Fall 2023 Programming Languages Homework 2

- Due on Wednesday, October 11, 2023 at 11:59 PM, Eastern Time (ET).
- The homework must be submitted through NYU BrightSpace—do not send by email. Due to timing considerations, late submissions will not be accepted after the deadline above. No exceptions will be made.
- I strongly recommend that you submit your solutions well in advance of the deadline, in case you have issues using the system or are unfamiliar with NYU BrightSpace. Be very careful while submitting to ensure that you follow all required steps.
- Do not collaborate with any person for the purposes of answering homework questions.
- Use the Racket Scheme interpreter for the programming portion of the assignment. *Important*: Be sure to select "R5RS" from the language menu before beginning the assignment. You can save your Scheme code to an .rkt file by selecting *Save Definitions* from the File menu. Be sure to comment your code appropriately and submit the .rkt file.
- When you're ready to submit your homework upload a single file, hw2-<netID>.zip, to NYU BrightSpace. The .zip archive should contain two files: hw2-<netID>.pdf containing solutions to the first four questions, and hw2-<netID>.rkt containing solutions to the Scheme programming question. Make sure that running your .rkt file in the DrRacket interpreter does not cause any errors. Non-compiling programs will not be graded.

1. [25 points] Activation Records and Lifetimes

- 1. In class, we discussed an implementation issue in the C programming language relating to the printf function. Recall that reversing the order of the arguments was the solution to the problem of not being able to access the format string using a constant frame pointer offset. Such a scheme allows the format string to be accessed and inspected by the language runtime to determine the number of arguments, their types, and sizes.
 - Put yourself in the shoes of a language designer. Consider an alternate method of implementing a variable-argument functions that does not use a format string at all. Assume it is up to the compiler to figure out how many parameters there are and their sizes. You should assume the usual C convention of call-by-value parameter passing. Explain at a high level how such a scheme could work. A good starting point is to consider what information the compiler has available to it. Here are some questions to contemplate in arriving at your answer. How might the compiler organize the activation record? How might it use the information available to identify where all of the arguments are located in the activation record? How would the function access the formals?
- 2. Consider a programming language "NoRec." In this language, programmers cannot write programs with recursion (i.e., procedures cannot call themselves, directly or indirectly through other subprograms). Is it possible for a language to enforce this rule statically? Assume NoRec has no function types (i.e., variables you can declare which "point" to functions).
 - Please note that the answer may differ based upon your assumptions. There may not be a single correct answer. We are more interested in how you apply your reasoning. Hint to get you thinking: how might the presence of control structures such as if-then-else or loops affect the answer? What about unused subprograms?
- 3. Now consider another programming language "AllRec," where every subprogram *must* terminate in a recursive call—again, either directly or indirectly through other subprograms. Is it possible to have such a language? If so, how might it work?
- 4. Refer to slide 27 of the Subprograms lecture. This slide demonstrates the limits of stack-based allocation. Specifically, the activation record of Make_Incr will disappear after Make_Incr returns and along with it will go Make_Incr's formal parameter, X.
 - The way functional languages overcome this problem is to place all activation records in the heap so that activation records like Make_Incr can be kept around longer than they ordinarily would. This allows Make_Incr's formal parameter, X, to be available when "Add_Five" is called on the last line of the slide.
 - Suppose storing activation records in the heap wasn't an option. Can you think of other ways to overcome the "Limits of Stack Based Allocation"?

2. [15 points] Nested Subprograms

Consider the following pseudo-code:

```
procedure MAIN;
    var X : integer = 3;
    procedure BIGSUB;
        var A : integer = 1;
        var B : integer = 2;
        procedure SUB1;
            var A : integer = 7;
            var C : integer = 3
        begin {SUB1}
                            <----- (1)
            A := B + C;
            print(A, B, C);
        end; {SUB1}
        procedure SUB2(X : integer);
            var B : integer = 2;
            var E : integer = 4;
            procedure SUB3;
                var C: integer = 9;
            begin {SUB3}
                SUB1;
                E := B + C;
                print(E);
            end; {SUB3}
        begin {SUB2}
            SUB3;
            A := E;
        end; {SUB2}
    begin {BIGSUB}
        SUB2(7);
    end; {BIGSUB}
begin
    BIGSUB;
end; {MAIN}
```

Please answer the following:

a. Write the name and actual parameter value of every subprogram that is called, in the order in which each is activated, starting with a call to MAIN. Assume static scoping rules apply.

```
Example: MAIN \rightarrow BIGSUB \rightarrow \dots
```

b. Over the lifetime of the program above, which variables hold values that never change (e.g., are never assigned in the scope in which they exist)? Don't forget to consider formal parameters. Identify the scope of the variables to be clear about which declaration you are referring to.

Example: FOO.X, BAR.Y ...

c. For the remaining variables that *did* change, what is the last value each variable held during their lifetime?

Example: FOO.Y=11, BAR.Z=2...

- d. Assume now that dynamic scoping rules are in effect. Does this change the behavior of the program above? Explain why or why not. You don't have to perform an exhaustive trace, but identify at least one behavior that would be different under dynamic scoping rules.
- e. Draw the runtime stack as it will exist when execution finishes the line marked (1), after first invoking procedure MAIN. Your drawing must contain the following details:
 - Write the activation records in the proper order. The position of *MAIN* in your stack will imply the stack orientation, so no need to specify that separately.
 - Each activation record must show the name of the procedure and its local variable bindings.
 - Assume static linkages are used and draw them.
- f. According to the static scoping rules we've learned, can MAIN invoke SUB3? Give brief explanation for your answer. Can SUB3 invoke MAIN?

3. [10 points] Parameter Passing

1. Trace the following code assuming all parameters are passed using *call-by-name* semantics. Evaluate each formal parameter and show its value after each loop iteration (as if each one was evaluated at the bottom of the loop.)

Example:

```
After iteration 1: a1 = ?, a2 = ?, a3 = ?, a4 = ?
After iteration 2: a1 = ?, ...
```

- 2. Perform the same trace as above, where a1 and a5 are passed using call-by-name semantics, a2 and a3 are passed using call-by-need semantics, and a4 is passed using call-by-value semantics.
- 3. Perform the same trace as above, where all arguments are passed by call-by-value.

```
var i=1, j=10;

mystery(i, i+1, i*3, i, j-2)

procedure mystery (a1, a2, a3, a4, a5)

for count from 1 to 3 do  // 1 to 3 inclusive
    a1 = a2 + a3 + a5;
    a4 = a4 + a1;
    end for;

end procedure;
```

4. [25 points] Lambda Calculus

1. This first set of problems will require you to correctly interpret the precedence and associativity rules for Lambda calculus and also properly identify free and bound variables. For each of the following expressions, rewrite the expression using parentheses to make the structure of the expression explicit (make sure it is equivalent to the original expression). Remember the "application over abstraction" precedence rule together with the left-associativity of application and right-associativity of abstraction. Make sure your solution covers both precedence and associativity.

Now, the expressions:

```
a. (λx.x) y z
Example: (((λx.x) y) z) (Only associativity is necessary in this example since parentheses are already present to force abstraction)
b. λx . λy . λz . z y x
c. λx . x y λz . w λw . w x z
```

```
c. \lambda x . x y \lambda z . w \lambda w . w x z d. x \lambda z . x \lambda w . w z y
```

e.
$$\lambda z.((\lambda s.s \ q) \ (\lambda q.q \ z)) \ \lambda z.z \ z$$

2. Circle all of the free variables (if any) for each of the following lambda expressions:

```
a. \lambda z \cdot z x \lambda y \cdot y z
b. (\lambda x.x) (\lambda x.x (\lambda y.y)) z
c. \lambda p.(\lambda z.f \lambda x.z y) p x
d. \lambda x \cdot x y \lambda x \cdot y x
e. \lambda x \cdot x (x y)
```

3. This next set of questions is intended to help you understand more fully why α -conversions are needed: namely, to avoid having a free variable in an actual parameter captured by a formal parameter of the same name. This would result in a different (incorrect) solution. Remember that when performing an α -conversion, we always change the name of the *formal* parameter—never the free variable. Consider the following lambda expressions. For each of the expressions below, state whether the expression can be legally β -reduced without any α -conversion at any of the steps, according to the rule we learned in class. For any expression below requiring an α -conversion, perform the β -reduction twice: once after performing the α -conversion (the correct way) and once after not performing it (the incorrect way). Do the two methods reduce to the same expression?

```
a. (\lambda xy \cdot z x)(\lambda x \cdot x y)
b. (\lambda x \cdot \lambda yz \cdot x y z)(\lambda z \cdot z x)
c. (\lambda x \cdot x z)(\lambda xz \cdot x y)
d. (\lambda x \cdot x y)(\lambda x \cdot y)
```

Note: All the variables are single letters $\{x, y, z\}$, i.e, expression $(\lambda x . \lambda yz . xyz)$ is equivalent to $(\lambda x . \lambda y . \lambda z . (xyz))$.

4. For each of the expressions below, β -reduce each to normal form (provided a normal form exists) using applicative order reduction. For each, perform α conversions where required. For clarity, please show each step individually—do not combine multiple reductions on a single line.

```
a. ((\lambda y \cdot z \ y) \ x)(\lambda x \cdot x \ y)
b. (\lambda x \cdot x \ x \ x) \ (\lambda x \cdot x \ x \ x)
c. (\lambda x \cdot x)(\lambda y \cdot x \ y)(\lambda z \cdot x \ y \ z)
d. MULT 「0¬ 「3¬
e. EXP 「2¬ 「1¬
```

If the tools you are using to submit your solution supports the λ character, please use it in your solution. If not, you may write \lam as a substitute for λ .

5. [25 points] Scheme For the questions below, turn in your solutions in a single Scheme (.rkt) file, placing your prose answers in source code comments. Multi-line comments start with #| and end with |#.

In all parts of this section, implement iteration using recursion. Do NOT use the iterative features such as set, while, display, begin, etc. Do not use any function ending in "!" (e.g. set!). These are imperative features which are not permitted in this assignment. Use only the functional subset discussed in class and in the lecture slides. Do not use Scheme library functions in your solutions, except those noted below and in the lecture slides.

Some helpful tips:

- Scheme library function list turns an atom into a list.
- You might find it helpful to define separate "helper functions" for some of the solutions below.
 Consider using one of the let forms for these.
- the conditions in "if" and in "cond" are considered to be satisfied if they are not #f. Thus (if '(A B C) 4 5) evaluates to 4. (cond (1 4) (#t 5)) evaluates to 4. Even (if '() 4 5) evaluates to 4, as in Scheme the empty list () is not the same as the Boolean #f. (Other versions of LISP conflate these two.)
- You may call any functions defined in the Scheme lecture slides in your solutions. (For that reason, you may obviously include the source code for those functions in your solution without any need to cite the source.)
- You may not look at or use solutions from any other source when completing these exercises.
 Plagiarism detection will be utilized for this portion of the assignment. DO NOT PLAGIARIZE YOUR SOLUTION.

Please complete the following:

1. Write a function chain that expects two arguments: a list of unary functions f_1, f_2, \ldots, f_n , and an initial value v. The chain function should compute $f_n(f_2(\ldots, f_1(v)))$

```
>(define inc (a) (+ a 1))
>(define dec (a) (- a 1))
>(chain (list inc dec inc dec) 5)
5
>(chain (list dec dec dec) 5)
2
>(chain (list inc) 5)
6
>(chain '() 2)
```

Note: The type of n will not necessarily be numeric. Moreover, for any function f_i the input type will not necessarily be the same as the output type.

2. Implement a function chain_odd that expects two arguments: a list of unary functions f_1, f_2, \ldots, f_n , and an initial value v. Like above the type of v may not be numeric, but unlike above, the inputs/output types for each function f_i are the same.

The chain_odd function should behave in the same way as chain, except that for each list of functions provided as input f_1, f_2, \ldots, f_n , we define another list of functions g_1, g_2, \ldots, g_n exhibiting the following behavior:

Function $g_i(n) = f_i(n)$ if n is a number and n is odd. Otherwise, $g_i(n) = n$. The chain_odd function should then compute $g_n(g_2(\ldots,g_1(v)))$. You might find the built-in predicate odd? handy.

```
>(define (inc n) (+ n 1))
>(define (dec n) (- n 1))
>(define (plus2 n) (+ n 2))
```

```
>(define (minus2 n) (- n 2))
>(define (ident s) s)

>(chainodd (list inc inc inc inc) 3)
4
>(chainodd (list plus2 plus2 dec minus2) 3)
6
>(chainodd '() 2)
2
>(chainodd (list ident ident) "hey")
"hey"
```

3. Implement a function **zip** which takes two input lists (assume they are both the same size n) and outputs a list of n pairs, where pair i contains values from the ith position of each input list. If the input lists are empty, the output list should be empty.

```
>(zip '(1 2 3) '(4 5 6))
((1 4) (2 5) (3 6))
>(zip '(1 2) '(2 3))
((1 2) (2 3))
```

4. Implement a function unzip which computes the reverse of zip. That is, given a list of pairs of size n, evaluate to a list of two lists, each of size n where output list i contains values from the ith position of each input list. If the input list is empty, the two output lists should be empty.

```
>(unzip '((1 4) (2 5) (3 6))
((1 2 3) (4 5 6))
>(unzip ('(1 2) '(2 3))
>((1 2) (2 3))
```

5. Implement a function cancellist which given two lists, will remove from both lists all occurrences of numbers appearing in both.

```
>(cancellist '() '())
(() ())
>(cancellist '(1 3) '(2 4))
((1 3) (2 4))
>(cancellist '(1 2) '(2 4))
((1) (4))
>(cancellist '(1 2 3) '(1 2 2 3 4))
(() (4))
```

6. Implement a function reverse, which expects a list X and returns the same list reversed.

```
>(reverse '(1 2 3))
(3 2 1)
```

7. Implement a function interleave_outer, which expects as arguments two lists X and Y, and returns a single list obtained by choosing elements from the beginning of X and the end of Y. If the sizes of the lists are not the same, the excess elements on the longer list will appear at the end of the resulting list. Input lists can be empty as well.

```
>(interleave_outer '(1 2 3) '(a b c))
(1 c 2 b 3 a)
>(interleave_outer '(1 2 3) '(a b c d e f))
(1 f 2 e 3 d c b a)
>(interleave_outer '(1 2 3 4 5 6) '(a b c))
(1 c 2 b 3 a 4 5 6)
```

8. Write a function $count_occurrences$ that takes two arguments: a list lst and an element x. The function should return the number of times x appears in lst.

Example:

```
>(count-occurrences '(1 2 3 2 4) 2)
2
>(count-occurrences '(1 2 3 2 4) 1)
1
>(count-occurrences '(1 2 3 2 4) 6)
0
```