Semantic Templates and Semantic Functions

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Semantic Functions

Semantic Functions will be denoted with small cap Greek letters capturing the semantics of the specific function such as the *Action function* δ (from Greek δράση for *Action*).
Real valued Semantic function $\varphi: \mathbf{\Sigma} \rightarrow \mathbb{R}$ is function defined on semantic space $\mathbf{\Sigma}$ and having a value on the real axis $\mathbb{R}$. Every object in semantic space is represented by its semantic signature.

Semantic Action Functions

What is a Semantic Template?

Every Semantic Template is represented by an incomplete semantic structure which contains missing substructures (i.e. *compound semantic particles*) and/or missing *primitive semantic particles* and/or missing *semantic property particles*. The place of each missing particle is occupied by a relevant *replacement particle* which contains properties generating the necessary binding force and has an appropriate semantic mass which match the position of the particle in the semantic template. The Semantic Templates will be denoted capital fraktur letters ($\mathfrak{T}$, $\mathfrak{P}$, $\mathfrak{J}$, …) subscripted with an index appropriately. The constructs within the Semantic Templates will be denoted with capital Latin letters $M(\mathfrak{T})$, $I(\mathfrak{T})$ where the fraktur letter inside the parentheses indicates the template those constructs are part of. The various semantic spaces such regular semantic space and template space will be denoted with capital Greek letters $\mathbf{\Sigma}$, $\mathbf{T}$ subscripted with index appropriately.

Depending on what is being matched we divide all Semantic Templates into two categories – *Logical Semantic Templates* and *Physical Semantic Templates*. With Logical Semantic Templates we are matching **only** traits of the semantic signature within the specified Semantic region. With Physical Semantic Templates we are matching **any physical properties** pertaining to the structures and particles within the specified Semantic region.

Every Semantic Template $\mathfrak{T}$ consists of two constructs – *pattern matching construct* $M(\mathfrak{T})$ and *inference construct* $I(\mathfrak{T})$.

Definition: *Centroid of Semantic Template*: represents the mass center of the template structure using the semantic masses of the replacement particles.

Definition: *Regular Semantic Space (or just Semantic Space)*: Semantic space of dimension L which is populated with the semantic structures created by parsing external constructs or by inference. Denoted with $\mathbf{\Sigma}$.

Definition: *Semantic Template Space (or just Template Space)*: Pattern-matching structures exist in a space having the same number of dimensions L as regular semantic space. The template space is parallel to *regular semantic space*. Denoted with $\mathbf{T}$ (tau). Unlike regular semantic space the *template space* is populated with (fuzzy) semantic constructs in which some of the particles (properties, primitive semantic particles, compound semantic particles) are replaced by *template particles*. Each semantic template $\mathfrak{T}$ is associated with a region $\mathfrak{A}(\mathfrak{T})$ (region of *applicability*) of regular semantic space $\mathbf{\Sigma}$ in which the template is valid. To be precise, $\mathfrak{A}(\mathfrak{T}) \subset \mathbf{\Sigma}$ is a region in which its centroid $C(\mathfrak{T})$ is allowed to be positioned without violating the applicability condition of $\mathfrak{T}$. Obviously, this region changes with the elapsed time as the semantic structures of interest (relevant semantic context) move through $\mathbf{\Sigma}$.

Definition: *Template Inference Space* (or just *Inference Space*):
Denoted with $\mathbf{I}$ (*iota* Greek). Has the same number of dimensions L as regular semantic space $\mathbf{\Sigma}$.

Definition: *Intermediate Space Stack*:
A countable set of Semantic Space sheets each of which is parallel to $\mathbf{\Sigma}$ used to facilitate the template matching and inference. In a sense it plays the role of a semantic scratch pad. Each semantic sheet has the same number of dimensions L as regular semantic space $\mathbf{\Sigma}$. Each semantic sheet is denoted with $\mathbf{\Sigma}_{\boldsymbol{\alpha}}$ where $\boldsymbol{\alpha}$ is the sheet index.

Definition: *Extended Semantic Space*.
Denoted with $\mathbf{E}$. Has one more dimension $L+1$ than regular semantic space $\mathbf{\Sigma}$. Introduced to facilitate semantic computations. All defined so far semantic spaces will be considered part of the extended semantic space. Thus $\mathbf{\Sigma}, \mathbf{\Sigma}_{\alpha}, \mathbf{I}, \mathbf{T} \subset \mathbf{E}$.

Definition: *Semantic Template*: It is a semantic relation which maps a semantic structure from semantic space $\mathbf{\Sigma}$ to new *non-empty* semantic structure from $\mathbf{\Sigma}$ if the pattern matching region $\mathfrak{P}(\mathfrak{T})$ has been matched to some semantic structure S from $\mathbf{\Sigma}$ or it is the empty semantic structure $[]$ if no match is found.

Definition: *Centroid and Radius of Semantic Template*: *Centroid* is the current point C in Semantic Space where the pattern matching construct $M(\mathfrak{T})$ is centered thereby assuming *Radius (or Range)* R. The centroid of the pattern-matching construct is mapped to a point in regular semantic space indicating the possible location of the root node of the semantic structure S which will be pattern-matched by $M(\mathfrak{T})$. Let us denote with $O(\mathfrak{T}, C, R)$ the semantic output of the pattern matching region centered in C with radius R. The structures of $O(\mathfrak{T}, C, R)$ will be created in one of the semantic sheets $\mathbf{\Sigma}_{\boldsymbol{\alpha}}$.

Definition: *Matching of Semantic Template*: the centroid of the pattern matching construct $M(\mathfrak{T})$ moves within the region of applicability $\mathfrak{A}(\mathfrak{T})$ in Semantic Template Space $\mathbf{T}$. When the semantic latch μ associated with $\mathfrak{T}$ is triggered the centroid of $\mathfrak{T}$ is affixed to the point which has triggered the latch. The radius of the pattern matching region starts expanding until *optimal match* is selected. For definition of optimal match refer to Pattern Matching Structure of Semantic Template.
Matching of logical semantic template

Matching of physical semantic template

Pattern Matching Structure of Semantic Template

The pattern matching construct $\mathfrak{P}(\mathfrak{T})$ of any template $\mathfrak{T}$ is represented by a semantic tree T in which every node is one of the three:

a) semantic structure S

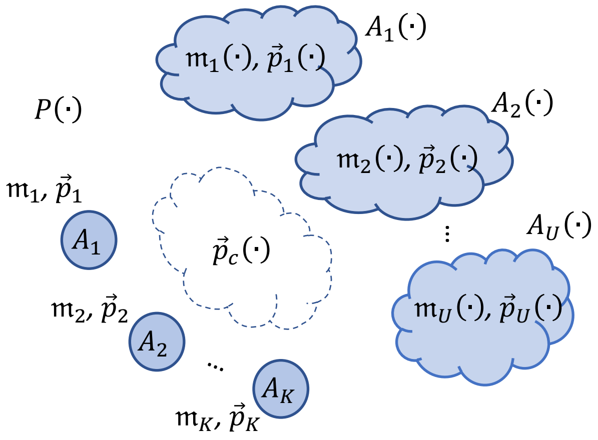
b) primitive semantic particle V
c) template particle X

Template Particles

A template particle can be viewed as stochastic generalization of regular semantic particles. Instead of a single semantic particle on a given position in semantic space and semantic time a template particle will define a *cloud* of *stochastic* semantic particles in a region of semantic space-time.
We will consider template property particles and template semantic particles

Definition: *Template property particle*:

Every template property particle P at a moment of semantic time t is defined in terms of two sets of aspects – the set of *deterministic* aspects $\mathcal{D}$ and set of *stochastic* aspects $\mathcal{T}$.
Each aspect A_i in the set of *deterministic* aspects $\mathcal{D} = \{A_1, \ldots, A_K\}$ is characterized by its deterministic mass $\mathfrak{m}_i$ and deterministic position in semantic space $\vec{p}_i$, $i = 1..K$. The semantic aspects in the set of stochastic aspects $\mathcal{T}$ form a *stochastic cloud*. Each stochastic aspect $A_j(\cdot)$ in the *cloud* $\{A_1(\cdot), \ldots, A_U(\cdot)\}$ is characterized by its stochastic mass $\mathfrak{m}_j(\cdot)$ and stochastic location $\vec{p}_j(\cdot)$, $j = 1..U$. Here we have introduced the postscript notation $(\cdot)$ to denote that we are dealing with stochastic quantity which is characterized by a probability distribution $\mathfrak{f}(\cdot)$. When the stochastic quantity is scalar the corresponding probability distribution $\mathfrak{f}(\cdot)$ is a function of a single variable; in case the stochastic quantity is a vector then the probability distribution $\mathfrak{f}(\cdot)$ is a function of the same number of variables as the quantity dimension. Using the introduced postscript notation $(\cdot)$ we will denote the cloud of stochastic aspects with $\mathcal{T}(\cdot)$ and the template particle with $P(\cdot)$ as shown on the Figure below:


$A_1(\cdot)$
$\mathfrak{m}_1(\cdot), \vec{p}_1(\cdot)$
$P(\cdot)$
$A_2(\cdot)$
$\mathfrak{m}_2(\cdot), \vec{p}_2(\cdot)$
$\mathfrak{m}_1, \vec{p}_1$
A_1
$\vec{p}_c(\cdot)$
$A_U(\cdot)$
$\vdots$
$\mathfrak{m}_U(\cdot), \vec{p}_U(\cdot)$
$\mathfrak{m}_2, \vec{p}_2$
A_2
$\ddots$
A_K
$\mathfrak{m}_K, \vec{p}_K$

For the centroid of $P(\cdot)$ we write:

$$\vec{p}_c(\cdot) = \sum_{i=1}^{K} \frac{\mathfrak{m}_i}{\mathfrak{m}_{tot}(\cdot)} \vec{p}_i + \sum_{j=1}^{U} \frac{\mathfrak{m}_j(\cdot)}{\mathfrak{m}_{tot}(\cdot)} \vec{p}_j(\cdot) \text{ where } \mathfrak{m}_{tot}(\cdot) = \sum_{i=1}^{K} \mathfrak{m}_i + \sum_{j=1}^{U} \mathfrak{m}_j(\cdot) \qquad (1)$$

The moment in time t_c in which the centroid of the template property assumes position $\vec{p}_c(\cdot)$ can also be stochastic quantity which will be denoted with $t_c(\cdot)$. We will denote with $\vec{P}_c$ the four-vector corresponding to the space-time position of the template property centroid. Obviously,

$\vec{P}_c = \begin{Bmatrix} \vec{p}_c \\ t_c \end{Bmatrix}$ (2)

In general, the four-vector of the template centroid will be a stochastic quantity: $\vec{P}_c(\cdot)$.
Let us denote the four-vectors of the aspects of the template property by $\vec{P}_i(\cdot)$.
Let us denote the distance between the i-th aspect and the centroid with $\vec{d}_i(\cdot)$ and the four-vector corresponding to that distance with $\vec{D}_i(\cdot)$.

In the template property we can have a stochastic cloud $\mathcal{A}(\cdot)$ which matches any subset of aspects $\{A_1, \dots, A_U\}$ such that certain stochastic quantity is preserved. For instance such quantity could be the total semantic mass of the subset of aspects :

$\mathfrak{m}_{\mathcal{A}}(\cdot) = \sum_{j=1}^{U} \mathfrak{m}_j(\cdot)$ (3)

//TODO: elaborate on this item

Definition: *Representation of Template Particle*
The representation of Template Particle exist in template space.

Definition: Optimal Match of The Pattern Matching Region

Inference Structure of Semantic Template

Example of Semantic Template: Calculation of attractive force between semantic structures

Let us consider a newly formed semantic structure S_1. The closest semantic structure will be denoted with S_0. On aggregation level l the nearby semantic structure S_0 can be represented as a graph of n_l substructures.