Note on modeling binding and repulsion force in semantic properties

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We already have stated that the internal structure of a semantic property can be represented by a set of semantic regions occupying a subset of semantic dimensions. Each region denotes a specific semantic aspect of the property. Thus, the total binding / repulsion force is equal to the sum of the of the binding forces between all relevant region pairs minus the sum of the repulsion forces between all relevant region pairs $(\mathbf{r}_a, \mathbf{r}_b)$:

$$f(\mathbf{p}_1, \mathbf{p}_2) = \sum_{a,b} f^+(\mathbf{r}_a, \mathbf{r}_b) + \sum_{c,d} f^-(\mathbf{r}_c, \mathbf{r}_d)$$

The relevant region pairs $(\mathbf{r}_a, \mathbf{r}_b)$ are defined as follows. Let us sort the pairs of regions from \mathbf{p}_1 and \mathbf{p}_2 by the absolute value of the binding force.

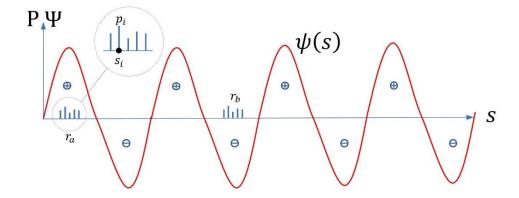
Definition: relevant region pair $(\mathbf{r}_a, \mathbf{r}_b)$ is such pair which has absolute binding force value not in the first ℓ -quantile for some $\ell > 0$. In other words, all region pairs which are *in* the first ℓ -quantile are *irrelevant*.

The question now is how do we want to model the binding / repulsion force between a pair of regions. Here we are proposing a possible way to calculate the binding and repulsion forces and will discuss why it is useful to be done this way.

A pair of regions $(\mathbf{r}_a, \mathbf{r}_b)$ from the properties \mathbf{p}_1 and \mathbf{p}_2 are depicted on the discrete horizontal axis s on the Figure below. The horizontal axis s is discrete in nature and represents the entire set of semantic dimensions for every point in Semantic Space. Let us imagine that region \mathbf{r}_a , composed of a set of semantic values p_i , i=1. dim (\mathbf{r}_a) , will somehow generate a semantic energy ψ_a which will span the entire horizontal axis s and propagate as wave. This wave is depicted in red in the Figure below. Each region will encode the parameters of the impulse $\psi_a(s)$ in its values p_i . $\psi_a(s)$ will, in general, span all dimensions of the semantic space i.e. the integer coordinate s. Obviously, s0 will be periodic function along the semantic dimensions axis s1. As we said the amplitude s2, the frequency s3 and the phase s4 of the impulse are somehow encoded in a portion of each region values. Hence, we can write:

$$\psi_a = \psi_a(s; A, \omega, \varphi)$$
 and $\mathbf{r}_a = \mathbf{r}_a(A, \omega, \varphi)$

Now let us introduce the second region \mathbf{r}_b coming from the other property \mathbf{p}_2 .



The region \mathbf{r}_b is composed of a set of semantic values p_j , $i=1..\dim(\mathbf{r}_b)$ which generate an energy wave ψ_b .

We postulate that the two regions will interact with each other through binding or repulsive force only if the frequencies of the corresponding energy waves <u>are the same</u> i.e. $\omega_a = \omega_b = \omega$.

Let us denote with f_a the following sum $f_a = \sum_{i \in a} \psi_a(s_i)$; Here $\psi_a(s_i)$ is the value of the energy wave at the i-th dimension of region \mathbf{r}_a

Let us denote with f_b the following sum $f_b = \sum_{j \in b} \psi_b(s_j) < 0$; Here $\psi_b(s_j)$ is the value of the energy wave at the j-th dimension of region \mathbf{r}_b

We postulate that region \mathbf{r}_a will attract region \mathbf{r}_b iff:

- 1. The frequencies of the corresponding to each region energy wave are the same i.e. $\omega_a=\omega_b=\omega$
- 2. $f_a f_b < 0$. In other words, either $f_a > 0$ $\land f_b < 0$ or $f_a < 0$ $\land f_b > 0$.

Then the attraction force between the two regions \mathbf{r}_a and \mathbf{r}_b will be given by the product of the absolute values:

$$f^+(\mathbf{r}_a, \mathbf{r}_b) = |f_a||f_b|$$

If $f_a f_b > 0$ then we have a repulsive force instead of attracting one:

$$f^{-}(\mathbf{r}_a, \mathbf{r}_b) = -|f_a||f_b|$$

If we have more than one region with the same frequency ω in one of the properties we sum them up and then multiply with the sum of the regions of the other property:

$$f(\mathbf{p}_1, \mathbf{p}_2; \omega) = \sum_{a,b} f^+(\mathbf{r}_a(\omega), \mathbf{r}_b(\omega)) + \sum_{c,d} f^-(\mathbf{r}_c(\omega), \mathbf{r}_d(\omega))$$

Finally, the total binding/repulsive force between the two properties is given as the sum of all binding/repulsive forces on all frequencies:

$$f(\mathbf{p}_1, \mathbf{p}_2) = \sum_{\omega} f(\mathbf{p}_1, \mathbf{p}_2; \omega)$$

Relation between Semantic Mass and Semantic Energy

Let us consider a property *P* which has some number of non-zero regions:

 $\mathbf{p} = [\mathbf{r}_1, \mathbf{0}, \mathbf{r}_2, \mathbf{0}, ..., \mathbf{0}, \mathbf{r}_k]^T$ where \mathbf{r}_i , i = 1..k are the proper regions in the property signature \mathbf{p} . Let us group the regions by two different criteria – size and frequency. The sets in which the grouping of the regions is done by region size will be denoted with \mathcal{S} . The sets in which the grouping is done by the frequency of semantic energy will be denoted with \mathcal{F} .

For the grouping by region size we have the following sets $S_1, S_2, ..., S_l, l \leq k$. Here the regions which have the largest size are in set S_1 , the second largest regions are in S_2 , ..., and the smallest regions are in S_1 .

For the grouping by energy wave frequency we have the following sets $\mathcal{F}_1, \mathcal{F}_2, \dots, \mathcal{F}_m, m \leq k$.

Every region which generates a wave with the largest frequency ω_1 will be in set \mathcal{F}_1 , every region which generates wave with second largest frequency ω_2 will be in set \mathcal{F}_2 ,..., and the regions with the lowest frequency ω_m will be in set \mathcal{F}_m .

Each semantic region \mathbf{r}_i is constructed by a repetition of a single atomic block \aleph_i :

 $\mathbf{r}_i = \aleph_i \aleph_i ... \aleph_i$ (\aleph_i repeats α times). The atomic block \aleph contains only few data points over a subset of semantic dimensions and encodes the frequency and phase of the energy wave.

The amplitude of the generated energy wave is proportional to the size (length) of the region. In other

The amplitude of the generated energy wave is proportional to the size (length) of the region. In other words, the larger is the repetition count α the larger will be the amplitude A of the energy wave. Based on this we can write the energy function $\psi_{\bf r}$ of region ${\bf r}$ as:

$$\psi_{\mathbf{r}}(s) = A(\alpha)\sin(\omega(\aleph)s + \varphi(\aleph))$$
 where $\mathbf{r} = \aleph \aleph ... \aleph$ (\aleph repeats α times)

and for the semantic mass $M_{\mathbf{r}}$ of the region \mathbf{r} :

 $M_{\mathbf{r}} = \mathcal{C}(\aleph) M(\alpha)$ where $\mathcal{C}(\aleph)$ is some coefficient which possibly depends on the semantic values contained in \aleph and $M(\alpha)$ is monotonously increasing function of the repetition count α . These two expressions for $\psi_{\mathbf{r}}$ and $M_{\mathbf{r}}$ give us the relationship between semantic energy and semantic mass.

Let us return on our previous example with two P-particles each of which has a single region. Particle P_1 has a region \mathbf{r}_1 and Particle P_2 has a region \mathbf{r}_2 . If the two regions are not built from atomic blocks which encode the same frequency the binding/repelling force between the two regions will be 0. Let us assume that the two regions are built from the same atomic block \aleph so they share frequency ω and phase φ . Let us denote by α_1 the repetition count of \aleph in region \mathbf{r}_1 and by α_2 the repetition count of \aleph in region \mathbf{r}_2 . Let us denote by $s_{i_1}, s_{i_2}, \ldots, s_{i_m}$ the semantic dimensions which region \mathbf{r}_1 is spanning. Similarly, by $s_{j_1}, s_{j_2}, \ldots, s_{j_n}$ we denote the semantic dimensions which region \mathbf{r}_2 is spanning. Clearly either m is multiple of n or n is multiple of m.

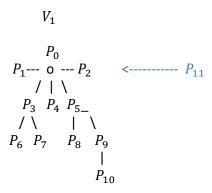
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Relation between Binding/Repulsive Force and Semantic Energy in property

Definition: **Mirror unit particle** of given P-particle P: We denote it with $\mathbb{I}(P)$ and when it is obvious from the context to which P-particle we are referring we will just use the symbol \mathbb{I} .

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Constructing the property tree: constraints and inequalities based on binding force Let is consider the property tree of a *V*-particle:



Let us imagine we want to add new P-particle to the property tree. The following steps toward forming a new ensemble take place:

Step 1. All P-particles which are about to participate in the new ensemble become disassociated / disentangled.

Step 2. The common center of semantic mass for the new ensemble is determined as we already know the semantic masses of all properties in the new ensemble. For details about determining of the semantic mass of an ensemble of properties follow the discussion in On The Semantic Position Of Semantic Structures.

Step 3. The particle with the largest mass will be closest to the common center of gravity and will be root to the property tree.

Special Case:

there are two *P*-particles with the same semantic mass which happens to be the largest mass in the particle tree. Then the particle with the lower semantic energy will be closer to the semantic center than the particle with the higher semantic energy. (not sure about the energy condition). An ensemble in which the heaviest two particles are having the same masses and same energies is ill-formed and one of the two properties has to have a region discarded so it will end up with lower semantic mass.

Step 4. Let us have two particles P-particles P_j and P_k such that $M_{P_j} \ge M_{P_k}$. Let us denote with P_i the particle with the closest but larger semantic mass than that of P_j and P_k . Thus $M_{P_i} > M_{P_j} \ge M_{P_k}$. Then each one of the following configurations are possible:

Case a) will occur when there is non-zero binding force $f_{i,j}^+ = f^+(\mathbf{p}_i, \mathbf{p}_j) > 0$ between P_i and P_j and also between P_i and $P_k - f_{i,k}^+ = f^+(\mathbf{p}_i, \mathbf{p}_k) > 0$. In this case either $M_{P_j} > M_{P_k}$ or $M_{P_j} = M_{P_k}$ and $f_{i,j}^+ > f_{i,k}^+$.

Case b) will occur when there is non-zero binding force $f^+(\mathbf{p}_i,\mathbf{p}_j)>0$ between P_i and P_j and also between P_i and P_k - $f^+(\mathbf{p}_i,\mathbf{p}_k)>0$. In this case $M_{P_j}=M_{P_k}$ and $f_{i,k}^+>f_{i,j}^+$.

Case c) will occur when $f_{i,j}^+>0$, $f_{i,k}^+=0$, and $f_{j,k}^+>0$ when either $M_{P_j}>M_{P_k}$ or $M_{P_j}=M_{P_k}$.

Case d) will occur when $f_{i,k}^+>0$, $f_{i,j}^+=0$, and $f_{j,k}^+>0$ when $M_{P_j}=M_{P_k}$.

Case e) will occur when $f_{i,j}^{\,+}>0$ and $f_{i,k}^{\,+}=0$

Case f) will occur when $f_{i,j}^{\,+}=0$ and $f_{i,k}^{\,+}>0$

Case g) will occur when $f_{i,j}^{\,+}=0$ and $f_{i,k}^{\,+}=0$

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