

## On the need of Dynamic Simulation when modeling interactions of Semantic Structures

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*The machine was all glass retorts and valves and delicately balanced see-saws. Tinted fluids represented different market pressures and financial parameters: interest rates, inflation, trade deficits. The machine sloshed and gurgled, computing ferociously difficult integral equations by the power of applied fluid dynamics. It had enchanted her. She had remade the prototype, adding a few sly refinements of her own. But though the machine had provided some amusement, she had seen only glimpses of emergent behaviour. The machine was too ruthlessly deterministic to throw up any genuine surprises.*

From "Redemption Ark", Chapter 7, Alastair Reynolds, 2002

### Reinforcement learning models for the behavior of Semantic Structures

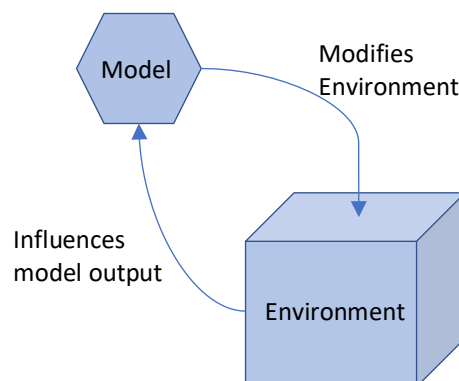
We are considering reinforcement learning models where both are true:

- 1) The environment influences the model
- 2) The model influences the environment

The model influences the environment in such a way that the environment gets conditioned to support certain interactions and encourages forming certain types of ensembles. The pertinent question here is what constitutes the environment. We will consider both a static model and dynamic model for semantic structure interactions. In both static and dynamic modeling the environment is represented by some kind of a *field* which will influence the particles entering semantic space either via inference or via parsing. The environment will condition those new particles to form certain kinds of ensembles and to associate them in a certain preferred way with the existing semantic structures.

### The Role of the Environment in parsing and inference of semantic structures

The model of semantic structure interactions in conjunction of the Environment determines how the incoming semantic particles will form semantic structures and how the newly formed structures will interact with the existing ones.



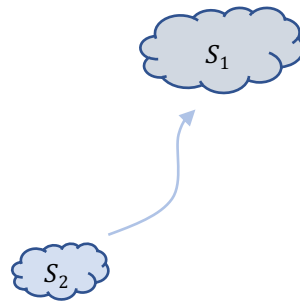
When semantic structures are formed from semantic particles certain semantic paths will be reinforced by the Model while other paths will be discouraged. The reinforcement happens based on certain statistics computed for every newly formed structure. Discouragement happens when the attempt to form a semantic structure fails.

## Dynamic vs Static models of the behavior and interactions of Semantic Structures

### What is Static Modeling of the Semantic Structures behavior?

Static modeling implies that we do not model *the time* and we do not have *time coordinate* in our models of the interactions of Semantic Structures. We do not have explicit or implicit *time dependence* in any of our relations and the concept of *passed time* is devoid of meaning.

This brings a simplicity to our models as all adjustments in the positions and the interactions between Semantic Structures are instantaneous. For instance, suppose we have an existing semantic structure  $S_1$  which is located on a particular position in Semantic Space. We have just constructed another semantic structure  $S_2$  and we would like to evaluate how much it will displace  $S_1$  and in which direction.



One can use a static model to calculate what will be the new position of  $S_1$  and  $S_2$  given their total mass and given the attractive and repulsive forces acting on substructures of  $S_1$  and  $S_2$ . Specifically, let us assume that there are  $m$  substructure pairs in  $S_1$  and  $S_2$  which attract each other pairwise. Also, we will assume that there are  $n$  substructure pairs in  $S_1$  and  $S_2$  which repel each other pairwise.

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### Introducing Dynamic Model of Semantic Structures behavior

In the Dynamic models for Semantic Structures we define the concept of *time* in semantic space. We also define the vector *velocity* of a semantic particle/structure. We will use both time and velocity to determine the exact time and the amount of interaction between semantic structures which will take place at some future moment.

Let us define a  $L$ -dimensional vector field  $\mathfrak{F}$  in  $L$ -dimensional semantic space. This field will have an effect of the semantic particles in such a way that it will apply an additional momentum to the particle which will be proportional to the travel path of the particle and to the strength and orientation of  $\mathfrak{F}$ . Let us denote by  $\vec{f}$  a vector from the field  $\mathfrak{F}$  at position  $\vec{r}$  and time  $t$ :

$$\vec{f} = \vec{f}(\vec{r}, t) \quad (1)$$

For instance, let us consider an ensemble of four properties  $P_i, i = 1..4$ . which are not in their bound state positions but in some general positions.



One could think of the vector field  $\vec{f}(\vec{r}, t)$  as a Force field distributed along the travel path of a semantic particle. The path of any semantic particle in Semantic Space can be expressed in terms of its natural coordinate  $s$ . On the Figure below it is shown the path of a particle with starting point  $s_0$ . Let us denote



with  $t_0$  the moment of time in which the particle has been at position  $s_0$ . The particle is in position  $s_{k-1}$  at a moment  $t_{k-1}$ , it is in position  $s_k$  at a moment  $t_k$  after traveling  $\Delta s_k$  and finally it ends up in position  $s_e$ . Let us write the recursive relation between two consecutive positions denoted with  $k - 1$  and  $k$  accordingly. Since we are creating a dynamic model which includes a time dependence in each model parameter we are no longer going to use subscripts to denote the positions but rather will use the functional dependence  $(\cdot)$  to indicate implicit time dependence for every model parameter. With that note in mind the recursive relation for two consecutive positions given in their natural coordinates  $s(k - 1)$  and  $s(k)$  become:

$$s(k) = s(k - 1) + \Delta s(k) \quad (2)$$

In case of a property  $P$  travelling toward its bound state we will have:

$$E_P(k) = E_P(k - 1) + \sum_{j=1}^{N(P)} \vec{f}(\vec{p}_j(k - 1) + \Delta \vec{p}(k), l_j) \Delta \vec{p}(k) \quad (3)$$

Here  $N(P)$  represents the number of semantic aspects in  $P$ . The vector in semantic space  $\vec{p}_j(k-1)$  represents the position of the aspect  $A_j(P)$  in a previous time moment  $t_{k-1}$

Thus, for each aspect  $A_j(P)$  we can write the following recurrent relation between  $A_j(P)$ 's previous position and the current one:

$$\vec{p}_j(k) = \vec{p}_j(k-1) + \Delta\vec{p}(k) \quad (4)$$

If we denote with  $\vec{p}_c(k)$  the position of the centroid of the property  $P$  at time  $t_k$  we have similar to (4) recurrent relation for the centroid of  $P$ :

$$\vec{p}_c(k) = \vec{p}_c(k-1) + \Delta\vec{p}(k) \quad (5)$$

Let us denote with  $\vec{p}_E(k)$  the position of energy weighted center of the ensemble  $V$  at time  $t_k$ . Then we have:

$$\Delta\vec{p}(k) = \frac{\vec{p}_E(k) - \vec{p}_c(k)}{|\vec{p}_E(k) - \vec{p}_c(k)|} \Delta s(k) \quad (6)$$

Note that at every moment  $t_k$  we can calculate:

- the energy-weighted center  $\vec{p}_E(k)$  of the ensemble
- the increments  $\Delta\vec{p}_i(k)$  of the new positions of the centroids  $\vec{p}_{c,i}$  of the properties  $P_i$
- the energy  $E(\vec{p}_{c,i}(k))$  at the new positions of the centroids  $\vec{p}_{c,i}$  of the properties  $P_i$
- harmonic energy aggregate  $\tilde{E}(k)$  of the ensemble

from the coupled system of equations:

$$\left\{ \begin{array}{l} E(\vec{p}_{c,i} + \Delta\vec{p}_i) = E(\vec{p}_{c,i}) + \sum_{j=1}^{N_i} \vec{f}(\vec{p}_{i,j} + \Delta\vec{p}_i, l_{i,j}) \Delta\vec{p}_i \\ \tilde{E} = \frac{\sum_{i=1}^M m_i}{\sum_{i=1}^M \frac{m_i}{E_t(\vec{p}_{c,i} + \Delta\vec{p}_i)}} \\ \vec{p}_E = \sum_{i=1}^M \frac{\tilde{E}_t m_i}{E_t(\vec{p}_{c,i} + \Delta\vec{p}_i)} (\vec{p}_{c,i} + \Delta\vec{p}_i) \\ \Delta\vec{p}_i = \frac{\vec{p}_E - \vec{p}_{c,i}}{|\vec{p}_E - \vec{p}_{c,i}|} \Delta s \end{array} \right. \quad (7)$$

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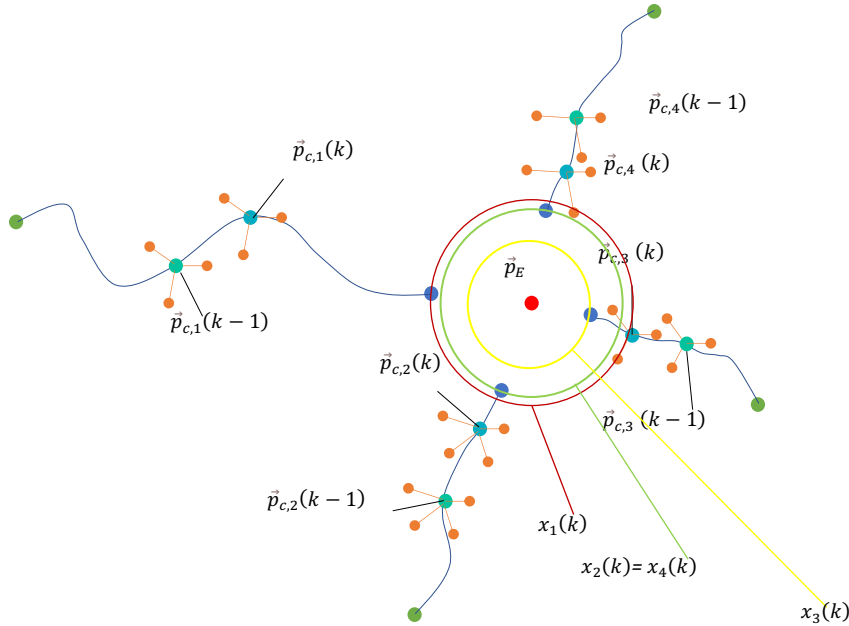
So using the relations (1) - (7) one can determine the movements of the centroids of each of the properties, the energies stored in the properties and the position of the energy weighted centroid of the ensemble for each moment of time. However, we will not be able to determine the positions or the behavior of each property near their bound states. For this we will need to add one extra piece to our dynamic model.

## Dynamic modeling of bound state behavior

With static models the bound state of each property is represented by two semantic quantities – the ending position of the travel path and the net energy of the property at that position. Implicitly assumed in static models is that the environment (e.g. scalar energy field) is conditioned in such way that each property will reach the ending position of its bound state.

$$\left\{ \begin{array}{l} E(\vec{p}_{c,i} + \Delta\vec{p}_i) = E(\vec{p}_{c,i}) + \sum_{j=1}^{N_i} \vec{f}(\vec{p}_{i,j} + \Delta\vec{p}_i, l_{i,j}) \Delta\vec{p}_i - E_b(\vec{p}_{c,i} + \Delta\vec{p}_i) + E_b(\vec{p}_{c,i}) \\ x_i = \sqrt{\frac{E(\vec{p}_{c,i} + \Delta\vec{p}_i)}{m_i}} K_i \quad ; \quad K_i = 1 + \frac{\lambda_i}{2} + \frac{\lambda_i^2}{3} + \mathcal{O}(\lambda_i^3) \quad ; \quad \lambda_i = \frac{E(\vec{p}_{c,i} + \Delta\vec{p}_i)}{\sum_{i=1}^M E(\vec{p}_{c,i} + \Delta\vec{p}_i)} \\ F_b(\vec{p}_{c,i}) = C_b \left( \frac{\tanh\left(\frac{x_i - |\vec{p}_E - \vec{p}_{c,i}|}{x_u}\right) + 1}{2} \right) \left( \frac{x_i}{|\vec{p}_E - \vec{p}_{c,i}|} - 1 \right) (\vec{p}_E - \vec{p}_{c,i}) \\ E_b(\vec{p}_{c,i} + \Delta\vec{p}_i) - E_b(\vec{p}_{c,i}) = F_b(\vec{p}_{c,i}) \Delta\vec{p}_i \\ \tilde{E} = \frac{\sum_{i=1}^M m_i}{\sum_{i=1}^M \frac{m_i}{E(\vec{p}_{c,i} + \Delta\vec{p}_i)}} \\ \vec{p}_E = \sum_{i=1}^M \frac{\tilde{E} m_i}{E(\vec{p}_{c,i} + \Delta\vec{p}_i)} (\vec{p}_{c,i} + \Delta\vec{p}_i) \\ \Delta\vec{p}_i = \frac{\vec{p}_E - \vec{p}_{c,i}}{|\vec{p}_E - \vec{p}_{c,i}|} \Delta s \end{array} \right.$$

Here  $x_u \ll \min_i x_i$ .



Let us

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Initial conditions in the dynamic equations of an ensemble

Let us have the following initial conditions: Each property  $P_i$  of the ensemble is subjected to initial impulse  $L_0^{(i)} = m_i \vec{v}_0^{(i)}$  applied at the centroid  $\vec{p}_{c,i}$ . With

$$\left\{ \begin{array}{l} E(\vec{p}_{c,i} + \Delta \vec{p}_i) = E(\vec{p}_{c,i}) + \sum_{j=1}^{N_i} \vec{f}(\vec{p}_{i,j} + \Delta \vec{p}_i, l_{i,j}) \Delta \vec{p}_i \\ \tilde{E} = \frac{\sum_{i=1}^M m_i}{\sum_{i=1}^M \frac{m_i}{E_t(\vec{p}_{c,i} + \Delta \vec{p}_i)}} \\ \vec{p}_E = \sum_{i=1}^M \frac{\tilde{E}_t m_i}{E_t(\vec{p}_{c,i} + \Delta \vec{p}_i)} (\vec{p}_{c,i} + \Delta \vec{p}_i) \\ \Delta \vec{p}_i = \frac{\vec{p}_E - \vec{p}_{c,i}}{|\vec{p}_E - \vec{p}_{c,i}|} \frac{E(\vec{p}_{c,i} + \Delta \vec{p}_i)}{E(\vec{p}_{c,i} + \Delta \vec{p}_i) + E_0^{(i)}} \Delta s + \frac{\vec{p}_0^{(i)} - \vec{p}_{c,i}}{|\vec{p}_0^{(i)} - \vec{p}_{c,i}|} \frac{E_0^{(i)}}{E(\vec{p}_{c,i} + \Delta \vec{p}_i) + E_0^{(i)}} \Delta s \end{array} \right.$$

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