Notes on Reinforcement Learning and Deep Reinforcement Learning

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# Introductory Notes

What is Reinforcement Learning: branch of machine learning concerned with making decisions and taking sequences of actions based on some current state thereby maximizing some reward objective over time.

action

Environment

Agent

state, reward

Figure 1: Feedback loop between the Agent and the Environment in RL

The Agent and the Environment interact with each other on discrete timesteps creating a feedback loop depicted in Figure 1. The Agent has a goal of maximizing the cumulative reward while interacting with the Environment.

Observations in RL:

Robotics: camera images, joint angles

Actions in RL:

Robotics: joint torques

Rewards in RL:

Robotics: stay balanced, navigate to target locations

Approaches to RL

Dynamic Programming

Policy Optimization

Value Iteration

Policy Iteration

Policy Gradients

DFO / Evolution

Q Learning

Actor-Critic Methods

Two approaches to RL – the first approach is to optimize policy and the second one is dynamic programming.

Policy is the function which takes the observations with the state of the system and outputs actions. The Policy Optimization approach looks at the RL problem as an optimization problem trying to optimize the expected reward , there are parameters in the policy, and we want to find such set of parameters which maximizes the expectation of the stochastic reward. Posing the problem as an optimization problem ignores all of the structure of the problem conveyed through the Bellman’s equations. We are getting a noisy estimate of how good each parameter is and try to move toward that part of the parameter space where we are getting better performance – that is, higher expected reward. So, this is how the Derivative Free Optimization (DFO) methods and Evolutionary algorithms work – they work as a black box which takes a policy parameter vector and outputs a noisy performance number. These methods are very simple to implement, and they work surprisingly well. The other approach for Policy Optimization is by using Policy Gradient methods trying to measure the gradient of the performance with respect to the parameter vector of the policy. These second type of Policy Optimization methods scale better with respect to the number of parameters. Dynamic Programming / Approximate Dynamic Programming is a very different approach to solving RL problems. In certain cases, we can solve control problems exactly. What if we have slightly different parameter settings, will these algorithms still work? It turns out we can modify these algorithms in certain ways which can keep them valid. Policy Iteration and Value Iteration are the two algorithms which will exactly solve the MDP formulation of the RL problem and finding the optimal policy, but they only work if you have discrete state space and action space. If these spaces are finite sets, we can solve exactly the RL problem. In many real world problems, we need to do approximate versions of these algorithms. There is a dedicated field developing approximate dynamic programming algorithms for those real world problems which cannot be solved exactly. Q-Learning is one quite popular and successful method in this category. We can do Q Learning with function approximation performed by Neural network. Lastly, there are Actor-Critic methods – they are policy gradient methods, but they also use value functions helping the policy gradient method. These methods can scale well and be used to solve large / hard problems.

What is Deep RL?

It is RL using nonlinear function approximators, which do not make a lot of assumptions about the form of the approximated function. At any given time, the algorithm is solving optimization problem with gradient descent.

Markov Decision Process (MDP)

MDP is defined by the triplet where

is the state space

is the action space

is the transition probability distribution

tells us the probability of the reward (scalar) , the next state (vector) given the current state (vector) and the action (vector).

Extra objects can be defined depending on the problem setting:

- initial state distribution

– discount factor

In each episode, the initial state is sampled from , and the process proceeds until terminal state is reached.

In the episodic setting the agent experiences are broken up into a sequence of episodes. In each episode a reward and a new state are generated from the old state after action is chosen. And this process continuous for each episode sequentially until we reach a terminal state. The terminal state is a special state with 0 reward from which there is no continuation. We can have different termination semantics – termination can indicate a good outcome (example: taxi robot reaches its destination), termination is neither good nor bad and always occurs (waiter robot finishes its shift after fixed amount of time), termination indicates bad outcome (walking robot fails over).

We want to maximize the expected reward per episode.

We consider two kinds of policies:

deterministic policies

stochastic policies – in this case the policy defines a conditional probability distribution over actions.

The policy will be the optimized function in our optimization problem.

Parametrized policy

there is some parameter vector which indexes over the policy.

So based on this discussion we can write:

– terminal state (in.1)

Objective:

maximize , where

(in.2)

//TODO: finish this section (Lecture 1 of John Schulman)

# Intro to Policy Optimization

We consider the case of stochastic parametrized policy . We want to maximize the expected return . For the purposes of this derivation, we will take to give the finite horizon undiscounted return, but the derivation for the infinite horizon discounted return setting is almost identical.

We would like to optimize the policy by gradient ascent as

(ipo.1)

The gradient of policy performance, , is called policy gradient, and algorithms that optimize the policy this way are called *policy gradient algorithms*. Examples of such algorithms include Vanilla Policy Gradient and TRPO. PPO is often referred to as a policy gradient algorithm, though this is slightly inaccurate as PPO uses value functions to obtain better policy approximation.

To actually use this algorithm, we need an expression for the policy gradient which we can numerically compute. This involves two steps : 1) deriving the analytical gradient of policy performance, which turns out to have the form of an expected value, which can be computed with data from a finite number of agent-environment interaction steps.

We begin with few definitions and statements used in the derivation of policy gradient

**Definition** *Probability of a Trajectory*

The probability of a trajectory given that actions come from is

(ipo.2)

**Definition** *The Log-Derivative Trick*

**Definition** *Log-Probability of a Trajectory*

The log-prob of a trajectory is just

**Statement**: *The gradients of environment functions are zero*. This is because the environment has no dependence on , so gradients of , and are zero.

Then the expression of the Grad-Log-Prob of a trajectory is given with

.

Putting it all together, we derive the following:

Derivation for Basic Policy Gradient

(via the Log derivative trick)

(rewritten as expectation)

(expression for grad-log-prob)

This is an expectation, which means that we can estimate it with a sample mean. If we collect a set of trajectories where each trajectory is obtained by letting the agent act in the environment using the policy , the policy gradient can be estimated with

,

where is the number of trajectories in (here, ).

This last expression is the simplest version of the computable expression we desired. Assuming that we have represented our policy in a way which allows us to calculate , and if we are able to run the policy in the environment to collect the trajectory dataset, we can compute the policy gradient and take an update step.

**Lemma** *EGLP Lemma*

Expected Grad-Log-Prob is zero.

Suppose that is a parametrized probability distribution over a random variable, . Then:

Proof:

Since is a distribution, we have:

Applying gradient on both sides gives us:

Use the log derivative trick to get:

Let us examine the most recent expression for the policy gradient:

Taking a step with this gradient pushes up the log-probabilities of each action in proportion to which of course is the sum of all rewards obtained along the trajectory . However, such proportional push for *all* possible actions does not make much sense. Instead, agents should really only reinforce actions on the basis of their *consequences*. Rewards obtained before taking an action have no bearing on how good the action was: only rewards that come *after*. We can express this intuition with the expression for the policy gradient:

In this form, actions are only reinforced based on rewards obtained after they are taken.

We’ll call this form the “reward-to-go gradient”, because the sum of rewards after a point in a trajectory,

is called the reward-to-go from that point, and this policy gradient expression depends on the reward-to-go from state-action pairs.

A key problem with policy gradients is how many sample trajectories are needed to get a low-variance estimate for them. The formula we started with-

includes terms for reinforcing actions proportional to past rewards all of which had zero mean but non-zero variance: as a result, they would just add noise to sample estimates of the policy gradient. By removing them we reduce the number of sample trajectories needed.

## Baselines in Policy Gradients

An immediate consequence of the EGLP lemma is that for any function which only depends on state,

This allows us to add or subtract any number of terms like this from our expression for the policy gradient, without changing it in expectation:

Any function used in this way is called a *baseline*.

The most common choice of baseline is the on-policy value function . Recall that this is the average return an agent gets if it starts in state and then acts according to policy for the rest of its life.

Empirically, the choice has the desirable effect of reducing variance in the sample estimate for the policy gradient. This results in faster and more stable policy learning. Conceptually, it encodes the intuition that if an agent gets what it expected, it should “feel” neutral about it.

**Note**:

In reality, cannot be computed exactly, so it has to be approximated. This is usually done with a neural network, , which is updated concurrently with the policy so that the value network always approximates the value function of the most recent policy.

The simplest method for learning , used in most implementations of policy optimization algorithms (including VPG, TRPO, PPO and A2C) is to minimize a mean-squared-error objective

where is the policy at epoch . This is done with one or more steps of gradient descent, starting from the previous value parameters .

## Other Forms of the Policy Gradient

What we have seen so far is that the policy gradient has the general form

where could be any of

,

or

or

All of this forms of lead to the same expected value for the policy gradient, despite having different variances.

There are two more good choices of weights which we will discuss

1 ) ***On-Policy Action-Value Function***

is a good choice for policy gradient weights.

Proof:

We need to prove that

. We will prove it for finite-horizon undiscounted return setting. We will sketch a proof for the infinite horizon discounted return.

We rewrite the expression for the policy gradient, using an expression for the reward-to-go as:

Define as the trajectory up to time t, and as the remainder of the trajectory after that. By the law of iterated expectations, we can break up the preceding expression into:

The grad-log-prob is constant with respect to the inner expectation because it depends on and , which the inner expectation conditions on as fixed in . Thus, the grad-log-prob can be pulled out of the inner expectation expression:

In MDP, the future only depends on the most recent state and action. As a result, the inner expectation, which expects over the future, conditioned on the entirety of the past (everything up to time ) – is equal to the same expectation if it only conditioned on the last timestep :

which is the definition of : expected return, starting from state and action , when acting on-policy for the rest of the trajectory.

2 ) **The Advantage Function**

The Advantage of an action is given with

describes how much better or worse it is than other actions on average relative to the current policy.

This choice is a good choice for policy gradient weights.

Proof: The argument is equivalent to the argument that and then use the value function as a baseline which leads to an unbiased estimate.

## Vanilla Policy Gradient

Background

The key idea underlying policy gradients is to push up the probabilities of actions that lead to higher return and push down the probabilities of actions that lead to lower return, until we arrive at optimal policy.

VPG is on-policy algorithm and can be used as a model with environments with either discrete or continuous action spaces.

As before, let denote the expected finite-horizon undiscounted return of the policy. The gradient of is

where is a trajectory and is the advantage function for the current policy.

The policy gradient algorithm works by updating the policy parameters via stochastic gradient descent on policy performance:

Policy gradient implementations typically compute advantage function estimates based on the infinite-horizon discounted return, despite otherwise using the finite-horizon undiscounted policy gradient formula.

VPG trains a stochastic policy in an on-policy way. This means that it explores by sampling actions according to the latest version of its stochastic policy. The amount of randomness in action selection depends on both initial conditions and the training procedure.

//TODO: finish the VPG algorithm

## Generalized Advantage Estimator

As specified in [35] let us consider an undiscounted formulation of the policy optimization problem. The initial state is sampled from distribution . A trajectory is generated by sampling actions according to policy and sampling the states according to the dynamics , until a terminal absorbing state is reached. A reward is received at each timestep. The goal is to maximize the expected total reward , which is assumed to be finite for all policies. Notice that discount is not introduced yet in the algorithm. Discount will be introduced at a later step as an algorithm parameter that adjusts the bias-variance tradeoff. In [35] Schulman asserts that we can absorb the discount factor in the reward function by making it time dependent.

Recall that policy gradient methods maximize the expected total reward by repeatedly estimating the gradient . There are several different related expressions for the policy gradient, which have the form:

(gae.1)

where may be one of the following:

1 ) total reward of the trajectory:

2 ) reward following action :

3 ) baselined version of the reward following action :

4 ) state-action value function:

5 ) advantage function:

6 ) TD residual:

The latter formulas use the definitions

(gae.2)

(gae.3) Advantage function

Here the subscript of enumerates the variables being integrated over, where states and actions are sampled sequentially from the dynamics function and policy , respectively. The colon notation refers to the inclusive range .

We will introduce a parameter that allows us to reduce variance by downweighing rewards corresponding to delayed effects, at the cost of introducing bias. This parameter corresponds to the discount factor used in discounted formulations of MDPs, but it can be treated as a variance reduction parameter in an undiscounted problem. For details on this technique to incorporate the discount factor see [36].

The discounted value functions are given by:

(gae.4)

(gae.5) Discounted advantage function

The discounted approximation to the policy gradient is defined as follows:

(gae.6)

Question: how to obtain a reasonably biased estimator for which will give us a noisy estimate for the discounted policy gradient in (gae.6)?

### -just estimator

We will introduce the notion of a -just estimator of the advantage function. The -just estimator is an estimator which does not introduce bias when we use it in place of the unknown quantity in the expression for .

Note that we have already introduced bias by using in place of ; here we are concerned with obtaining an unbiased estimate of , which is a biased estimate of the policy gradient of the undiscounted MDP.

Consider an advantage estimator which in general is a function of the entire trajectory.

**Definition**: The estimator is -just if

(gae.7)

It follows immediately that if is -just for all , then

(gae.8)

One sufficient condition for to be -just is that decomposes as the difference between two functions and , where can depend on any trajectory variables from the moment but gives an unbiased estimator of the -discounted -function, and is an arbitrary function of the states and actions sampled before .

**Proposition**: Suppose that can be written in the form such that for all , . Then is -just.

Proof:

First, we split the expectation in the approximate expression for into two terms involving and :

(gae.9)

We’ll consider the terms with and in turn:

(gae.10)

Next,

(gae.11)

The last identity is true due to the EGLP Lemma proven earlier*.*

Thus we have shown that when holds then (gae.12)

**Proposition**: The following expressions are -just advantage estimators for :

, , , (gae.13)

Proof:

Let us start with – according to the definition of -just advantage estimator we must show that

(gae.14)

where .

Thus, the LHS of (gae.14) becomes (gae.15)

The last expression in (gae.15) is obviously the RHS of (gae.14).

Notice that in order to obtain (gae.15) we have used the fact that which follows from (gae.11).

//TODO: finish the section on Generalized Advantage Estimator

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# Appendix

## Stochastic Gradient Descent

### Gradient Bandit Algorithm and Stochastic Gradient Descent

//TODO: finish Gradient Bandit interpretation as SGD

//TODO: finish the appendix on SGD