IT 427, Design and Analysis of Algorithms

Programming Assignment 8: Maximum Match

Due date: Dec. 3, 2023, Sunday, 11:59 PM 50 points (40 on programs, 10 on report)

In this assignment, we will determine whether a given undirected graph is bipartite, and if it is, we will find the maximum number of matches between the two disjoint and independent sets of vertices. We will not use a new algorithm to solve the problem. Instead, we will *reduce* the problem to a max-flow problem that you have solved in the previous assignment.

Prepare your programs on Linux Server:

- Make your directory ~/IT427/asg8/. All programs and needed files should be saved under this directory before run submit427.sh for submission.
- Check the contents of my /home/ad.ilstu.edu/cli2/Public/IT427/asg8. There are four files: undG1.txt, undG2.txt, undG3.txt and undG4.txt under the directory.

Program requirement: The name of the program should be maxMatch.java and I will compile and run your program on our Linux server as follows.

```
javac maxMatch.java
java maxMatch undG1.txt
```

If your program fails to compile, you will get 0 point. In addition to the four standard input files, I will test your program on some different files that contains undirected graphs in the same format.

Input: The input file is formatted exactly same as Assignment 2. Since undirected graphs must be symmetric, if vertices x and y are adjacent, only one of (x, y) and (y, x) is shown in the edge section.

20 Undirected Graphs in undG1.txt.

```
** G1: |V|=10, V=0..9
Edges (u, v) E = {
            (0, 2)
            (0, 4)
            (0, 5)
            (0, 9)
            (1, 2)
            .....
            (7, 9)
            (8, 9) }
------

** G2: |V|=10 V={0..9}
            .....

** G20: |V|=40 V={0..39}
            .....
```

Output: For each graph, if the graph is bipartite, show the maximum matches followed by a line to indicate how many pairs are there. Note that, there may be many different maximum matches and due to different implementation, the set of pairs may be different, but the maximum size must be the same. If the graph is not bipartite, indicate so. Follow the following output format:

Maximum number of matches in bipartite graphs in [undG1.txt]

```
** G1: |V|=10
     (0, 2)
     (1, 3)
     (6, 4)
     (7, 5)
     (8, 9)
     Matches:
               5 pairs (5 ms)
** G2: |V|=10
     (0, 2)
     (1, 4)
     (3, 9)
     (5, 8)
     Matches: 4 pairs (0 ms)
     . . . . . .
** G5: |V|=10
     Not a bipartite graph (0 ms)
** G6: |V|=20
     Not a bipartite graph (0 ms)
     . . . . . .
     . . . . . .
```

Submission: Programs (40 points) and Reports (10 points)

\bigstar Any plagiarism will receive 0 and be reported to the school \bigstar

1. Submission details are same as the previous assignment. Run the submission script with the submission number changed to 8, but you can use the same secret name as follow:

bash /home/ad.ilstu.edu/cli2/Public/IT427/submit427.sh peekapoo 8

The score is based on the correctness and the programming style, which includes efficiency, appropriateness of data structures, and documentation of your programs. At the beginning of every program file, put a section of comments including (1) your full name, (2) student ID, (3) a pledge of honesty that you do not copy/modify from other's codes and (4) a declaration of your copyright that no one else should copy/modify the codes. You will receive:

- (a) 40 points: No error with a good programming style.
- (b) $35 \sim 39$ points: Minor error and fair programming style.
- (c) $30 \sim 34$ points: Some error and not so good but acceptable programming style.
- (d) $20 \sim 29$ points: Too many error and bad programming style, but meaningful.
- (e) $10 \sim 19$ points: Compilable but not working and the program must show reasonable trying.
- (f) 0 points: Fail to meet any of aforementioned qualities or plagiarism involved.
- 2. Report: 10 points. Submission through Canvas.

You have to write up a report and prepare it in pdf format. You don't have to put program output on the report as I will run and exam your program directly on some different input files.

- (a) 2 points on the cover page, and
- (b) 8 points on algorithm descriptions, summary of the methods, data structures, and efficiency analysis on time and space in details in terms of big-O notations. If your analysis is not clearly related to your program and provides sufficient justification, your report score will not be higher than 50%. You don't have to analyze the algorithm of maximum flow, which is done in the previous assignment. You can directly use the analysis result from the previous assignment. However, you have explain how does your program reduce the maximum match problem to maximum flow problem.

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