

**Question 1: (10 + 10 = 20 points)**

- (a) Perform the following arithmetic operations using non signed numbers representation.

1-  $(1001.01)_2 - (10101.10)_2$

(show the carry after each addition of two digits)

2-  $(10100.011)_2 + (11001)_2$  (show the carry after addition of each two digits)

- (b) Convert  $A = (15.5)_{10}$  and  $B = (16.45)_{10}$  into binary format employing 6 bits for the integer part and 2 for the fractional part, including the sign bit. Perform the following operations using the signed 1's complement representation.

(i)  $C = A + B$

(ii)  $D = -A + B$

**Question 2: (10 + 10 + 10 = 30 points)**

Given the following Boolean function together with the "don't care" conditions X:

$F(a,b,c,d) = \sum m(2,3,4,6,9, 11,12)$  and  $X(a,b,c,d) = \sum m(0,1,14,15)$

$G(a,b,c,d) = \sum m(2,6,10,11,12)$  and  $X(a,b,c,d) = \sum m(0,1,14,15)$

- Find the minimal Sum-of-products expressions of the given functions using K-map.
- Implement your minimized functions with NAND gates only and draw the logic diagram of your circuit.
- Use a multiplexer to implement G (assume that any type of gates with any number of inputs are available)

**Question 3: (15 points)**

Design a ripple (asynchronous) counter with JK flip flops that having to count sequences from 0000 (zero) to 1001 (9) and draw the corresponding logic circuit.

- Build the state table for the counter the first 8 clock pulse
- Draw the logic circuit
- What is the Modulus of the counter?