

# Activity Analysis: Finding Explanations for Sets of Events

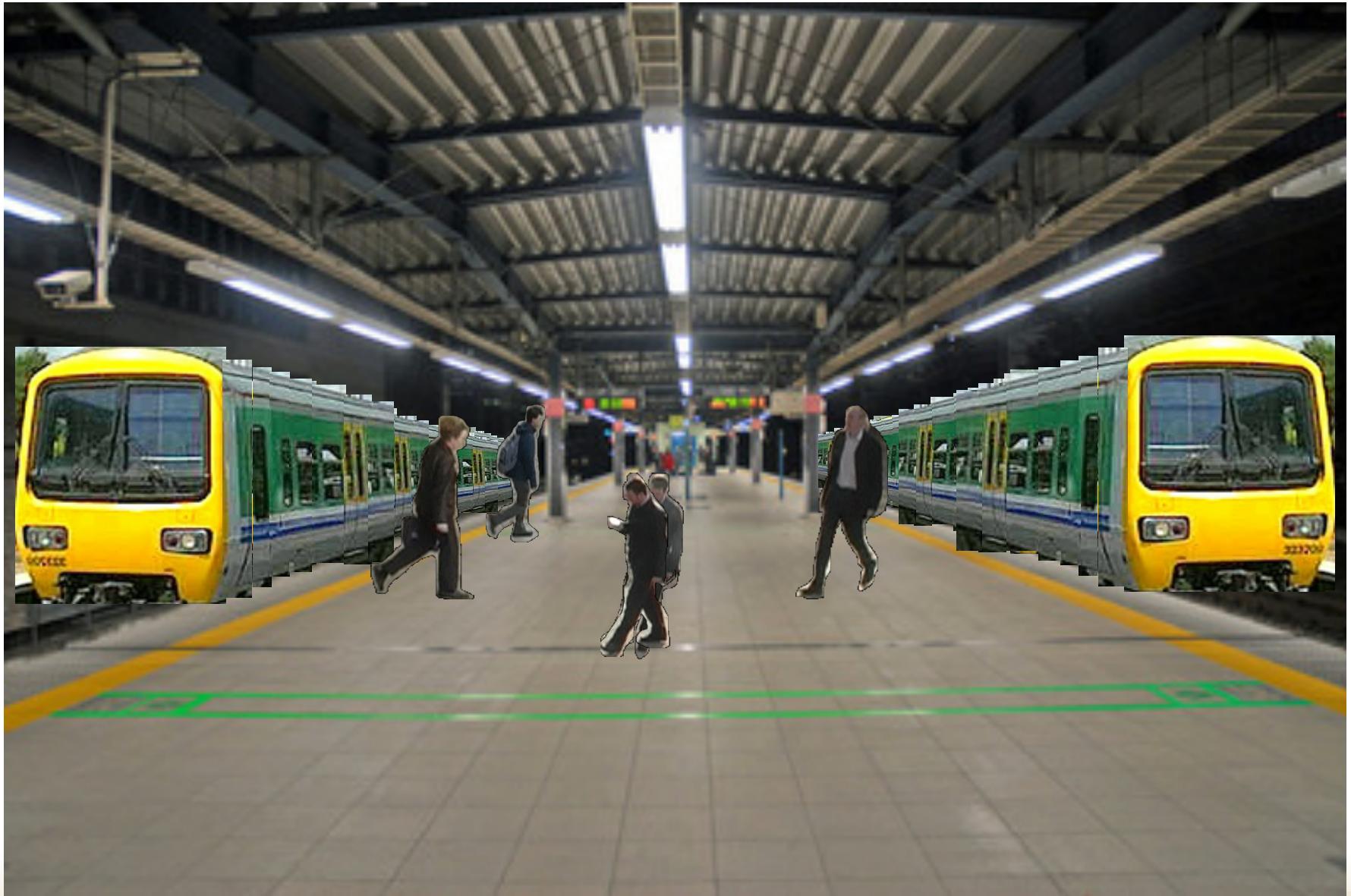
Dima Damen, David Hogg  
Computer Vision Group



# Activity Recognition



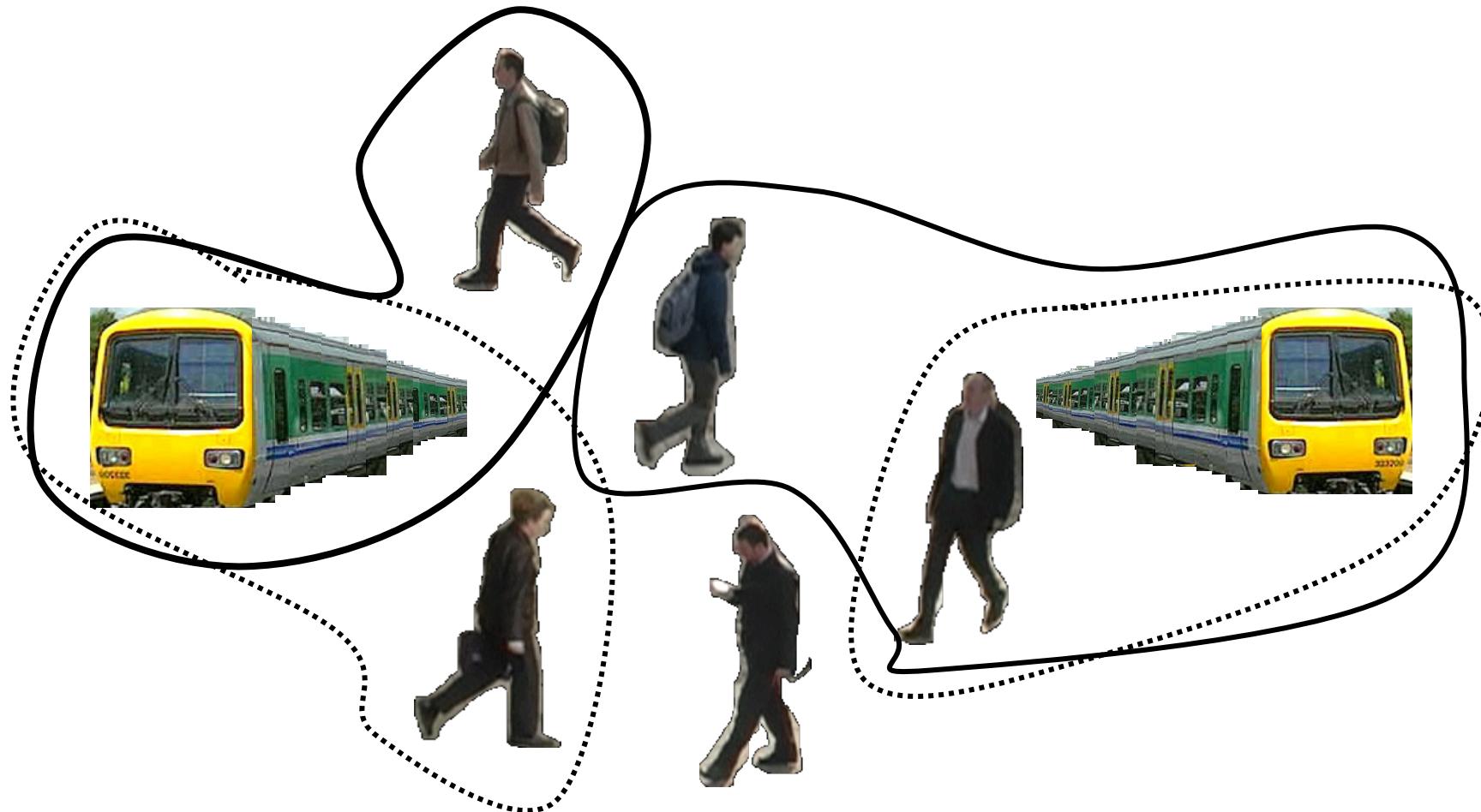
# Activity Recognition



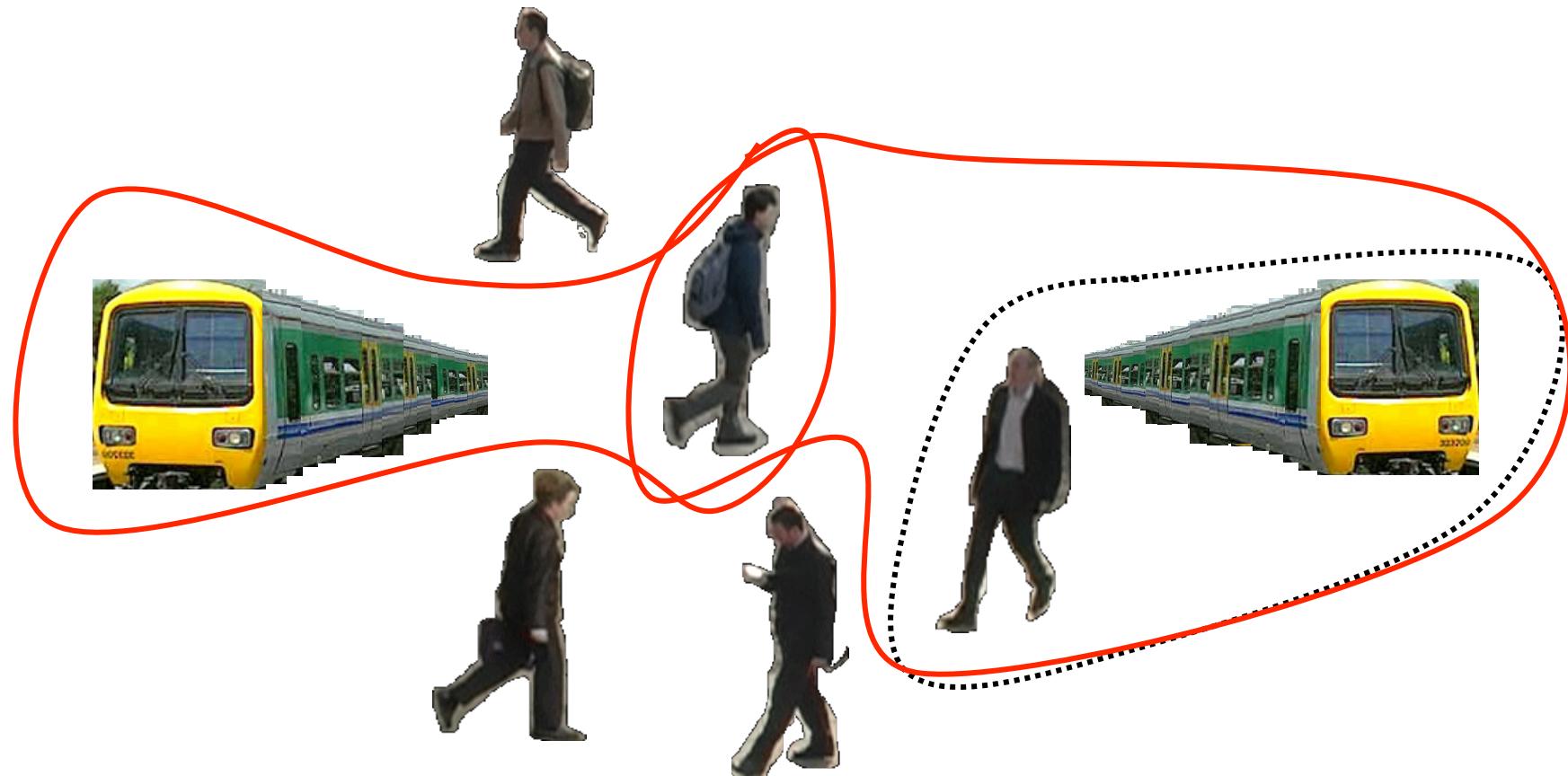
# Activity Recognition



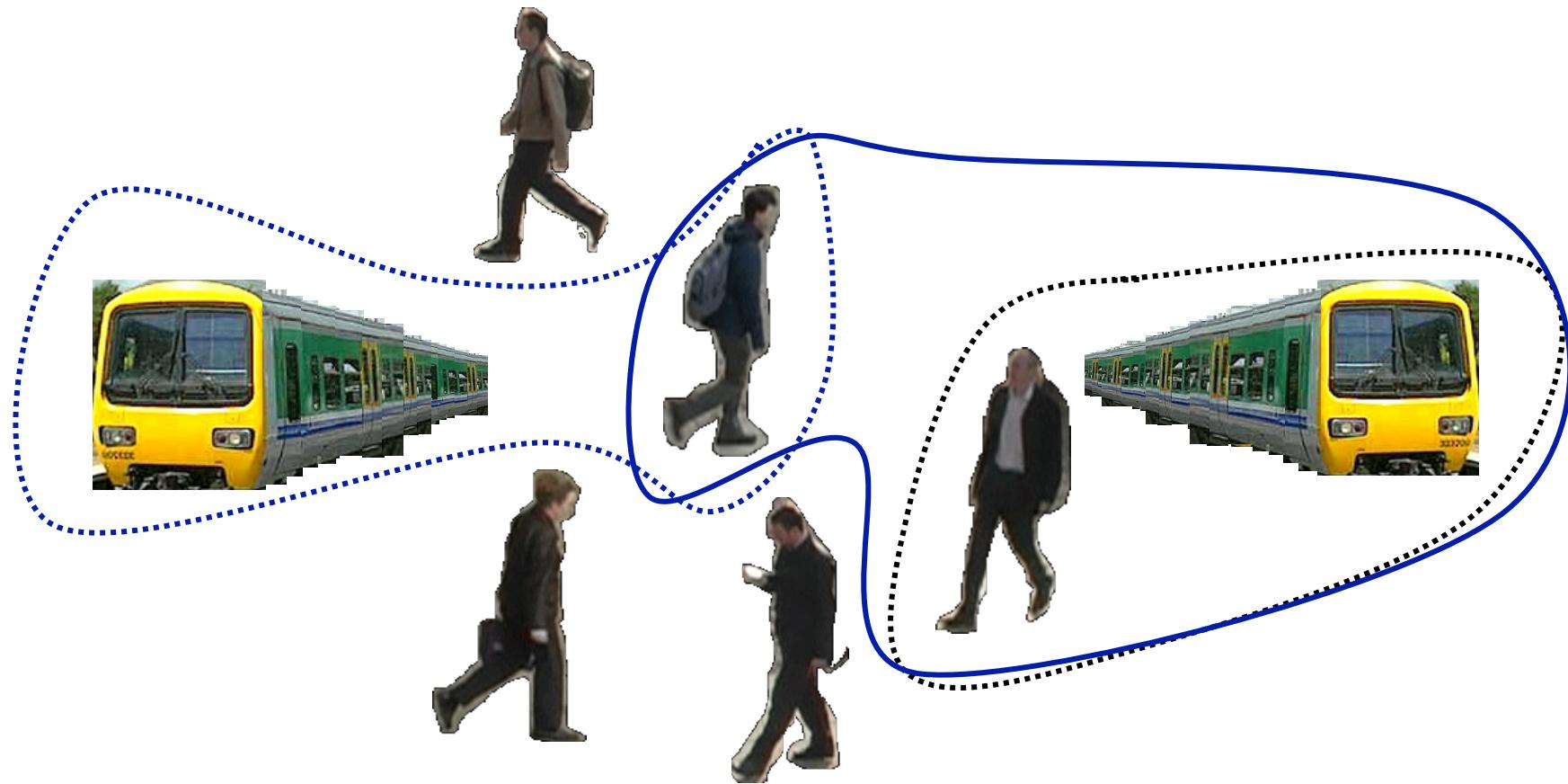
# Activity Recognition



# Activity Recognition

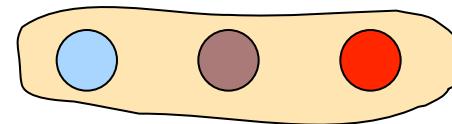


# Activity Recognition

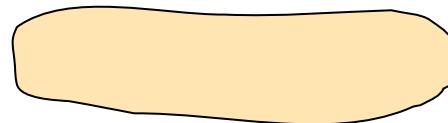


# Activity Recognition

## Event Definition

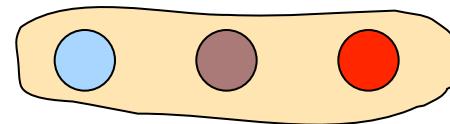


1 event

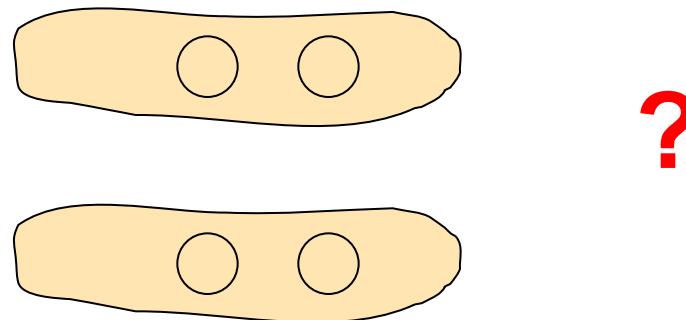


# Activity Recognition

## Event Definition

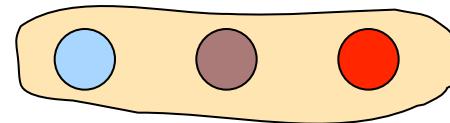


## Event Threads

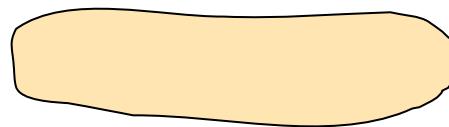
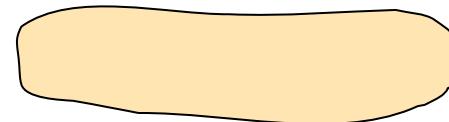


# Activity Recognition

**Event Definition**

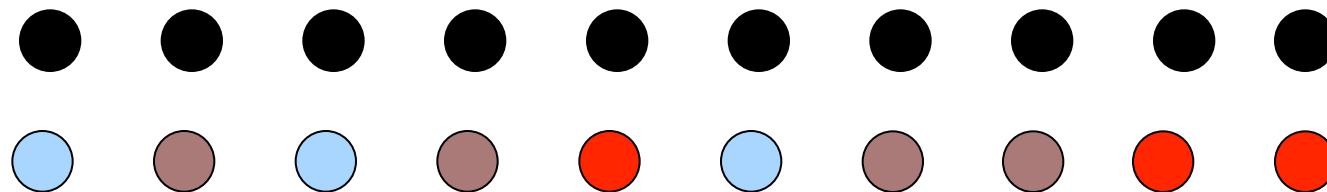


**Global Explanation**

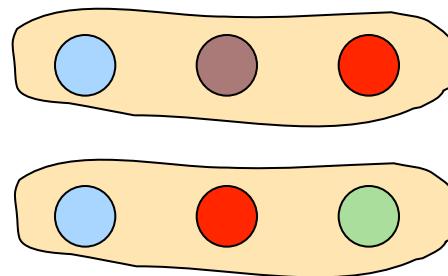


# Activity Recognition

- Uncertain detections



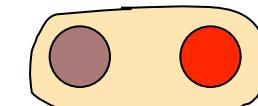
- Multiple definitions



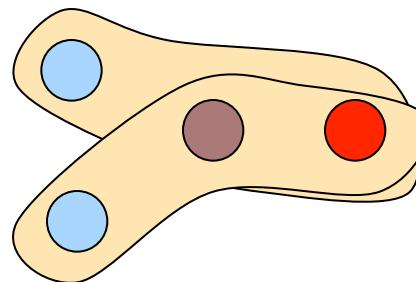
# Activity Recognition

- Intra-activity constraints
  - Temporal Constraints
  - Spatial Constraints
  - Other Geometric Constraints

pos = pos  
time < time  

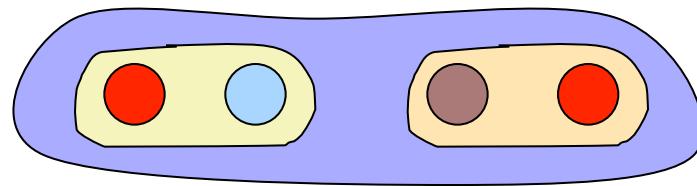



- Inter-activity constraints

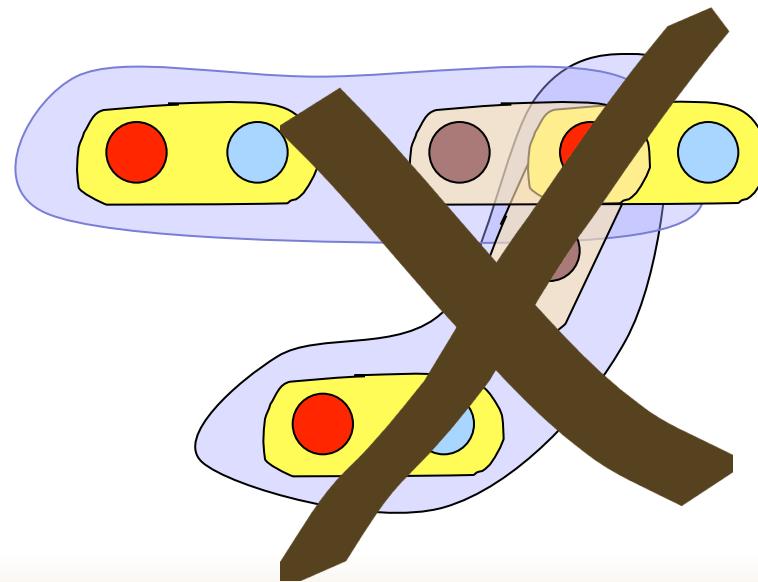
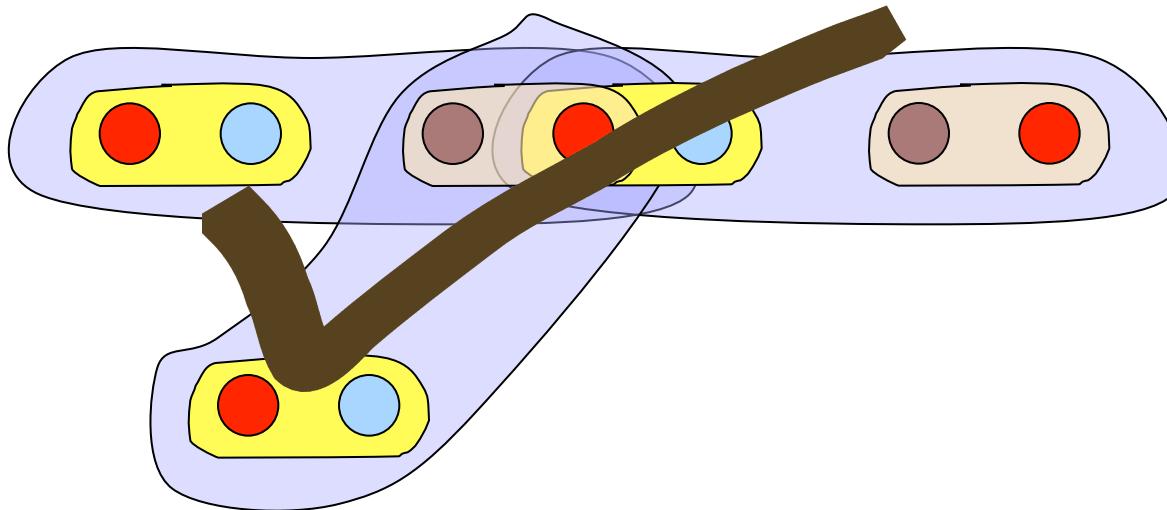


# Activity Recognition

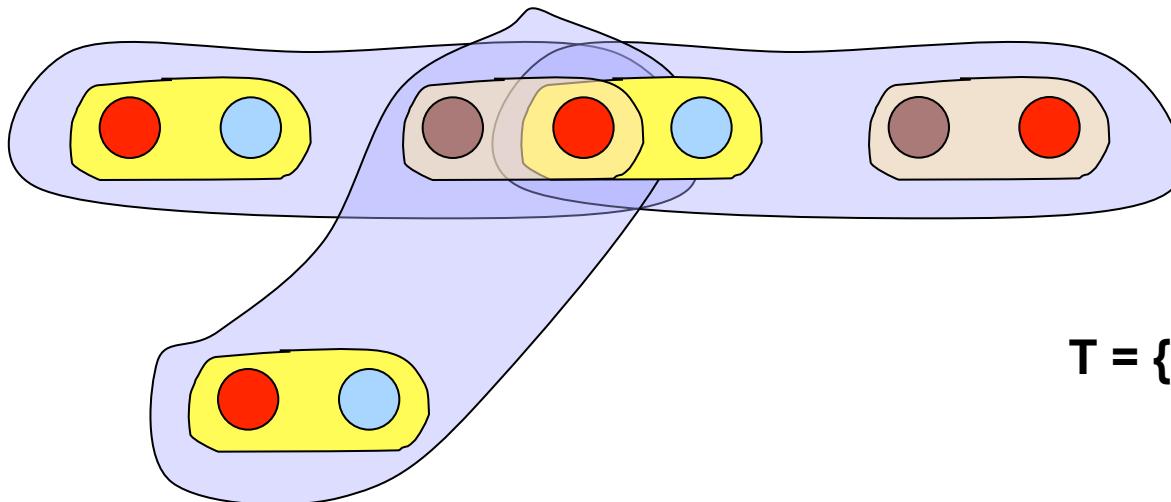
- Complex events



# Definition using AMG



# Definition using AMG



$$T = \{ \begin{matrix} \text{red circle} \\ \downarrow \\ a \end{matrix}, \begin{matrix} \text{blue circle} \\ \downarrow \\ b \end{matrix}, \begin{matrix} \text{brown circle} \\ \downarrow \\ c \end{matrix} \}$$

$$N = \{ \begin{matrix} \text{yellow square} \\ \downarrow \\ A \end{matrix}, \begin{matrix} \text{orange square} \\ \downarrow \\ E \end{matrix}, \begin{matrix} \text{purple square} \\ \downarrow \\ D \end{matrix} \}$$

**Synthetic Rule**

$$A \rightarrow a, b$$

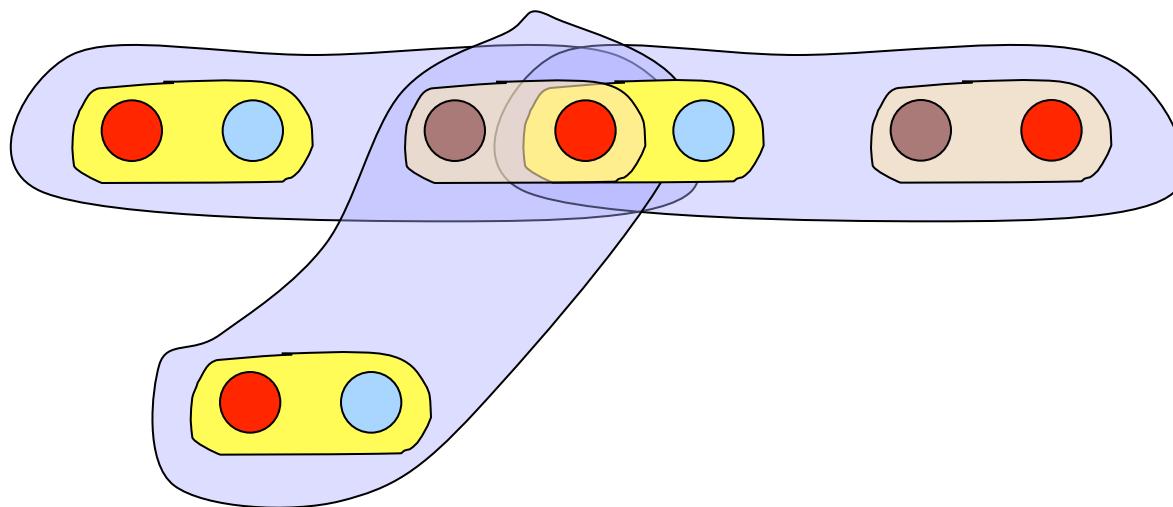
**Attribute Rule**

...

**Attribute Constraints**

$$a.\text{time} < b.\text{time}$$

# Definition using AMG



$E \rightarrow a, c$

$c.count < 1$

$D \rightarrow A, E$

....

**Synthetic Rule**

$A \rightarrow a, b$

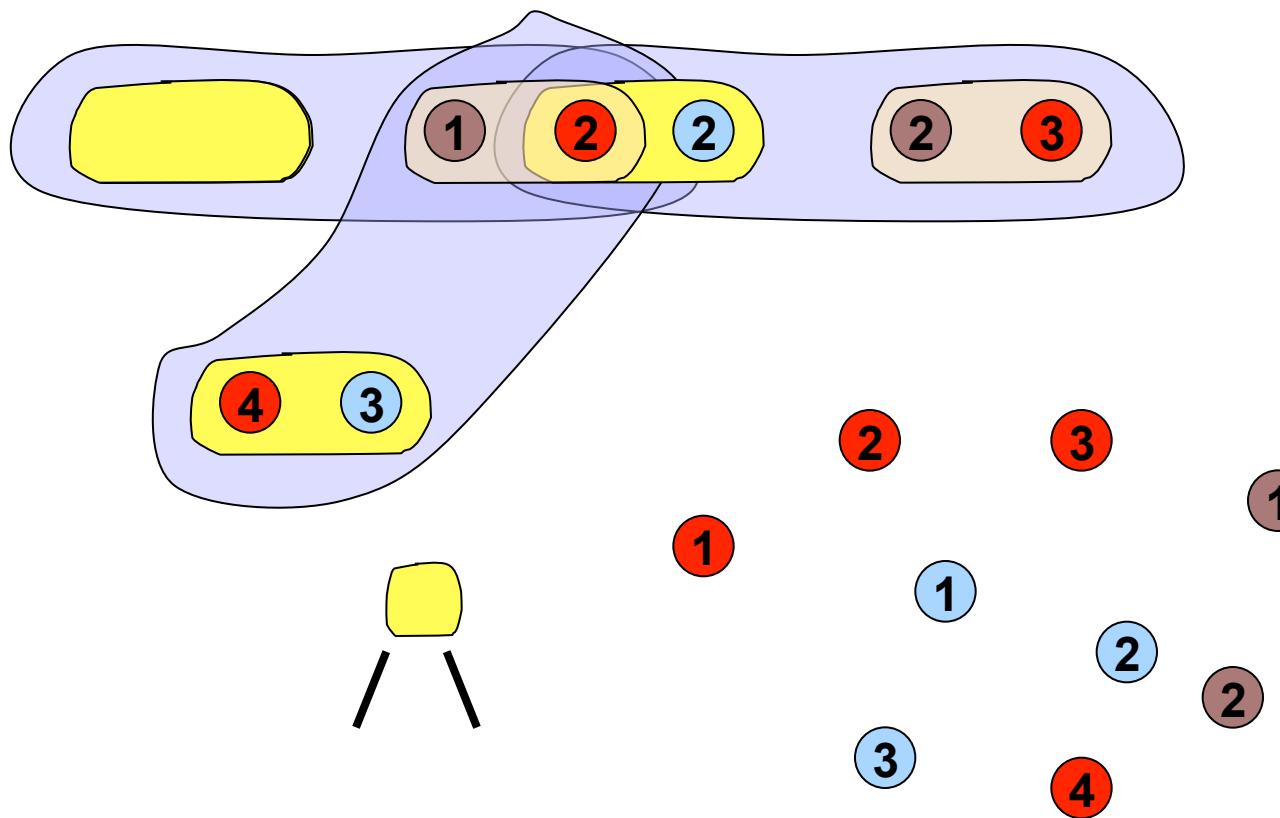
**Attribute Rule**

...

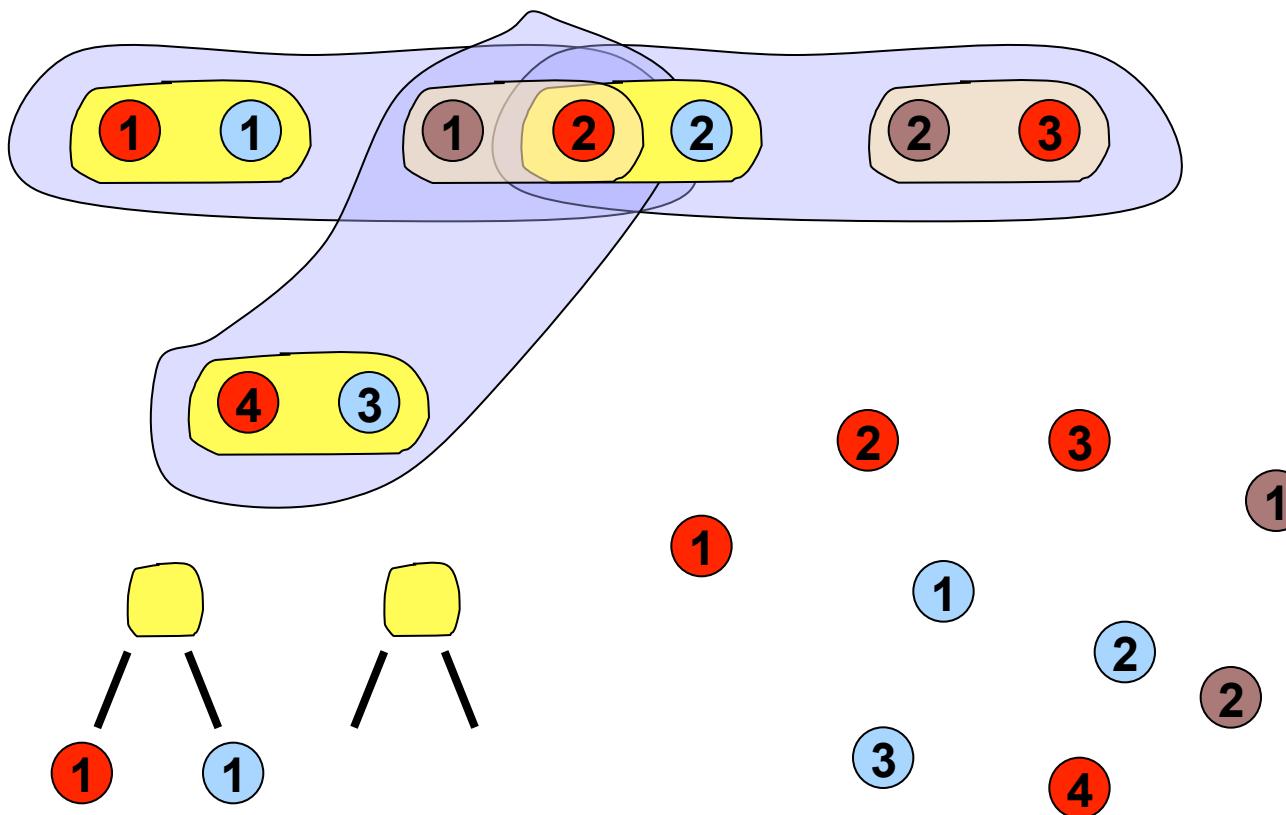
**Attribute Constraints**

$a.time < b.time$

# Definition using AMG



# Definition using AMG



Syntactic Rule

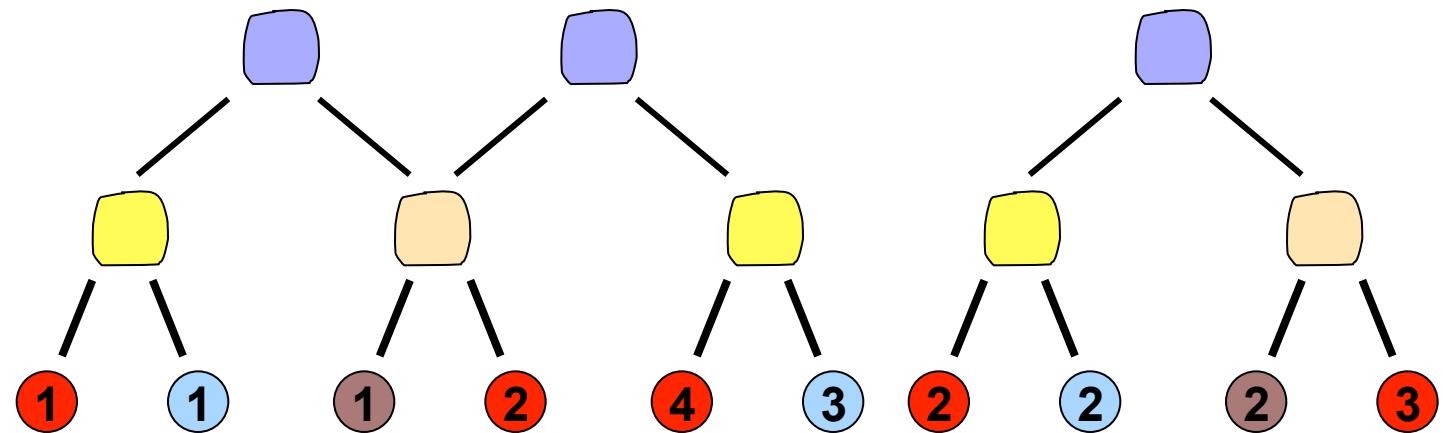
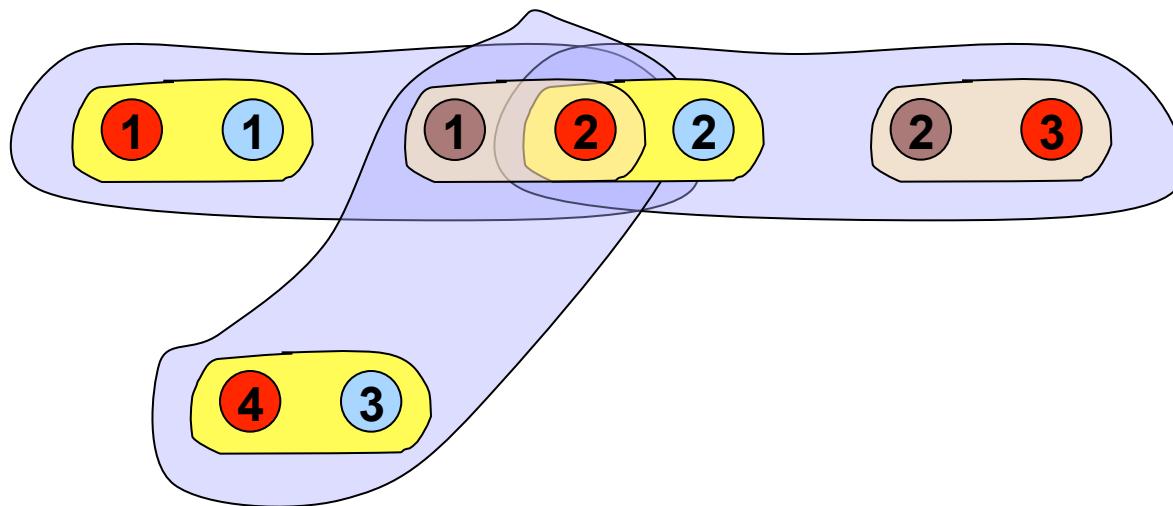
$$A \rightarrow a, b A.dist = a.pos - b.pos$$

Attribute Rule

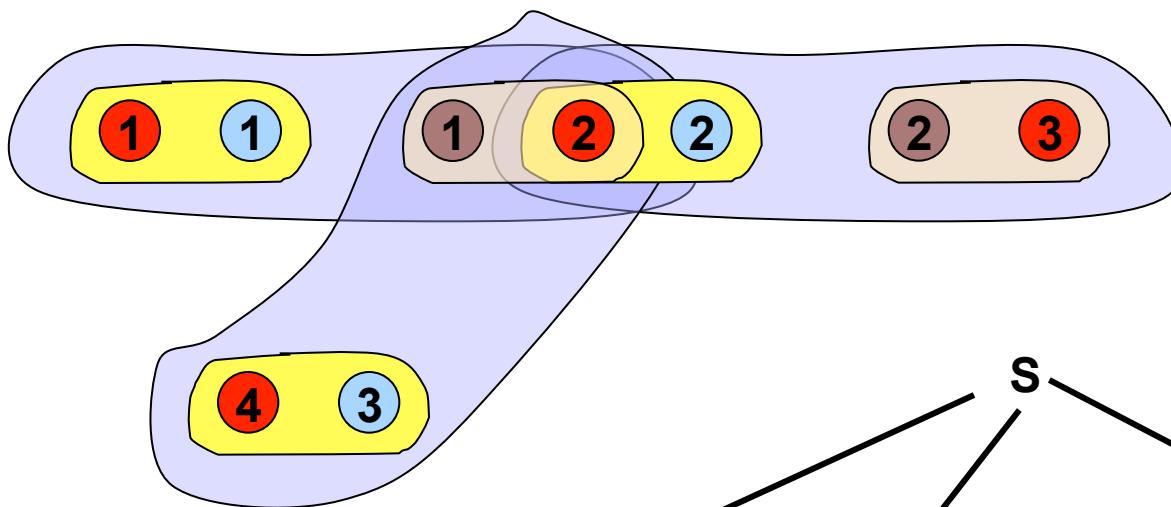
Attribute Constraints

$$a.time < b.time$$

# Definition using AMG



# Definition using AMG

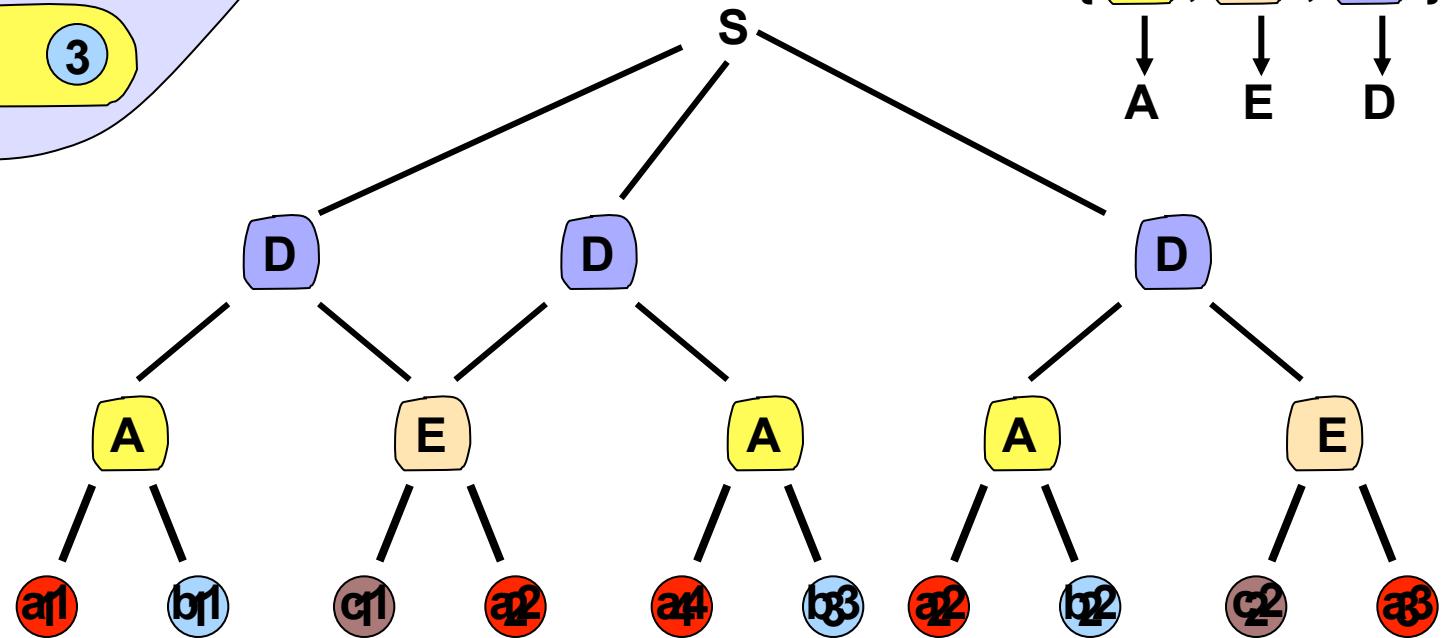


$$T = \{ \textcolor{red}{\bullet}, \textcolor{blue}{\bullet}, \textcolor{brown}{\bullet} \}$$

↓  
a      ↓  
b      ↓  
c

$$N = \{ \textcolor{yellow}{\square}, \textcolor{orange}{\square}, \textcolor{blue}{\square} \}$$

↓  
A      ↓  
E      ↓  
D

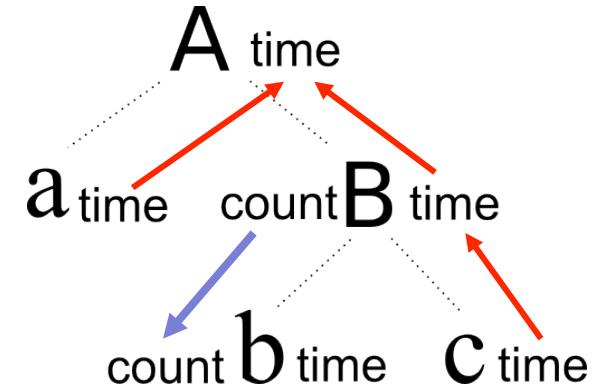


# Definition using AMG

- Attribute Multiset Grammars

$$G = (N, T, S, A, P)$$

detections

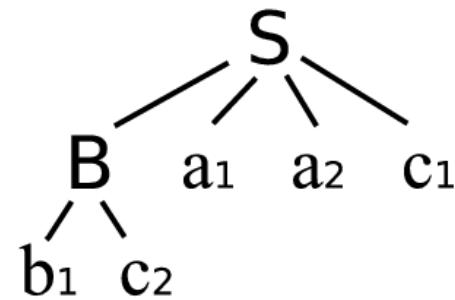
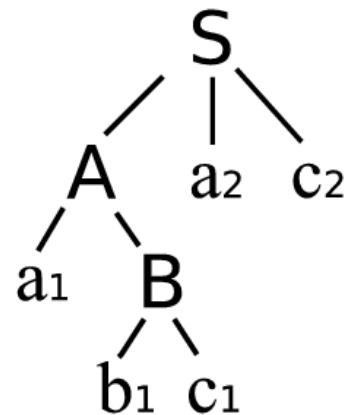


## Production Rules (P):

rule	Syntactic Rule (r)	Attribute Rules (M)		Attribute Constraints (C)		
p <sub>1</sub>	S → A <sup>*</sup> , B <sup>*</sup> , a <sup>*</sup> , c <sup>*</sup>					
p <sub>2</sub>	A → a, B	A.time = a.time+B.time	B.count = 1	a.time < B.time	B.count ≠ 1	
p <sub>3</sub>	B → b, c	B.time = c.time	b.count = B.count	b.time < c.time	b.count ≠ 1	

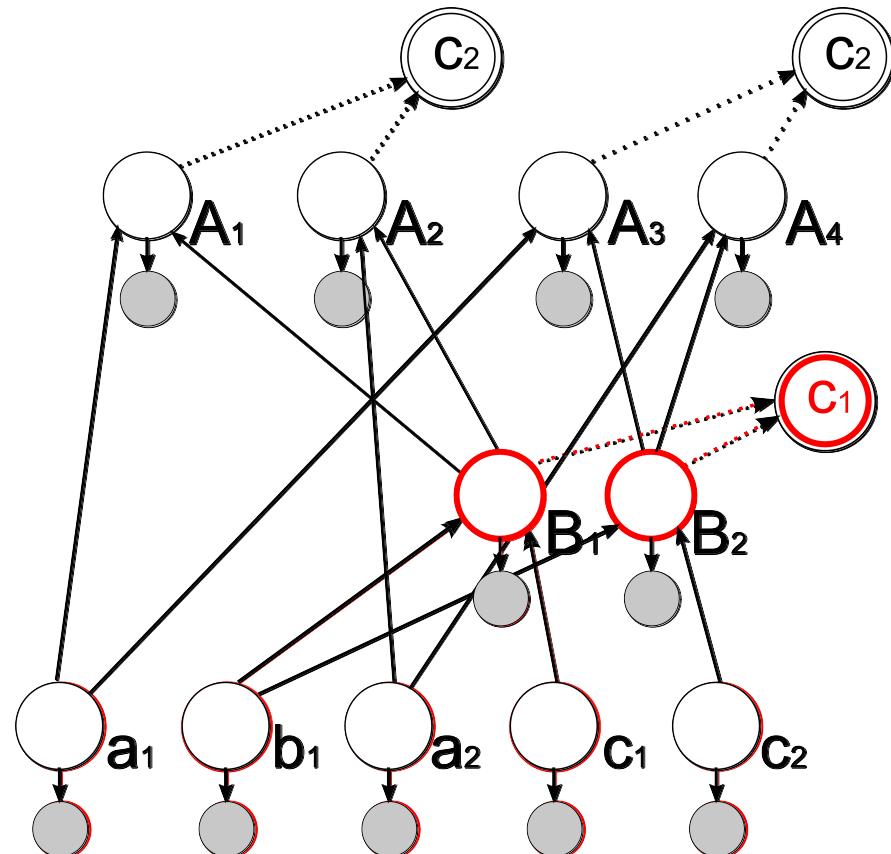
# Recognition using AMG

$$D = \{a_1, a_2, b_1, c_1, c_2\}$$



# Recognition using AMG

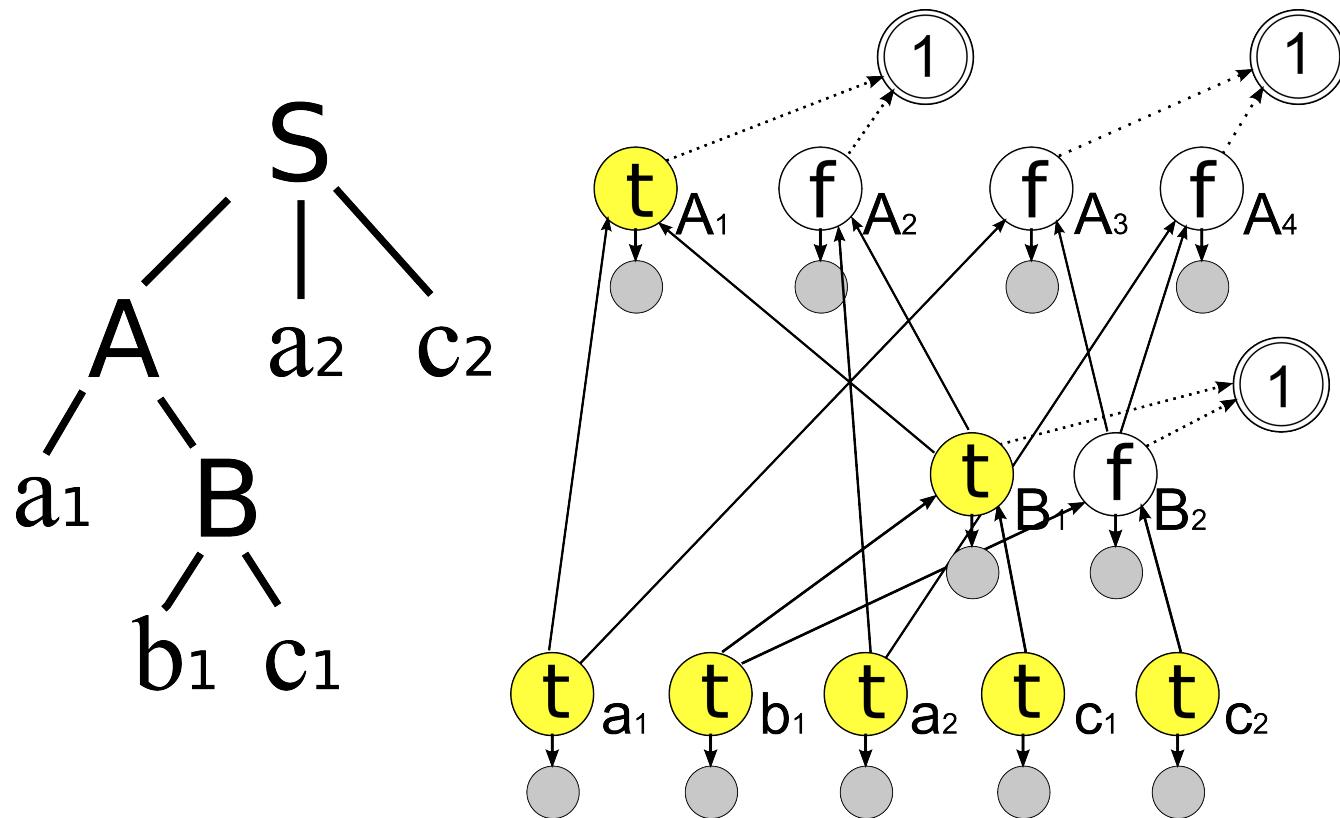
$$D = \{a_1, a_2, b_1, c_1, c_2\}$$



Algorithm

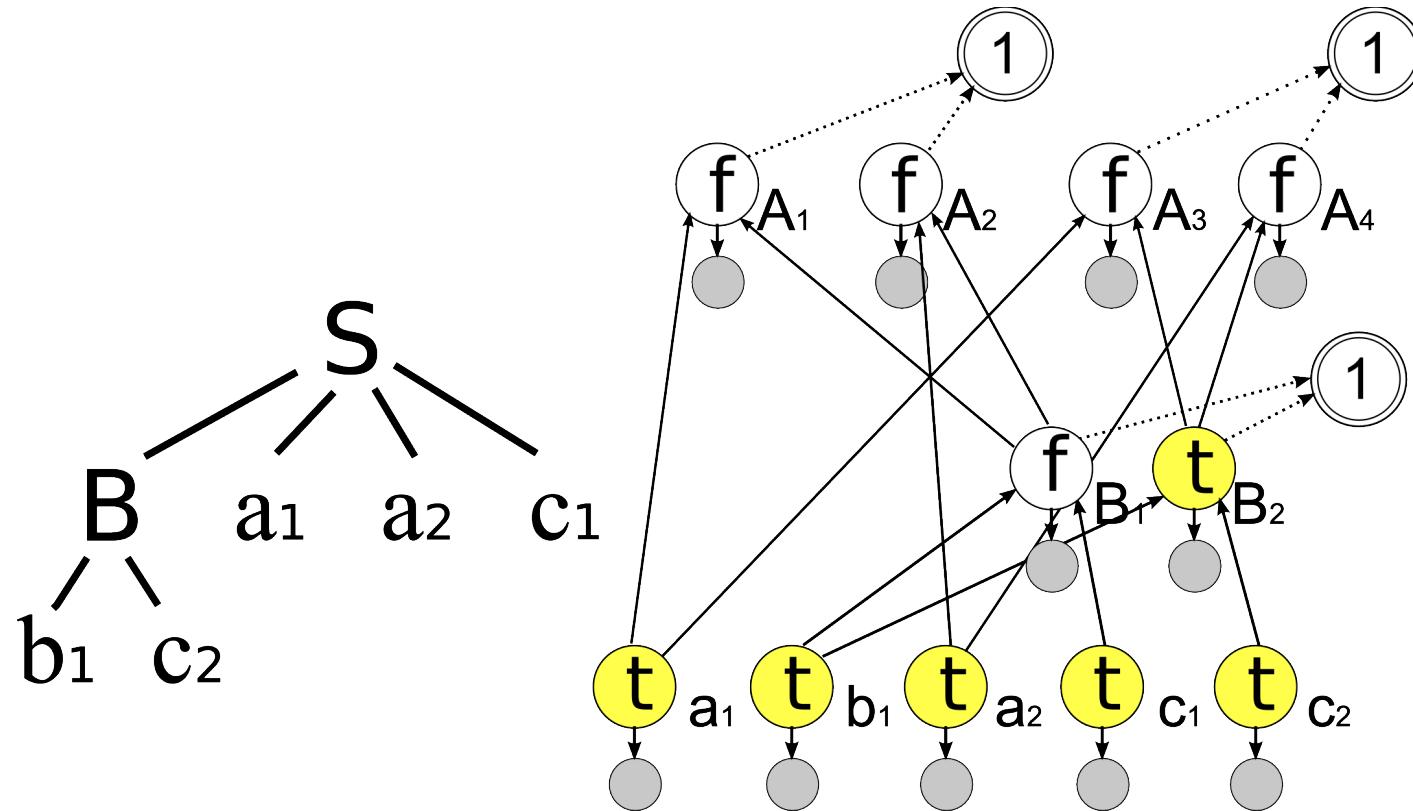
# Recognition using AMG

$$D = \{a_1, a_2, b_1, c_1, c_2\}$$

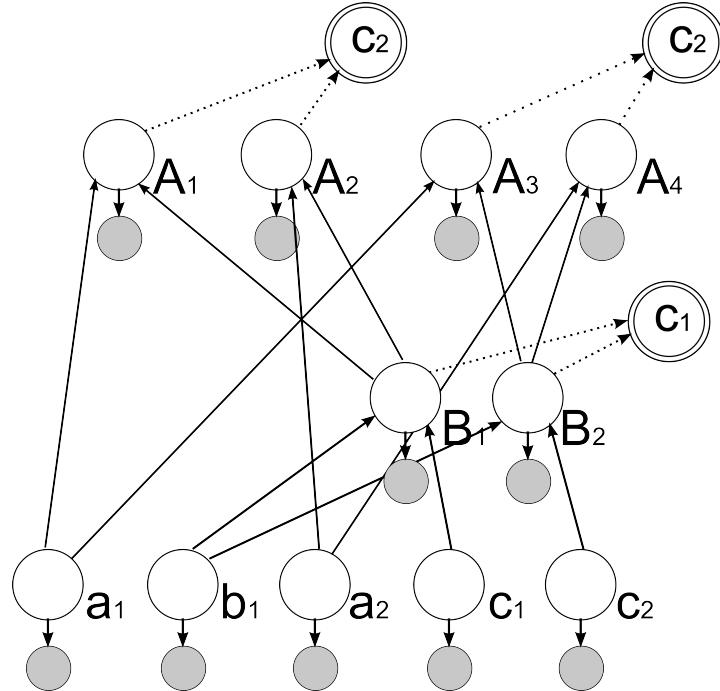


# Recognition using AMG

$$D = \{a_1, a_2, b_1, c_1, c_2\}$$



# Recognition using AMG



## Searching the space of explanations

- Greedy Search
- Multiple Hypotheses Tree [BMVC 07]
- Reversible Jump Markov Chain [CVPR 09]
- Monte Carlo
- Integer Programming

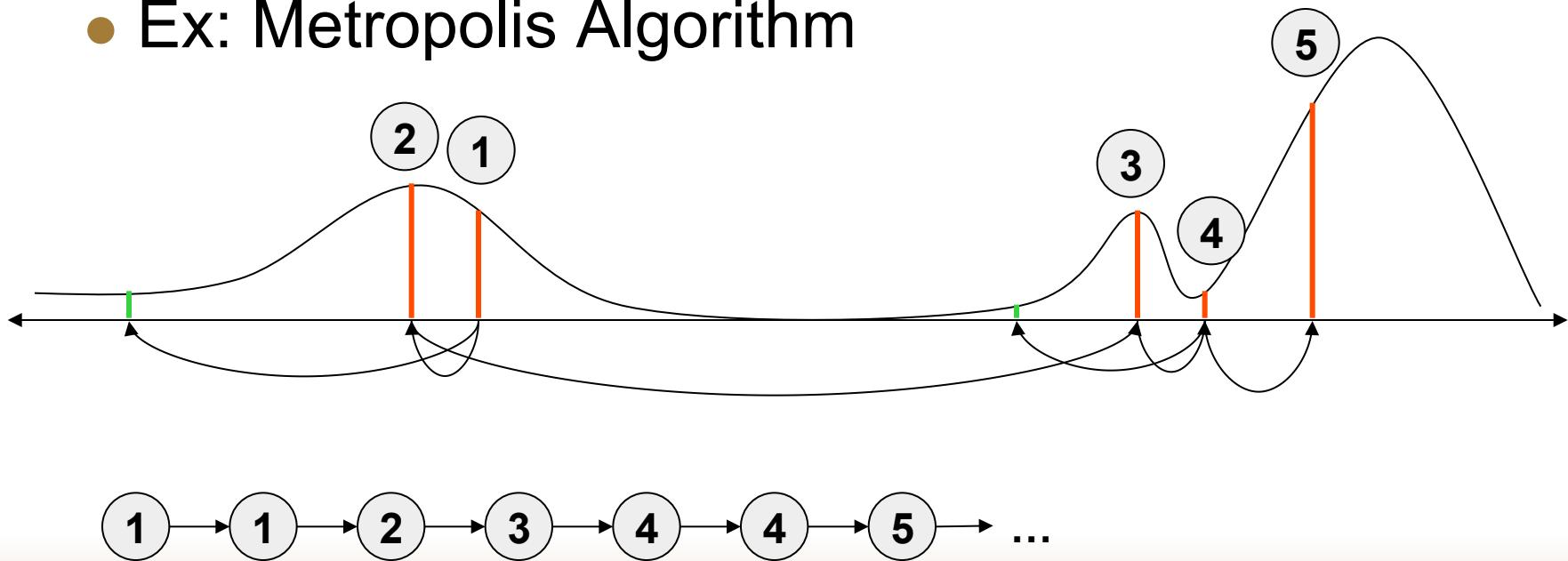
# Searching the space of Explanations

$$\omega^* = \arg \max_{\omega} p(\omega | Y)$$

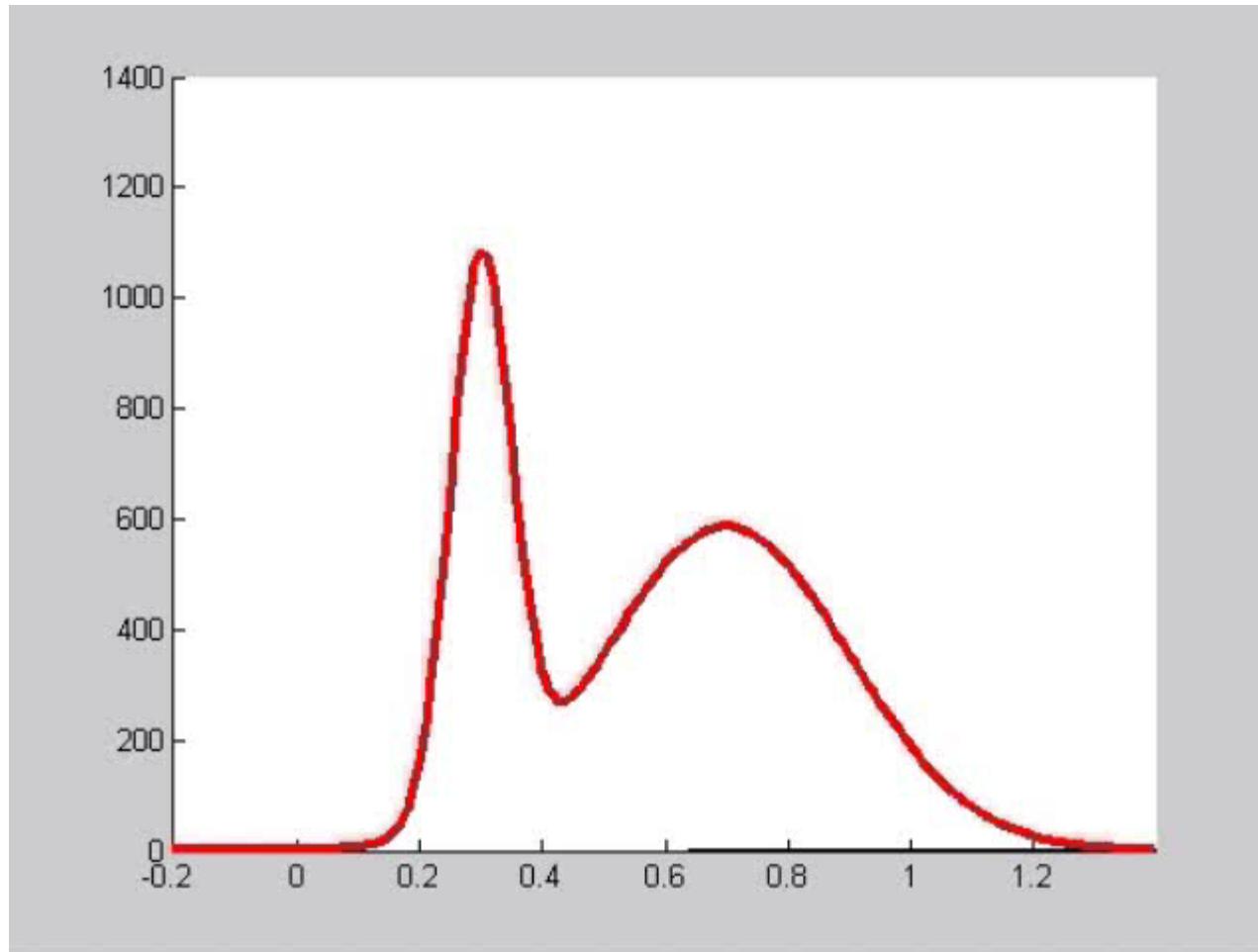
- MCMC samples the space focusing on where posterior is concentrated

# Introduction to MCMC

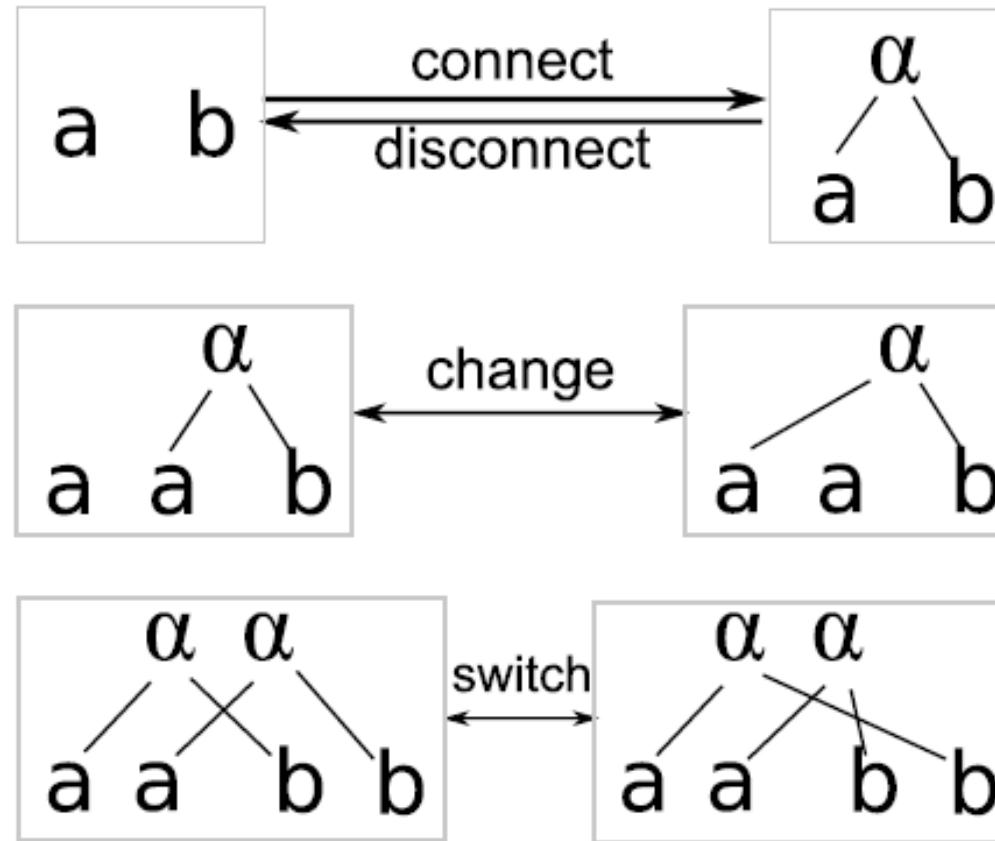
- MCMC – Markov Chain Monte Carlo
- When?
  - You can't sample from the distribution itself
  - Can evaluate it at any point
  - Ex: Metropolis Algorithm



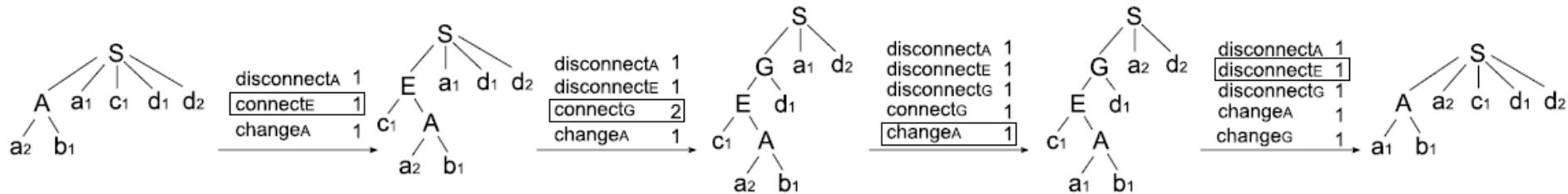
# Introduction to MCMC



# Suggested Moves



# Reversible Moves



# MCMC General Algorithm

---

Markov Chain Monte Carlo

---

initialize  $\omega_0$

for  $i = 1$  to  $n_{mc}$

sample  $m$  from  $\xi_i$

sample  $\omega^*$  from  $Q_m(\omega^* | \omega_{i-1})$

calculate  $\alpha(\omega^* | \omega_{i-1}) = \left( \frac{\pi(\omega^*)}{\pi(\omega)} \right) \frac{Q(\omega | \omega^*)}{Q(\omega^* | \omega)}$

sample  $u$  from  $\mathcal{U}[0,1]$

if  $u < \alpha(\omega^* | \omega_{i-1})$

$\omega_i = \omega^*$

else

$\omega_i = \omega_{i-1}$

# MCMC General Algorithm

---

Markov Chain Monte Carlo

---

initialize  $\omega_0$

for  $i = 1$  to  $n_{mc}$

sample  $m$  from  $\xi_i$

sample  $\omega^*$  from  $Q_m(\omega^* | \omega_{i-1})$

calculate  $\alpha(\omega^* | \omega_{i-1}) = \left( \frac{\pi(\omega^*)}{\pi(\omega)} \right) \frac{Q(\omega | \omega^*)}{Q(\omega^* | \omega)}$

sample  $u$  from  $\mathcal{U}[0,1]$

if  $u < \alpha(\omega^* | \omega_{i-1})$

$\omega_i = \omega^*$

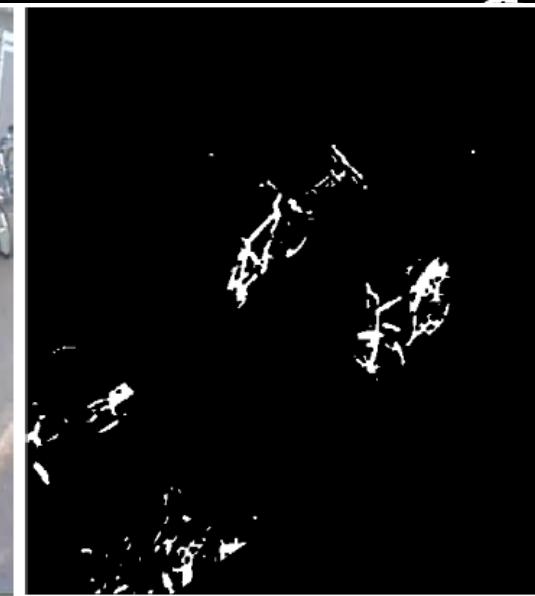
else

$\omega_i = \omega_{i-1}$

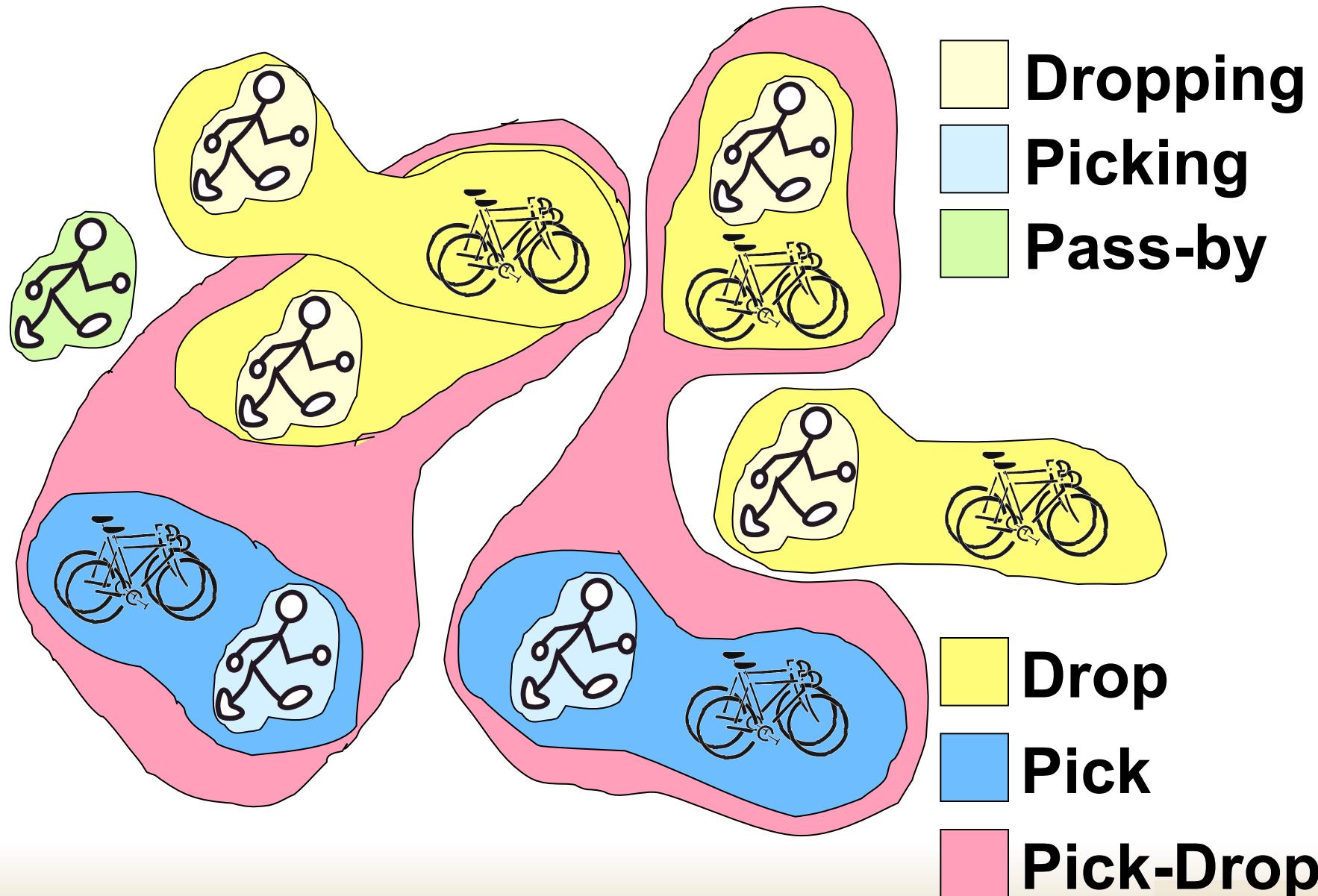
# Case I : The Bicycles Problem



# The Bicycles Problem



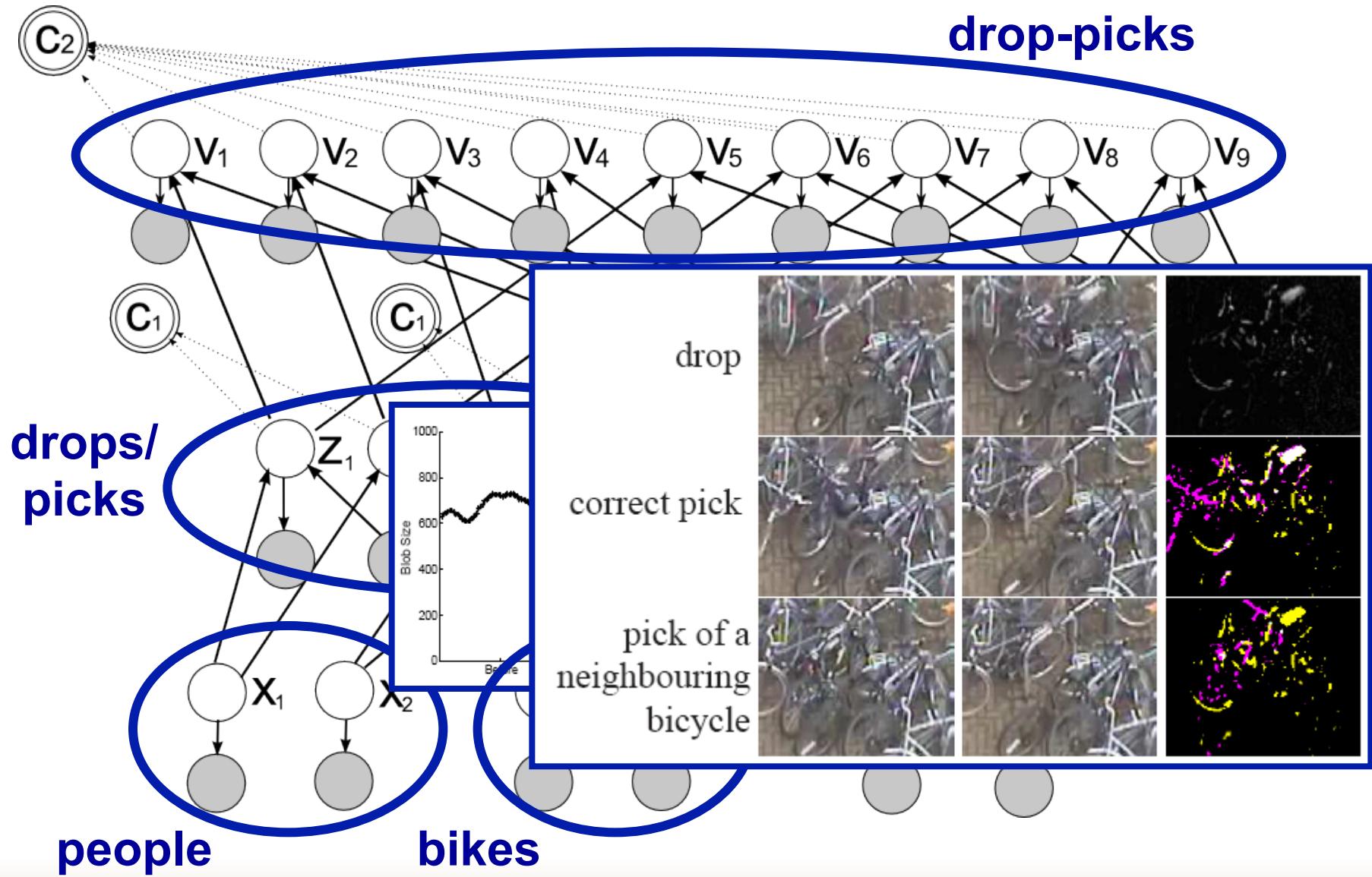
# The Bicycles Problem



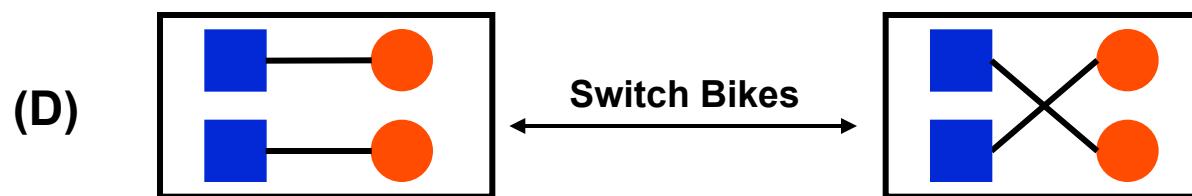
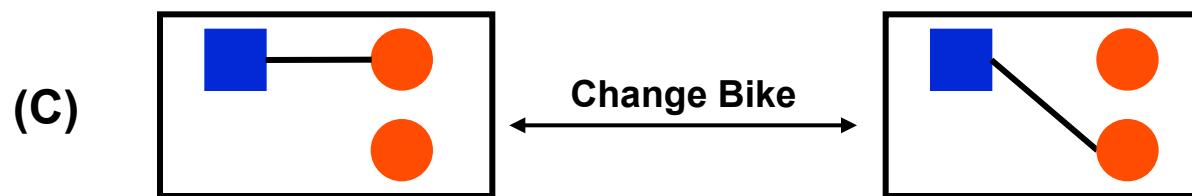
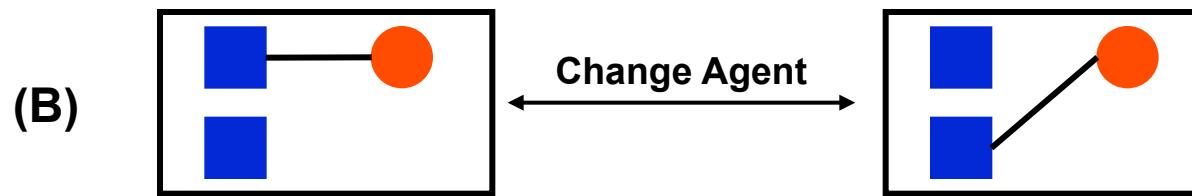
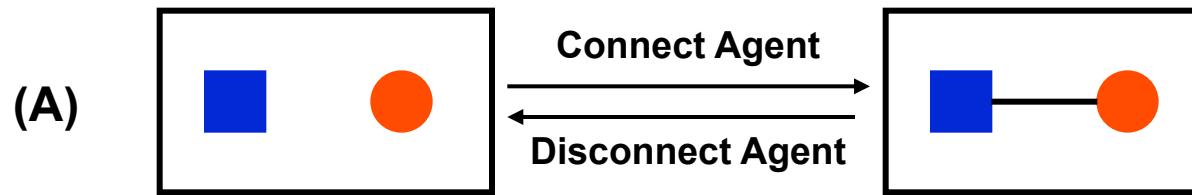
# The Bicycles AMG

Syntactic Rule (r)				Attribute Rules (M)			Attribute Constraints (C)		
p1	S	$\rightarrow V^*, x^*, y^*$		y.action	=	"noise"	y.count < 1		
				x.action	=	"pass-by"		x.count $\neq$ 1	
p2	V	$\rightarrow Z_1, Z_2$		V.action	=	"drop-pick"	Z <sub>1</sub> .au < Z <sub>2</sub> .au		
				Z <sub>1</sub> .action	=	"drop"		Z <sub>1</sub> .count $\neq$ 1	
				Z <sub>2</sub> .action	=	"pick"		Z <sub>2</sub> .count $\neq$ 1	
				V.match	=	$\psi_V(Z_1.\text{pos}, Z_2.\text{pos})$			
				Z <sub>1</sub> .count	=	Z <sub>2</sub> .count = 1			
p3	V	$\rightarrow Z, u$		V.action	=	"drop-only"	Z.count $\neq$ 1		
				Z.action	=	"drop"			
				Z.count	=	1			
p4	V	$\rightarrow u, Z$		V.action	=	"pick-only"	Z.count $\neq$ 1		
				Z.action	=	"pick"			
				Z.count	=	1			
p5	Z	$\rightarrow x, y$		x.action	=	Z.action	x.au = y.au		
				y.action	=	Z.action		x.count $\neq$ 1	
				Z.au	=	x.au			
				Z.pos	=	y.pos			
				Z.match	=	$\psi_Z(x.\text{traj}, y.\text{pos})$			
				x.count	=	1			
				y.count	=	y.count+1			

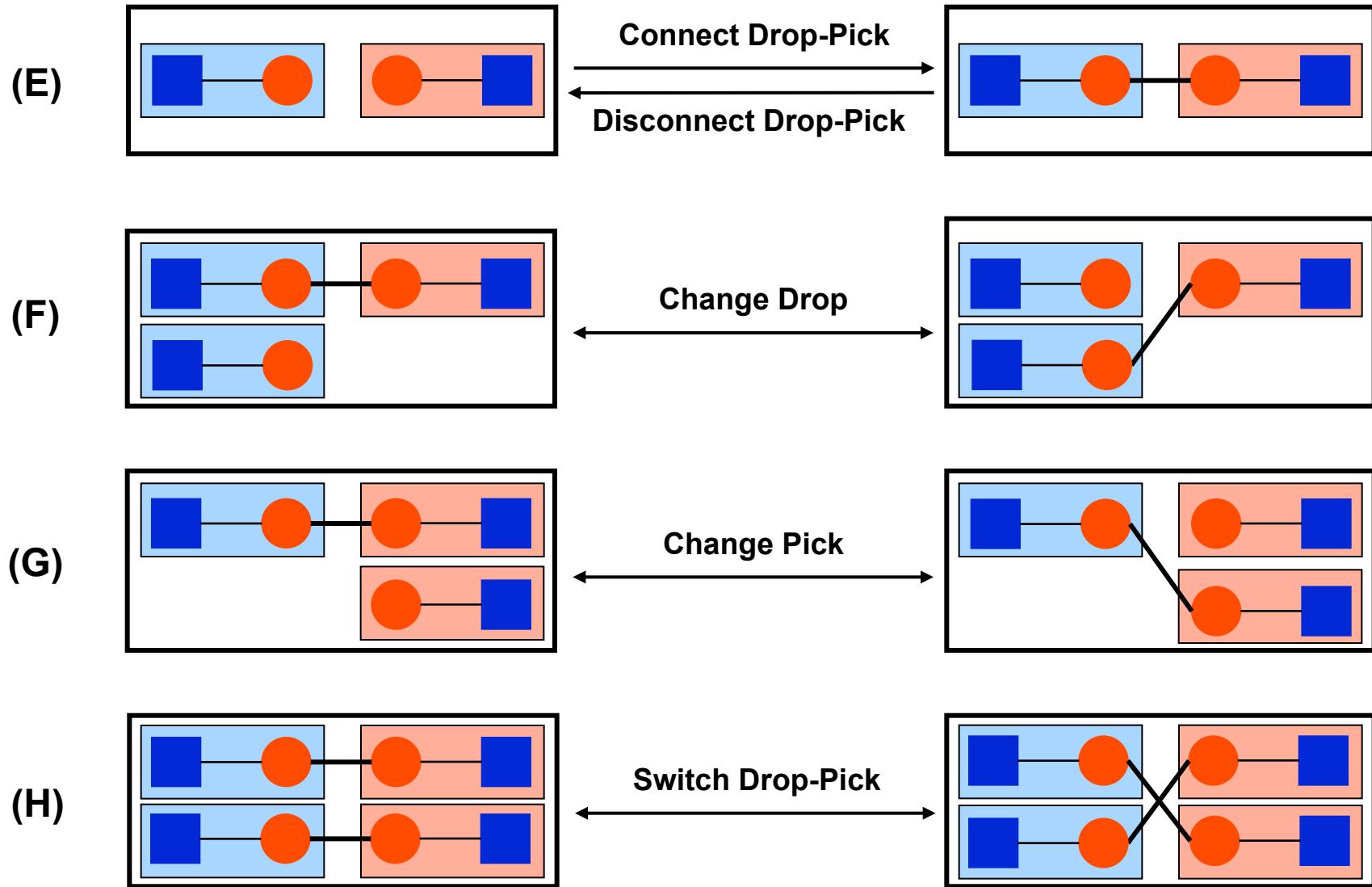
# The Bicycles BN



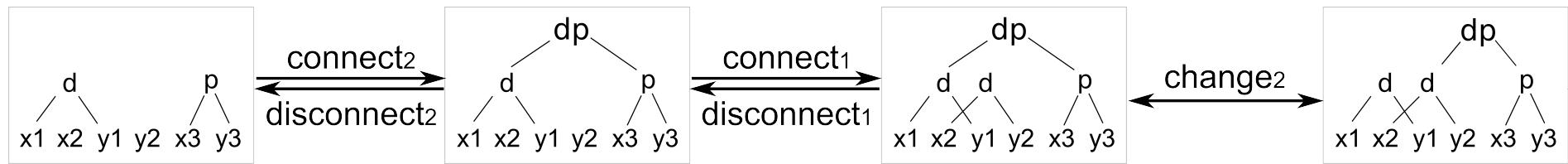
# Suggested Moves – Bicycles 1



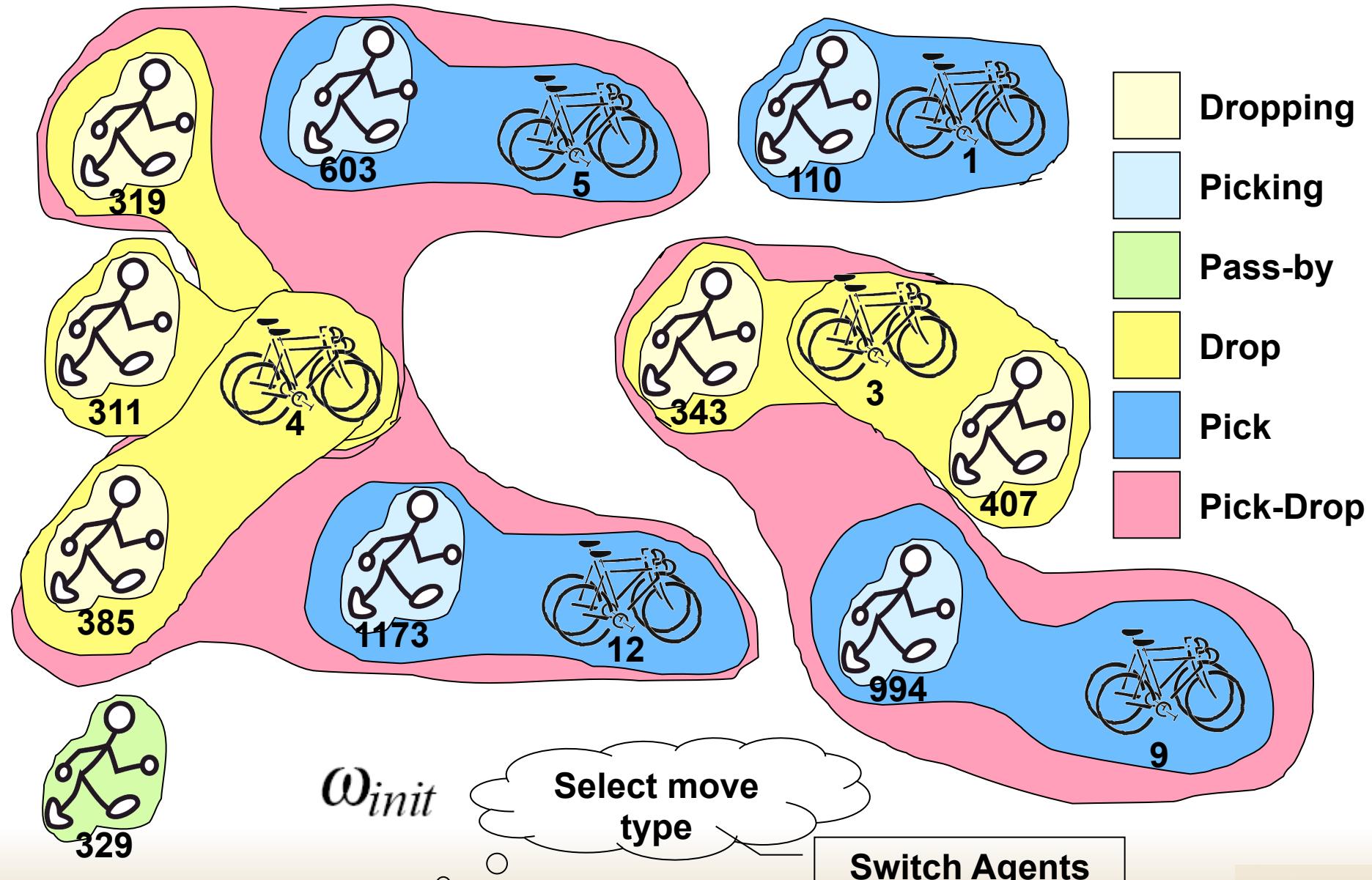
# Suggested Moves – Bicycles 2



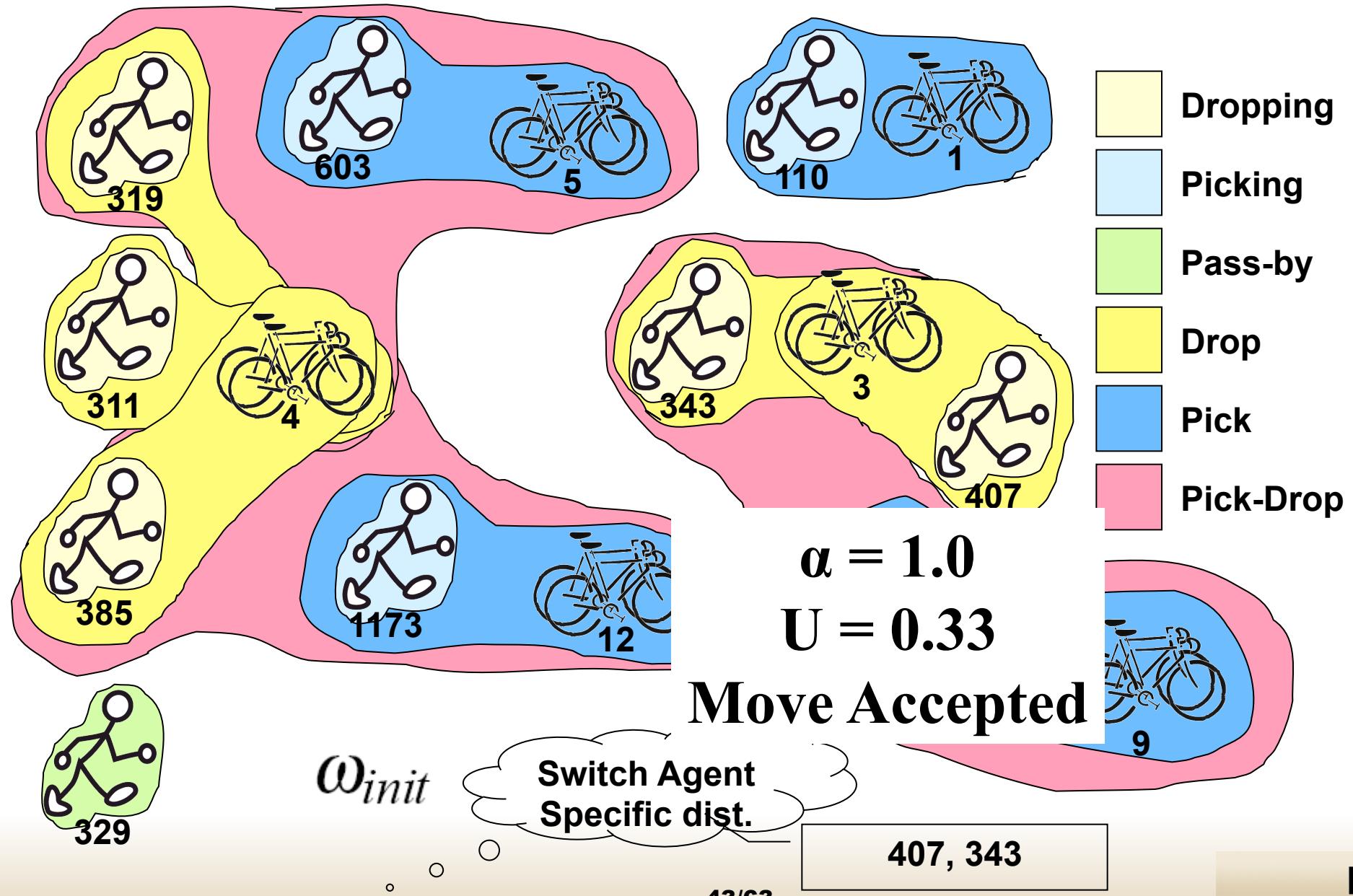
# RJMCMC



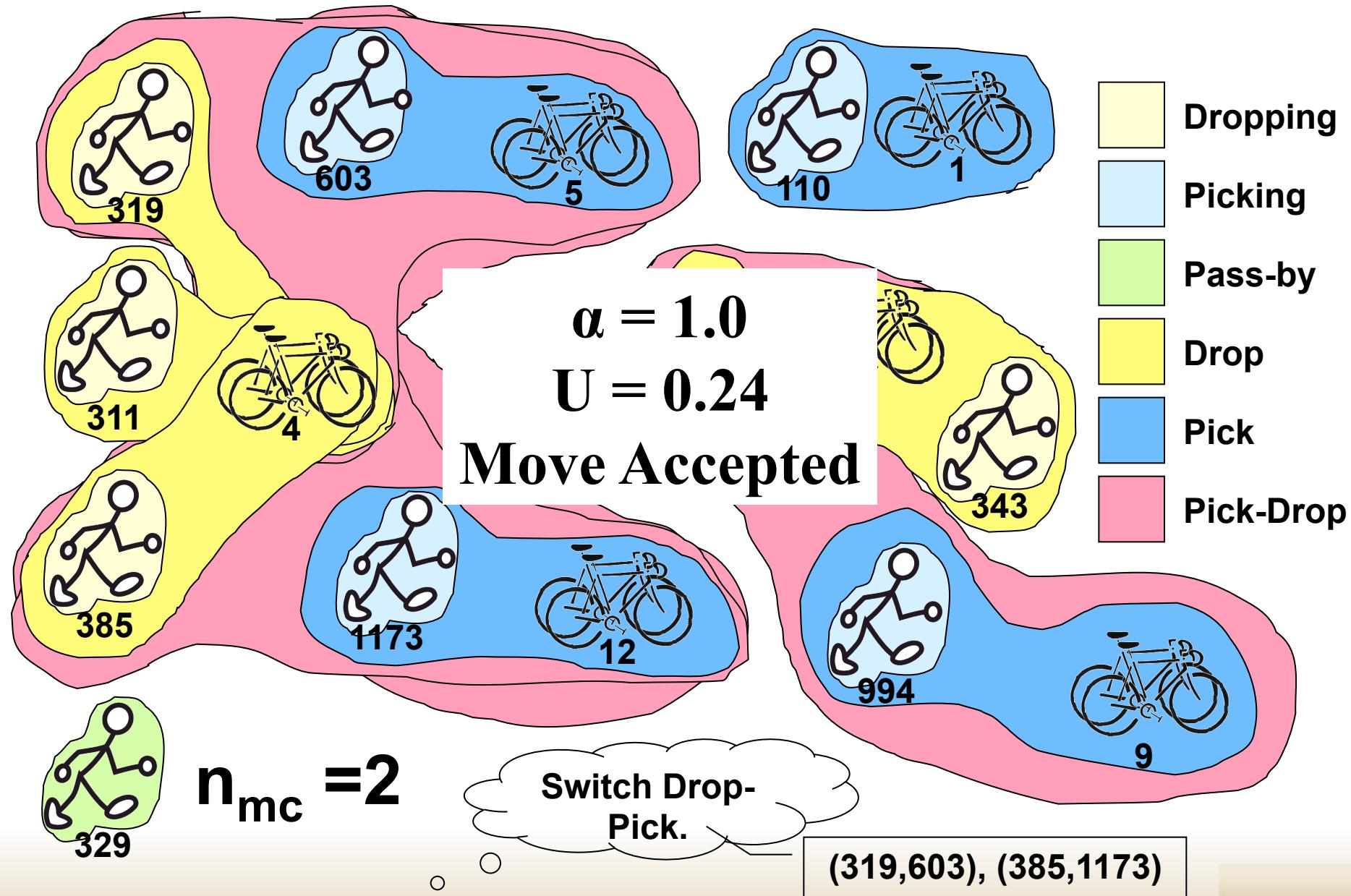
# Examples



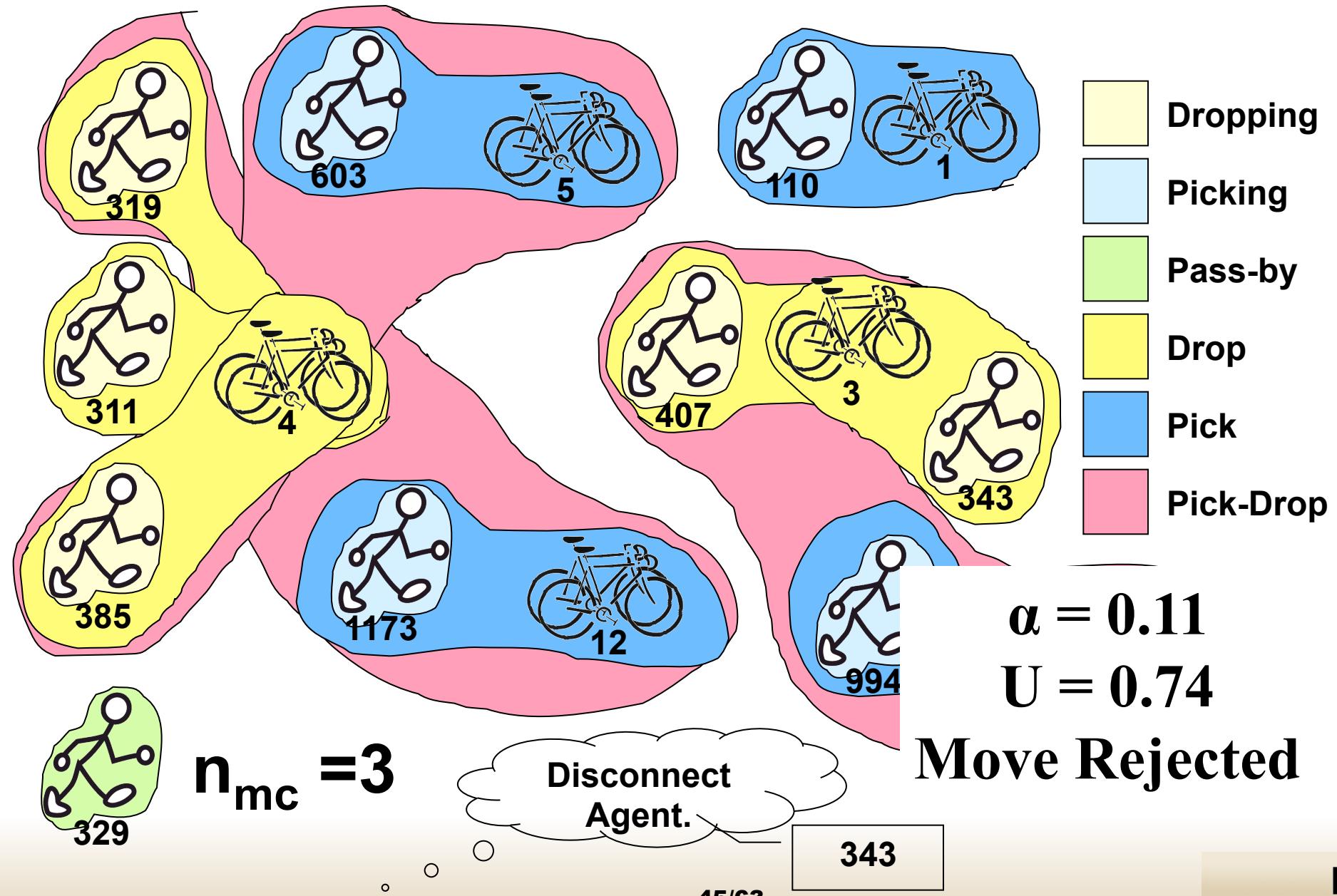
# Examples



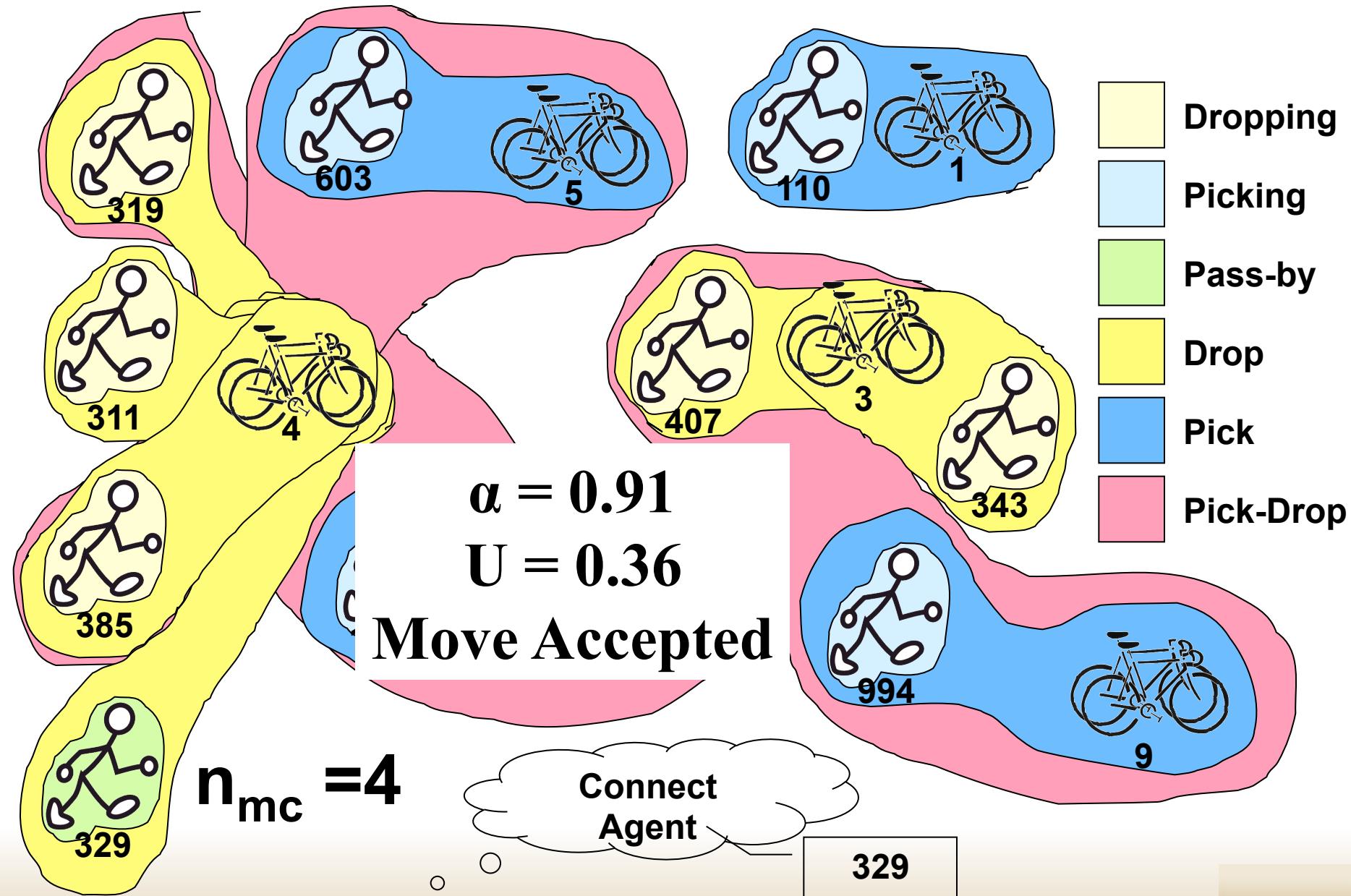
# Examples



# Examples



# Examples



# Dataset

Site 1

3 days (37 hours)

476 people

453 bicycle clusters

82 drop-picks



Site 2

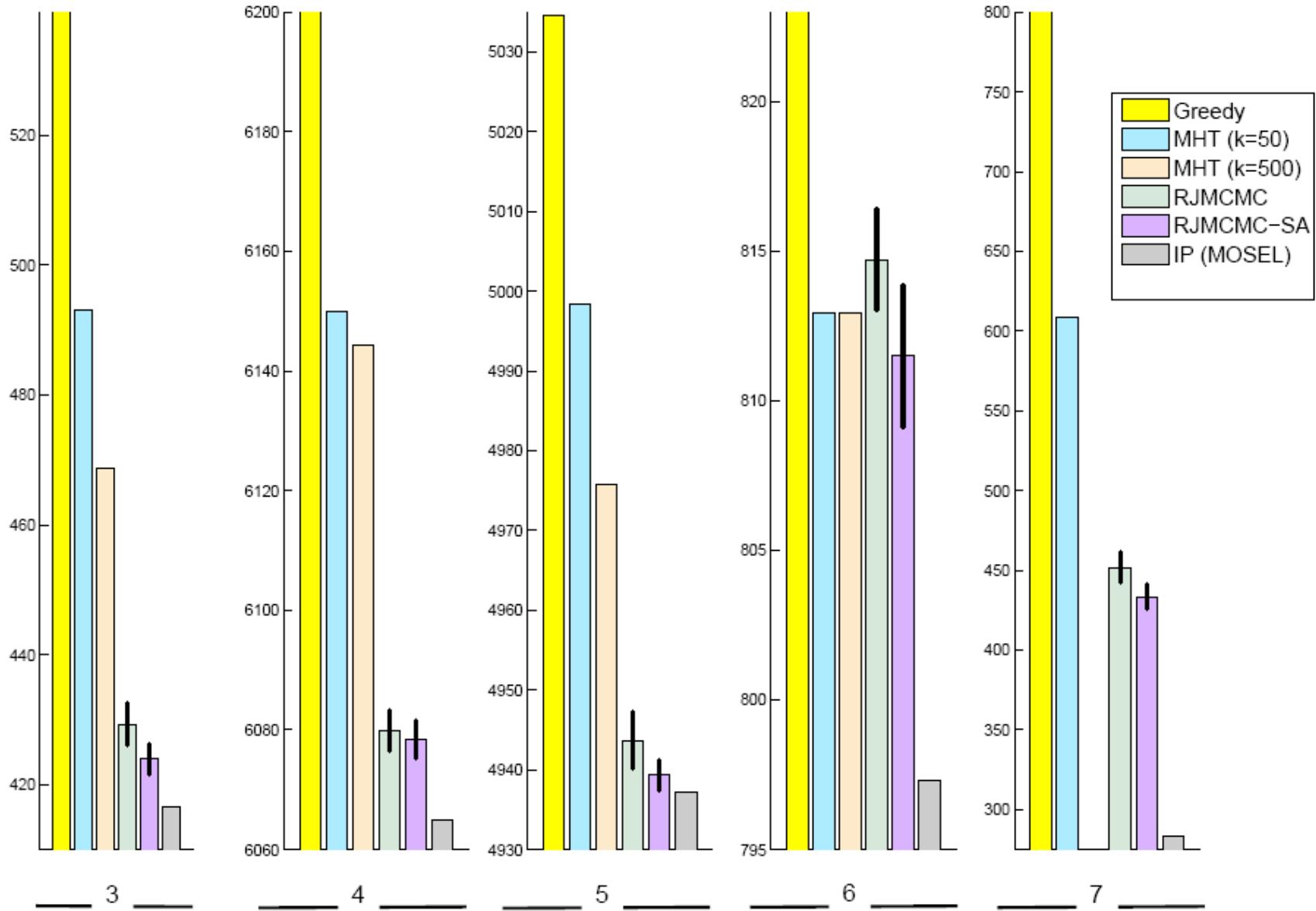
2 days (30 hours)

309 people

2053 bicycle clusters

36 drop-picks

# Results



# Results

**-log(p)**

	Greedy	MHT			RJMCMC		RJMCMC-SA		IP	
		k=50	k=100	k=500	$\mu$	$\sigma$	$\mu$	$\sigma$	MATLAB	XPRESS-MP
1	102.25	58.78	58.78	57.86	57.90	0.11	57.86	0.00	57.86	57.86
2	23.54	4.64	4.64	4.64	4.64	0.00	4.64	0.00	4.64	4.64
3	609.66	493.18	468.80	468.80	429.30	3.23	423.98	2.36	416.64	416.64
4	6272.69	6149.95	6144.98	6144.30	6079.88	3.43	6078.40	3.23	6065.0	6065.00
5	5034.46	4998.39	4982.86	4975.82	4943.71	3.59	4939.33	1.87	4937.1	4937.08
6	860.37	812.96	812.96	812.96	814.71	1.69	811.50	2.36	797.29	797.29
7	934.36	608.92	607.39	-	451.92	9.29	433.50	7.76	-	283.51

**accuracy**

	Local	Global									
		Greedy	MHT			RJMCMC		RJMCMC-SA		IP	
			k=50	k=100	k=500	$\mu$	$\sigma$	$\mu$	$\sigma$	MATLAB	XPRESS-MP
1	74.13	72.41	91.38	91.38	91.38	88.36	1.09	87.46	1.79	91.38	91.38
2	85.19	85.19	100.00	100.00	100.00	100.00	0.00	100.00	0.00	100.00	100.00
3	64.06	58.59	84.38	84.38	84.38	87.68	0.89	83.36	1.65	88.28*	87.5*
4	74.60	73.81	74.60	75.40	75.40	83.93	1.09	83.15	1.31	81.75*	83.33*
5	86.13	89.05	82.48	84.67	88.32	91.90	0.79	92.65*	0.90	94.16	94.16
6	65.18	66.07	60.71	60.71	60.71	68.53	1.68	70.98	1.04	73.21	73.21
7	46.18	45.69	44.67	45.69	-	47.28	1.18	47.61	0.88	-	46.70



# Results



# We actually caught thieves!!



**Recorded time: 11 hours and 30 minutes**  
**Warning time: 13 minutes**

# Case II: The Enter-Exit Problem



# Global Explanation

- Global explanation



# Global Explanation

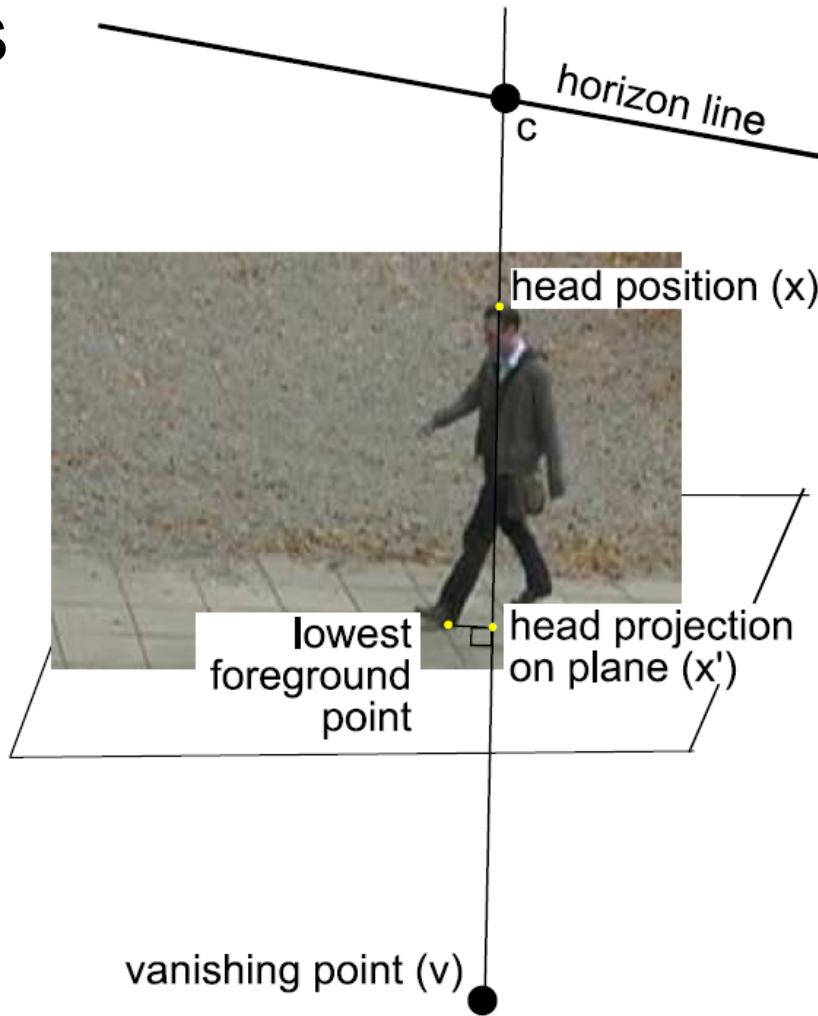


# Using Baggage Detector [ECCV 08]



# Selected Features

## 1. Matching Heights



# Selected Features

## 2. Clothing Colour



# Selected Features

## 3. Baggage Colour



# Selected Features

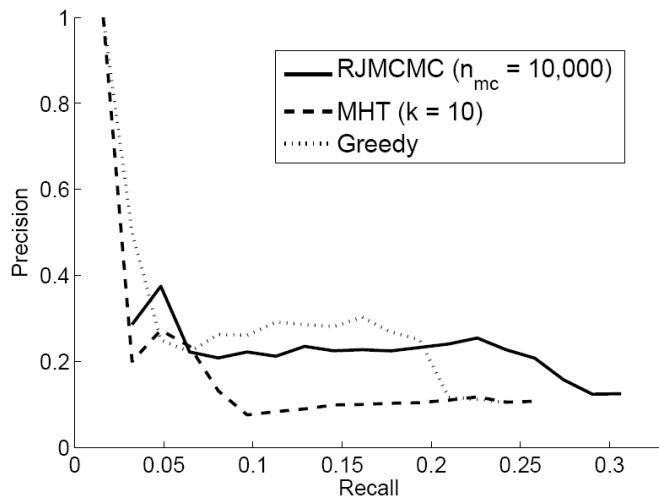
## 4. Baggage Relative Height



# Experiment

- 12 hours
- 326 people
- 429 candidate bags
- 62 ground truth pairs

# Results



	Local	Global		
		Greedy	MHT	RJMCMC
Paired	13	14	16	19
Unpaired	49	48	46	43
Incorrect Pairs	173	133	135	142

# Conclusion

- Defining activity using AMG
  - Hierarchies of events
  - Multisets
  - Intra-activity constraints → synthetic attributes
  - Inter-activity constraints → inherited attributes
- Finding the best parse tree → Recognition
  - Building BN
  - Searching for MAP
- Two case studies

# Thank you 😊

Damen, Dima and Hogg, David (Sep 2009). Attribute Multiset Grammars for Global Explanations of Activities. British Machine Vision Conference (BMVC).

Damen, Dima and Hogg, David (June 2009). Recognizing Linked Events: Searching the Space of Feasible Explanations. Computer Vision and Pattern Recognition (CVPR).

Damen, Dima and Hogg, David (Oct 2008). Detecting Carried Objects from Short Video Sequences. European Computer Vision Conference (ECCV).