RAJALAKSHMI ENGINEERING COLLEGE

RAJALAKSHMI NAGAR, THANDALAM – 602 105

RAJALAKSHMI
ENGINEERING COLLEGE

FUNDAMENTALS OF MACHINE LEARNING

LABORATORY OBSERVATION NOTEBOOK

2nd Year/ AIML / A

2024- 2025 3rd Semester 231501041

Dilshad

Name : . . . . . .

Year / Branch / Section : . . . . . .

Register No. : . . . . . .

Semester : . . . . . .

Academic Year : . . . . . .

S.No.	Date	Title	Page No.	Teacher's Signature / Remarks
1.	/ /24	A PYTHON PROGRAM TO IMPLEMENT UNIVARIATE, BIVARIATE AND MULTIVARIATE REGRESSION		
2.	/ /24	A PYTHON PROGRAM TO IMPLEMENT SIMPLE LINEAR REGRESSION USING LEAST SQUARE METHOD		
3.	/ /24	A PYTHON PROGRAM TO IMPLEMENT LOGISTIC MODEL		
4.	/ /24	A PYTHON PROGRAM TO IMPLEMENT SINGLE LAYER PERCEPTRON		
5.	/ /24	A PYTHON PROGRAM TO IMPLEMENT MULTI LAYER PERCEPTRON WITH BACK PROPOGATION		
6.	/ /24	A PYTHON PROGRAM TO IMPLEMENT SVM CLASSIFIER MODEL		
7.	/ /24	A PYTHON PROGRAM TO IMPLEMENT DECISION TREE		
8.	/ /24	A PYTHON PROGRAM TO IMPLEMENT ADA BOOSTING		
9.	/ /24	A PYTHON PROGRAM TO IMPLEMENT KNN MODEL		
10.	/ /24	A PYTHON PROGRAM TO IMPLEMENT DIMENSIONALITY REDUCTION USING PCA		

Ex No: 1
Date:

A PYTHON PROGRAM TO IMPLEMENT UNIVARIATE, BIVARIATE AND MULTIVARIATE REGRESION

Aim:

To implement a python program using univariate, bivariate and multivariate regression features for a given iris dataset.

Algorithm:

Step 1: Import necessary libraries:

- pandas for data manipulation, numpy for numerical operations, and matplotlib.pyplot for plotting.

Step 2: Read the dataset:

- Use the pandas `read_csv` function to read the dataset.
- Store the dataset in a variable (e.g., `data`).

Step 3: Prepare the data:

- Extract the independent variable(s) (X) and dependent variable (y) from the dataset.
- Reshape X and y to be 2D arrays if needed.

Step 4:Univariate Regression:

- For univariate regression, use only one independent variable.
- Fit a linear regression model to the data using numpy's polyfit function or sklearn's LinearRegression class.
- Make predictions using the model.
- Calculate the R- squared value to evaluate the model's performance.

Step 5: Bivariate Regression:

- For bivariate regression, use two independent variables.
- Fit a linear regression model to the data using numpy's

`polyfit` function or sklearn’ s `LinearRegression` class.

- Make predictions using the model.
- Calculate the R- squared value to evaluate the model’ s performance.

Step 6: Multivariate Regression:

- For multivariate regression, use more than two independent variables.
- Fit a linear regression model to the data using sklearn’ s `LinearRegression` class.
- Make predictions using the model.
- Calculate the R- squared value to evaluate the model’ s performance.

Step 7: Plot the results:

- For univariate regression, plot the original data points (X, y) as a scatter plot and the regression line as a line plot.
- For bivariate regression, plot the original data points (X1, X2, y) as a 3D scatter plot and the regression plane.
- For multivariate regression, plot the predicted values against the actual values.

Step 8: Display the results:

- Print the coefficients (slope) and intercept for each regression model.
- Print the R- squared value for each regression model.

Step 9: Complete the program:

- Combine all the steps into a Python program.
- Run the program to perform univariate, bivariate, and multivariate regression on the dataset.

Code:

```
import pandas as pd

import matplotlib.pyplot as plt

import seaborn as sns

import numpy as np

df=pd.read_csv('/content/drive/MyDrive/Datasets/iris.csv')

df.head(150)
```

```
df.shape
df

df_Setosa=df.loc[df['species']=='setosa']
df_Virginica=df.loc[df['species']=='virginica']
df_Versicolor=df.loc[df['species']=='versicolor']
df_Setosa

#univariate for sepal width
plt.scatter(df_Setosa['sepal_width'],np.zeros_like(df_Setosa['sepal_width']))
plt.scatter(df_Virginica['sepal_width'],np.zeros_like(df_Virginica['sepal_width']))
plt.scatter(df_Versicolor['sepal_width'],np.zeros_like(df_Versicolor['sepal_width']))
plt.xlabel('sepal_width')
plt.show()
#univariate for sepal length
plt.scatter(df_Setosa['sepal_length'],np.zeros_like(df_Setosa['sepal_length']))
plt.scatter(df_Virginica['sepal_length'],np.zeros_like(df_Virginica['sepal_length']))
plt.scatter(df_Versicolor['sepal_length'],np.zeros_like(df_Versicolor['sepal_length']))
plt.xlabel('sepal_length')
plt.show()

#univariate for sepal width
plt.scatter(df_Setosa['petal_width'],np.zeros_like(df_Setosa['petal_width']))
plt.scatter(df_Virginica['petal_width'],np.zeros_like(df_Virginica['petal_width']))
plt.scatter(df_Versicolor['petal_width'],np.zeros_like(df_Versicolor['pet
```

```
al_width']))
plt.xlabel('petal_width')
plt.show()
#univariate for sepal length
plt.scatter(df_Setosa['petal_length'],np.zeros_like(df_Setosa['petal_length']))
plt.scatter(df_Virginica['petal_length'],np.zeros_like(df_Virginica['petal_length']))
plt.scatter(df_Versicolor['petal_length'],np.zeros_like(df_Versicolor['petal_length']))
plt.xlabel('petal_length')
plt.show()

#bivariate sepal.width vs petal.width
sns.FacetGrid(df,hue='species',height=5).map(plt.scatter,"sepal_width","petal_width").add_legend();
plt.show()

#bivariate sepal.length vs petal.length
sns.FacetGrid(df,hue='species',height=5).map(plt.scatter,"sepal_length","petal_length").add_legend();
plt.show()

#multivariate all the features
sns.pairplot(df,hue='species',size=2)
```

Output:

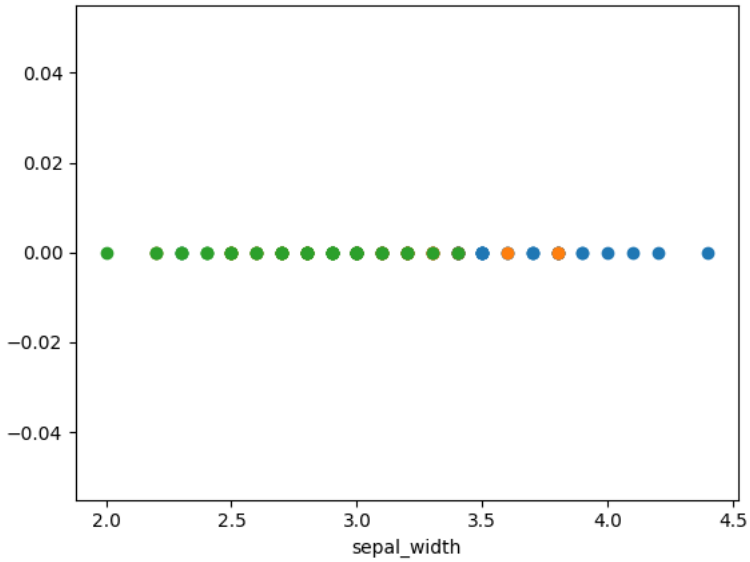
	sepal_length	sepal_width	petal_length	petal_width	species
0	5.1	3.5	1.4	0.2	setosa
1	4.9	3.0	1.4	0.2	setosa
2	4.7	3.2	1.3	0.2	setosa
3	4.6	3.1	1.5	0.2	setosa
4	5.0	3.6	1.4	0.2	setosa
...	...	...	...	...	...
145	6.7	3.0	5.2	2.3	virginica
146	6.3	2.5	5.0	1.9	virginica
147	6.5	3.0	5.2	2.0	virginica
148	6.2	3.4	5.4	2.3	virginica
149	5.9	3.0	5.1	1.8	virginica

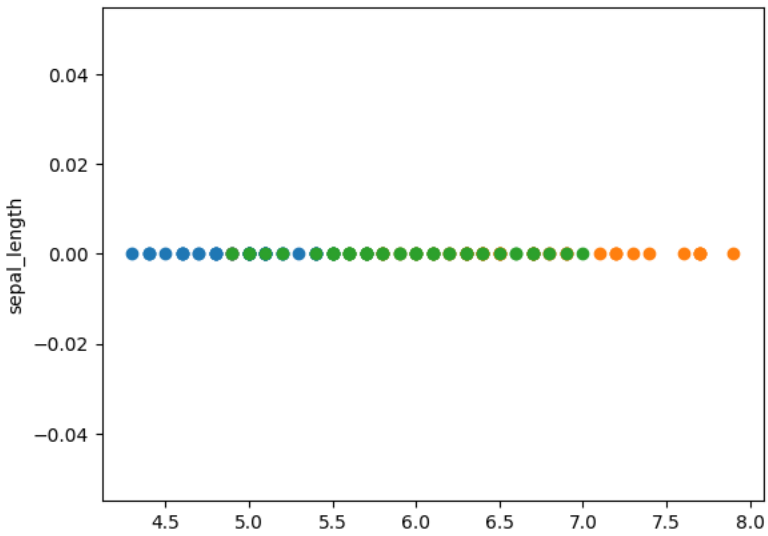
150 rows × 5 columns

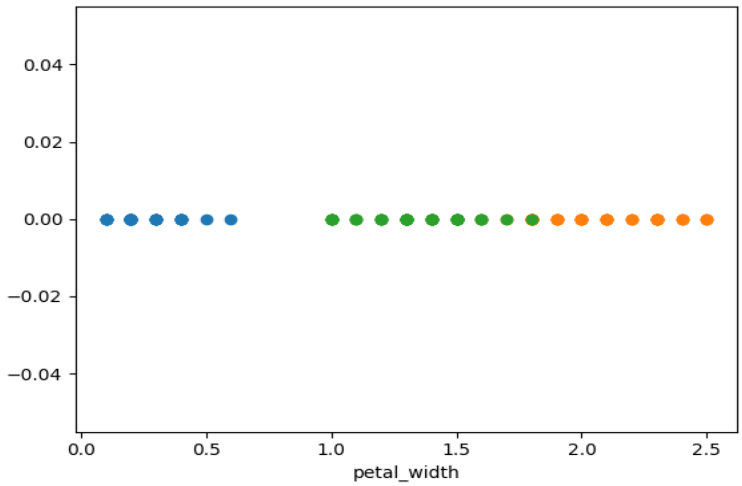
	sepal_length	sepal_width	petal_length	petal_width	species
0	5.1	3.5	1.4	0.2	setosa
1	4.9	3.0	1.4	0.2	setosa
2	4.7	3.2	1.3	0.2	setosa
3	4.6	3.1	1.5	0.2	setosa
4	5.0	3.6	1.4	0.2	setosa
5	5.4	3.9	1.7	0.4	setosa
6	4.6	3.4	1.4	0.3	setosa
7	5.0	3.4	1.5	0.2	setosa
8	4.4	2.9	1.4	0.2	setosa
9	4.9	3.1	1.5	0.1	setosa
10	5.4	3.7	1.5	0.2	setosa
11	4.8	3.4	1.6	0.2	setosa

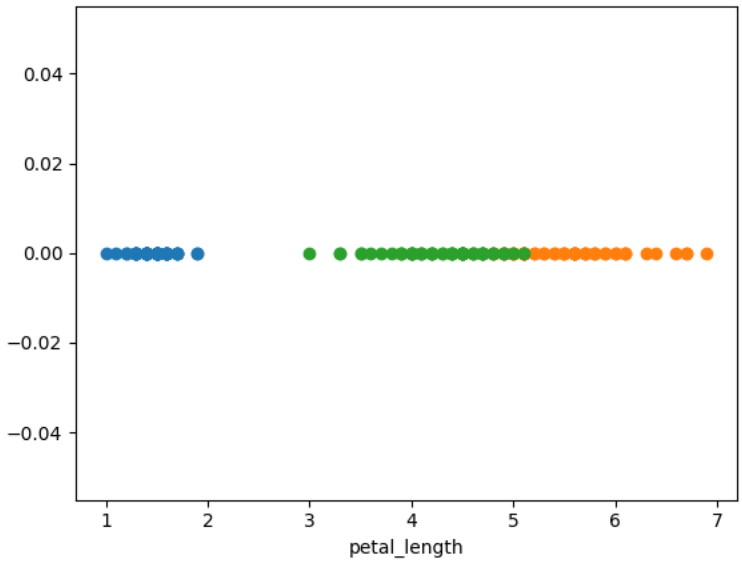
12	4.8	3.0	1.4	0.1	setosa
13	4.3	3.0	1.1	0.1	setosa
14	5.8	4.0	1.2	0.2	setosa
15	5.7	4.4	1.5	0.4	setosa
16	5.4	3.9	1.3	0.4	setosa
17	5.1	3.5	1.4	0.3	setosa
18	5.7	3.8	1.7	0.3	setosa
19	5.1	3.8	1.5	0.3	setosa
20	5.4	3.4	1.7	0.2	setosa
21	5.1	3.7	1.5	0.4	setosa
22	4.6	3.6	1.0	0.2	setosa
23	5.1	3.3	1.7	0.5	setosa
24	4.8	3.4	1.9	0.2	setosa
25	5.0	3.0	1.6	0.2	setosa
26	5.0	3.4	1.6	0.4	setosa
27	5.2	3.5	1.5	0.2	setosa
28	5.2	3.4	1.4	0.2	setosa
29	4.7	3.2	1.6	0.2	setosa
30	4.8	3.1	1.6	0.2	setosa
31	5.4	3.4	1.5	0.4	setosa
32	5.2	4.1	1.5	0.1	setosa
33	5.5	4.2	1.4	0.2	setosa
34	4.9	3.1	1.5	0.1	setosa
35	5.0	3.2	1.2	0.2	setosa
36	5.5	3.5	1.3	0.2	setosa
37	4.9	3.1	1.5	0.1	setosa
38	4.4	3.0	1.3	0.2	setosa
39	5.1	3.4	1.5	0.2	setosa
40	5.0	3.5	1.3	0.3	setosa
41	4.5	2.3	1.3	0.3	setosa
42	4.4	3.2	1.3	0.2	setosa
43	5.0	3.5	1.6	0.6	setosa

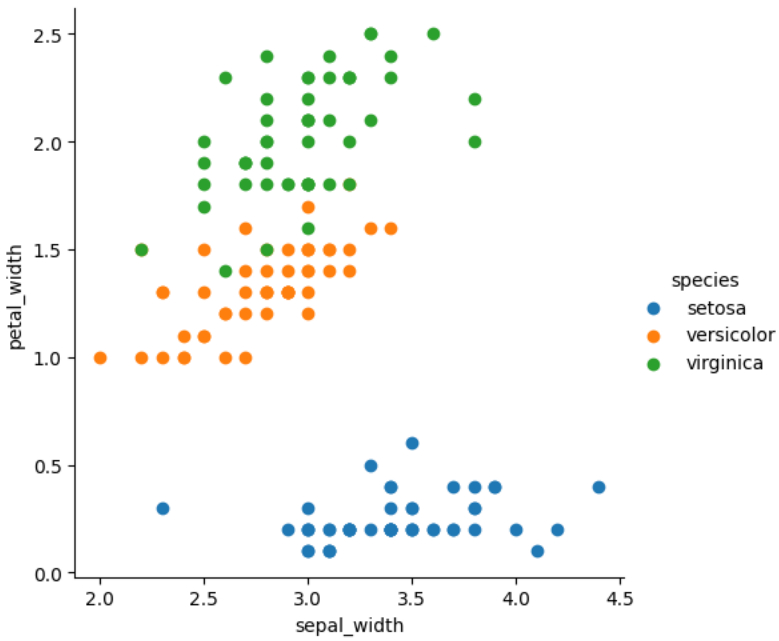
44	5.1	3.8	1.9	0.4	setosa
45	4.8	3.0	1.4	0.3	setosa
46	5.1	3.8	1.6	0.2	setosa
47	4.6	3.2	1.4	0.2	setosa
48	5.3	3.7	1.5	0.2	setosa
49	5.0	3.3	1.4	0.2	setosa

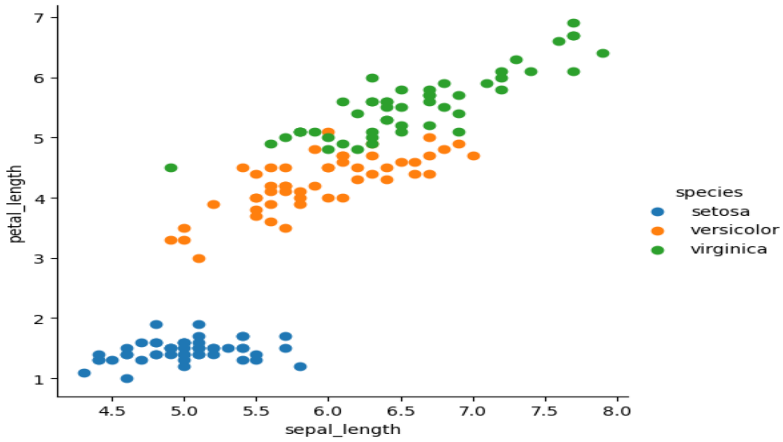




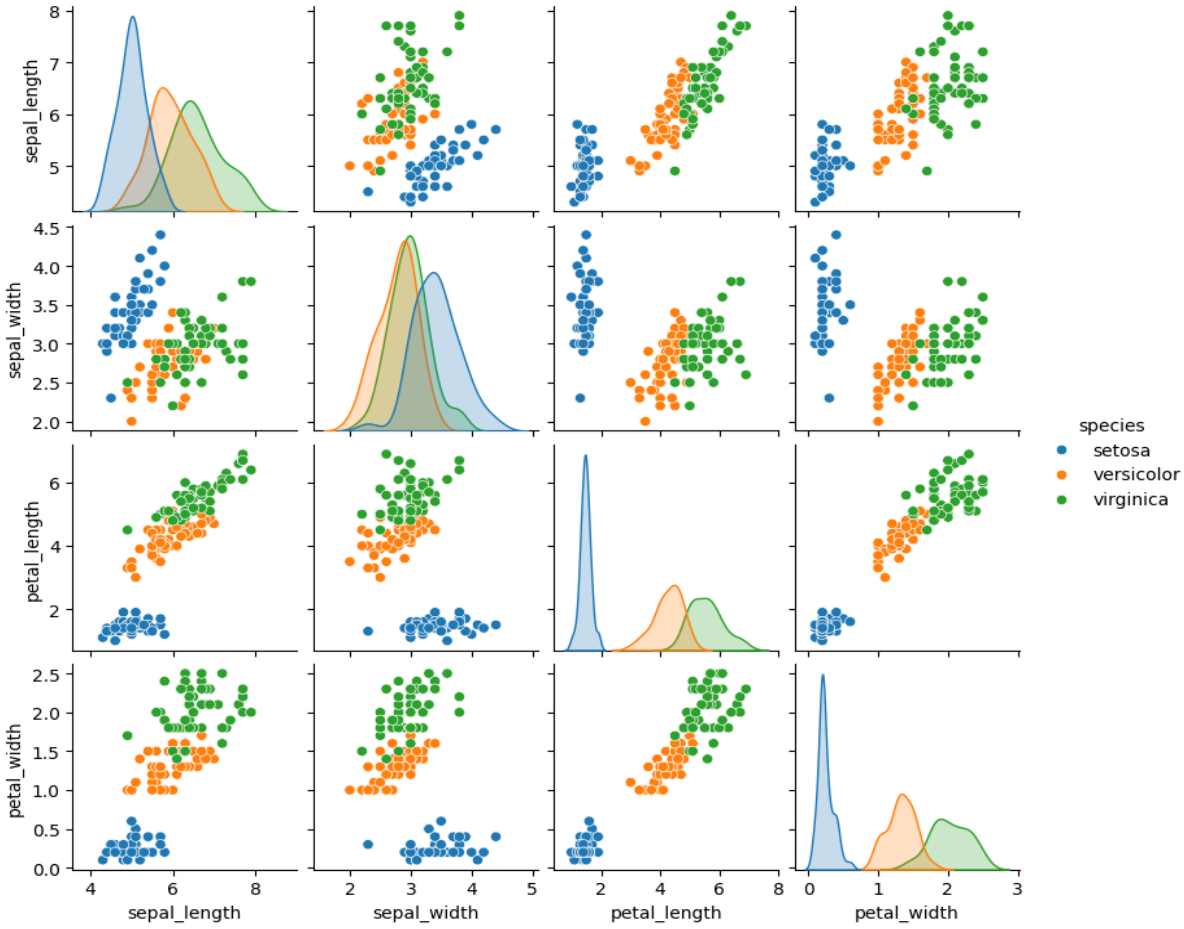

0.04
0.02
0.00
−0.02
−0.04
0.0
0.5
1.0
1.5
2.0
2.5
petal_width


0.04
0.02
0.00
−0.02
−0.04
1
2
3
4
5
6
7
petal_length


2.5
2.0
1.5
1.0
0.5
0.0
petal_width
2.0
2.5
3.0
3.5
4.0
4.5
sepal_width
species
setosa
versicolor
virginica




```
/usr/local/lib/python3.10/dist-packages/seaborn/axisgrid.py:2100: UserWarning: The `size` parameter has been renamed to `height`; please update your code.
  warnings.warn(msg, UserWarning)
<seaborn.axisgrid.PairGrid at 0x79f629c437c0>
```



Result:

Thus, the python program to implement univariate, bivariate and multivariate has been successfully implemented and the results

have been verified and analysed.
Ex No: 2

Date:

A PYTHON PROGRAM TO IMPLEMENT SIMPLE LINEAR REGRESSION USING LEAST SQUARE METHOD

Aim:

To implement a python program for constructing a simple linear regression using least square method.

Algorithm:

Step 1: Import necessary libraries:

- pandas for data manipulation and matplotlib.pyplot for plotting.

Step 2: Read the dataset:

- Use the pandas `read_csv` function to read the dataset (e.g., headbrain.csv).
- Store the dataset in a variable (e.g., `data`).

Step 3: Prepare the data:

- Extract the independent variable (X) and dependent variable (y) from the dataset.
- Reshape X and y to be 2D arrays if needed.

Step 4: Calculate the mean:

- Calculate the mean of X and y.

Step 5: Calculate the coefficients:

- Calculate the slope (m) using the formula:

$$m = \frac{\sum_{i=1}^{n}(X_i - \bar{X})(y_i - \bar{y})}{\sum_{i=1}^{n}(X_i - \bar{X})^2}$$

- Calculate the intercept (b) using the formula: $b = \bar{y} - m\bar{X}$

Step 6: Make predictions:

- Use the calculated slope and intercept to make predictions for each X value:

$$\hat{y} = mx + b$$

Step 7: Plot the regression line:

- Plot the original data points (X, y) as a scatter plot.
- Plot the regression line (X, predicted_y) as a line plot.

Step 8: Calculate the R- squared value:

- Calculate the total sum of squares (TSS) using the formula: $TSS = \sum_{i=1}^{n}(y_i - \bar{y})^2$
- Calculate the residual sum of squares (RSS) using the formula: $RSS = \sum_{i=1}^{n}(y_i - \hat{y}_i)^2$
- Calculate the R- squared value using the formula: $R^2 = 1 - \frac{RSS}{TSS}$

Step 9: Display the results:

- Print the slope, intercept, and R- squared value.

Step 10: Complete the program:

- Combine all the steps into a Python program.
- Run the program to perform simple linear regression on the dataset.

Code:

```
from google.colab import drive
```

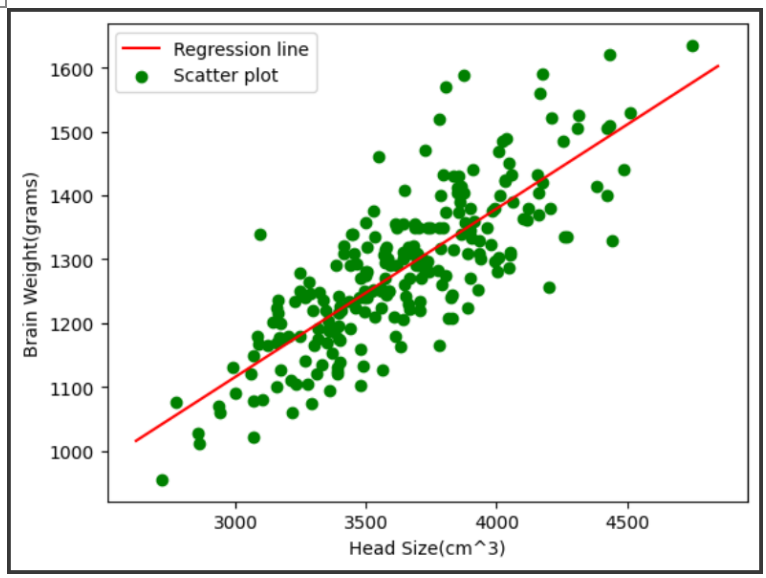
```
drive.mount('/content/drive')

import pandas as pd
import matplotlib.pyplot as plt
import numpy as np
data = pd.read_csv('/content/drive/MyDrive/Datasets/
headbrain.csv')

x, y = np.array(list(data['Head
Size(cm^3)'])),np.array(list(data['Brain Weight(grams)']))
print(x[:5], y[:5])

def get_line(x, y):
  x_m, y_m = np.mean(x), np.mean(y)
  print(x_m, y_m)
  x_d, y_d = x- x_m, y- y_m
  m = np.sum(x_d*y_d)/np.sum(x_d**2)
  c = y_m -  (m*x_m)
  print(m, c)
  return lambda x : m*x+c
lin = get_line(x, y)

X = np.linspace(np.min(x)- 100, np.max(x)+100, 1000)
Y = np.array([lin(x) for x in X])
plt.plot(X, Y, color='red', label='Regression line')
plt.scatter(x, y, color='green', label='Scatter plot')
plt.xlabel('Head Size(cm^3)')
plt.ylabel('Brain Weight(grams)')
plt.legend()
plt.show()

X = np.linspace(np.min(x)- 100, np.max(x)+100, 1000)

Y = np.array([lin(x) for x in X])
plt.plot(X, Y, color='red', label='Regression line')
```

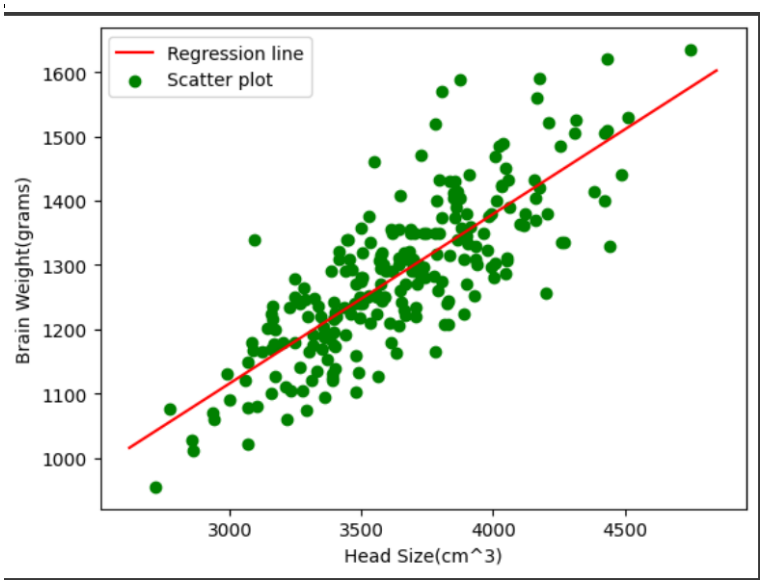
```
plt.scatter(x, y, color='green', label='Scatter plot')
plt.xlabel('Head Size(cm^3)')
plt.ylabel('Brain Weight(grams)')
plt.legend()
plt.show()

def get_error(line_fuc, x, y):
  y_m = np.mean(y)
  y_pred = np.array([line_fuc(_) for _ in x])
  ss_t = np.sum((y- y_m)**2)
  ss_r = np.sum((y- y_pred)**2)
  return 1- (ss_r/ss_t)
get_error(lin, x, y)

from sklearn.linear_model import LinearRegression
x = x.reshape((len(x),1))
reg=LinearRegression()
reg=reg.fit(x, y)
print(reg.score(x, y))
```

Output:

```
[4512 3738 4261 3777 4177] [1530 1297 1335 1282 1590]
```

```
3633.9915611814345 1282.873417721519
0.2634293394893993 325.5734210494428
```






```
0.639311719957
```

```
0.639311719957
```

Result:

Thus, the python program to Simple Linear Regression using Least Square Method has been successfully implemented and the results have been verified and analysed.

Ex no: 3

Date:

A PYTHON PROGRAM TO IMPLEMENT LOGISTIC MODEL

Aim:

To implement python program for the logistic model using suv car dataset.

Algorithm:

Step 1: Import Necessary Libraries:

- pandas for data manipulation
- sklearn.model_selection for train- test split
- sklearn.preprocessing for data preprocessing
- sklearn.linear_model for logistic regression
- matplotlib.pyplot for plotting

Step 2: Read the Dataset:

- Use pandas to read the suv_cars.csv dataset into a DataFrame.

Step 3: Preprocess the Data:

- Select the relevant columns for the analysis (e.g., 'Age', 'EstimatedSalary', 'Purchased').
- Encode categorical variables if necessary (e.g., using LabelEncoder or OneHotEncoder).
- Split the data into features (X) and target variable (y).

Step 4: Split the Data:

- Split the dataset into training and testing sets using train_test_split.

Step 5: Feature Scaling:

- Standardize the features using StandardScaler to ensure they have the same scale.

Step 6: Create and Train the Model:

- Create a logistic regression model using LogisticRegression from sklearn.linear_model.
- Train the model on the training data using the fit method.
    - oCreate a function named “ Sigmoid ()” which will define the sigmoid values using the
    - oformula (1/1+e- z) and return the computed value.
    - oCreate a function named “ initialize()” which will initialize the values with zeroes and assign the value to “ weights” variable, initializes with ones and assigns the value to variable “ x” and returns both “ x” and “ weights” .
    - oCreate a function named “ fit” which will be used to plot the graph according to the training data.
    - oCreate a predict function that will predict values according to the training model created using the fit function.
    - oInvoke the standardize() function for “ x- train” and “ x- test”

Step 7: Make Predictions:

- Use the trained model to make predictions on the test data using the predict method.
    - oUse the “ predict()” function to predict the values of the testing data and assign the value to “ y_pred” variable.
    - oUse the “ predict()” function to predict the values of the training data and assign the value to “ y_trainn” variable.
    - oCompute f1_score for both the training and testing data and assign the values to “ f1_score_tr” and “ f1_score_te” respectively

Step 8: Evaluate the Model:

- Calculate the accuracy of the model on the test data using the score method.

(Accuracy = (tp+tn)/(tp+tn+fp+fn)).

- Generate a confusion matrix and classification report to further evaluate the model's performance.

Step 9: Visualize the Results:

- Plot the decision boundary of the logistic regression model (optional).

Code:

```
import pandas as pd
import numpy as np
from numpy import log,dot,exp,shape
from sklearn.metrics import confusion_matrix
data = pd.read_csv('/content/drive/MyDrive/suv_data.csv')
```

```
print(data.head())

x = data.iloc[:, [2, 3]].values
y = data.iloc[:, 4].values

from sklearn.model_selection import train_test_split
x_train, x_test, y_train,
y_test=train_test_split(x,y,test_size=0.10, random_state=0)
from sklearn.preprocessing import StandardScaler
sc=StandardScaler()
x_train=sc.fit_transform(x_train)
x_test=sc.transform(x_test)
print (x_train[0:10,:])

from sklearn.linear_model import LogisticRegression
classifier=LogisticRegression(random_state=0)
classifier.fit(x_train,y_train)
LogisticRegression (random_state=0)
y_pred = classifier.predict(x_test)
print(y_pred)

from sklearn.metrics import confusion_matrix
cm = confusion_matrix(y_test, y_pred)
print ("Confusion Matrix : \n", cm)

from sklearn.metrics import accuracy_score
print ("Accuracy : ", accuracy_score(y_test, y_pred))
```

```
from sklearn.model_selection import train_test_split
x_train, x_test, y_train,
y_test=train_test_split(x,y,test_size=0.10, random_state=0)
def Std(input_data):
    mean0 = np.mean(input_data[:, 0])
    sd0 = np.std(input_data[:, 0])
    mean1 = np.mean(input_data[:, 1])
    sd1 = np.std(input_data[:, 1])
    return lambda x:((x[0]- mean0)/sd0, (x[1]- mean1)/sd1)
my_std = Std(x)
my_std(x_train[0])

def standardize(X_tr):
    for i in range(shape(X_tr)[1]):
        X_tr[:,i] = (X_tr[:,i] -  np.mean(X_tr[:,i]))/np.std(X_tr[:,i])
def F1_score(y,y_hat):
    tp,tn,fp,fn = 0,0,0,0
    for i in range(len(y)):
        if y[i] == 1 and y_hat[i] == 1:
                tp += 1
        elif y[i] == 1 and y_hat[i] == 0:
                fn += 1
        elif y[i] == 0 and y_hat[i] == 1:
                fp += 1
        elif y[i] == 0 and y_hat[i] == 0:
```

```
            tn += 1
    precision = tp/(tp+fp)
    recall = tp/(tp+fn)
    f1_score = 2*precision*recall/(precision+recall)
    return f1_score

class LogisticRegression:
    def sigmoid(self, z):
        sig = 1 / (1 + exp(- z))
        return sig

    def initialize(self, X):
        weights = np.zeros((shape(X)[1] + 1, 1))
        X = np.c_[np.ones((shape(X)[0], 1)), X]
        return weights, X

    def fit(self, X, y, alpha=0.001, iter=400):
        weights, X = self.initialize(X)

        def cost(theta):
            z = dot(X, theta)
            cost0 = y.T.dot(log(self.sigmoid(z)))
            cost1 = (1 - y).T.dot(log(1 - self.sigmoid(z)))
            cost = - ((cost1 + cost0)) / len(y)
            return cost
```

```
        cost_list = np.zeros(iter,)
        for i in range(iter):
            weights = weights -  alpha * dot(X.T,
self.sigmoid(dot(X, weights)) -  np.reshape(y, (len(y), 1)))
            cost_list[i] = cost(weights).item()
        self.weights = weights
        return cost_list


    def predict(self, X):
        z = dot(self.initialize(X)[1], self.weights)
        lis = []
        for i in self.sigmoid(z):
            if i > 0.5:
                lis.append(1)
            else:
                lis.append(0)
        return lis


standardize(x_train)
standardize(x_test)
obj1 = LogisticRegression()
model = obj1.fit(x_train, y_train)
y_pred = obj1.predict(x_test)
y_trainn = obj1.predict(x_train)
f1_score_tr = F1_score(y_train, y_trainn)
f1_score_te = F1_score(y_test, y_pred)
```

```
print(f1_score_tr)
print(f1_score_te)
conf_mat = confusion_matrix(y_test, y_pred)
accuracy = (conf_mat[0, 0] + conf_mat[1, 1]) /
sum(sum(conf_mat))
print("Accuracy is : ", accuracy)
```

Output:

```
     User ID  Gender  Age  EstimatedSalary  Purchased
0  15624510    Male   19            19000          0
1  15810944    Male   35            20000          0
2  15668575  Female   26            43000          0
3  15603246  Female   27            57000          0
4  15804002    Male   19            76000          0
```

```
[[- 1.05714987  0.53420426]
 [ 0.2798728  - 0.51764734]
 [- 1.05714987  0.41733186]
 [- 0.29313691 - 1.45262654]
 [ 0.47087604  1.23543867]
 [- 1.05714987 - 0.34233874]
 [- 0.10213368  0.30045946]
 [ 1.33039061  0.59264046]
 [- 1.15265148 - 1.16044554]
 [ 1.04388575  0.47576806]]
[0 0 0 0 0 0 0 1 0 1 0 0 0 0 0 0 0 0 1 0 0 1 0 1 1 0 1 0 0 0 0 0 1 0 0 0 0
 0 0 1]
Confusion Matrix :
 [[31  1]
 [ 1  7]]
Accuracy :  0.95
(- 1.017692393473028, 0.5361288690822568)
0.7583333333333334
0.823529411764706
```

Accuracy is : 0.925

Result:

Thus, the python program to implement logistic model has been successfully implemented and the results have been verified and analyzed.

Ex. No.: 4
Date:

A PYTHON PROGRAM TO IMPLEMENT SINGLE LAYER PERCEPTRON

Aim:

To implement python program for the single layer

perceptron.

Algorithm:

Step 1: Import Necessary Libraries:

- Import numpy for numerical operations.

Step 2: Initialize the Perceptron:

- Define the number of input features (input_dim).
- Initialize weights (W) and bias (b) to zero or small random values.

Step 3: Define Activation Function:

- Choose an activation function (e.g., step function, sigmoid, or ReLU).
- User Defined function - sigmoid_func(x):
  - oCompute 1/(1+np.exp(- x)) and return the value.
- User Defined function - der(x):
  - oCompute the product of value of sigmoid_func(x) and (1 - sigmoid_func(x)) and return the value.

Step 4; Define Training Data:

- Define input features (X) and corresponding target labels (y).

Step 5: Define Learning Rate and Number of Epochs:

- Choose a learning rate (alpha) and the number of training epochs.

Step 6: Training the Perceptron:

- For each epoch:
  - oFor each input sample in the training data:
  - oCompute the weighted sum of inputs (z) as the dot product of input features and weights plus bias (z = np.dot(X[i], W) + b).
  - oApply the activation function to get the predicted output (y_pred).
  - oCompute the error (error = y[i] - y_pred).
  - oUpdate the weights and bias using the learning rate and error (W += alpha * error * X[i]; b += alpha * error).

Step 7: Prediction:

- Use the trained perceptron to predict the output for new input data.

Step 8: Evaluate the Model:

- Measure the performance of the model using metrics such as accuracy, precision, recall, etc.

Code:

```
import numpy as np
from sklearn.metrics import accuracy_score,
precision_score, recall_score, f1_score

input_dim=2
W=np.zeros(input_dim)
b=0.0

def sigmoid_func(x):
    return 1/(1+np.exp(-x))
def der(x):
    sigmoid = sigmoid_func(x)
    return sigmoid * (1- sigmoid)
```

```
np.random.seed(42)
x = np.array([[150,8],
              [130,7],
              [180,6],
              [170,5]])
y = np.array([0,0,1,1])

alpha = 0.1
epochs = 10000

for epoch in range(epochs):
    for i in range(len(x)):
        z = np.dot(x[i], W) + b
        y_pred = sigmoid_func(z)
        error = y[i] -  y_pred
        W += alpha * error * x[i]
        b += alpha * error

def predict(X):
    z = np.dot(X, W) + b
    return (sigmoid_func(z) > 0.5).astype(int)
y_pred = predict(x)
accuracy = accuracy_score(y, y_pred)
precision = precision_score(y, y_pred)
recall = recall_score(y, y_pred)

F1_score = f1_score(y, y_pred)

print("Prediction:",y_pred)
print("Accuracy:", accuracy)
print("Precision:", precision)
print("Recall:", recall)
print("F1 Score:", F1_score)
```

Output:

Prediction: [0 0 1 1]
Accuracy: 1.0
Precision: 1.0
Recall: 1.0
F1 Score: 1.0

Result:

Thus, the python program to implement single layer perceptron has been successfully implemented and the results have been verified and analysed.

Ex. No.: 5
Date:

A PYTHON PROGRAM TO IMPLEMENT MULTI LAYER PERCEPTRON WITH BACK PROPOGATION

Aim:

To implement multilayer perceptron with back propagation using python.

Algorithm:

Step 1: Import the Necessary Libraries

- Import pandas as pd.
- Import numpy as np.

Step 2: Read and Display the Dataset

- Use `pd.read_csv("banknotes.csv")` to read the dataset.
- Assign the result to a variable (e.g., `data`).
- Display the first ten rows using `data.head(10)`.

Step 3: Display Dataset Dimensions

- Use the `.shape` attribute on the dataset (e.g., `data.shape`).

Step 4: Display Descriptive Statistics

- Use the `.describe()` function on the dataset (e.g., `data.describe()`).

Step 5: Import Train- Test Split Module

- Import `train_test_split` from `sklearn.model_selection`.

Step 6: Split Dataset with 80- 20 Ratio

- Assign the features to a variable (e.g., `X = data.drop(columns='target')`).
- Assign the target variable to another variable (e.g., `y = data['target']`).
- Use `train_test_split` to split the dataset into training and testing sets with a ratio of 0.2.

- Assign the results to `x_train`, `x_test`, `y_train`, and `y_test`.

Step 7: Import MLPClassifier Module
- Import `MLPClassifier` from `sklearn.neural_network`.

Step 8: Initialize MLPClassifier
- Create an instance of `MLPClassifier` with `max_iter=500` and `activation='relu'`.
- Assign the instance to a variable (e.g., `clf`).

Step 9: Fit the Classifier
- Fit the model using `clf.fit(x_train, y_train)`.

Step 10: Make Predictions
- Use the `.predict()` function on `x_test` (e.g., `pred = clf.predict(x_test)`).
- Display the predictions.

Step 11: Import Metrics Modules
- Import `confusion_matrix` from `sklearn.metrics`.
- Import `classification_report` from `sklearn.metrics`.

Step 12: Display Confusion Matrix
- Use `confusion_matrix(y_test, pred)` to generate the confusion matrix.
- Display the confusion matrix.

Step 13: Display Classification Report
- Use `classification_report(y_test, pred)` to generate the classification report.
- Display the classification report.

Step 14: Repeat Steps 9- 13 with Different Activation Functions
- Initialize `MLPClassifier` with `activation='logistic'`.

- Fit the model and make predictions.
- Display the confusion matrix and classification report.
- Repeat for `activation='tanh'`.
- Repeat for `activation='identity'`.

Step 15: Repeat Steps 7- 14 with 70- 30 Ratio

- Use `train_test_split` to split the dataset into training and testing sets with a ratio of 0.3.
- Assign the results to `x_train`, `x_test`, `y_train`, and `y_test`.
- Repeat Steps 7- 14 with the new training and testing sets.

Code:

```
import pandas as pd
import numpy as np
from sklearn.model_selection import train_test_split
from sklearn.neural_network import MLPClassifier
from sklearn.metrics import classification_report, confusion_matrix

bnotes = pd.read_csv('../content/drive/MyDrive/bank_note_data.csv')
print(bnotes.head(10))

x = bnotes.drop('Class', axis=1)
y = bnotes['Class']
print(x.head(2))
print(y.head(2))

def train_and_evaluate(activation, x_train, y_train, x_test, y_test):
    mlp = MLPClassifier(max_iter=500, activation=activation)
    mlp.fit(x_train, y_train)

    pred = mlp.predict(x_test)
    print(f"Predictions using activation function '{activation}':\n{pred}
\n")

    cm = confusion_matrix(y_test, pred)
    print(f"Confusion Matrix for '{activation}':\n{cm}\n")

    report = classification_report(y_test, pred)
    print(f"Classification Report for '{activation}':\n{report}\n")
```

```
x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.2)

for activation in ['relu', 'logistic', 'tanh', 'identity']:
    train_and_evaluate(activation, x_train, y_train, x_test, y_test)

x_train, x_test, y_train, y_test = train_test_split(x, y, test_size=0.3)
for activation in ['relu', 'logistic', 'tanh', 'identity']:
    train_and_evaluate(activation, x_train, y_train, x_test, y_test)
```

Output:

```
   Image.Var  Image.Skew  Image.Curt  Entropy  Class
0    3.62160      8.6661    -2.80730 -0.44699      0
1    4.54590      8.1674    -2.45860 -1.46210      0
2    3.86600     -2.6383     1.92420  0.10645      0
3    3.45660      9.5228    -4.01120 -3.59440      0
4    0.32924     -4.4552     4.57180 -0.98880      0
5    4.36840      9.6718    -3.96060 -3.16250      0
6    3.59120      3.0129     0.72888  0.56421      0
7    2.09220     -6.8100     8.46360 -0.60216      0
8    3.20320      5.7588    -0.75345 -0.61251      0
9    1.53560      9.1772    -2.27180 -0.73535      0
   Image.Var  Image.Skew  Image.Curt  Entropy
0     3.6216      8.6661     -2.8073 -0.44699
1     4.5459      8.1674     -2.4586 -1.46210
0    0
1    0
Name: Class, dtype: int64
Predictions using activation function 'relu':
[1 1 1 1 0 0 1 1 1 0 0 0 1 1 0 0 0 1 1 1 1 0 0 1 0 0 0 0 0 1 0 0 1 0 0 0 0
 0 0 0 1 0 0 0 1 1 1 0 0 1 1 0 0 0 1 0 1 1 1 1 0 0 0 0 1 1 0 0 1 0 1 0 1 1
 1 1 0 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 0 1 1 0 0 0 1 0 0 1 1 1 1 0 1 0
 1 1 1 0 1 1 1 0 0 0 1 1 1 0 1 1 0 1 0 1 1 0 0 1 0 1 1 0 0 0 0 0 0 1 0 0 0
 1 0 1 1 1 0 1 1 1 0 1 1 0 0 1 0 1 1 0 0 0 0 1 0 1 1 1 1 1 1 1 0 1 0 0 1 0
 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 1 0 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 1 1
 0 0 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 0 0 1 0 1 1 1 0 1 1 0 0 0 0 0 1 0 0 0
 0 0 1 1 0 0 0 0 0 1 1 1 1 1 1 0]

Confusion Matrix for 'relu':
[[143   0]
 [  0 132]]
```

```
Classification Report for 'relu':
              precision    recall  f1-score   support

           0       1.00      1.00      1.00       143
           1       1.00      1.00      1.00       132

    accuracy                           1.00       275
   macro avg       1.00      1.00      1.00       275
weighted avg       1.00      1.00      1.00       275


Predictions using activation function 'logistic':
[1 1 1 1 0 0 1 1 1 0 0 0 1 1 0 0 0 1 1 1 1 0 0 1 0 0 0 0 0 1 0 0 1 0 0 0 0
 0 0 0 1 0 0 0 1 1 1 0 0 1 1 0 0 0 1 0 1 1 1 1 0 0 0 0 1 1 0 0 1 0 1 0 1 1
 1 1 0 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 0 1 1 0 0 0 1 0 0 1 1 1 1 0 1 0
 1 1 1 0 1 1 1 0 0 0 1 1 1 0 1 1 0 1 0 1 1 1 0 0 1 0 1 1 0 0 0 0 0 0 1 0 0 0
 1 0 1 1 1 0 1 1 1 0 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 1 1 1 1 1 1 1 1 0 1 0 0 1 0
 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 1 0 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 1 1
 0 0 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 0 0 1 0 1 1 1 0 1 1 0 0 0 0 0 1 0 0 0
 0 0 1 1 0 0 0 0 0 1 1 1 1 1 1 1 0]

Confusion Matrix for 'logistic':
[[143   0]
 [  0 132]]

Classification Report for 'logistic':
              precision    recall  f1-score   support

           0       1.00      1.00      1.00       143
           1       1.00      1.00      1.00       132

    accuracy                           1.00       275
   macro avg       1.00      1.00      1.00       275
weighted avg       1.00      1.00      1.00       275
```

```
Predictions using activation function 'tanh':
[1 1 1 1 0 0 1 1 1 0 0 0 1 1 0 0 0 1 1 1 1 0 0 1 0 0 0 0 0 1 0 0 1 0 0 0 0
 0 0 0 1 0 0 0 1 1 1 0 0 1 1 0 0 0 1 0 1 1 1 1 0 0 0 0 1 1 0 0 1 0 1 0 1 1
 1 1 0 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 0 1 1 0 0 0 1 0 0 1 1 1 1 0 1 0
 1 1 1 0 1 1 1 0 0 0 1 1 1 0 1 1 0 1 0 1 1 1 0 0 1 0 1 1 0 0 0 0 0 0 1 0 0 0
 1 0 1 1 1 0 1 1 1 0 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 1 1 1 1 1 1 1 1 0 1 0 0 1 0
 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 1 0 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 1 1
 0 0 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 0 0 1 0 1 1 1 0 1 1 0 0 0 0 0 1 0 0 0
 0 0 1 1 0 0 0 0 0 1 1 1 1 1 1 1 0]

Confusion Matrix for 'tanh':
[[143   0]
 [  0 132]]

Classification Report for 'tanh':
              precision    recall  f1-score   support

           0       1.00      1.00      1.00       143
           1       1.00      1.00      1.00       132

    accuracy                           1.00       275
   macro avg       1.00      1.00      1.00       275
weighted avg       1.00      1.00      1.00       275


Predictions using activation function 'identity':
[1 1 1 1 0 0 1 1 1 0 0 0 1 1 0 0 0 1 1 1 1 0 0 1 0 0 0 0 0 1 0 0 1 0 0 0 1
 0 0 0 1 0 0 0 1 1 1 0 0 1 1 0 0 0 1 0 1 1 1 1 0 0 0 0 1 1 0 0 1 0 1 0 1 1
 1 1 0 1 1 1 0 0 0 0 0 1 1 0 0 0 0 0 0 1 1 0 1 1 0 0 0 1 0 0 1 1 1 1 0 1 0
 1 1 1 0 1 1 1 0 0 0 1 1 1 0 1 1 0 1 0 1 1 1 0 0 1 0 1 1 0 0 0 0 0 0 1 0 1 0
 1 0 1 1 1 0 1 1 1 0 1 1 0 0 1 0 1 1 1 0 0 0 0 1 0 1 1 1 1 1 1 1 1 0 1 0 0 1 0
 0 1 1 0 0 1 0 0 1 1 0 1 0 0 0 1 1 1 1 0 1 1 1 0 0 1 1 0 1 0 0 0 1 0 0 1 1
 0 0 0 1 1 1 1 1 0 0 1 0 1 0 0 0 0 1 0 0 1 0 1 1 1 0 1 1 0 0 0 0 0 1 0 0 0
 0 0 1 1 0 0 0 0 0 1 1 1 1 1 1 1 0]
```

```
Confusion Matrix for 'identity':
[[141   2]
 [  0 132]]

Classification Report for 'identity':
              precision    recall  f1-score   support

           0       1.00      0.99      0.99       143
           1       0.99      1.00      0.99       132

    accuracy                           0.99       275
   macro avg       0.99      0.99      0.99       275
weighted avg       0.99      0.99      0.99       275


Predictions using activation function 'relu':
[0 0 0 0 0 1 0 0 1 0 1 1 1 1 1 0 0 1 0 0 0 1 1 0 1 0 0 1 1 0 0 1 0 1 0 0 0
 0 1 0 0 1 1 0 1 1 1 0 1 1 0 0 1 1 0 1 1 1 1 1 1 0 1 0 1 1 0 0 0 1 1 0 1 0
 1 0 0 0 0 0 0 0 0 0 1 0 1 0 0 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 1 0 1 1 0
 0 0 0 0 0 1 0 0 0 0 1 1 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 0 1 0 0 0 1 0 0 0 0
 0 0 0 1 1 1 1 0 0 0 0 0 1 0 1 0 0 1 0 1 1 0 1 1 0 1 1 0 0 1 0 0 1 1 1 1 1
 0 0 1 1 0 0 1 0 0 0 0 0 1 0 1 1 0 0 0 1 0 1 1 0 1 0 0 0 0 1 1 0 0 0 0 0 0
 1 1 1 0 0 0 1 0 0 0 0 1 1 0 0 1 1 1 0 0 1 1 1 1 1 0 0 0 1 0 1 0 0 1 1 1 1
 0 0 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 1 0 0 1 0 1 0 0 0 0 0 1 0 0 0
 0 0 0 1 1 1 0 0 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 1 0 0 1 1 1 1 0 0 0 1 1
 0 0 0 0 1 0 1 0 0 0 0 0 1 1 1 1 0 0 0 1 0 1 0 1 0 1 0 1 1 1 0 0 0 1 0 0 0
 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 1 1 1 1 0 0 0 1 1 1 0 0 0 0 0 0 1 0 0 1 0 0
 0 0 1 0 1]

Confusion Matrix for 'relu':
[[239   0]
 [  0 173]]
```

```
Classification Report for 'relu':
              precision    recall  f1-score   support

           0       1.00      1.00      1.00       239
           1       1.00      1.00      1.00       173

    accuracy                           1.00       412
   macro avg       1.00      1.00      1.00       412
weighted avg       1.00      1.00      1.00       412


Predictions using activation function 'logistic':
[0 0 0 0 0 1 0 0 1 0 1 1 1 1 1 0 0 1 0 0 0 1 1 0 1 0 0 1 1 0 0 1 0 1 0 0 0
 0 1 0 0 1 1 0 1 1 1 0 1 1 0 0 1 1 0 1 1 1 1 1 1 0 1 1 1 1 0 0 0 1 1 0 1 0
 1 0 0 0 0 0 0 0 0 0 1 0 1 1 0 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 1 0 1 1 0
 0 0 0 0 0 1 0 0 0 0 1 1 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 0 1 0 0 0 1 0 0 0 0
 0 0 0 1 1 1 1 0 0 0 0 0 1 0 1 0 0 1 0 1 1 0 1 1 0 1 1 0 0 1 0 0 1 1 1 1 1
 0 0 1 1 0 0 1 0 0 0 0 0 1 0 1 1 0 0 0 1 0 1 1 0 1 0 0 0 0 1 1 0 0 0 0 0 0
 1 1 1 0 0 0 1 0 0 0 0 1 1 0 0 1 1 1 0 0 1 1 1 1 1 0 0 0 1 0 1 0 0 1 1 1 1
 0 0 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 1 0 0 1 0 1 0 0 1 0 0 1 0 0 0
 0 0 0 1 1 1 0 0 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 1 0 0 1 1 1 1 0 0 0 1 1
 0 0 0 1 1 0 1 0 0 0 0 0 1 1 1 1 0 0 0 1 0 1 0 1 0 1 0 1 1 1 0 0 0 1 0 0 0
 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 1 1 1 1 0 0 0 1 1 1 0 0 0 0 0 0 1 0 0 1 0 0
 0 0 1 1 1]

Confusion Matrix for 'logistic':
[[234   5]
 [  0 173]]
```

```
Classification Report for 'logistic':
              precision    recall  f1-score   support

           0       1.00      0.98      0.99       239
           1       0.97      1.00      0.99       173

    accuracy                           0.99       412
   macro avg       0.99      0.99      0.99       412
weighted avg       0.99      0.99      0.99       412


Predictions using activation function 'tanh':
[0 0 0 0 0 1 0 0 1 0 1 1 1 1 1 0 0 1 0 0 0 1 1 0 1 0 0 1 1 0 0 1 0 1 0 0 0
 0 1 0 0 1 1 0 1 1 1 0 1 1 0 0 1 1 0 1 1 1 1 1 1 0 1 1 1 1 0 0 0 1 1 0 1 0
 1 0 0 0 0 0 0 0 0 0 1 0 1 0 0 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 0 1 1 0
 0 0 0 0 0 1 0 0 0 0 1 1 1 1 0 1 1 1 0 1 1 1 1 0 1 0 0 0 1 0 0 0 1 0 0 0 0 0
 0 0 0 1 1 1 1 0 0 0 0 0 1 0 1 0 0 1 0 1 1 0 1 1 0 1 1 0 0 1 0 0 1 1 1 1 1
 0 0 1 1 0 0 1 0 0 0 0 0 1 0 1 1 0 0 0 1 0 1 1 0 1 0 0 0 0 1 1 0 0 0 0 0 0
 1 1 1 0 0 0 1 0 0 0 0 1 1 0 0 1 1 1 0 0 1 1 1 1 1 0 0 0 1 0 1 0 0 1 1 1 1
 0 0 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 1 0 1 0 0 1 0 0 1 0 0 1 0 0 0
 0 0 0 1 1 1 0 0 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 1 0 0 1 1 1 1 0 0 0 1 1
 0 0 0 0 1 0 1 0 0 0 0 0 1 1 1 1 0 0 0 1 0 1 0 1 0 1 0 1 1 1 0 0 0 1 0 0 0
 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 1 1 1 1 0 0 0 1 1 1 0 0 0 0 0 0 1 0 0 1 0 0
 0 0 1 1 1]

Confusion Matrix for 'tanh':
[[236   3]
 [  0 173]]



Classification Report for 'tanh':
              precision    recall  f1-score   support

           0       1.00      0.99      0.99       239
           1       0.98      1.00      0.99       173

    accuracy                           0.99       412
   macro avg       0.99      0.99      0.99       412
weighted avg       0.99      0.99      0.99       412


Predictions using activation function 'identity':
[0 0 0 0 0 1 0 0 1 0 1 1 1 1 1 0 0 1 0 0 0 1 0 0 1 0 0 1 1 0 0 1 0 1 0 0 0
 0 1 0 0 1 1 0 1 1 1 0 1 1 0 0 1 1 0 1 1 1 1 1 1 0 1 1 1 1 0 0 0 1 1 0 1 0
 1 0 0 0 0 0 0 0 0 0 1 0 1 1 0 1 0 0 0 1 0 0 1 0 1 0 1 0 1 0 0 0 0 1 0 1 1 0
 0 0 0 0 0 1 0 1 0 0 1 0 1 1 0 1 1 1 1 0 1 1 1 1 0 1 0 0 0 1 0 0 0 1 0 0 0 0
 0 0 0 1 1 1 1 0 0 0 0 0 1 0 1 0 0 1 0 1 1 1 0 1 1 0 1 1 0 0 1 0 0 1 1 1 1 1
 0 0 1 1 0 0 1 0 0 0 0 0 1 0 1 1 0 0 0 1 0 1 1 0 1 0 0 0 0 1 1 0 0 0 0 0 0
 1 1 1 0 0 0 1 0 0 0 0 1 1 0 0 1 1 1 0 0 1 1 1 1 1 0 0 0 1 0 1 0 0 1 1 1 1
 0 0 1 0 1 0 0 1 0 1 0 0 0 0 1 0 1 0 1 1 0 0 1 0 0 1 0 1 0 0 1 0 0 1 0 0 0
 0 0 0 1 1 1 0 0 1 0 1 0 1 0 0 1 0 0 0 0 1 0 1 1 0 1 0 0 1 1 1 1 0 0 0 1 1
 0 0 0 1 1 0 1 0 0 0 0 0 1 1 1 1 0 0 0 1 0 1 0 1 0 1 0 1 1 1 0 0 0 1 0 0 0
 0 1 0 1 0 1 0 0 1 0 0 0 0 0 0 1 1 1 1 0 0 0 1 1 1 0 0 0 0 0 0 1 0 0 1 0 0
 0 0 1 1 1]

Confusion Matrix for 'identity':
[[233   6]
 [  2 171]]

Classification Report for 'identity':
              precision    recall  f1-score   support

           0       0.99      0.97      0.98       239
           1       0.97      0.99      0.98       173

    accuracy                           0.98       412
   macro avg       0.98      0.98      0.98       412
weighted avg       0.98      0.98      0.98       412
```

Result:

Thus, the python program to implement multi- layer perceptron has been successfully implemented and the results have been verified and analysed.

Ex no: 6
Date:

A PYTHON PROGRAM TO IMPLEMENT SVM CLASSIFIER MODEL

Aim:

To implement a SVM classifier model using python and determine its accuracy.

Algorithm:

Step 1: Import Necessary Libraries

- Import numpy as np.
- Import pandas as pd.
- Import SVM from sklearn.
- Import matplotlib.pyplot as plt.
- Import seaborn as sns.
- Set the font_scale attribute to 1.2 in seaborn.

Step 2: Load and Display Dataset

- Read the dataset (muffins.csv) using `pd.read_csv()`.
- Display the first five instances using the `head()` function.

Step 3: Plot Initial Data

- Use the `sns.lmplot()` function.
- Set the x and y axes to "Sugar" and "Flour".
- Assign "recipes" to the data parameter.
- Assign "Type" to the hue parameter.
- Set the palette to "Set1".
- Set fit_reg to False.
- Set scatter_kws to {"s": 70}.
- Plot the graph.

Step 4: Prepare Data for SVM

- Extract "Sugar" and "Butter" columns from the recipes dataset and assign to variable `sugar_butter`.
- Create a new variable `type_label`.
- For each value in the "Type" column, assign 0 if it is "Muffin" and 1 otherwise.

Step 5: Train SVM Model

- Import the SVC module from the svm library.
- Create an SVC model with kernel type set to linear.
- Fit the model using `sugar_butter` and `type_label` as the

parameters.

Step 6: Calculate Decision Boundary

- Use the `model.coef_` function to get the coefficients of the linear model.
- Assign the coefficients to a list named `w`.
- Calculate the slope `a` as `w[0] / w[1]`.
- Use `np.linspace()` to generate values from 5 to 30 and assign to variable `xx`.
- Calculate the intercept using the first value of the model intercept and divide by `w[1]`.
- Calculate the decision boundary line `y` as `a * xx - (model.intercept_[0] / w[1])`.

Step 7: Calculate Support Vector Boundaries

- Assign the first support vector to variable `b`.
- Calculate `yy_down` as `a * xx + (b[1] - a * b[0])`.
- Assign the last support vector to variable `b`.
- Calculate `yy_up` using the same method.

Step 8: Plot Decision Boundary

- Use the `sns.lmplot()` function again with the same parameters as in Step 3.
- Plot the decision boundary line `xx` and `yy`.

Step 9: Plot Support Vector Boundaries

- Plot the decision boundary with `xx`, `yy_down`, and `'k--'`.
- Plot the support vector boundaries with `xx`, `yy_up`, and `'k--'`.
- Scatter plot the first and last support vectors.

Step 10: Import Additional Libraries

- Import `confusion_matrix` from `sklearn.metrics`.
- Import `classification_report` from `sklearn.metrics`.
- Import `train_test_split` from `sklearn.model_selection`.

Step 11: Split Dataset

- Assign `x_train`, `x_test`, `y_train`, and `y_test` using `train_test_split`.
- Set the test size to 0.2.

Step 12: Train New Model

- Create a new SVC model named `model1`.
- Fit the model using the training data (`x_train` and `y_train`).

Step 13: Make Predictions

- Use the `predict()` function on `model1` with `x_test` as the parameter.
- Assign the predictions to variable `pred`.

Step 14: Evaluate Model

- Display the confusion matrix.
- Display the classification report.

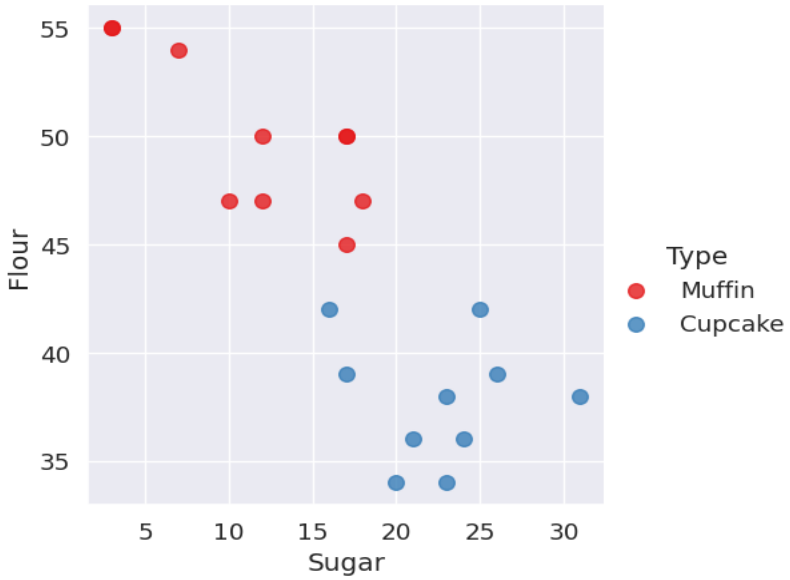
Code:

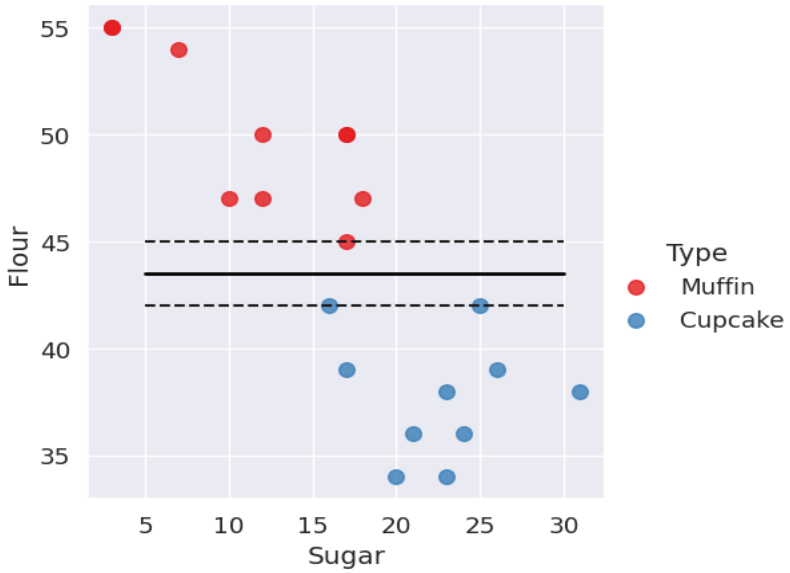
```
import numpy as np
import pandas as pd
from sklearn import svm
import matplotlib.pyplot as plt
import seaborn as sns
from sklearn.metrics import confusion_matrix, classification_report
from sklearn.model_selection import train_test_split

sns.set(font_scale=1.2)

recipes = pd.read_csv('recipes_muffins_cupcakes.csv')
print(recipes.head())
print(recipes.shape)

sns.lmplot(x='Sugar', y='Flour', data=recipes, hue='Type',
palette='Set1', fit_reg=False, scatter_kws={"s": 70})

sugar_butter = recipes[['Sugar', 'Flour']].values
type_label = np.where(recipes['Type'] == 'Muffin', 0, 1)

model = svm.SVC(kernel='linear')
model.fit(sugar_butter, type_label)

w = model.coef_[0]
a = - w[0] / w[1]
xx = np.linspace(5, 30)
yy = a * xx -  (model.intercept_[0] / w[1])
```

```
b = model.support_vectors_[0]
yy_down = a * xx + (b[1] -  a * b[0])

b = model.support_vectors_[- 1]
yy_up = a * xx + (b[1] -  a * b[0])

sns.lmplot(x='Sugar', y='Flour', data=recipes, hue='Type',
palette='Set1', fit_reg=False, scatter_kws={"s": 70})
plt.plot(xx, yy, linewidth=2, color='black')
plt.plot(xx, yy_down, 'k- - ')
plt.plot(xx, yy_up, 'k- - ')
plt.scatter(model.support_vectors_[:, 0], model.support_vectors_[:, 1],
s=80, facecolors='none')

x_train, x_test, y_train, y_test = train_test_split(sugar_butter,
type_label, test_size=0.2)
model1 = svm.SVC(kernel='linear')
model1.fit(x_train, y_train)
pred = model1.predict(x_test)

print(pred)
print(confusion_matrix(y_test, pred))
print(classification_report(y_test, pred, zero_division=1))

plt.show()
```

Output:

```
     Type  Flour  Milk  Sugar  Butter  Egg  Baking Powder  Vanilla  Salt
0  Muffin     55    28      3       7    5              2        0     0
1  Muffin     47    24     12       6    9              1        0     0
2  Muffin     47    23     18       6    4              1        0     0
3  Muffin     45    11     17      17    8              1        0     0
4  Muffin     50    25     12       6    5              2        1     0
(20, 9)
[1 0 1 0]
[[2 0]
 [0 2]]
              precision    recall  f1-score   support

           0       1.00      1.00      1.00         2
           1       1.00      1.00      1.00         2

    accuracy                           1.00         4
   macro avg       1.00      1.00      1.00         4
weighted avg       1.00      1.00      1.00         4
```





Result:

Thus, the python program to implement SVM classifier model has been successfully implemented and the results have been verified and analysed.

Ex. No.: 7
Date:

A PYTHON PROGRAM TO IMPLEMENT DECISION TREE

Aim:
To implement a decision tree using a python program for the given dataset and plot the trained decision tree.

Algorithm:
Step 1: Import the Iris Dataset
1. Import `load_iris` from `sklearn.datasets`.

Step 2: Import Necessary Libraries
1. Import numpy as np.
2. Import matplotlib.pyplot as plt.
3. Import `DecisionTreeClassifier` from `sklearn.tree`.

Step 3: Declare and Initialize Parameters
1. Declare and initialize `n_classes = 3`.
2. Declare and initialize `plot_colors = "ryb"`.
3. Declare and initialize `plot_step = 0.02`.

Step 4: Prepare Data for Model Training
1. Load the iris dataset using `load_iris()`.
2. Assign the dataset's data to variable `X`.
3. Assign the dataset's target to variable `Y`.

Step 5: Train the Model
1. Create an instance of `DecisionTreeClassifier`.
2. Fit the classifier using `clf.fit(X, Y)`.

Step 6: Initialize Pair Index and Plot Graph
1. Loop through each pair of features using `for pairidx, pair in enumerate(combinations (range(X.shape[1]), 2)):`
2. Inside the loop, assign `X` with the selected pair of features (e.g., `X = iris.data[:, pair]`).
3. Assign `Y` with the target list (e.g., `Y = iris.target`).

Step 7: Assign Axis Limits
1. Inside the loop, assign `x_min` with the minimum value of the selected feature minus 1 (e.g., `x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1`).

2. Assign `x_max` with the maximum value of the selected feature plus 1.
3. Assign `y_min` with the minimum value of the second selected feature minus 1 (e.g., `y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1`).
4. Assign `y_max` with the maximum value of the second selected feature plus 1.

Step 8: Create Meshgrid
1. Use `np.meshgrid` to create a grid of values from `x_min` to `x_max` and `y_min` to `y_max` with steps of `plot_step`.
2. Assign the results to variables `xx` and `yy`.

Step 9: Plot Graph with Tight Layout
1. Use `plt.tight_layout()` to adjust the layout of the plots.
2. Set `h_pad=0.5`, `w_pad=0.5`, and `pad=2.5`.

Step 10: Predict and Reshape
1. Use the classifier to predict on the meshgrid (e.g., `Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])`).
2. Reshape `Z` to the shape of `xx`.

Step 11: Plot Decision Boundary
1. Use `plt.contourf(xx, yy, Z, cmap=plt.cm.RdYlBu)` to plot the decision boundary with the "RdYlBu" color scheme.

Step 12: Plot Feature Pairs
1. Inside the loop, label the x- axis and y- axis with the feature names (e.g., `plt.xlabel(iris.feature_names[pair[0]])` and `plt.ylabel(iris.feature_names[pair[1]])`).

Step 13: Plot Training Points
1. Use `plt.scatter(X[:, 0], X[:, 1], c=Y, cmap=plt.cm.RdYlBu, edgecolor='k', s=15)` to plot the training points with the

"RdYlBu" color scheme, black edge color, and size 15.

Step 14: Plot Final Decision Tree
1. Set the title of the plot to "Decision tree trained on all the iris features" (e.g., `plt.title("Decision tree trained on all the iris features")`).
2. Display the plot using `plt.show()`.

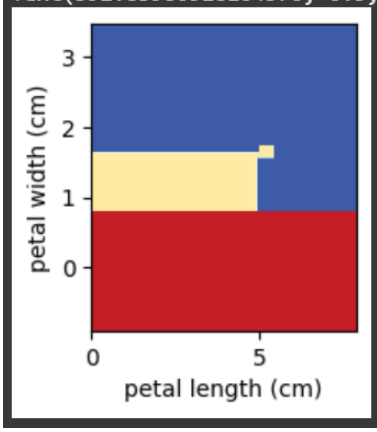
Code:

```
from sklearn.datasets import load_iris
iris = load_iris()
import numpy as np
import matplotlib.pyplot as plt
from sklearn.tree import DecisionTreeClassifier

# Parameters
n_classes = 3
plot_colors = "ryb"
plot_step = 0.02
for pairidx, pair in enumerate([[0, 1], [0, 2], [0, 3], [1, 2], [1, 3], [2, 3]]):
  # We only take the two corresponding features
  X = iris.data[:, pair]
  y = iris.target

# Train
clf = DecisionTreeClassifier().fit(X, y)

# Plot the decision boundary
plt.subplot(2, 3, pairidx + 1)
x_min, x_max = X[:, 0].min() -  1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() -  1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, plot_step), np.arange(y_min, y_max, plot_step))
plt.tight_layout(h_pad=0.5, w_pad=0.5, pad=2.5)
```

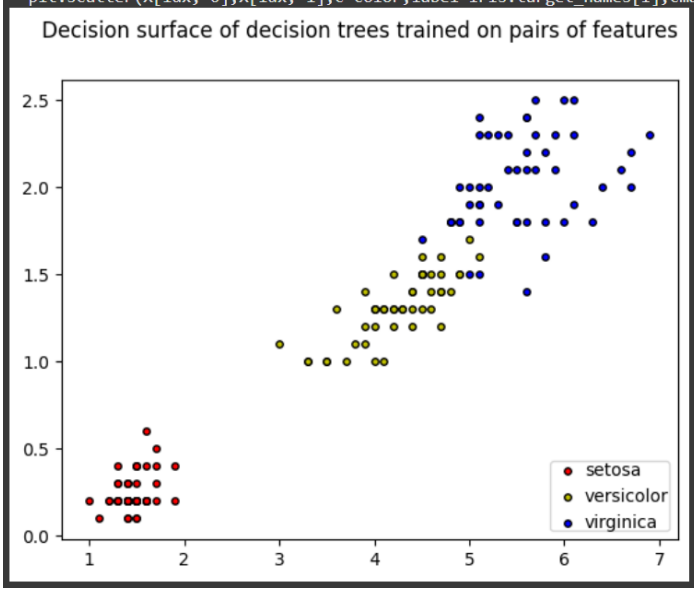
```
Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
cs = plt.contourf(xx, yy, Z, cmap=plt.cm.RdYlBu)
plt.xlabel(iris.feature_names[pair[0]])
plt.ylabel(iris.feature_names[pair[1]])

# Plot the training points
for i, color in zip(range(n_classes), plot_colors):
  idx = np.where(y == i)
  plt.scatter(X[idx, 0],X[idx,
1],c=color,label=iris.target_names[i],cmap=plt.cm.RdYlBu,e
dgecolor="black",s=15)
plt.suptitle("Decision surface of decision trees trained on
pairs of features")
plt.legend(loc="lower right", borderpad=0,
handletextpad=0)
plt.axis("tight")
plt.show()

from sklearn.tree import plot_tree
plt.figure()
clf = DecisionTreeClassifier().fit(iris.data,iris.target)
plot_tree(clf, filled=True)
plt.title("Decision tree trained on all the iris features")
plt.show()
```

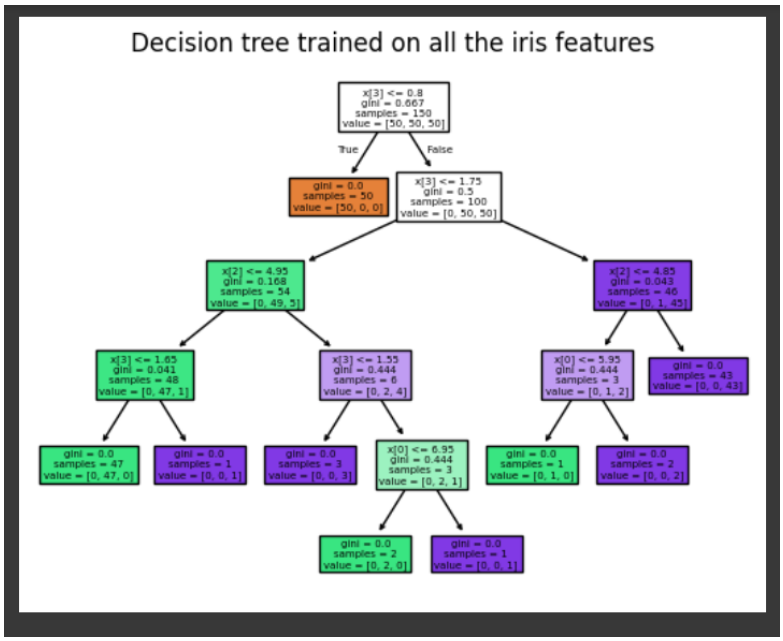
OUTPUT:

```
Text(392.83986928104576, 0.5, 'petal width (cm)')
```




```
<ipython-input-14-332623287b3a>:4: UserWarning: No data for colormapping provided via 'c'. Parameters 'cmap' will be ignored
  plt.scatter(X[idx, 0],X[idx, 1],c=color,label=iris.target_names[i],cmap=plt.cm.RdYlBu,edgecolor="black",s=15)
```





Result:

Thus, the python program to implement Decision Tree has been successfully implemented and the results have been

verified and analysed.

Ex. No.: 8

Date:

A PYTHON PROGRAM TO IMPLEMENT ADA BOOSTING

Aim:
To implement a python program for Ada Boosting.

Algorithm:
Step 1: Import Necessary Libraries
Import numpy as np.
Import pandas as pd.
Import DecisionTreeClassifier from sklearn.tree.
Import train_test_split from sklearn.model_selection.
Import accuracy_score from sklearn.metrics.
Step 2: Load and Prepare Data
Load your dataset using pd.read_csv() (e.g., df = pd.read_csv('data.csv')).
Separate features (X) and target (y).
Split the dataset into training and testing sets using train_test_split().
Step 3: Initialize Parameters
Set the number of weak classifiers n_estimators.
Initialize an array weights for instance weights, setting each weight to 1 / number_of_samples.
Step 4: Train Weak Classifiers
Loop for n_estimators iterations:
Train a weak classifier using DecisionTreeClassifier(max_depth=1) on the training data weighted by weights.
Predict the target values using the trained weak classifier.
Calculate the error rate err as the sum of weights of misclassified samples divided by the sum of all weights.
Compute the classifier's weight alpha using 0.5 * np.log((1 - err) / err).
Update the weights: multiply the weights of misclassified

samples by np.exp(alpha) and the weights of correctly classified samples by np.exp(- alpha).
Normalize the weights so that they sum to 1.
Append the trained classifier and its weight to lists classifiers and alphas.
Step 5: Make Predictions
For each sample in the testing set:
Initialize a prediction score to 0.
For each trained classifier and its weight:
Add the classifier's prediction (multiplied by its weight) to the prediction score.
Take the sign of the prediction score as the final prediction.
Step 6: Evaluate the Model
Compute the accuracy of the AdaBoost model on the testing set using accuracy_score().
Step 7: Output Results
Print or plot the final accuracy and possibly other evaluation metrics.

Code:

```
import pandas as pd
import numpy as np
from mlxtend.plotting import plot_decision_regions
df = pd.DataFrame()
df['X1']=[1,2,3,4,5,6,6,7,9,9]
df['X2']=[5,3,6,8,1,9,5,8,9,2]
df['label']=[1,1,0,1,0,1,0,1,0,0]
import seaborn as sns
sns.scatterplot(x=df['X1'],y=df['X2'],hue=df['label'])
df['weights']=1/df.shape[0]

from sklearn.tree import DecisionTreeClassifier

dt1 = DecisionTreeClassifier(max_depth=1)
x = df.iloc[:,0:2].values
```

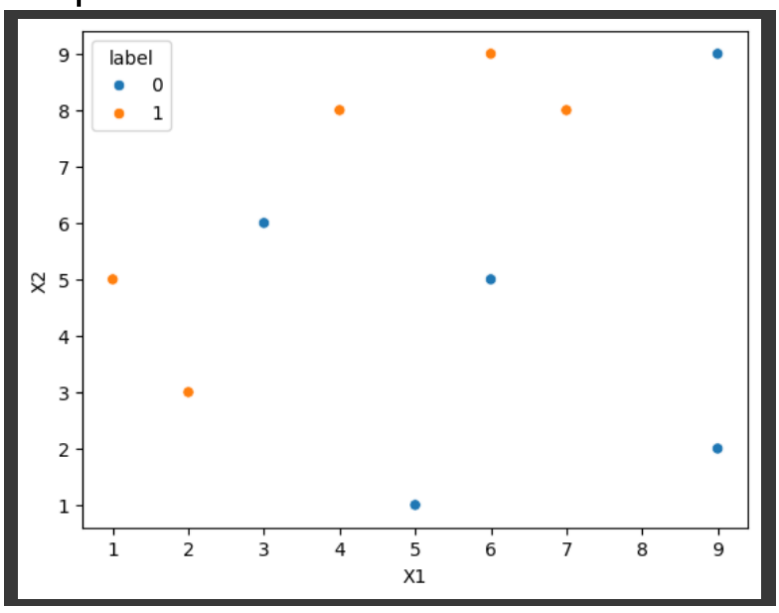
```
y = df.iloc[:,2].values
# Step 2 -  Train 1st Model

dt1.fit(x,y)
from sklearn.tree import plot_tree

plot_decision_regions (x,y,clf=dt1, legend=2)
df['y pred'] = dt1.predict(x)

def calculate_model_weight(error):
  return 0.5*np.log((1- error)/(error))

# Step -  3 Calculate model weight
alpha1 = calculate_model_weight(0.3)
alpha1

# Step - 4 Update weights
def update_row_weights(row,alpha=0.423):
    if row['label'] == row['y_pred']:
        return row['weights']* np.exp(- alpha)
    else:
        return row['weights']* np.exp(alpha)
df['updated_weights'] =
df.apply(update_row_weights,axis=1)

df['normalized_weights'] = df['updated_weights'] /
df['updated_weights'].sum() # Calculating normalized
weights by dividing updated weights by sum of all updated
weights

df['normalized_weights'].sum()

df['cumsum_upper'] =
np.cumsum(df['normalized_weights'])
df['cumsum_lower']=df['cumsum_upper'] -
```

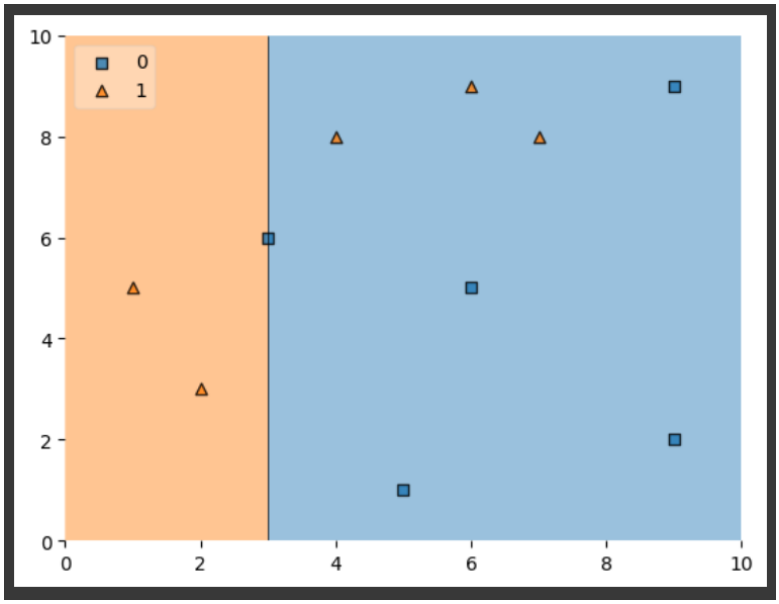
```
df['normalized_weights']
df[['X1','X2','label','weights','y_pred','updated_weights','cum
sum_lower','cumsum_upper']]

def create_new_dataset(df):
    indices= []
    for i in range(df.shape[0]):
        a = np.random.random()
        for index,row in df.iterrows():
            if row['cumsum_upper']>a and
a>row['cumsum_lower']:
                indices.append(index)
    return indices
index_values =  create_new_dataset(df)
index_values

second_df = df.iloc[index_values,[0,1,2,3]]
second_df

dt2 = DecisionTreeClassifier(max_depth=1)

x = second_df.iloc[:,0:2].values
y = second_df.iloc[:,2].values

dt2.fit(x,y)

plot_tree(dt2)

plot_decision_regions(x, y, clf=dt2, legend=2)

second_df['y_pred'] = dt2.predict(x)
second_df
alpha2 = calculate_model_weight(0.1)
alpha2
```

```
# Step 4 -  Update weights
def update_row_weights(row,alpha=1.09):
    if row['label'] == row['y_pred']:
        return row['weights'] * np.exp(- alpha)
    else:
        return row['weights'] * np.exp(alpha)

second_df['updated_weights'] =
second_df.apply(update_row_weights,axis=1)
second_df
second_df['normalized_weights'] =
second_df['updated_weights'] /
second_df['updated_weights'].sum()

second_df['normalized_weights'].sum()
second_df['cumsum_upper'] =
np.cumsum(second_df['normalized_weights'])
second_df['cumsum_lower'] = second_df['cumsum_upper']
-  second_df['normalized_weights']
second_df[['X1','X2','label','weights','y_pred','normalized_we
ights','cumsum_lower','cumsum_upper']]

alpha3 = calculate_model_weight(0.7)
alpha3

from sklearn.tree import DecisionTreeClassifier

print(alpha1,alpha2,alpha3)

dt3 = DecisionTreeClassifier(max_depth=2)

# Fit dt3 before making predictions
dt3.fit(x, y) # Assuming 'x' and 'y' are your training data
from previous cells.
```

```
query = np.array([1,5]).reshape(1,2)
dt1.predict(query)
dt2.predict(query)
dt3.predict(query)

alpha1*1 + alpha2*(1) + alpha3*(1)

np.sign(1.09)

query = np.array([9,9]).reshape(1,2)
dt1.predict(query)

dt2.predict(query)

dt3.predict(query)

alpha1*(1) + alpha2*(- 1) + alpha3*(- 1)

np.sign(- 0.25)
```

Output:

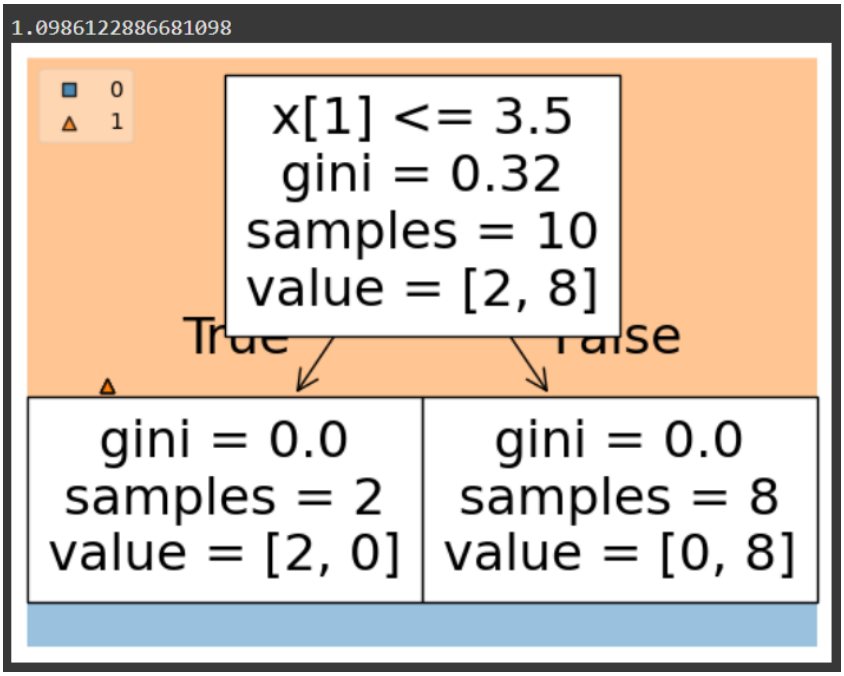




	X1	X2	label	weights	y_pred	updated_weights	cumsum_lower	cumsum_upper
0	1	5	1	0.1	1	0.065508	0.000000	0.071475
1	2	3	1	0.1	1	0.065508	0.071475	0.142950
2	3	6	0	0.1	0	0.065508	0.142950	0.214425
3	4	8	1	0.1	0	0.152653	0.214425	0.380983
4	5	1	0	0.1	0	0.065508	0.380983	0.452458
5	6	9	1	0.1	0	0.152653	0.452458	0.619017
6	6	5	0	0.1	0	0.065508	0.619017	0.690492
7	7	8	1	0.1	0	0.152653	0.690492	0.857050
8	9	9	0	0.1	0	0.065508	0.857050	0.928525
9	9	2	0	0.1	0	0.065508	0.928525	1.000000

	X1	X2	label	weights
5	6	9	1	0.1
0	1	5	1	0.1
0	1	5	1	0.1
9	9	2	0	0.1
5	6	9	1	0.1
9	9	2	0	0.1
3	4	8	1	0.1
0	1	5	1	0.1
3	4	8	1	0.1
0	1	5	1	0.1

```
1.0986122886681098
```




```
0.9999999999999999
```

```
-0.4236489301936017
```

```
0.42364893019360184 1.0986122886681098 -0.4236489301936017
-1.0
```

Result:
Thus the python program to implement ADA Boosting has been successfully implemented and the results have been verified and analyzed.

Ex. No.: 9
Date:

A PYTHON PROGRAM TO IMPLEMENT KNN MODEL

Aim:
To implement a python program using a KNN Algorithm in a model.

Algorithm:

1. Import Necessary Libraries

- Import necessary libraries: pandas, numpy, train_test_split from sklearn.model_selection, StandardScaler from sklearn.preprocessing, KNeighborsClassifier from sklearn.neighbors, and classification_report and confusion_matrix from sklearn.metrics.

2. Load and Explore the Dataset

- Load the dataset using pandas.
- Display the first few rows of the dataset using df.head().
- Display the dimensions of the dataset using df.shape().
- Display the descriptive statistics of the dataset using df.describe().

0. Preprocess the Data

- Separate the features (X) and the target variable (y).
- Split the data into training and testing sets using train_test_split.
- Standardize the features using StandardScaler.

0. Train the KNN Model

- Create an instance of KNeighborsClassifier with a specified number of neighbors (k).
- For each data point, calculate the Euclidean distance to all other data points.
- Select the K nearest neighbors based on the calculated Euclidean distances.
- Among the K nearest neighbors, count the number of data points in each category.
- Assign the new data point to the category for which the number of neighbors is maximum.

0. Make Predictions

- Use the trained model to make predictions on the test data.

- Evaluate the Model
- Generate the confusion matrix and classification report using the actual and predicted values.
- Print the confusion matrix and classification report.

Code:

```
import numpy as np
import matplotlib.pyplot as plt
import pandas as pd

dataset = pd.read_csv('../input/mall- customers/
Mall_Customers.csv')
X = dataset.iloc[:,[3,4]].values
print(dataset)

from sklearn.cluster import KMeans
wcss =[]
for i in range (1,11):
    kmeans = KMeans(n_clusters = i, init = 'k- means++',
max_iter =300, n_init = 10, random_state = 0)
    kmeans.fit(X)
    wcss.append(kmeans.inertia_)

# Plot the graph to visualize the Elbow Method to find the
optimal number of cluster
plt.plot(range(1,11),wcss)
plt.title('The Elbow Method')
plt.xlabel('Number of clusters')
plt.ylabel('WCSS')
plt.show()

kmeans=KMeans(n_clusters= 5, init = 'k- means++',
max_iter = 300, n_init = 10, random_state = 0)
y_kmeans = kmeans.fit_predict(X)
```

```
y_kmeans

type(y_kmeans)

y_kmeans

plt.scatter(X[y_kmeans == 0, 0], X[y_kmeans == 0, 1], s =
100, c = 'red', label = 'Cluster 1')

plt.scatter(X[y_kmeans == 1, 0], X[y_kmeans == 1, 1], s =
100, c = 'blue', label = 'Cluster 2')

plt.scatter(X[y_kmeans == 2, 0], X[y_kmeans == 2, 1], s =
100, c = 'green', label = 'Cluster 3')

plt.scatter(X[y_kmeans == 3, 0], X[y_kmeans == 3, 1], s =
100, c = 'cyan', label = 'Cluster 4')

plt.scatter(X[y_kmeans == 4, 0], X[y_kmeans == 4, 1], s =
100, c = 'magenta', label = 'Cluster 5')

plt.scatter(kmeans.cluster_centers_[:, 0],
kmeans.cluster_centers_[:, 1], s = 300, c = 'yellow', label =
'Centroids')

plt.title('Clusters of customers')
plt.xlabel('Annual Income (k$)')
plt.ylabel('Spending Score (1- 100)')
plt.legend()
plt.show()

plt.scatter(X[y_kmeans == 0, 0], X[y_kmeans == 0, 1], s =
100, c = 'red', label = 'Cluster 1')
plt.scatter(X[y_kmeans == 1, 0], X[y_kmeans == 1, 1], s =
100, c = 'blue', label = 'Cluster 2')
```

```
plt.scatter(X[y_kmeans == 2, 0], X[y_kmeans == 2, 1], s =
100, c = 'green', label = 'Cluster 3')
plt.scatter(X[y_kmeans == 3, 0], X[y_kmeans == 3, 1], s =
100, c = 'cyan', label = 'Cluster 4')
plt.scatter(X[y_kmeans == 4, 0], X[y_kmeans == 4, 1], s =
100, c = 'magenta', label = 'Cluster 5')
plt.scatter(kmeans.cluster_centers_[:, 0],
kmeans.cluster_centers_[:, 1], s = 300, c = 'yellow', label =
'Centroids')
plt.title('Clusters of customers')
plt.xlabel('Annual Income (k$)')
plt.ylabel('Spending Score (1- 100)')
plt.legend()
plt.show()
```

Output
:- -

Result: -

Thus the python program to implement KNN model has been successfully implemented and the results have been verified and analyzed.

Ex. No.: 10
Date:

A PYTHON PROGRAM TO IMPLEMENT DIMENSIONALITY REDUCTION USING PCA

Aim:
To implement Dimensionality Reduction using PCA in a python program.

Algorithm:
Step 1: Import Libraries
Import necessary libraries, including pandas, numpy, matplotlib.pyplot, and sklearn.decomposition.PCA.
Step 2: Load the Dataset (iris dataset)
Load your dataset into a pandas DataFrame.
Step 3: Standardize the Data
Standardize the features of the dataset using StandardScaler from sklearn.preprocessing.
Step 4: Apply PCA

- Create an instance of PCA with the desired number of components.
- Fit PCA to the standardized data.
- Transform the data to its principal components using transform.

Step 5: Explained Variance Ratio

- Calculate the explained variance ratio for each principal component.
- Plot a scree plot to visualize the explained variance ratio.

Step 6: Choose the Number of Components
Based on the scree plot, choose the number of principal components that explain a significant amount of variance.
Step 7: Apply PCA with Chosen Components

Apply PCA again with the chosen number of components.
Step 8: Visualize the Reduced Data

- Transform the original data to the reduced dimension using the fitted PCA.
- Visualize the reduced data using a scatter plot.

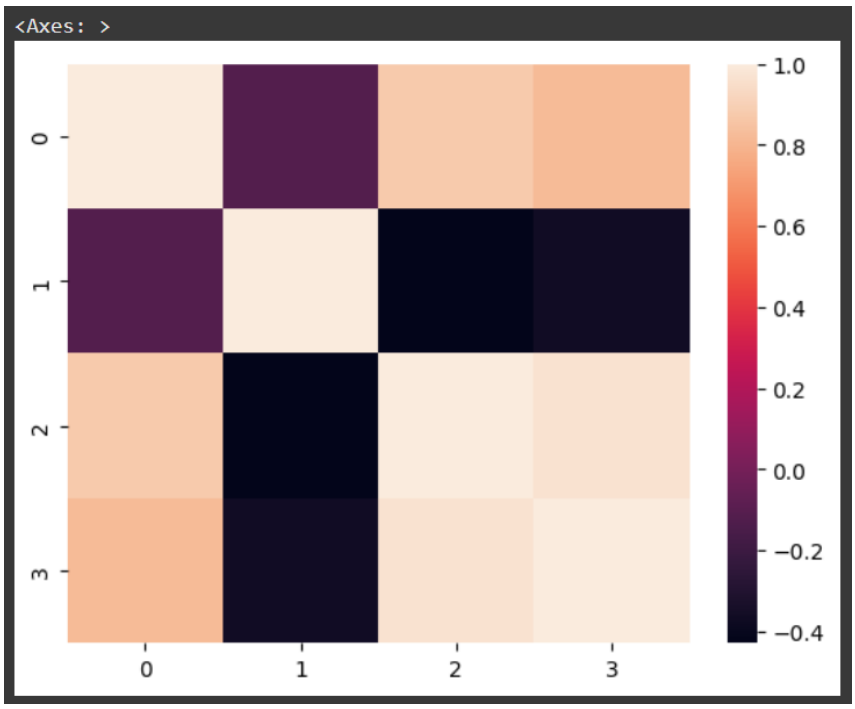
Step 9: Interpretation
Interpret the results, considering the trade- offs between dimensionality reduction and information loss.

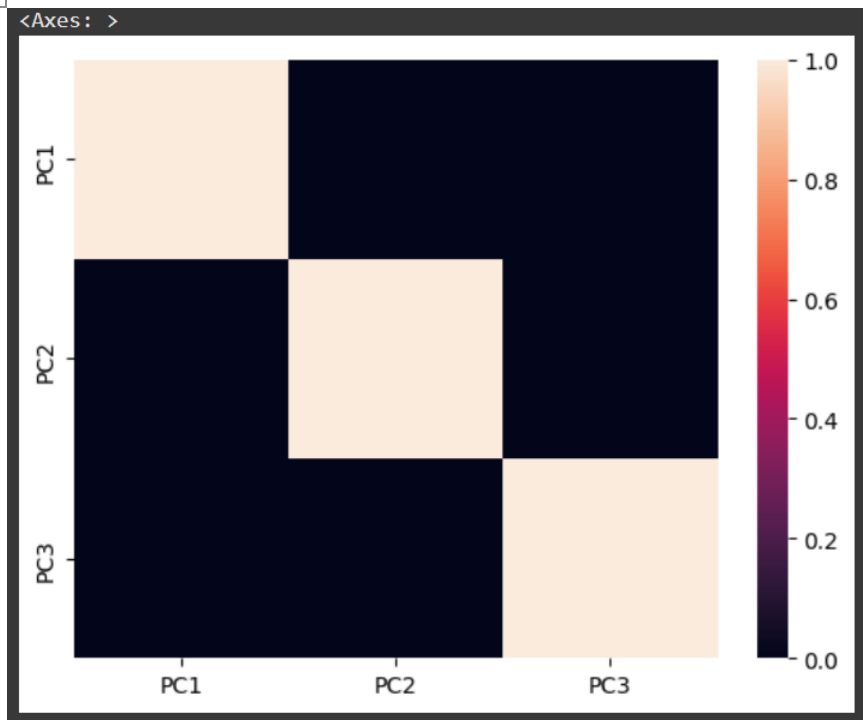
Code:

```
from sklearn import datasets
import pandas as pd
from sklearn.preprocessing import StandardScaler
from sklearn.decomposition import PCA
import seaborn as sns
iris = datasets.load_iris()
df = pd.DataFrame(iris['data'], columns =
iris['feature_names'])
df.head()

scalar = StandardScaler()
scaled_data = pd.DataFrame(scalar.fit_transform(df))
#scaling the data
scaled_data

sns.heatmap(scaled_data.corr())

pca = PCA(n_components = 3)
pca.fit(scaled_data)
data_pca = pca.transform(scaled_data)
data_pca =
pd.DataFrame(data_pca,columns=['PC1','PC2','PC3'])
data_pca.head()
sns.heatmap(data_pca.corr())
```

Output:

	sepal length (cm)	sepal width (cm)	petal length (cm)	petal width (cm)
0	5.1	3.5	1.4	0.2
1	4.9	3.0	1.4	0.2
2	4.7	3.2	1.3	0.2
3	4.6	3.1	1.5	0.2
4	5.0	3.6	1.4	0.2





Result:
Thus the python program to implement Dimensionality Reduction using PCA has been successfully implemented and the results have been verified and analyzed.