

Bellman Ford

- It is a “single source shortest path” algorithm.
- Time Complexity: $O(V \cdot E)$
- **Dijkstra's** is much faster when we use a heap priority Queue.
But can fail when the graph $G(V,E)$ has negative edge weights!
- Bellman Ford can be used to: detect negative cycles.

Algorithm():

input: V (num of vertices), E (num of edges), s the source node,
 D (array of size V) that tracks the best distance from s to any other node.

```
> Set every entry in D to +∞ // distance unknown
> D[s] = 0 ; // we're already there
> // Relax every edge V-1 times
  for(i=0; i<V-1; i++){
    for(edge in graph.edges){
      // Relax edge(update D with a shorter path)
      if(D[edge.from] + edge.cost < D[edge.to]){
        D[edge.to] = D[edge.from] + edge.cost ;
      }
    }
  }
> // Repeat to find nodes part or caught up in a negative cycles
  for(i=0; i<V-1; i++){
    for(edge in graph.edges){
      // Relax edge(update D with a shorter path)
      if(D[edge.from] + edge.cost < D[edge.to]){
        D[edge.to] = -∞ ;
      }
    }
  }
```

Comment: You may be able to detect the cycles at the 1st loop !
But worst case is $V-1$ loops!