can $k \downarrow$ be made competitive for vertex labels?
- Relationships between clique algorithm's runtime and properties of the association graph
- How the association graph changes after making a decision
- Merging $k \downarrow$ and clique