NCERT 10.5.2 17Q

EE23BTECH11012 - Chavan Dinesh*

Question: Find the 20^{th} term from the last term of the AP: 3, 8, 13.....253.

Solution:

As the 20th term is considered from last,

Parameter	Description	Value
x(0)	first term	3
d	common difference	8 - 3 = 5
x(N)	$(N+1)^{th}$ term	x(0) + Nd
x(N-n)	$(n+1)^{th}$ term from last	x(0) + (N-n)d

TABLE 1: Input table

From Table 1:

$$x(N) = x(0) + Nd \tag{1}$$

$$253 = 3 + 5N \tag{2}$$

$$250 = 5N \tag{3}$$

$$N = 50 \tag{4}$$

From Table 1:

$$x(N - n) = x(0) + (N - n)d$$
 (5)

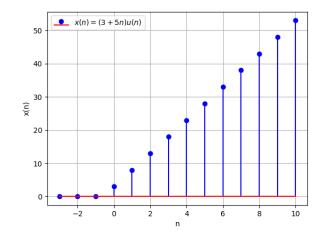
$$x(N-19) = 3 + (50 - 19)(5) \tag{6}$$

$$= 3 + 155$$
 (7)

$$= 158$$
 (8)

From equation (??) and (??): Z-Transform of x(N):

$$X(z) = \frac{3}{1 - z^{-1}} + \frac{5z^{-1}}{(1 - z^{-1})^2}; \{ z \in \mathbb{C} : |z| > 1 \}$$
(9)



1

Fig. 1