## NCERT 11.9.3 28Q

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**Question:** The sum of two numbers is 6 times their geometric mean, show that num-

bers are in the ratio  $\frac{(3+2\sqrt{2})}{(3-2\sqrt{2})}$ .

**Solution:** Let the two numbers be x(0) and x(2) such that  $x(2) \ge x(0)$  and x(1) is G.M of x(0) and x(2).

Parameter	Description	Value
x(0)	first number	
x(2)	second number	$x(0)r^2$
r	common ratio	
x(n)	$(n+1)^{th}$ term	$(x(0)r^n)u(n)$

TABLE 1: Input table

## From Table 1:

$$x(0) + x(2) = 6x(1) \tag{1}$$

$$x(0) + x(0)r^2 = 6x(0)r$$
 (2)

$$r^2 - 6r + 1 = 0 (3)$$

$$r = 3 \pm 2\sqrt{2} \tag{4}$$

$$\therefore \frac{x(2)}{x(0)} = (3 \pm 2\sqrt{2})^2 \tag{5}$$

$$=\frac{(3+2\sqrt{2})}{(3-2\sqrt{2})}\tag{6}$$