Notes on Vector Retrieval

Compiled by D. Gueorguiev, 10/18/2025, following Sebastian Bruch’s *“Foundations of Vector Retrieval”*

# Introductory Notes

A diagram of a number

AI-generated content may be incorrect.Let us consider a text document in English. Strip the document of grammar and word order and we end up with *a set* of words a.k.a. “bag of words” (BoW).

Figure: Vector representation of a piece of text by adopting BoW approach: a text document, when stripped of grammar and word order, is represented by a vector where each coordinate represents a term in our vocabulary and its value records the frequency of that term or represent some function of the frequency. The resulting vectors are *sparse* – that is , they have few non-zero coordinates.

Transformer-based models ([5], [6]) brought about vector representations that beyond the elementary formation above. The resulting vector representation is referred to as an *embedding*, instead of a “feature vector”, though the underlying concept is the same – an object is encoded as a real -dimensional vector, a point in .

Question: how the embedding of a text document differs from its representation as a frequency-based feature vector?

In the lexical BoW representation if a coordinate is non-zero, that implies that the corresponding term is present in the document and its value indicates its frequence-based feature. In the embedding representation our embedding algorithm *learns* to turn coordinates on or off and when a coordinate is turned on , its value must predict the significance of the corresponding term based on semantics and contextual information. For example, the absent synonyms of a present term may get a non-zero value, and terms that offer little discriminative power in the given context become 0 or close to it.

Similarity in vector space must imply similarity between objects. So, as we engineer features to be extracted from an object or design a protocol to learn a model to produce embeddings of data, we must choose the dimensionality of the target space (a subset of ) along with a distance function . Together, these define an inner product of metric space.

Consider the lexical representation of a text document where d is the size of the English vocabulary

# References

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[5] [Attention is all you need, Ashish Vaswani, Google Brain, 2017](https://github.com/dimitarpg13/transformers_intro/blob/main/articles_and_books/Attention-is-all-you-need-NIPS-2017.pdf)

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