Generating Random Logic Programs Using Constraint Programming

Paulius Dilkas

AIAI Seminar





Anytime Inference in Probabilistic Logic Programs with T_p -Compilation

Jonas Vlasselaer, Guy Van den Broeck, Ange ka Kimmig, Wannes Meert, Luc De Raedt Department of the Imputer Science

firstname.lastname@cs.kuleuven.be

Anytime Inference in Probabilistic Logic Programs with T_p -Compilation

Jonas Vlasselaer, Guy Van den Broeck, Angelka Kimmig, Wannes Meert, Luc De Raedt firstname.lastname@cs.kuleuven.be

Inference and learning in probabilistic logic programs using weighted Boolean formulas

DAAN FIERENS, GUY VAN DEN BROECK, JORIS RENKENS, DIMITAR SHTERIONOV, BENED GUTMANN, INGO THON, GERDA JANSSENS and LUC DE RAEDT

Department of Computer Science, KU Leuven, Celestiinenlaan 200A, 3001 Heverlee, Belgium (c-mail: FirstName.LastName@cs.kuleuven.be)

Anytime Inference in Probabilistic Logic Programs with T_p -Compilation

Jonas Vlasselaer, Guy Van den Broeck, Aye ka Kimmig, Wannes Meert, Luc De Raedt Department of each uputer Science KU Leuven, Belgium firstname.lastname@es.kuleuven.be

Inference and learning in probabilistic logic programs using weighted Boolean formulas

DAAN FIERENS, GUY VAN DEN BROECK, JORIS RENKENS, DIMITAR SHTERIONOV, BENND GUTMANN, INGO THON, GERDA JANSSENS and LUC DE RAEDT

Department of Computer Science, KU Lewen, Celestijnenlaan 200A, 3001 Heverlee, Belgium (e-mail: FirstName.LastName@cs.kuleuven.be)

k-Optimal: a novel approximate inference algorithm for ProbLog

Joris Renkens · Guy Van den Broeck · Siegfried Nijssen

Anytime Inference in Probabilistic Logic Programs with T_p -Compilation

Jonas Vlasselaer, Guy Van den Broeck, Angelka Kimmig, Wannes Meert, Luc De Raedt firstname.lastname@cs.kuleuven.be

Inference and learning in probabilistic logic programs using weighted Boolean formulas

DAAN FIERENS, GUY VAN DEN BROECK, JORIS RENKENS, DIMITAR SHTERIONOV, BENED GUTMANN, INGO THON, GERDA JANSSENS and LUC DE RAEDT

Department of Computer Science, KU Leuven, Celestiinenlaan 200A, 3001 Heverlee, Belgium (c-mail: FirstName.LastName@cs.kuleuven.be)

k-Optimal: a novel approximate inference algorithm for ProbLog

Joris Renkens · Guy Van den Broeck · Siegfried Nijssen

On the Efficient Execution of ProbLog Programs

Angelika Kimmig¹, Vítor Santos Cost², Ricardo Rocha², Bart Demoen¹, and Luc De Raedt¹

Anytime Inference in Probabilistic Logic Programs with To-Compilation

Jonas Vlasselaer, Guy Van den Broeck, Ange ka Kimmig, Wannes Meert, Luc De Raedt Department of en apputer Science KU Leuven, Belgium firstname.lastname@cs.kuleuven.be

Inference and learning in probabilistic logic programs using weighted Boolean formulas

DAAN FIERENS, GUY VAN DEN BROECK, JORIS RENKENS, DIMITAR SHTERIONOV, BENED GUTMANN, INGO THON, GERDA JANSSENS and LUC DE RAEDT

Department of Computer Science, KU Leuven, Celestiinenlaan 200A, 3001 Heverlee, Belgium (e-mail: FirstName.LastName@cs.kuleuven.be)

k-Optimal: a novel approximate inference algorithm for ProbLog

Joris Renkens · Guy Van den Broeck · Siegfried Nijssen

On the Efficient Execution of ProbLog Programs

Angelika Kimmig¹, Vítor Santos Cost ², Ricardo Rocha², Bart Demoen¹, and Luc De Raedt¹

On the Implementation of the Probabilistic Logic Programming Language ProbLog

Angelika Kimmig, Bart Demoen and Luc De Raedt Departement Computerwe inschappen, K.U. Leuven Celestijnenlaan 200A - bus 24 2, B-3001 Heverlee, Belgium (e-mail: {Angelika.Kimmig,Bart.Deceap,Luc.DeRaedt}@cs.kuleuven.be)

Vítor Santos Costa and Ricardo Rocha

CRACS & INESC-Porto LA, Faculty of Sciences, University of Porto R. do Campo Alegre 1021/1055, 4169-007 Porto, Portugal (e-mail: {vsc,ricroc}@dcc.fc.up.pt)

Anytime Inference in Probabilistic Logic Programs with To-Compilation

Jonas Vlasselaer, Guy Van den Broeck, Ange ka Kimmig, Wannes Meert, Luc De Raedt Department of en apputer Science KU Leuven, Belgium firstname.lastname@cs.kuleuven.be

Inference and learning in probabilistic logic programs using weighted Boolean formulas

DAAN FIERENS, GUY VAN DEN BROECK, JORIS RENKENS, DIMITAR SHTERIONOV, BENED GUTMANN, INGO THON, GERDA JANSSENS and LUC DE RAEDT

Department of Computer Science, KU Leuven, Celestiinenlaan 200A, 3001 Heverlee, Belgium (e-mail: FirstName.LastName@cs.kuleuven.be)

k-Optimal: a novel approximate inference algorithm for ProbLog

Joris Renkens · Guy Van den Broeck · Siegfried Nijssen

On the Efficient Execution of ProbLog Programs

Angelika Kimmig¹, Vítor Santos Cost², Ricardo Rocha², Bart Demoen¹, and Luc De Raedt¹

On the Implementation of the Probabilistic Logic Programming Language ProbLog

Angelika Kimmig, Bart Demoen and Luc De Raedt Departement Computerwe inschappen, K.U. Leuven Celestijnenlaan 200A - bus 24 2, B-3001 Heverlee, Belgium (e-mail: {Angelika.Kimmig,Bart.Deceap,Luc.DeRaedt}@cs.kuleuven.be)

Vítor Santos Costa and Ricardo Rocha

CRACS & INESC-Porto LA, Faculty of Sciences, University of Porto R. do Campo Alegre 1021/1055, 4169-007 Porto, Portugal (e-mail: {vsc,ricroc}@dcc.fc.up.pt)

ProbLog Technology for Inference in a Probabilistic First Order Logic

Maurice Bruvnooghe and Theofrastos Mantalelia and Angelika Kimmig and Bernd Gutmann and Joost Vennekens and Gerda Janssens and Luc De Raedt1

Outline

Probabilistic Logic Programming

The Constraint Model

Experimental Results

Summary

Probabilistic Logic Programs (PROBLOG)

"Smokers" (Domingos et al. 2008; Fierens et al. 2015)

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P):-cancer_spont(P).
    cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

Applications



Probabilistic Logic Programming

000000



Moldovan et al. 2012

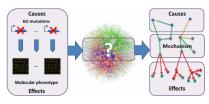
```
is_malignant(Case):-
        biopsyProcedure(Case,usCore),
        changes_Sizeinc(Case.missing).
        feature_shape(Case).
is malignant(Case):-
        assoFinding(Case, asymmetry),
        breastDensity(Case.scatteredFDensities).
        vacuumAssisted(Case, yes).
is_malignant(Case):-
        needleGauge(Case.9).
        offset(Case, 14),
        vacuumAssisted(Case, yes).
```

Côrte-Real, Dutra, and Rocha 2017

Q1: In a group of 10 people, 60 percent have brown eyes. Two people are to be selected at random from the group. What is the probability that neither person selected will have brown eves?

Q2: Mike has a bag of marbles with 4 white, 8 blue, and 6 red marbles. He pulls out one marble from the bag and it is red. What is the probability that the second marble he pulls out of the bag is white?

Dries et al. 2017



De Maeyer et al. 2013

000000

```
Let a \oplus b := a + b - ab. Then
Pr[cancer(michelle)] = Pr[cancer_spont(michelle)]
                     ⊕ Pr[smokes(michelle)]
                     × Pr[cancer_smoke(michelle)]
```

```
cancer(P):-cancer\_spont(P).
cancer(P):-smokes(P), cancer_smoke(P).
```

Probabilistic Logic Programming

000000

Let
$$a \oplus b := a + b - ab$$
. Then $Pr[cancer(michelle)] = 0.1 \oplus 0.3 \times Pr[smokes(michelle)]$

```
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
```

```
Let a \oplus b := a + b - ab. Then
Pr[cancer(michelle)] = 0.1 \oplus 0.3 \times Pr[smokes(michelle)]
Pr[smokes(michelle)] = Pr[stress(michelle)]
                       \oplus \Pr[smokes(timothy)]
                       × Pr[influences(timothy, michelle)]
```

```
smokes(X):-stress(X).
smokes(X):-smokes(Y), influences(Y, X).
```

```
Let a \oplus b := a + b - ab. Then
Pr[cancer(michelle)] = 0.1 \oplus 0.3 \times Pr[smokes(michelle)]
Pr[smokes(michelle)] = 0.2 \oplus 0.3 \times Pr[smokes(timothy)]
```

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
```

```
Let a \oplus b := a + b - ab. Then Pr[cancer(michelle)] = 0.1 \oplus 0.3 \times Pr[smokes(michelle)] Pr[smokes(michelle)] = 0.2 \oplus 0.3 \times Pr[smokes(timothy)] Pr[smokes(timothy)] = Pr[stress(timothy)] = 0.2
```

```
0.2::stress(P):-person(P).
smokes(X):-stress(X).
```

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P):-cancer_spont(P).
    cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

```
cancer(michelle) = T
     Pr(world) = 0.2 \times (1 - 0.3) \times 0.1 \times 0.3
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):=friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
     smokes(X):-stress(X).
     smokes(X):-smokes(Y), influences(Y, X).
     cancer(P): - cancer\_spont(P).
     cancer(P): - smokes(P), cancer\_smoke(P).
     person(michelle).
     person(timothy).
     friend(timothy, michelle).
```

000000

```
cancer(michelle) = T
     Pr(world) = 0.2 \times 0.3 \times 0.1 \times (1 - 0.3)
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
     smokes(X):-stress(X).
     smokes(X):-smokes(Y), influences(Y, X).
     cancer(P): - cancer\_spont(P).
     cancer(P):=smokes(P), cancer\_smoke(P).
     person(michelle).
     person(timothy).
     friend(timothy, michelle).
```

```
cancer(michelle) = \top
  Pr(world) = (1 - 0.2) \times (1 - 0.3) \times 0.1 \times 0.3
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
     smokes(X):-stress(X).
     smokes(X):-smokes(Y), influences(Y, X).
     cancer(P):-cancer\_spont(P).
     cancer(P):=smokes(P), cancer\_smoke(P).
     person(michelle).
     person(timothy).
     friend(timothy, michelle).
```

```
cancer(michelle) = \bot
Pr(world) = (1 - 0.2) \times (1 - 0.3) \times (1 - 0.1) \times (1 - 0.3)
   0.2::stress(P):-person(P).
   0.3::influences(P_1, P_2):-friend(P_1, P_2).
   0.1::cancer_spont(P):-person(P).
   0.3::cancer_smoke(P):-person(P).
        smokes(X):-stress(X).
        smokes(X):-smokes(Y), influences(Y, X).
        cancer(P):-cancer_spont(P).
        cancer(P):=smokes(P), cancer\_smoke(P).
        person(michelle).
        person(timothy).
        friend(timothy, michelle).
```

NNF negation normal form

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$\begin{array}{c} XX & (A \lor C) \land (A \lor \neg B) \\ C \land (A \lor \neg B) \end{array}$$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$

 $(A \lor C) \land (A \lor \neg B)$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$
 $(A \lor A) \land (A \lor \neg B)$

```
NNF negation normal form
```

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$

 $(A \lor \neg B)$
 $(A \lor \neg B)$
 $(A \lor \neg B)$
 $(A \lor \neg B)$
 $(A \lor \neg B)$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$\begin{array}{c} XX & (A \lor C) \land (A \lor \neg B) \\ X\checkmark & C \land (A \lor \neg B) \end{array}$$

```
NNF negation normal form
```

Probabilistic Logic Programming

000000

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$\begin{array}{c} XX & (A \lor C) \land (A \lor \neg B) \\ X \checkmark & C \land (A \lor \neg B) \end{array}$$

- NNF negation normal form
- BDD binary decision diagrams
- SDD sentential decision diagrams
- k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$XX (A \lor C) \land (A \lor \neg B)$$

$$X \sim C \wedge (A \vee \neg B)$$

$$\checkmark \times B \land C \land [(B \land A) \lor \neg B]$$

 $C \land [(B \land A) \lor \neg B]$

```
NNF negation normal form
```

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$(A \lor C) \land (A \lor \neg B)$$
 $(A \lor C) \land (A \lor \neg B)$

$$\checkmark \times B \land C \land [(B \land A) \lor \neg B]$$

$$\checkmark \quad C \land [(B \land A) \lor \neg B]$$

```
NNF negation normal form
```

BDD binary decision diagrams

SDD sentential decision diagrams

k-Best only use the k most probable proofs

- for every pair $\alpha \vee \beta$, we have $\alpha \wedge \beta = \bot$
- for every pair $\alpha \wedge \beta$, no atoms are shared between α and β
- examples:

$$XX (A \lor C) \land (A \lor \neg B)$$

 $X \checkmark C \land (A \lor \neg B)$
 $\checkmark X B \land C \land [(B \land A) \lor \neg B]$
 $\checkmark \checkmark C \land [(B \land A) \lor \neg B]$

Example Diagrams for $C \wedge (A \vee \neg B)$

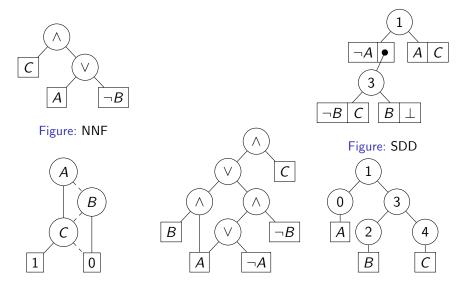


Figure: BDD

Probabilistic Logic Programming

000000

Figure: d-DNNF

Figure: vtree

•000000

```
0.2::stress(P):-person(P).
0.3: influences(P_1, P_2): -friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
    smokes(X) : - stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P):-cancer_spont(P).
    cancer(P) : -smokes(P), cancer_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

The Constraint Model

```
0.2:stress(P):-person(P).
0.3: :influences(P_1, P_2): -friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer\_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
     cancer(P): - cancer\_spont(P).
     cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

predicates, arities

The Constraint Model

```
0.2::stress(P):-person(P).
0.3: influences(P_1, P_2): -friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer\_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P):-cancer_spont(P).
    cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

- predicates, arities
- variables

The Constraint Model

```
0.2::stress(P):-person(P).
0.3: influences(P_1, P_2): -friend(P_1, P_2).
0.1::cancer\_spont(P):-person(P).
0.3::cancer\_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P):-cancer_spont(P).
    cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

- predicates, arities
- variables
- constants

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
    smokes(X):-stress(X).
    smokes(X):-smokes(Y), influences(Y, X).
    cancer(P): - cancer\_spont(P).
    cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
    friend(timothy, michelle).
```

- predicates, arities
- variables
- constants
- probabilities

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
     smokes(X):-stress(X).
     smokes(X):-smokes(Y), influences(Y, X).
     cancer(P): - cancer\_spont(P).
     cancer(P): - smokes(P), cancer\_smoke(P).
    person(michelle).
    person(timothy).
     friend(timothy, michelle).
```

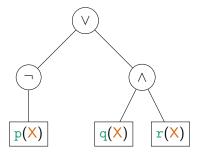
- predicates, arities
- variables
- constants
- probabilities
- length

```
0.2::stress(P):-person(P).
0.3::influences(P_1, P_2):-friend(P_1, P_2).
0.1::cancer_spont(P):-person(P).
0.3::cancer_smoke(P):-person(P).
     smokes(X):-stress(X).
     smokes(X):-smokes(Y), influences(Y, X).
     cancer(P): - cancer\_spont(P).
     cancer(P) := smokes(P), cancer_smoke(P).
    person(michelle).
    person(timothy).
     friend(timothy, michelle).
```

- predicates, arities
- variables
- constants
- probabilities
- length
- complexity

$$\neg p(X) \lor (q(X) \land r(X))$$

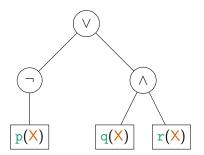
$$\neg p(X) \lor (q(X) \land r(X))$$



 $\neg p(X) \lor (q(X) \land r(X))$

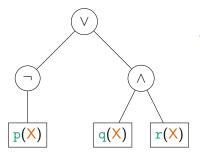
S: ۷:

0	0	0	1	2	2	6
\vee	_	\wedge	p(X)	q(X)	r(X)	T



$$\neg p(X) \lor (q(X) \land r(X))$$

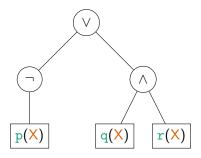
0 0 6 S: q(X)r(X)



• s is a forest with T=2 trees

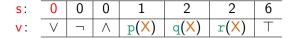
 $\neg p(X) \lor (q(X) \land r(X))$

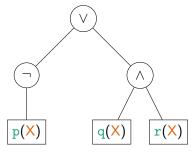
0 0 6 S: q(X)r(X)



• s is a forest with T=2 trees

$$\neg p(X) \lor (q(X) \land r(X))$$

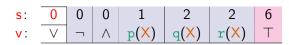


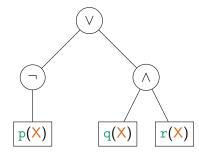


• s is a forest with T=2 trees

- s is sorted
- $s_i \neq i \implies v_i \neq \top$

$$\neg p(X) \lor (q(X) \land r(X))$$

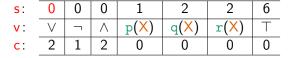


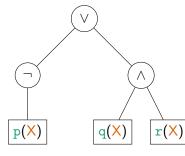


- s is a forest with T=2 trees
- length <u>L</u> = 7
- number of nodes N := L T + 1 = 6
- for i = 1, ..., L 1,
 - if i < N, then $s_i < i$
 - else $s_i = i$ and $v_i = T$

- s is sorted
- $s_i \neq i \implies v_i \neq \top$

$$\neg p(\mathsf{X}) \vee (q(\mathsf{X}) \wedge r(\mathsf{X}))$$





- s is a forest with T = 2 trees
- length L = 7
- number of nodes N := L T + 1 = 6
- for i = 1, ..., L 1,
 - if i < N, then $s_i < i$
 - else $s_i = i$ and $v_i = T$
- $c_i = 0 \iff v_i = T$ or is a predicate
- $c_i = 1 \iff v_i = \neg$
- $c_i > 1 \iff v_i \in \{\land, \lor\}$

- s is sorted
- $s_i \neq i \implies v_i \neq \top$

```
The Problem
Let \{W, X, Y\} be the set of variables. Then
          smokes(X):-smokes(Y), influences(Y, X)
is equivalent to
          smokes(Y):-smokes(X), influences(X, Y)
and to
         smokes(W):-smokes(X), influences(X, W)
```



Occurrences (channeling)

 $\mathsf{W}\mapsto\emptyset$ $X \mapsto \{0,3\}$

 $Y \mapsto \{1,2\}$

Introductions

 $1 + \min occurrences(v)$ or 0

 $W \mapsto 0$

 $\mathsf{X}\mapsto 1$

 $Y \mapsto 2$

sorted!



Occurrences (channeling)

 $\mathsf{W}\mapsto\emptyset$ $X \mapsto \{1,2\}$ $Y \mapsto \{0,3\}$

Introductions

 $1 + \min occurrences(v) \text{ or } 0$

 $\mathsf{W}\mapsto \mathsf{0}$

 $X \mapsto 2$

 $Y \mapsto 1$

not sorted!



Occurrences (channeling)

 $W \mapsto \{0,3\}$ $X \mapsto \{1,2\}$

 $Y \mapsto \emptyset$

Introductions

 $1 + \min occurrences(v) \text{ or } 0$

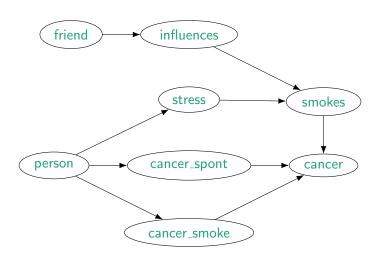
 $\mathsf{W}\mapsto 1$

 $X \mapsto 2$

 $Y \mapsto 0$

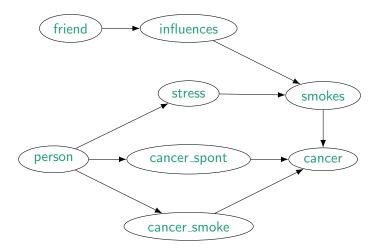
not sorted!

Predicate Dependency Graph



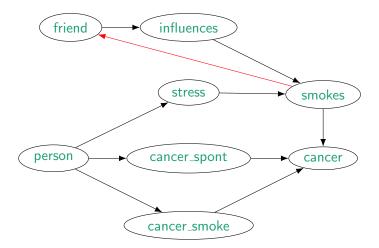
Stratification and Negative Cycles

0.1::friend(X, Y):-\+smokes(Y).



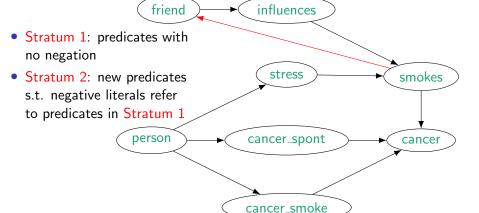
Stratification and Negative Cycles

0.1::friend(X, Y):-\+smokes(Y).

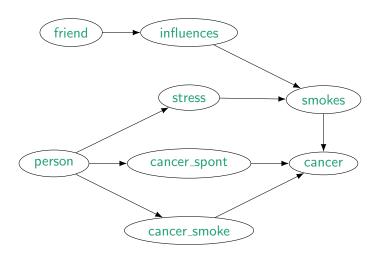


Stratification and Negative Cycles

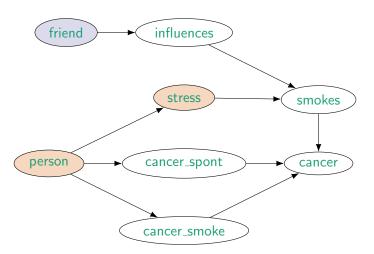




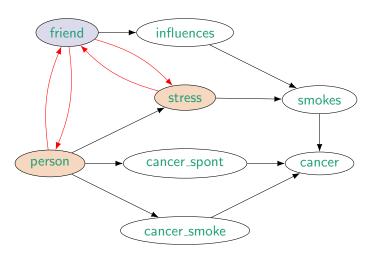
Independence: friend ⊥ stress



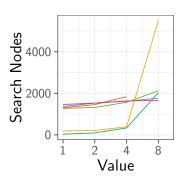
Independence: friend ⊥ stress



Independence: friend ⊥ stress



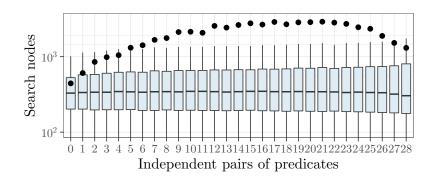
Scalability



Variable

- The number of predicates
- Maximum arity
- The number of variables
- The number of constants
- The number of additional clauses
- The maximum number of nodes

How Predicate Independence Affects Search Complexity



What Programs Should We Generate?

- each program is divided into:
 - rules
 - e.g., 0.2::stress(P):-person(P).
 - facts
 - e.g., friend(timothy, michelle).
- predicates, variables, nodes: 2, 4, 8
- maximum arity: 1, 2, 3
- all possible numbers of pairs of independent predicates
- 10 programs per configuration
 - fully restarting the constraint solver
- probabilities sampled from $\{0.1, 0.2, \dots, 0.9\}$
- query: random unlisted fact

Rules

```
0.2::stress(P):-person(P).
```

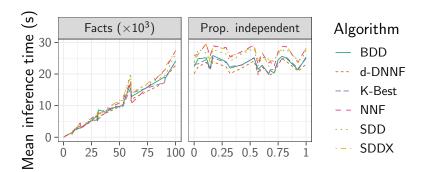
- no constants, no empty bodies
- one rule per predicate
- all rules are probabilistic

Facts

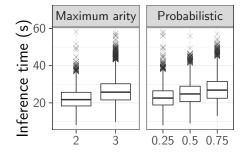
friend(timothy, michelle).

- proportion probabilistic: 25%, 50%, 75%
- constants: 100, 200, 400
- number of facts: 10³, 10⁴, 10⁵
 - but only up to 75% of all possible facts

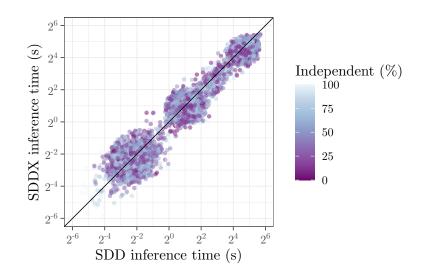
Properties of Programs vs. Inference Algorithms



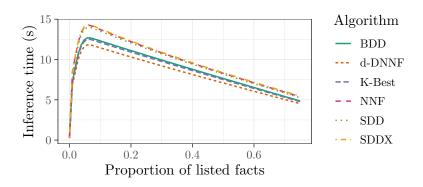
Properties of Programs vs. Inference Algorithms



How Encodings Compare Across Instances



The Ratio of Listed Facts to Possible Facts



Summary

- foo
- bar
- baz

The implementation of the model is available at https://github.com/dilkas/random-logic-programs

Adjacency matrix representation

 $A[i][j] = 0 \iff \nexists k : clauseAssignments[k] = j \text{ and } i \in clauses[k].treeValues}$

New constraints

- No (negative) cycles
 - No clever propagation, just entailment checking.
- Independence. Propagation:
 - Two types of dependencies: determined and one-undetermined-edge-away-from-being-determined.
 - Look up the dependencies of both predicates. For each pair of matching dependencies:
 - If both are determined, fail.
 - If one is determined, the selected edge of the other must not exist.