

Ellingham Diagram Data Extraction

Technical Guide

Honda CALPHAD Project — MSE 4381 Senior Design

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Contents

1	Introduction	2
1.1	Objective	2
1.2	What is an Ellingham Diagram?	2
2	Method	2
2.1	Software and Database	2
2.2	Oxides Calculated	2
2.3	Temperature Range	3
3	Calculation Details	3
3.1	Formation Energy Formula	3
3.2	Normalization per Mole O ₂	3
3.3	TC-Python Implementation	3
3.4	Technical Challenges Solved	4
4	Results	4
4.1	Gibbs Energies at 1000 K	4
4.2	Key Finding	4
4.3	Physical Stability: Melting Points	4
5	Implications for the Project	5
5.1	What This Tells Us	5
5.2	Alternative Cu Removal Mechanisms	5
5.3	Recommended Next Steps	5
6	Step-by-Step: Running on OSU Lab Machines	6
6.1	Accessing the Virtual Machine	6
6.2	Getting the Code from GitHub	6
6.3	Opening the Command Prompt	6
6.4	Running the TC-Python Script	6
6.5	Expected Output	6
6.6	Retrieving the Output	7
6.7	Troubleshooting	7
7	Files and Reproduction	8
7.1	Files Generated	8
7.2	How to Reproduce	8
7.3	Interactive Notebook	8

8 References

8

1 Introduction

1.1 Objective

Extract Gibbs energies of formation (ΔG_f°) for oxide materials from Thermo-Calc's TCOX14 database to create an Ellingham diagram. This diagram compares oxide stability and answers a key question for the Cu removal project:

Research Question

Can copper thermodynamically reduce ceramic oxides (Al_2O_3 , MgO , SiO_2 , TiO_2)?

1.2 What is an Ellingham Diagram?

An Ellingham diagram plots ΔG_f° per mole O_2 versus temperature for metal oxide formation reactions.

Key principles:

- Lower (more negative) ΔG = more stable oxide
- A metal can reduce another metal's oxide only if its oxide line is *below* the other
- The vertical gap between lines indicates the thermodynamic driving force

2 Method

2.1 Software and Database

- **Thermo-Calc 2025b** with **TC-Python API**
- **TCOX14** database (comprehensive oxide thermodynamics)
- Run on **OSU ETS Virtual Machine** (Windows, Thermo-Calc license)

2.2 Oxides Calculated

Table 1: Oxide phases and formation reactions normalized per mole O_2

Oxide	Mineral Name	TC Phase	Reaction (per mol O_2)
Cu_2O	Cuprite	CUPRITE#1	$4\text{Cu} + \text{O}_2 \rightarrow 2\text{Cu}_2\text{O}$
CuO	Tenorite	CUO#1	$2\text{Cu} + \text{O}_2 \rightarrow 2\text{CuO}$
Al_2O_3	Corundum	CORUNDUM#1	$\frac{4}{3}\text{Al} + \text{O}_2 \rightarrow \frac{2}{3}\text{Al}_2\text{O}_3$
MgO	Periclase	HALITE#1	$2\text{Mg} + \text{O}_2 \rightarrow 2\text{MgO}$
SiO_2	Quartz	QUARTZ#1	$\text{Si} + \text{O}_2 \rightarrow \text{SiO}_2$
TiO_2	Rutile	RUTILE#1	$\text{Ti} + \text{O}_2 \rightarrow \text{TiO}_2$
FeO	Wüstite	HALITE#1	$2\text{Fe} + \text{O}_2 \rightarrow 2\text{FeO}$

2.3 Temperature Range

- Range: 500 K to 2000 K
- Step size: 50 K
- Total: 31 data points per oxide

3 Calculation Details

3.1 Formation Energy Formula

For the general reaction: Metal + O₂ → Oxide

$$\Delta G_f^\circ = G_{oxide}^\circ - n \cdot G_{metal}^\circ - G_{O_2}^\circ \quad (1)$$

Where:

- G_{oxide}° = Gibbs energy of the oxide phase (per formula unit)
- G_{metal}° = Gibbs energy of pure metal reference state
- $G_{O_2}^\circ$ = Gibbs energy of O₂ gas at 1 atm
- n = stoichiometric coefficient for metal

3.2 Normalization per Mole O₂

All values are normalized per mole O₂ consumed for direct comparison on the Ellingham diagram.
For example:

- Cu₂O: $\Delta G_{per\ O_2} = 2 \times G(Cu_2O) - 4 \times G(Cu) - G(O_2)$
- Al₂O₃: $\Delta G_{per\ O_2} = \frac{2}{3} \times G(Al_2O_3) - \frac{4}{3} \times G(Al) - G(O_2)$

3.3 TC-Python Implementation

The extraction script performs four steps at each temperature:

1. **O₂ Reference:** Calculate $G(O_2)$ using pure O system
 - TC returns GM per mole O atoms → multiply by 2 for per mole O₂
2. **Metal Reference:** Calculate $G(metal)$ at near-zero oxygen ($X_O = 0.0001$)
3. **Oxide Phase:** Set stoichiometric composition, calculate equilibrium
 - Extract individual phase energy: GM(CUPRITE#1)
 - Convert per-atom to per-formula-unit: multiply by atoms per formula
4. **Formation Energy:** Apply the ΔG_f formula

Table 2: Bugs encountered and solutions implemented

Problem	Cause	Solution
Wrong sign for Cu ₂ O (+97 instead of -191 kJ/mol)	Two-phase equilibrium (CUPRITE + FCC_A1); system GM is mixture energy	Extract individual phase energy using GM (CUPRITE#1)
Values too small by factor of 2-5	TC returns GM per mole atoms, not per formula unit	Multiply atoms_per_formula by (e.g., 3 for Cu ₂ O)
O ₂ reference off by factor of 2	GM for pure O is per mole O atoms	Multiply by 2 for per mole O ₂

3.4 Technical Challenges Solved

4 Results

4.1 Gibbs Energies at 1000 K

Table 3: Gibbs energy of formation per mole O₂ at 1000 K (727°C)

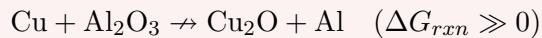
Oxide	ΔG_f° (kJ/mol O ₂)	Phase	Stability
MgO	-986.8	HALITE#1	Most stable
Al ₂ O ₃	-907.5	CORUNDUM#1	
TiO ₂	-760.2	RUTILE#1	
SiO ₂	-730.2	QUARTZ#1	
FeO	-411.2	HALITE#1	
Cu ₂ O	-190.8	CUPRITE#1	
CuO	-132.0	CUO#1	Least stable

4.2 Key Finding

Thermodynamic Conclusion

Cu₂O is the LEAST stable oxide among all candidates, with ΔG_f° approximately 800 kJ/mol O₂ less negative than MgO or Al₂O₃.

This means copper **cannot** reduce these ceramics:



The thermodynamic driving force is approximately +800 kJ/mol O₂ in the *wrong* direction.

4.3 Physical Stability: Melting Points

Cu oxides also melt at lower temperatures than the ceramic candidates:

Table 4: Melting points and phase behavior at steelmaking temperatures

Material	Melting Point (°C)	Status at 1500°C
Cu ₂ O	1235	Liquid
CuO	1326	Liquid
FeO	1377	Liquid
SiO ₂	1713	Solid
TiO ₂	1843	Solid
Al ₂ O ₃	2072	Solid
MgO	2852	Solid

5 Implications for the Project

5.1 What This Tells Us

1. **Direct oxide reduction is thermodynamically impossible** — Cu cannot “steal” oxygen from Al₂O₃, MgO, SiO₂, or TiO₂
2. **Previous Cu capture observations** must involve different mechanisms

5.2 Alternative Cu Removal Mechanisms

Table 5: Possible mechanisms for Cu capture by ceramics

Mechanism	Description	Key Factor
Solid Solution	Cu dissolves into oxide lattice (substitutional or interstitial)	High temperature (entropy-driven)
Spinel Formation	$\text{CuO} + \text{Al}_2\text{O}_3 \rightarrow \text{CuAl}_2\text{O}_4$	Requires Cu oxidation first
Surface Adsorption	Cu atoms adsorb on ceramic particle surfaces	Surface area, porosity
Capillary Penetration	Molten Cu wets porous ceramic structures	Porosity, wetting angle

5.3 Recommended Next Steps

1. Model Cu solubility in Al₂O₃ and MgO using Thermo-Calc
2. Calculate CuAl₂O₄ spinel stability conditions
3. Compare predictions with last year’s senior design experimental results
4. Design experiments to test the dominant mechanism

6 Step-by-Step: Running on OSU Lab Machines

This section documents exactly how the extraction was performed on the OSU ETS Virtual Machine.

6.1 Accessing the Virtual Machine

1. Go to <https://ets.engineering.osu.edu/>
2. Log in with OSU credentials
3. Select a Windows VM with Thermo-Calc installed
4. Open **File Explorer** and navigate to your U: drive

6.2 Getting the Code from GitHub

Since Git is not installed on the lab VMs, download the repository as a ZIP file:

1. Open a browser and go to: <https://github.com/dimascad/honda-calphad>
2. Click the green “**Code**” button
3. Select “**Download ZIP**”
4. Extract the ZIP to your U: drive, e.g., U:\4381\honda-calphad\

6.3 Opening the Command Prompt

1. Press Win + R, type cmd, press Enter
2. Navigate to the script directory:

```
cd U:\4381\honda-calphad\simulations\tcpython
```

6.4 Running the TC-Python Script

Thermo-Calc includes its own Python distribution. Use this exact path:

```
"C:\Program Files\Thermo-Calc\2025b\python\python.exe" extract_oxide_gibbs.py
```

Important: The quotes around the path are required because of the spaces in “Program Files”.

6.5 Expected Output

The script takes approximately 4–5 minutes to complete. You will see:

```
=====
TC-Python: Oxide Formation Energies for Ellingham Diagram
=====
Temperature range: 500-2000 K (31 points)
Connected to Thermo-Calc
```

```

--- Getting O2 reference energies ---
O2 reference at 1000K: -220766.0 J/mol-O2

--- Processing Cu2O ---
Getting CU reference...
Getting Cu2O oxide phase...
Completed: 31/31 temperatures
dG at 1000K: -190.8 kJ/mol O2
Stable phases: CUPRITE#1;FCC_A1#1
Used for calc: CUPRITE#1

[... continues for each oxide ...]

=====
Writing to ...\\data\\tcpthon\\raw\\oxide_gibbs_energies.csv
Done! 31 rows written.
=====
```

6.6 Retrieving the Output

The CSV file is saved to:

U:\\4381\\honda-calphad\\data\\tcpthon\\raw\\oxide_gibbs_energies.csv

To get the file back to your local machine:

- **Option A:** Copy to OneDrive/Google Drive from the VM
- **Option B:** Email the CSV to yourself
- **Option C:** Download directly from the VM browser

6.7 Troubleshooting

Table 6: Common issues and solutions

Issue	Solution
“python is not recognized”	Use the full path with quotes: "C:\\Program Files\\Thermo-Calc\\2025b\\python\\python.exe"
“tc_python not found”	You must use Thermo-Calc’s bundled Python, not system Python
“TCOX14 not found”	Check available databases with <code>check_databases.py</code> first
IONIC_LIQ warnings	These are normal and don’t affect results

Table 7: Output files from this analysis

File	Description
data/tcpython/raw/oxide_gibbs_energies.csv	Raw data (31 temps × 7 oxides)
data/tcpython/ellingham_diagram_tcox14.png	Static plot (PNG)
data/tcpython/ellingham_diagram_tcox14.pdf	Vector plot (PDF)
simulations/notebooks/ellingham_diagram.py	Interactive Marimo notebook
simulations/tcpython/extract_oxide_gibbs.py	TC-Python extraction script

7 Files and Reproduction

7.1 Files Generated

7.2 How to Reproduce

On OSU ETS Virtual Machine:

```
cd U:\4381\honda-calphad\simulations\tcpthon
"C:\Program Files\Thermo-Calc\2025b\python\python.exe" extract_oxide_gibbs.py
```

Output: data/tcpython/raw/oxide_gibbs_energies.csv

7.3 Interactive Notebook

The Marimo notebook can be accessed via GitHub import:

```
https://github.com/dimascad/honda-calphad/blob/main/simulations/notebooks/ellingham\_diagram.py
```

8 References

1. Thermo-Calc Software, *TCOX14 Database Documentation*, 2024.
2. Ellingham, H.J.T. (1944). “Reducibility of oxides and sulphides in metallurgical processes.” *J. Soc. Chem. Ind.* 63: 125–133.
3. Gaskell, D.R. *Introduction to the Thermodynamics of Materials*, 5th ed. Taylor & Francis, 2008.
4. NIST-JANAF Thermochemical Tables, <https://janaf.nist.gov/>